Arithmetic

for Ashton, Lyla, Neomi, Ruth, and Malakai

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Arithmetic Preface

Preface

for Ashton, Lyla, Neomi, Ruth, and Malakai

Arithmetic Publication

Publication

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Arithmetic Copying

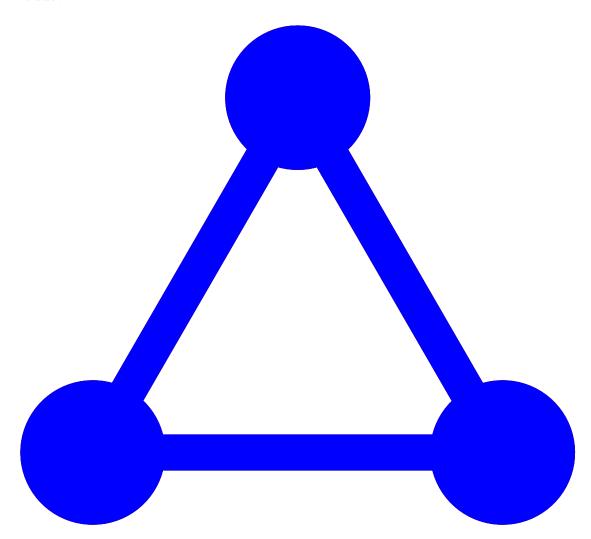
Copying

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Multiplication

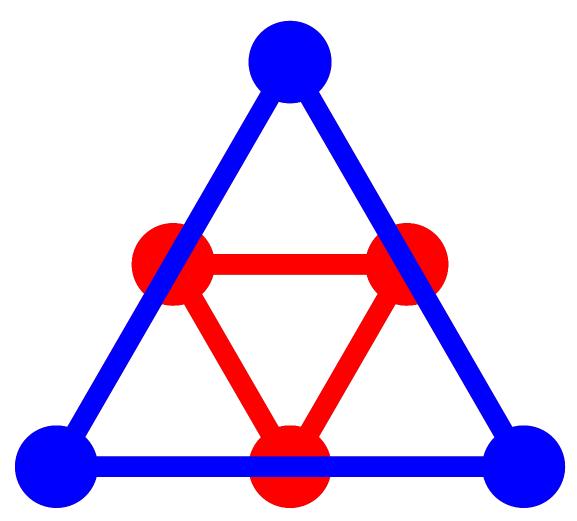
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Product $1 = 1 \times 1$

