

Home Work 4-2 - Recursion

A recursive method is a method that calls itself either directly or indirectly through another method. Recursion is discussed in an example on the course web page using the Triangle class.

Factorial is a popular mathematical operation. It is defined as follows:

The factorial of a non-negative integer " n ", written " $n!$ " (and pronounced "n factorial"), is defined as the product:

$$n! = n \times (n - 1) \times (n - 2) \times (n - 3) \dots \times 1$$

For example:

$$5! = 5 \times 4 \times 3 \times 2 \times 1 \quad \text{which is equal to 120.}$$

There are two special cases: $1! = 1$ and $0! = 1$.

Back in unit 1 you saw the following program. It calculates the factorial of any number using a simple loop (i.e. non-recursively).

```
import javax.swing.*;

public class Factorial
{
    public static long factorial (long number)
    {
        long fact = 1;
        for (long count = number ; count >= 1 ; count--)
        {
            fact = fact * count;
        }
        return fact;
    }

    public static void main (String [] args)
    {
        String input = JOptionPane.showInputDialog("Enter a non-negative integer: ");
        long num = Long.parseLong(input);

        JOptionPane.showMessageDialog ( null, num + "! = " + factorial(num),
                                       "Factorial", JOptionPane.PLAIN_MESSAGE);
        System.exit(1);
    }
}
```

Rewrite the above program using a recursive method.

Notice that given the above formula for factorial it can be expressed as follows:

$$n! = n \times (n - 1)!$$

Also note that the special case for the recursive method is that $0! = 1$ and $1! = 1$. Therefore the recursive factorial method can be started as follows:

```
public long factorial (long number)
{
    // special case code
    if (number <= 1)
    {
        return 1;
    }
    ...
}
```

Print out the new program and submit it.