

7. Local Beam Search

In this algorithm, it holds  $k$  no of states at any given time. At the start, these states are generated randomly. The successors of these  $k$  states are computed with the help of objective function. If any of these successors is the maximum value of the objective function, then the algorithm stops.

Otherwise the (initial  $k$  states and  $k$  no of successors of the states =  $2k$ ) states are placed in a pool. The pool is then sorted numerically. The highest  $k$  states are selected as new initial states. This process continues until a maximum value is reached.

Function BeamSearch(problem,  $k$ ) return a solution state  
start with  $k$  randomly generated states

loop

generate all successors of all  $k$  states

if any of the states = Solution, then return the state

else select the  $k$  best successors

end

9. Minimax is a kind of backtracking algorithm that is used in decision making and game theory to find the optimal move for a player, assuming that your opponent plays optimally. It is widely used in two player games such as Tic-Tac-Toe, chess etc

In minimax the two players are called maximizer and minimizer. The maximizer tries to get to highest score possible while the minimizer tries to do the opposite and get the lowest score possible

function MINIMAX-DECISION (state) return an action  
 return  $\arg \max_a \in \text{Actions} \quad \text{MIN-VALUE}(\text{RESULT}(\text{state}, a))$

function MAX-VALUE (state) returns a utility value  
 if TERMINAL-TEST (state) then return UTILITY (state)

$v \leftarrow -\infty$

for each  $a$  in ACTIONS (state) do

$v \leftarrow \text{MAX}(v, \text{MIN-VALUE}(\text{RESULT}(s, a)))$

return  $v$

function MIN-VALUE (state) returns utility value

if TERMINAL-TEST (state) then return UTILITY (state)

$v \leftarrow \infty$

for each  $a$  in ACTIONS (state) do

$v \leftarrow \text{MIN}(v, \text{MAX-VALUE}(\text{RESULT}(s, a)))$

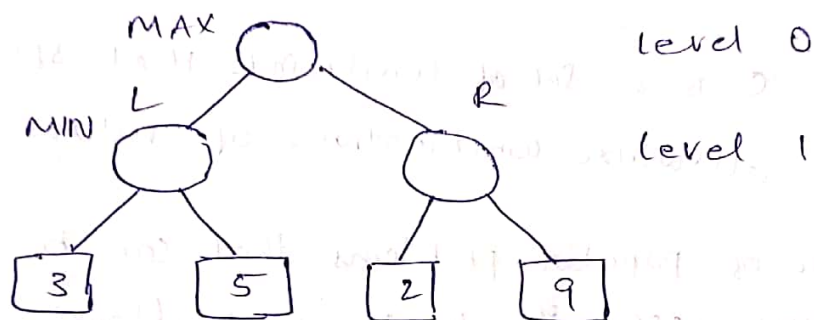
return  $v$



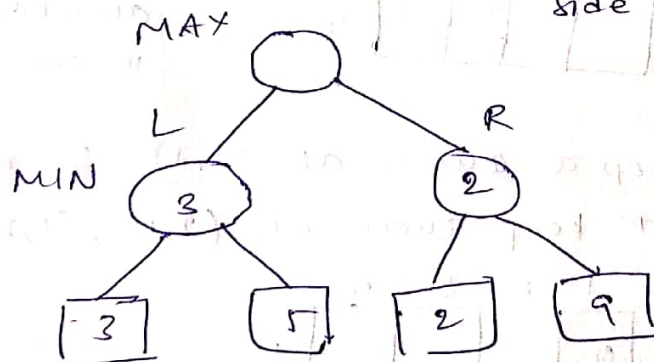
Example 1

Consider a game which has 4 final states and paths to reach final state are from root to 4 leaves of a perfect binary tree as shown.

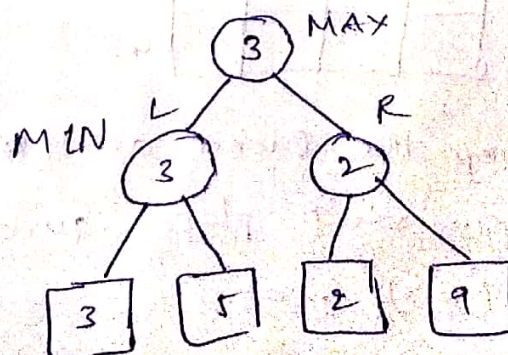
Assume you are the maximizing player and you get the first chance to move i.e., you are the root and your opponent at next level.



out of 3 & 5 3 is min so in left side  
Level 1 3 is filled in similar way on right  
side. out of 2 & 9  
2 is Min



out of 3 & 2 3 is Max so in root 3 is  
filled



Time	$O(b^d)$
space	$O(db)$

11. A Constraint Satisfaction problem is a problem that requires its solution within some limitations also known as constraints. It consists of the following

$X$  is a set of variables

$D$  is a set of Domains (one for each variable)

$C$  is a set of Constraints that specify allowable combinations of values

one of popular problems that can be solved using CSP is 4-queen problem

1.

	1	2	3	4
1	Q			
2				
3				
4				

Constraint

4 Queens must be placed in non attacking positions in every row

First keep a queen at  $(1,1)$  so now we can't keep queen at  $(2,1), (1,2), (2,2)$

2.

	1	2	3	4
1	Q			
2			Q	
3				
4				

Now keep the Queen at  $(3,2)$

now you can't place queens at  $(3,3)$

$(2,3), (4,3), \dots$  etc



Hence

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Our 1<sup>st</sup> move is wrong

Again start from 1<sup>st</sup>

Now keep Queen at (2,1)

1	2	3	4	
X	Q	X		1
X	X	X		2
				3
				4

Now keep another Queen at (4,2)

	Q	X	X
		X	Q
		X	X

Now keep third queen at (1,3)

1	2	3	4	
	Q			1
			Q	2
Q				3
				4

Now one more Queen at (3,4)

	Q		
			Q
Q			
		Q	

Hence solved

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 $c_2 c_1$   
 $c_3 E A T$   
 $c_4 \text{ THAT}$ 

{0, 1, 2, 3, 4, 5, 7, 8, 9}

 $c \in (0, 1)$ 

A PPLE

$$T + T = E + 10 \times c_1$$

$$A + A = L + 10 \times c_2$$

$$E + H = P + 10 \times c_3$$

$$c_3 + T = P + 10 \times c_4$$

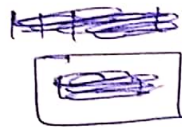
E	8
A	1
T	9
H	2
P	0
L	3

$$c_4 = A$$

leading value cannot be 0

$$\text{Hence } A = 1$$

	1		
	8	1	9
	9	2	9
	1	0	0
	3	8	



$$\text{if } c_1 = 1$$

$$c_1 + A + A = L$$

$$1 + 1 + 1 = L$$

$$L = 3$$

$$\Rightarrow c_2 = 0$$

For  $c_4$  to be 1  $c_3 + T = P$  must be  $\geq 10$ 

$$T = 9$$

$$c_3 = 1$$

$$P = 0$$

$$E + H = P + 10$$

$$E + H = 10$$

$$\Rightarrow E = 8, H = 2$$