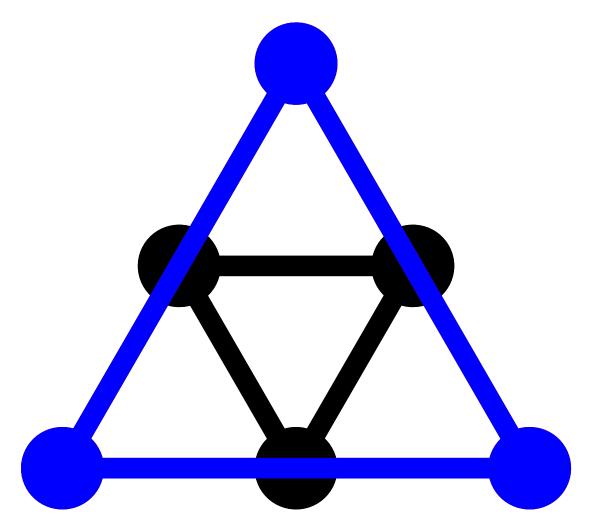


The Number 2

$\textbf{Product} \ 2 = 1 \times 2$

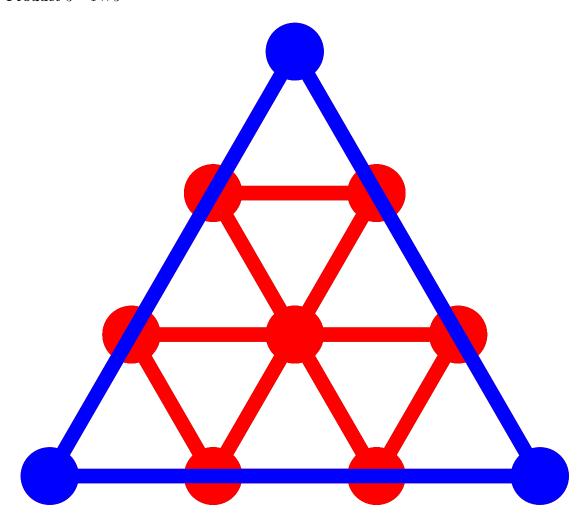


$\textbf{Product} \ 2 = 2 \times 1$

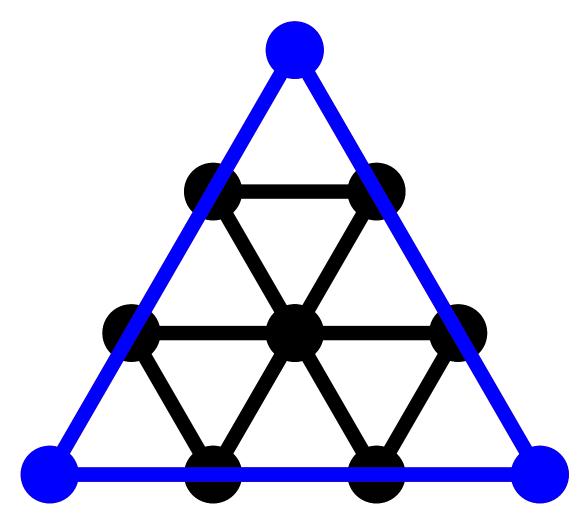


The Number 3

$\textbf{Product} \ 3 = 1 \times 3$

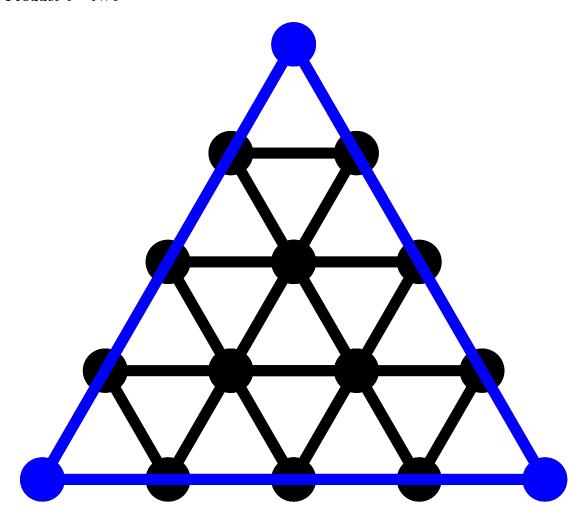


Product $3 = 3 \times 1$

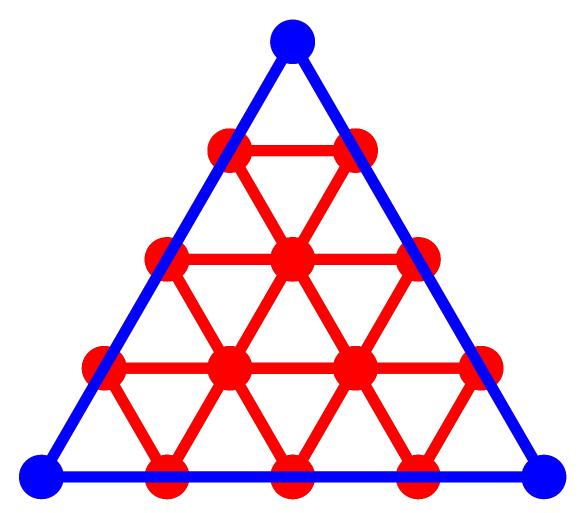


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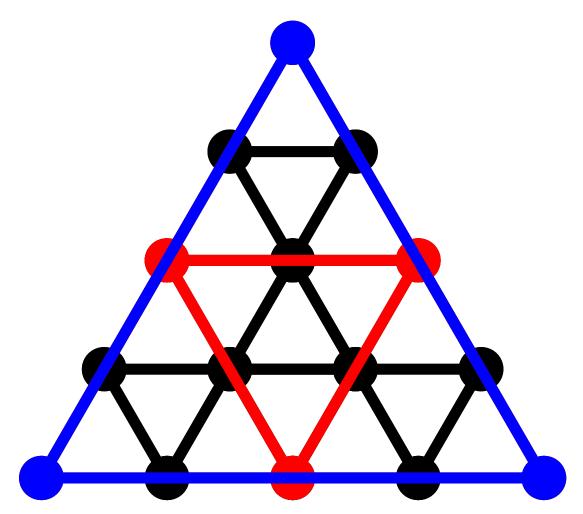
Product $4 = 4 \times 1$



