

1. $\text{graph}[][] = \begin{bmatrix} 0 & 5 & \infty & 10 \\ \infty & 0 & 3 & \infty \\ \infty & \infty & 0 & 1 \\ \infty & \infty & \infty & 0 \end{bmatrix}$

$$D_1 = \begin{bmatrix} 0 & 5 & \infty & 10 \\ \infty & 0 & 3 & \infty \\ \infty & \infty & 0 & 1 \\ \infty & \infty & \infty & 0 \end{bmatrix}$$

$$D_2 = \begin{bmatrix} 0 & 5 & 8 & 10 \\ \infty & 0 & 3 & \infty \\ \infty & \infty & 0 & 1 \\ \infty & \infty & \infty & 0 \end{bmatrix}$$

$$D_3 = \begin{bmatrix} 0 & 5 & 8 & 9 \\ \infty & 0 & 3 & 4 \\ \infty & \infty & 0 & 1 \\ \infty & \infty & \infty & 0 \end{bmatrix}$$

$$D_4 = \begin{bmatrix} 0 & 5 & 8 & 9 \\ \infty & 0 & 3 & 4 \\ \infty & \infty & 0 & 1 \\ \infty & \infty & \infty & 0 \end{bmatrix}$$

$$2. \text{ graph}[][] = \begin{bmatrix} 0 & \infty & -2 & \infty \\ 4 & 0 & 3 & \infty \\ \infty & \infty & 0 & 2 \\ \infty & -1 & \infty & 0 \end{bmatrix}$$

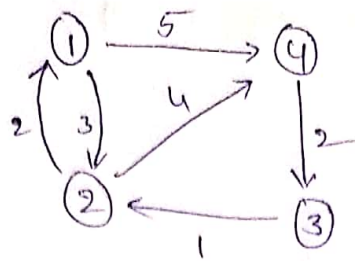
$$D_1 = \begin{matrix} & 1 \\ 1 & \begin{bmatrix} 0 & \infty & -2 & \infty \\ 4 & 0 & 2 & \infty \\ \infty & \infty & 0 & 2 \\ \infty & -1 & \infty & 0 \end{bmatrix} \end{matrix}$$

$$D_2 = \begin{matrix} & & 2 \\ & 2 & \begin{bmatrix} 0 & \infty & -2 & \infty \\ 4 & 0 & 2 & \infty \\ \infty & \infty & 0 & 2 \\ 3 & -1 & 2 & 0 \end{bmatrix} \end{matrix}$$

$$D_3 = \begin{matrix} & & & 3 \\ & & 3 & \begin{bmatrix} 0 & \infty & -2 & 0 \\ 4 & 0 & 2 & 4 \\ \infty & \infty & 0 & 2 \\ 3 & -1 & 2 & 0 \end{bmatrix} \end{matrix}$$

$$D_4 = \begin{matrix} & & & & 4 \\ & & & 4 & \begin{bmatrix} 0 & -1 & -2 & 0 \\ 4 & 0 & 2 & 4 \\ 5 & 1 & 0 & 2 \\ 3 & -1 & 2 & 0 \end{bmatrix} \end{matrix}$$

3.



$$\text{Graph} = \begin{bmatrix} 0 & 3 & \infty & 5 \\ 2 & 0 & \infty & 4 \\ \infty & 1 & 0 & \infty \\ \infty & \infty & 2 & 0 \end{bmatrix}$$

$$D_1 = \begin{matrix} 1 \\ \begin{bmatrix} 0 & 3 & \infty & 5 \\ 2 & 0 & \infty & 4 \\ \infty & 1 & 0 & \infty \\ \infty & \infty & 2 & 0 \end{bmatrix} \end{matrix}$$

$$D_2 = \begin{matrix} 2 \\ \begin{bmatrix} 0 & 3 & \infty & 5 \\ 2 & 0 & \infty & 4 \\ 3 & 1 & 0 & 5 \\ \infty & \infty & 2 & 0 \end{bmatrix} \end{matrix}$$

$$D_3 = \begin{matrix} 3 \\ \begin{bmatrix} 0 & 3 & \infty & 5 \\ 2 & 0 & \infty & 4 \\ 3 & 1 & 0 & 5 \\ 5 & 3 & 2 & 0 \end{bmatrix} \end{matrix}$$

$$D_4 = \begin{matrix} 4 \\ \begin{bmatrix} 0 & 3 & 7 & 5 \\ 2 & 0 & 6 & 4 \\ 3 & 1 & 0 & 5 \\ 5 & 3 & 2 & 0 \end{bmatrix} \end{matrix}$$

∴ Final Answer is

$$\begin{bmatrix} 0 & 3 & 7 & 5 \\ 2 & 0 & 6 & 4 \\ 3 & 1 & 0 & 5 \\ 5 & 3 & 2 & 0 \end{bmatrix}$$

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TUTORIAL-3

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In [1]: ▶ # Floyd-warshall algorithm

import sys
INF = sys.maxsize

def floydWarshall(graph):
    # number of vertices in the graph
    n = len(graph)

    # dist will be the output matrix that will have the shortest distances between every pair
    dist = [[[] for i in range(n)]

    # Initialize the dist matrix as same as the input graph matrix.
    for i in range(n):
        for j in range(n):
            dist[i].append(graph[i][j])

    # Taking all vertices one by one and setting them as intermediate vertices
    for k in range(n):
        # Pick all vertices as source one by one.
        for i in range(n):
            # Pick all vertices as the destination for the above choosen source vertex.
            for j in range(n):
                # Update the value of dist[i][j] if k provides a shortest path from i to j
                dist[i][j] = min(dist[i][j],dist[i][k]+dist[k][j])

    # Shortest distance for every pair of vertex.
    print('Shortest Distance between every pair of vertex:-')
    for i in range(n):
        for j in range(n):
            if dist[i][j]==INF:
                print ("%7s" % ("INF"),end=' ')
            else:
                print ("%7s" % (dist[i][j]),end=' ')
        print()

```

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In [2]: ▶ graph = [[0,5,INF,10],[INF,0,3,INF],[INF,INF,0,1],[INF,INF,INF,0]]

floydWarshall(graph)

```

Shortest Distance between every pair of vertex:-

0	5	8	9
INF	0	3	4
INF	INF	0	1
INF	INF	INF	0

In [3]: ▶ #Example-3

```

# Floyd Warshall Algorithm in python
# The number of vertices
nV = 4
INF = 999
# Algorithm implementation
def floyd_warshall(G):
    distance = list(map(lambda i: list(map(lambda j: j, i)), G))
    # Adding vertices individually
    for k in range(nV):
        for i in range(nV):
            for j in range(nV):
                distance[i][j] = min(distance[i][j], distance[i][k] + distance[k][j])
    print_solution(distance)
# Printing the solution
def print_solution(distance):
    for i in range(nV):
        for j in range(nV):
            if(distance[i][j] == INF):
                print("INF", end=" ")
            else:
                print(distance[i][j], end=" ")
        print(" ")
G = [[0, 3, INF, 5],
      [2, 0, INF, 4],
      [INF, 1, 0, INF],
      [INF, INF, 2, 0]]
floyd_warshall(G)

```

```

0 3 7 5
2 0 6 4
3 1 0 5
5 3 2 0

```

In [4]: ▶ # Problem 2

```

graph = [[0, INF, -2, INF], [4, 0, 3, INF], [INF, INF, 0, 2], [INF, -1, INF, 0]]

floydWarshall(graph)

```

Shortest Distance between every pair of vertex:-

```

0      -1      -2      0
4      0       2      4
5      1       0      2
3     -1       1      0

```