

6. unification is a process of making two different logical atomic expressions identical by finding a substitution

unification depends on the substitution process. It takes two literals as input and makes them identical using substitution.

Let ψ_1 and ψ_2 be two atomic sentences and σ be a unifier such that $\psi_1\sigma = \psi_2\sigma$, then it can be expressed as ~~unify~~

$\text{unify}(\psi_1, \psi_2)$

Example: Find the MGU for $\text{unify}\{\text{king}(x), \text{king}(\text{John})\}$

Let $\psi_1 = \text{king}(x)$,
 $\psi_2 = \text{king}(\text{John})$

substitution $\theta = \{(x/\text{John})\}$ is a unifier for these atoms and applying this substitution, and both expressions will be identical.

The UNIFY Algorithm is used for unification, which takes two atomic sentences and returns a unifier for these sentences (if any exist) unification is a key component of all first order ~~order~~ inference algorithms

It returns fail if the expressions do not match with each other.

The substitution variables are called Most General unifier (or) MGU.

unification Algorithm:

Algorithm: $\text{unify}(\psi_1, \psi_2)$

step-1 : If ψ_1 or ψ_2 is a variable or constant then

a) If ψ_1 or ψ_2 are identical then return NIL.

b) Else if ψ_1 is a variable,

a. then if ψ_1 occurs in ψ_2 , then return FAILURE

~~b. Else if ψ_2 occurs in ψ_1 , then return FAILURE~~

b. Else return $\{(\psi_2/\psi_1)\}$

c) Else if ψ_2 is a variable,

a. If ψ_2 occurs in ψ_1 , then return FAILURE

b. Else return $\{(\psi_1/\psi_2)\}$

d) Else return FAILURE

step-2 : If the initial predicate symbol in ψ_1 and ψ_2 are not same, then return FAILURE.

step-3 : If ψ_1 and ψ_2 have a different no. of arguments, then return FAILURE

step-4 : set substitution set (SUBST) to NIL.

step-5 : For $i=1$ to the no. of elements in ψ_1

a) call unify function with the i th element of ψ_1 and i th element of ψ_2 and put the result into s .

b) If $s = \text{failure}$ then returns FAILURE

c) If $s \neq \text{NIL}$ then do

a. Apply s to the remainder of both L_1 and L_2

b. $\text{SUBST} = \text{APPEND}(s, \text{SUBST})$

step-6 : Return SUBST

Example

→ UNIFY (knows (Richard, x), knows (Richard, John))

Here $\psi_1 = \text{knows}(\text{Richard}, x)$

$\psi_2 = \text{knows}(\text{Richard}, \text{John})$

$S_0 \Rightarrow \{ \text{knows}(\text{Richard}, x); \text{knows}(\text{Richard}, \text{John}) \}$

SUBST $\theta = \{ \text{John}/x \}$

$S_1 \Rightarrow \{ \text{knows}(\text{Richard}, \text{John}); \text{knows}(\text{Richard}, \text{John}) \}$

successfully unified

unifier = $\{ \text{John}/x \}$

→ $\{ P(x, x) \text{ and } P(z, f(z)) \}$

Here $\psi_1 = \{ P(x, x) \}$

$\psi_2 = P(z, f(z))$

$S_0 \Rightarrow \{ P(x, x), P(z, f(z)) \}$

SUBST $\theta = \{ x/z \}$

$S_1 \Rightarrow \{ P(z, z), P(z, f(z)) \}$

SUBST $\theta = \{ f(z)/z \}$, unification failed.