$\textbf{Product}\ 4 = 1 \times 4$

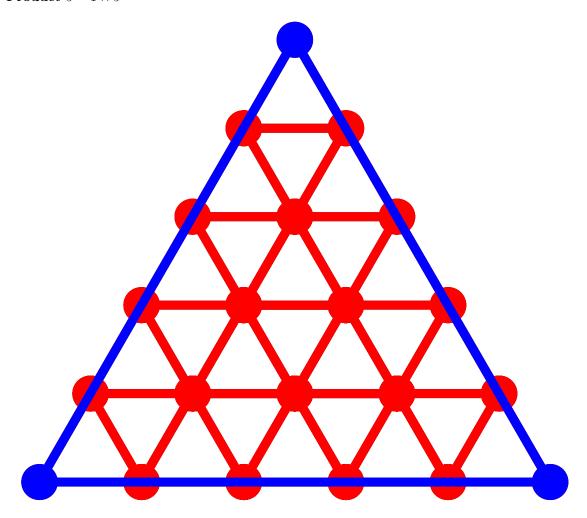


 $\textbf{Product}\ 4 = 2 \times 2$

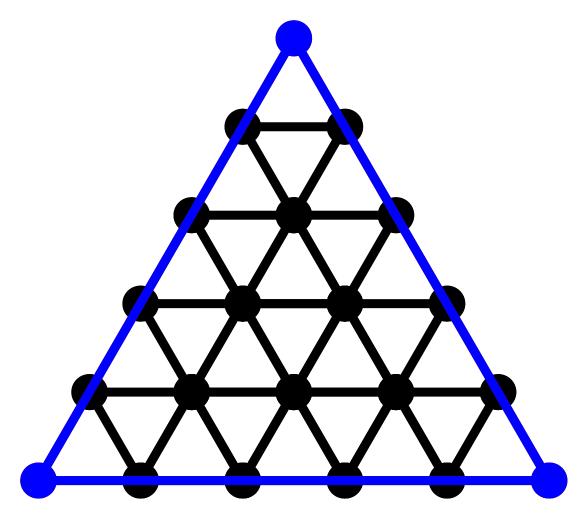


The Number 5

Product $5 = 1 \times 5$

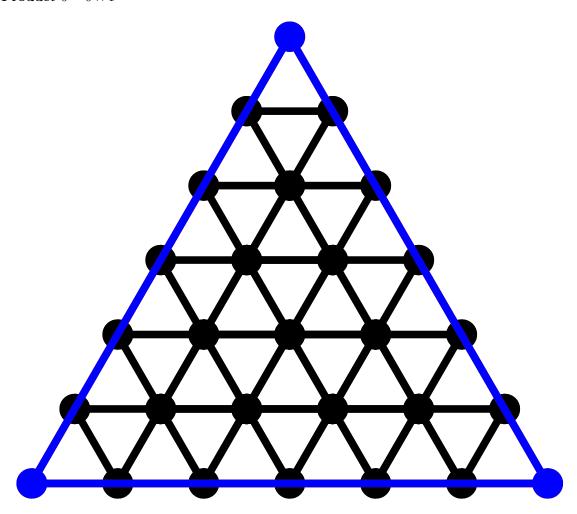


$\textbf{Product}\ 5 = 5 \times 1$

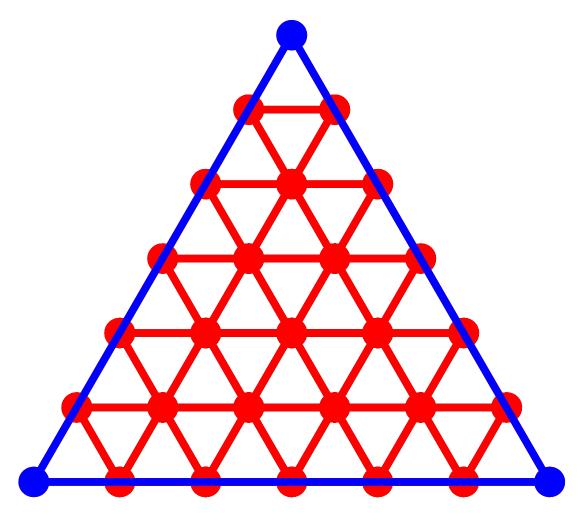


The Number 6

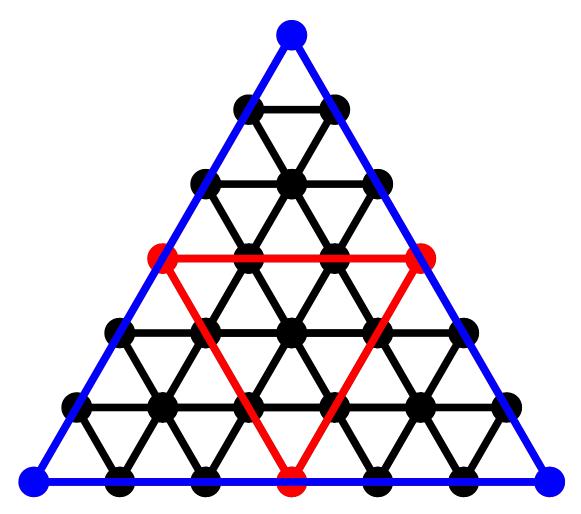
Product $6 = 6 \times 1$



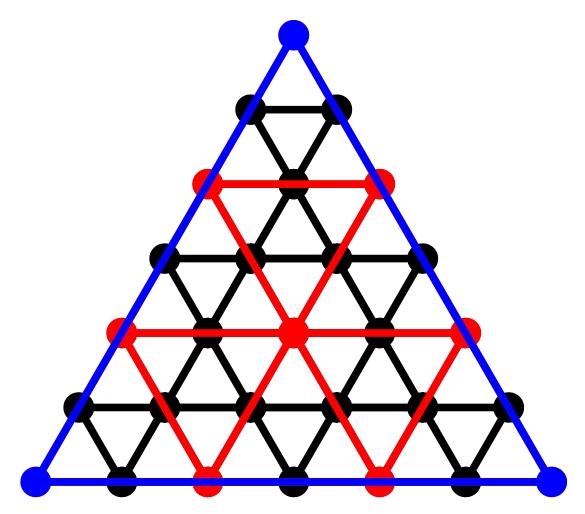
 $\textbf{Product} \ 6 = 1 \times 6$



$\textbf{Product} \ 6 = 3 \times 2$

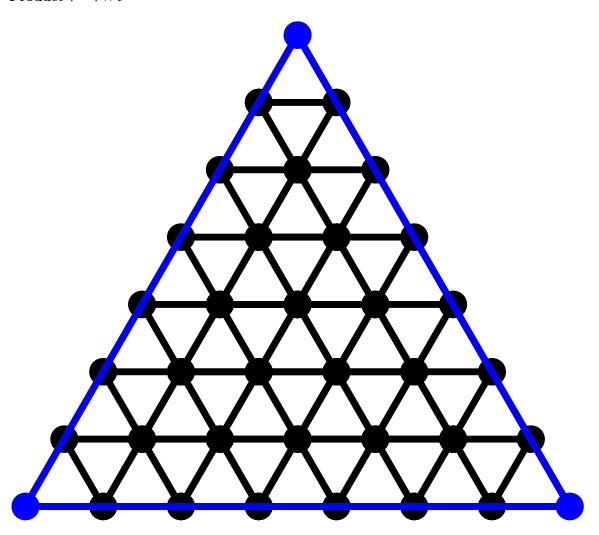


$\textbf{Product} \ 6 = 2 \times 3$

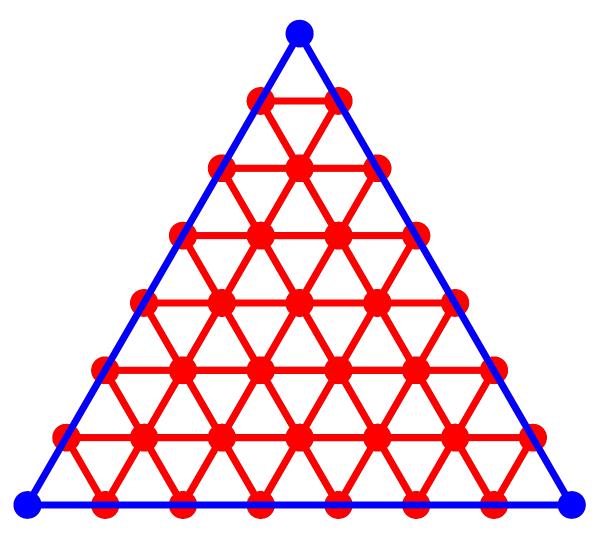


The Number 7

Product $7 = 7 \times 1$

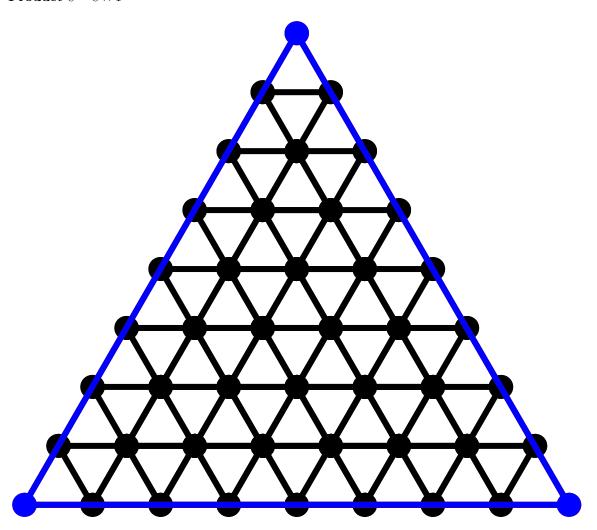


 $\textbf{Product} \ 7 = 1 \times 7$

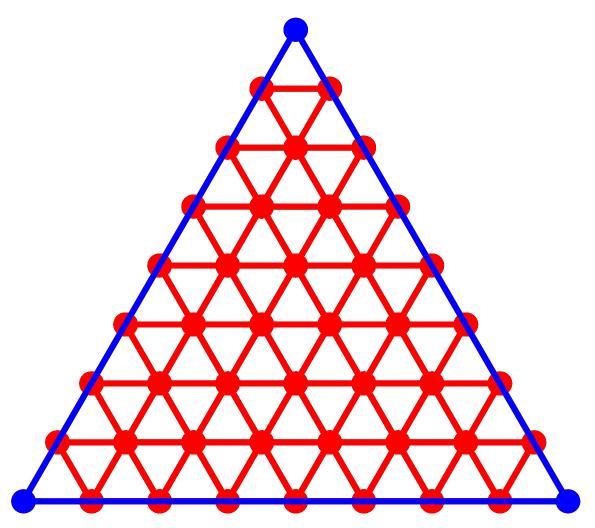


The Number 8

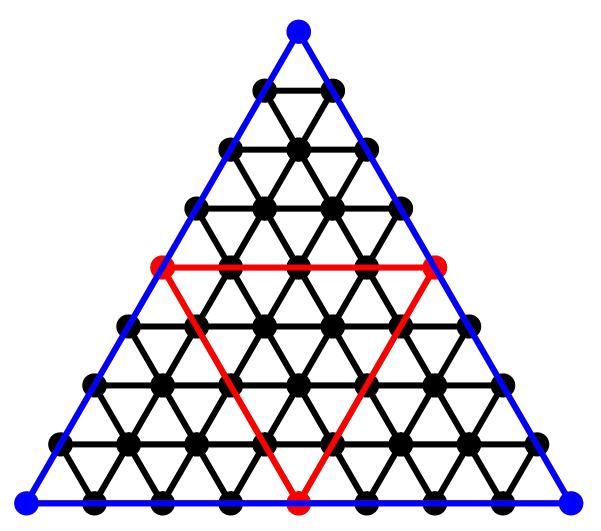
Product $8 = 8 \times 1$



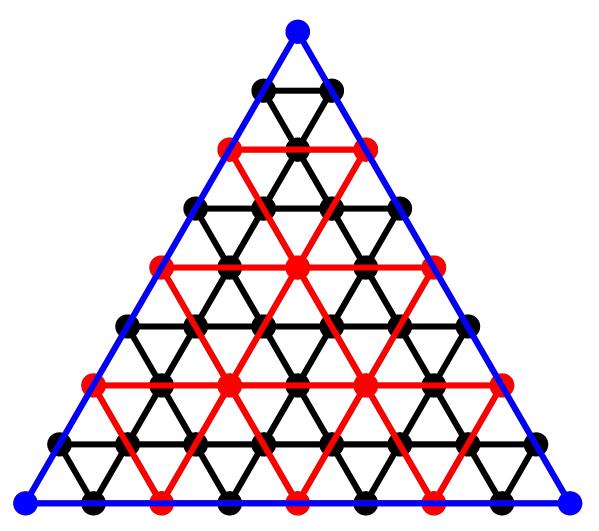
$\textbf{Product}\ 8 = 1 \times 8$



 $\textbf{Product}\ 8 = 4 \times 2$

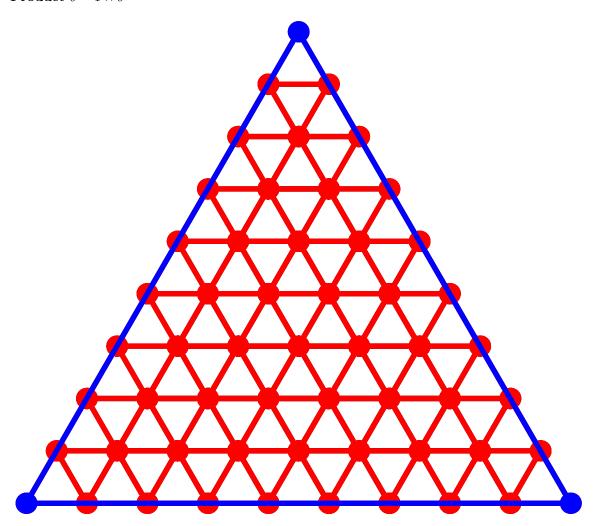


 $\textbf{Product}\ 8 = 2 \times 4$

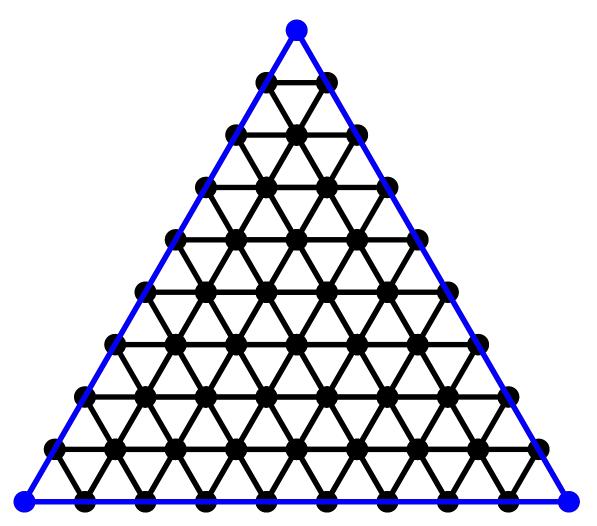


The Number 9

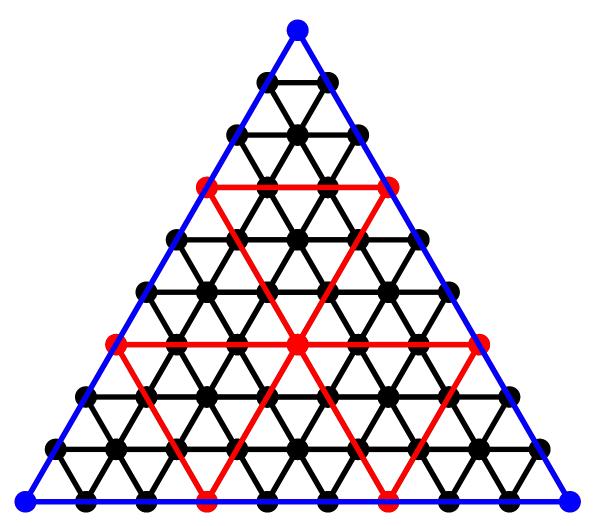
Product $9 = 1 \times 9$



$\textbf{Product} \ 9 = 9 \times 1$

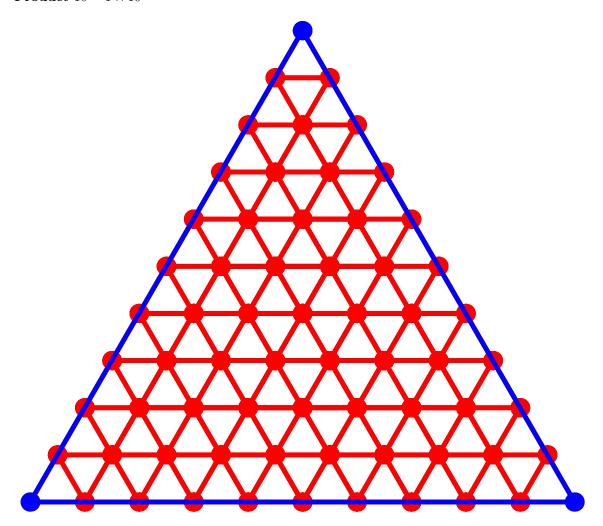


 $\textbf{Product} \ 9 = 3 \times 3$

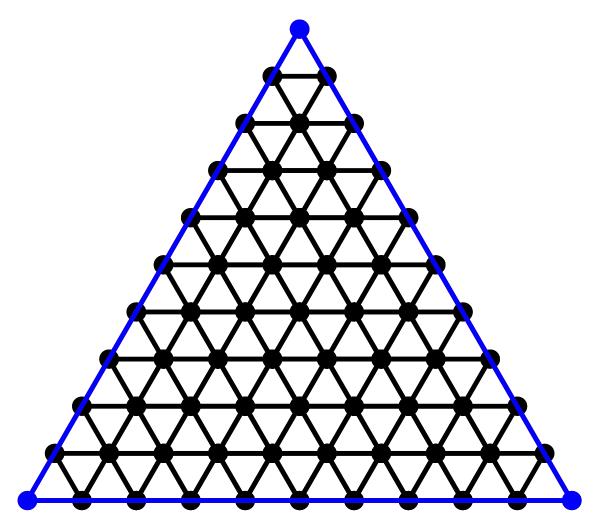


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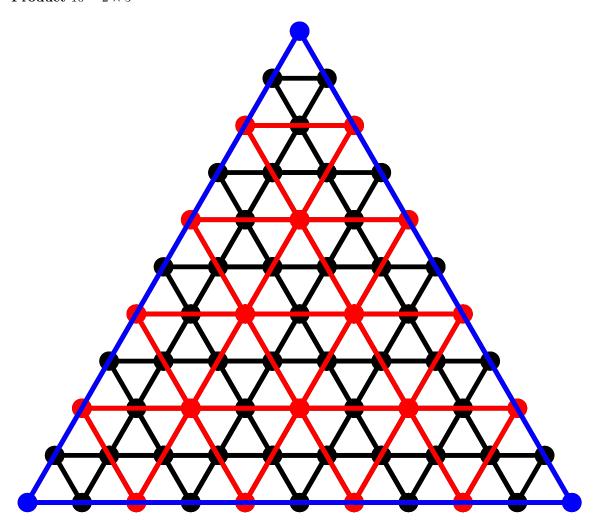
Product $10 = 1 \times 10$



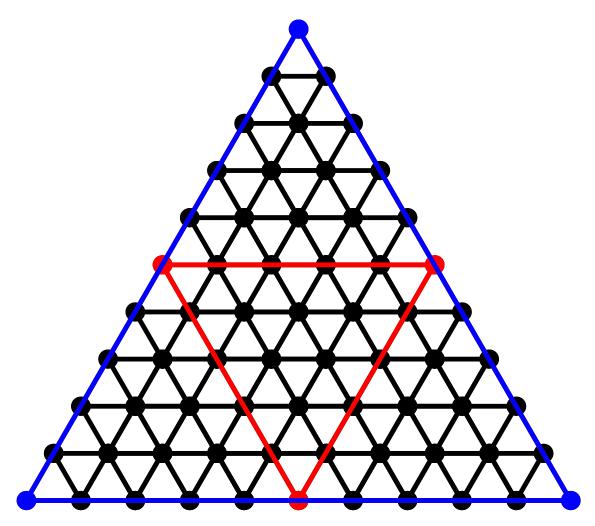
$\textbf{Product} \ 10 = 10 \times 1$



 $\textbf{Product} \ 10 = 2 \times 5$

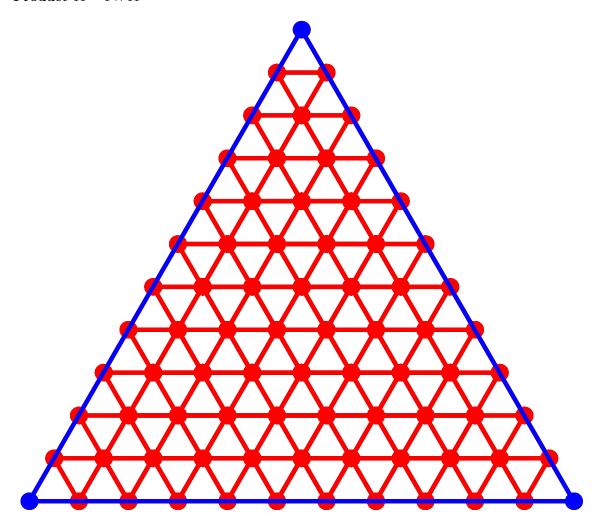


$\textbf{Product} \ 10 = 5 \times 2$

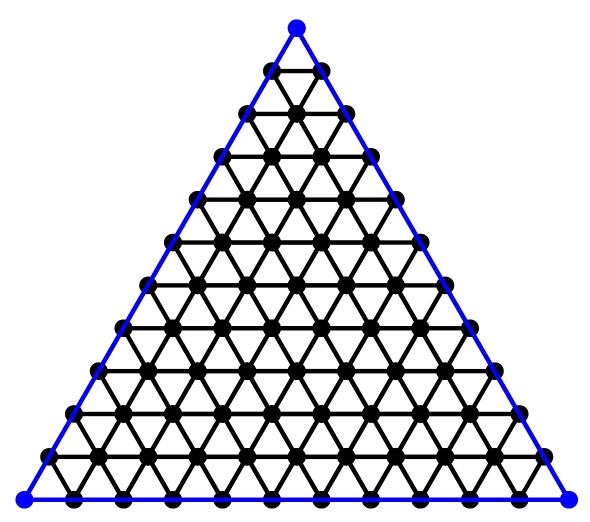


The Number 11

Product $11 = 1 \times 11$

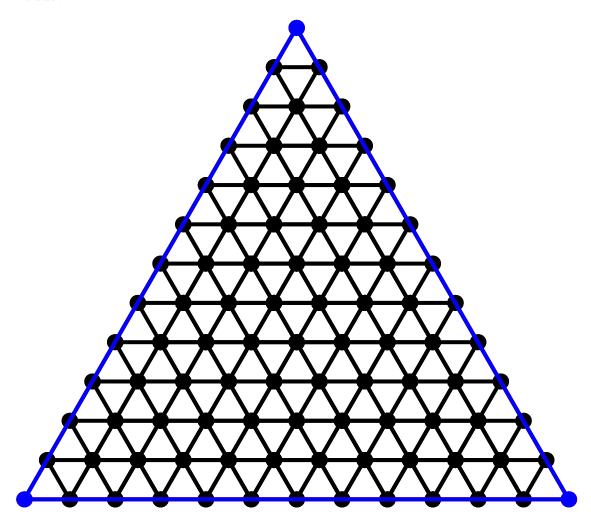


$\textbf{Product} \ 11 = 11 \times 1$

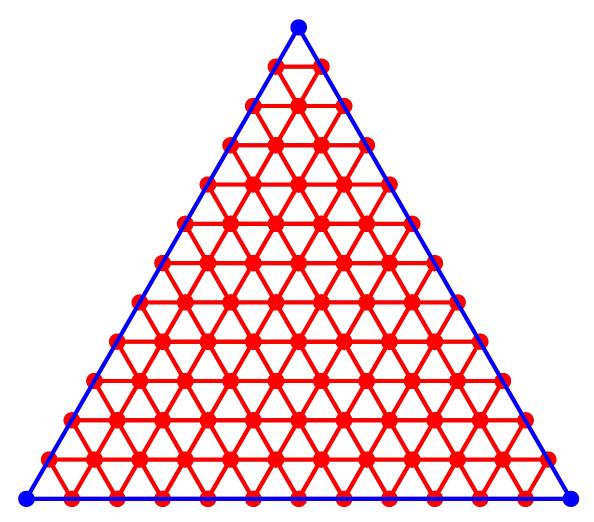


The Number 12

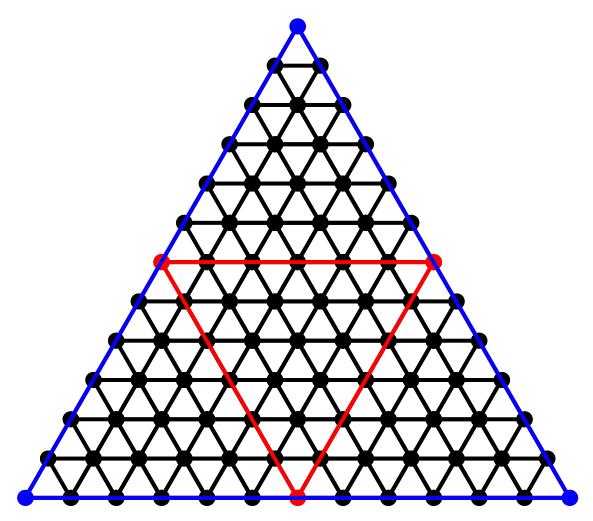
Product $12 = 12 \times 1$



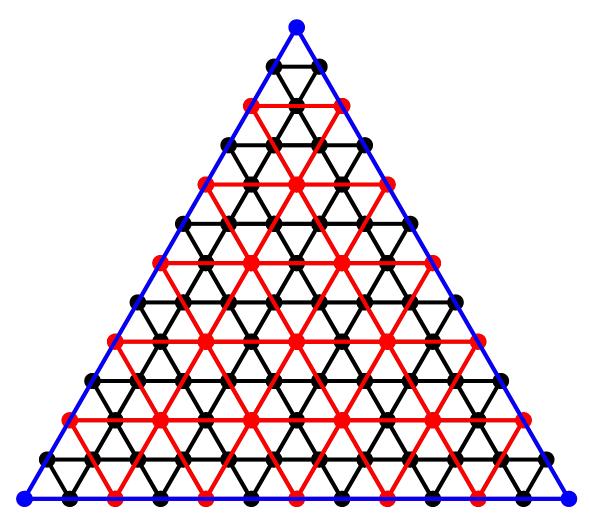
 $\textbf{Product} \ 12 = 1 \times 12$



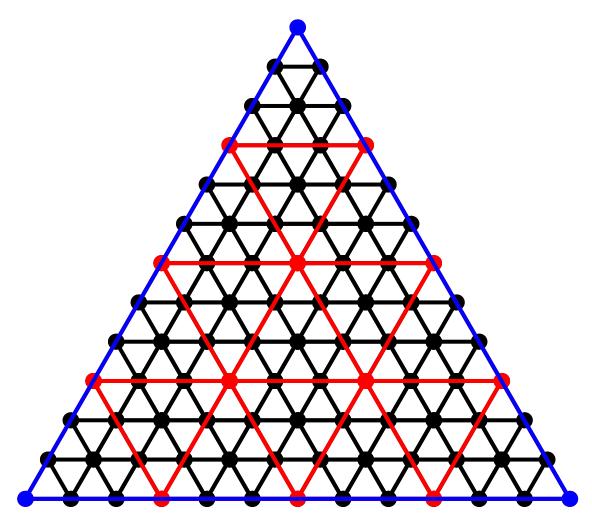
Product $12 = 6 \times 2$



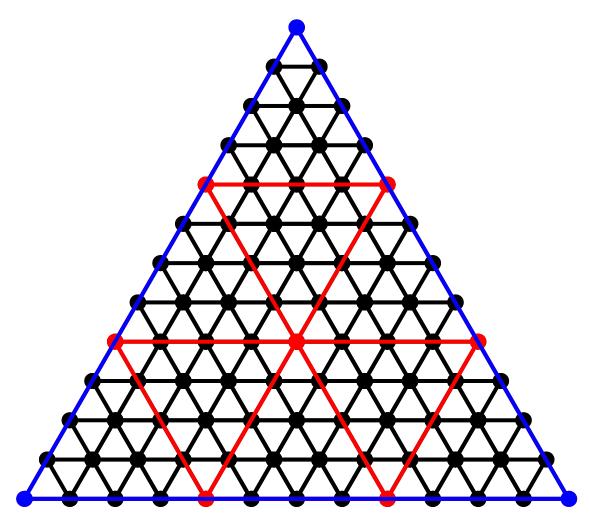
Product $12 = 2 \times 6$



 $\textbf{Product} \ 12 = 3 \times 4$

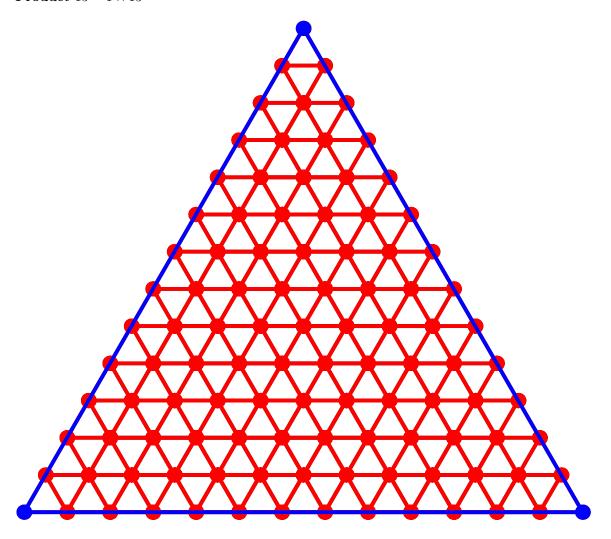


 $\textbf{Product} \ 12 = 4 \times 3$

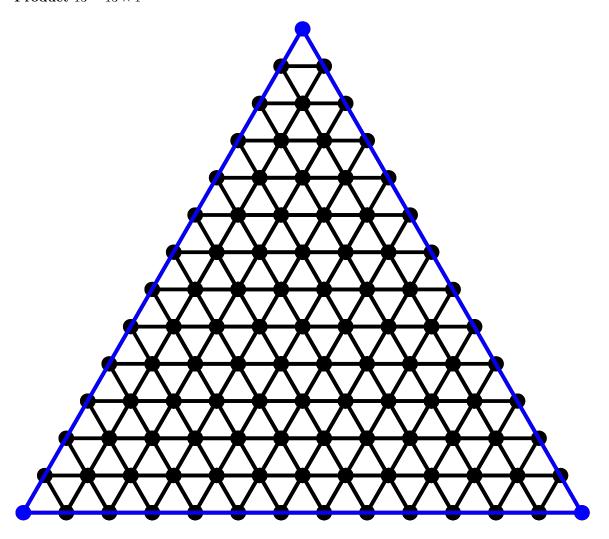


The Number 13

Product $13 = 1 \times 13$

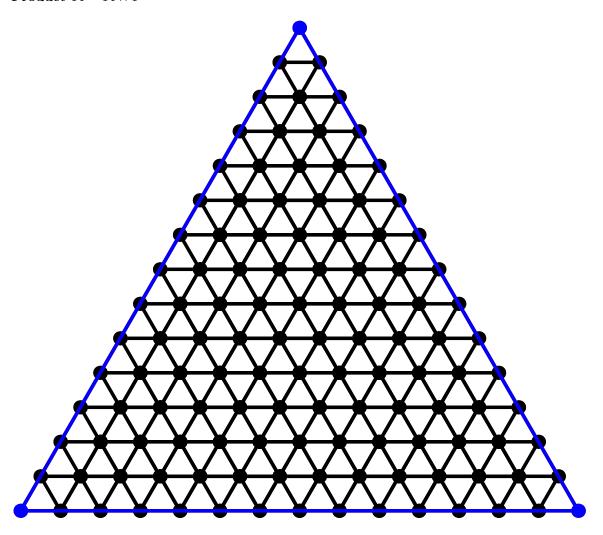


 $\textbf{Product} \ 13 = 13 \times 1$

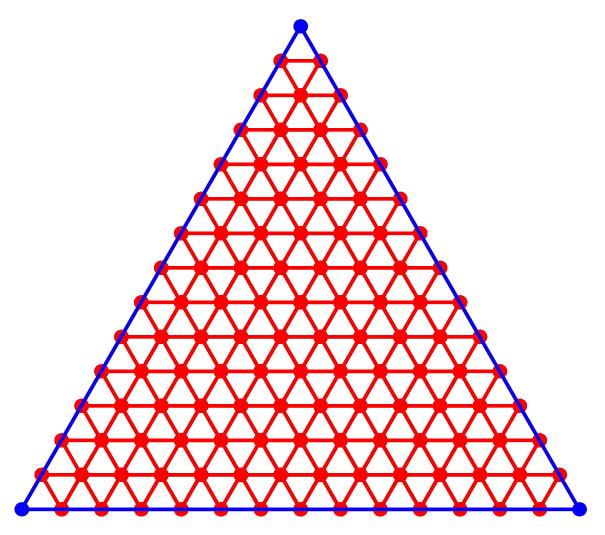


The Number 14

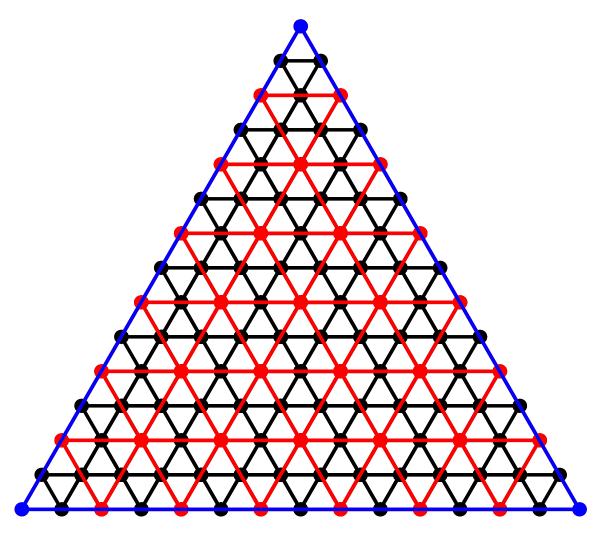
Product $14 = 14 \times 1$



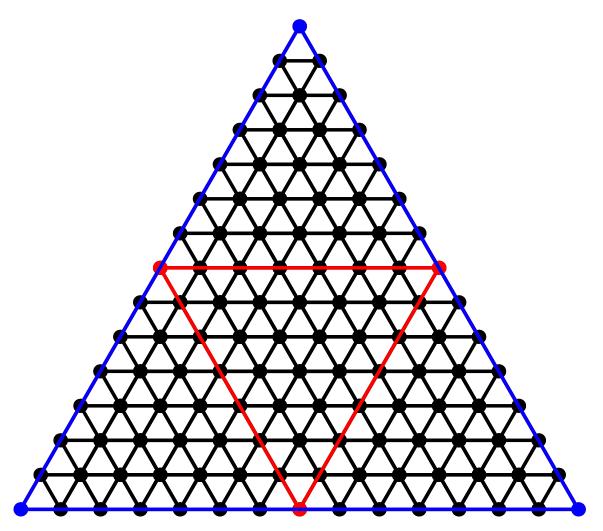
 $\textbf{Product} \ 14 = 1 \times 14$



Product $14 = 2 \times 7$

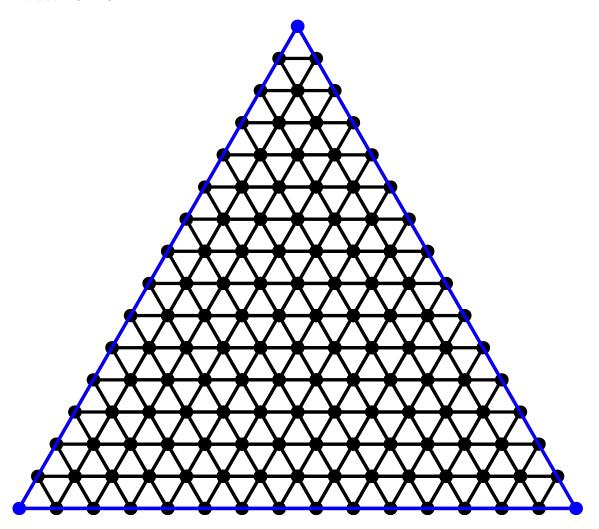


Product $14 = 7 \times 2$

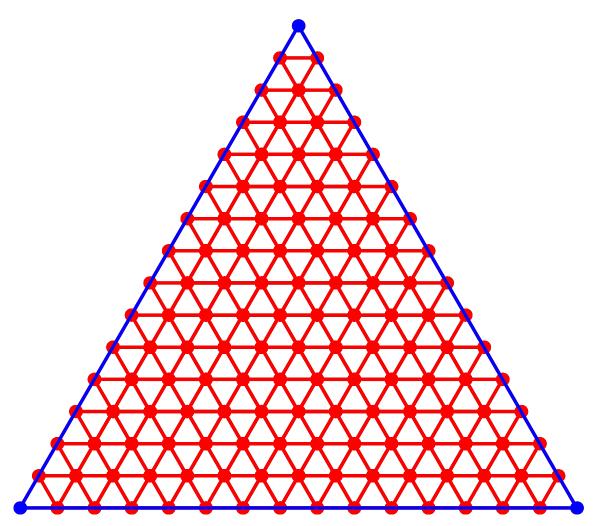


The Number 15

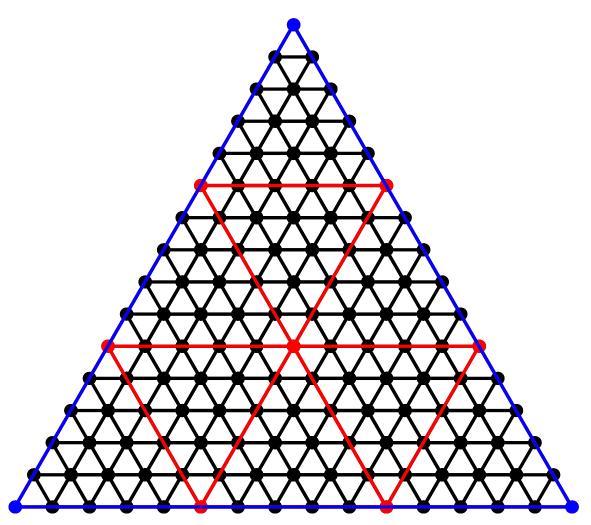
Product $15 = 15 \times 1$



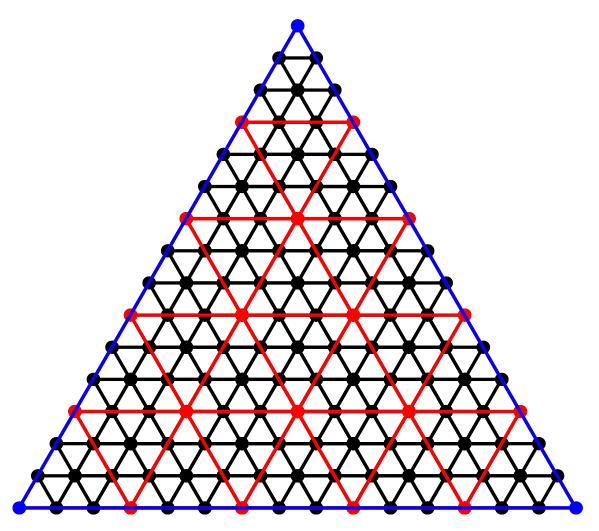
 $\textbf{Product} \ 15 = 1 \times 15$



Product $15 = 5 \times 3$

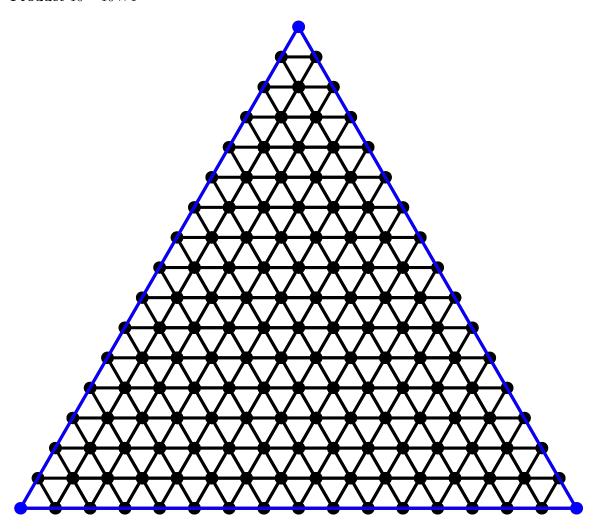


 $\textbf{Product}\ 15 = 3 \times 5$

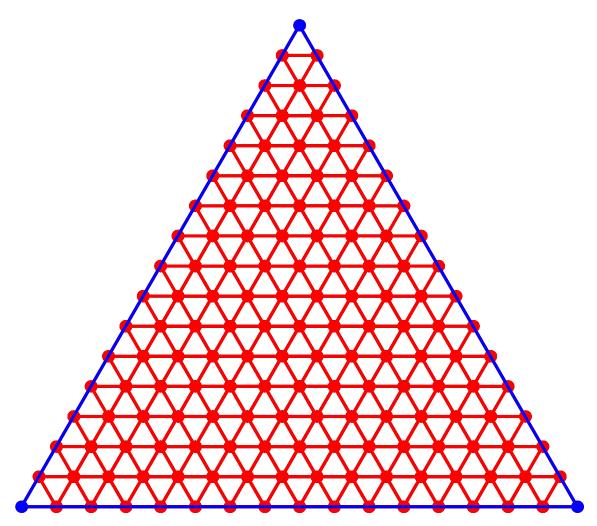


The Number 16

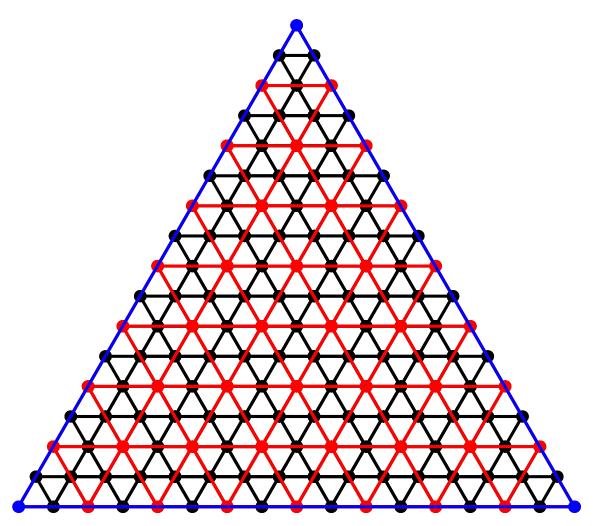
Product $16 = 16 \times 1$



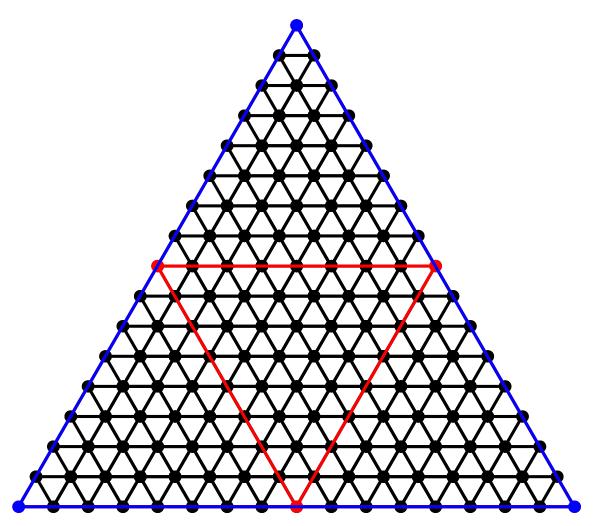
 $\textbf{Product} \ 16 = 1 \times 16$



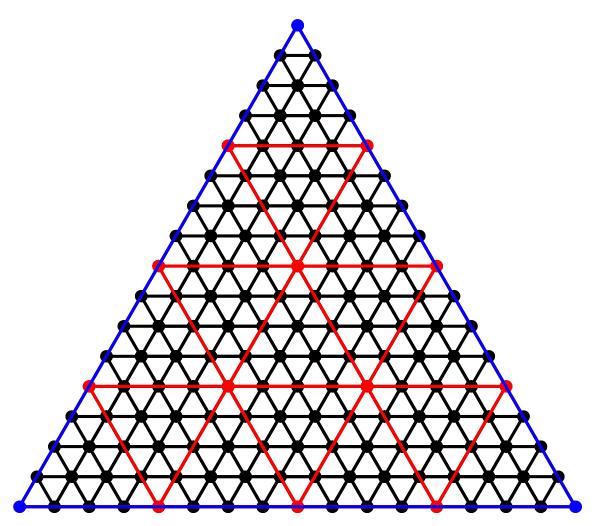
Product $16 = 2 \times 8$



Product $16 = 8 \times 2$

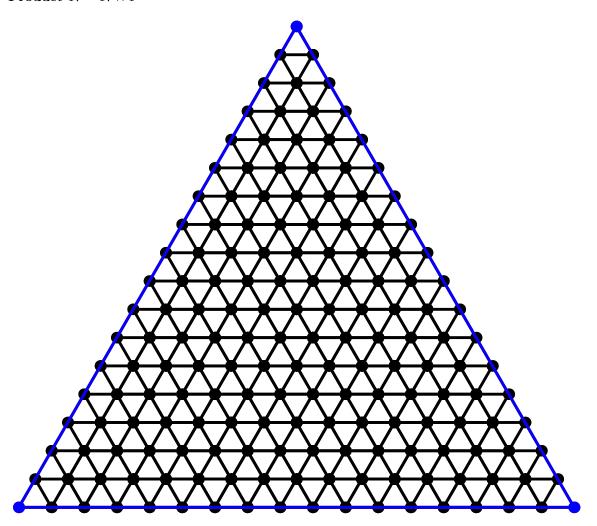


 $\textbf{Product}\ 16 = 4 \times 4$

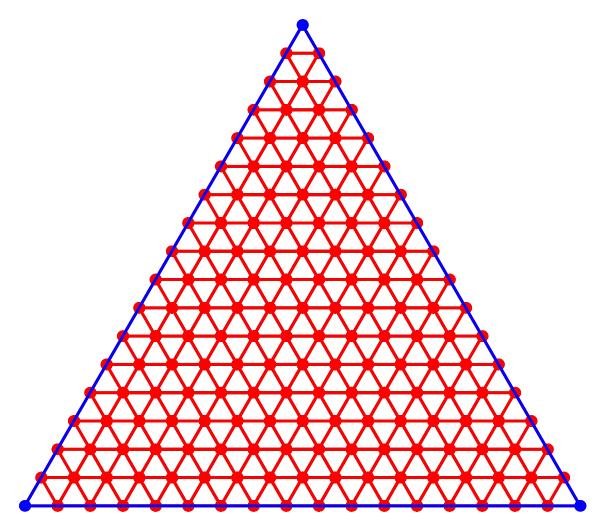


The Number 17

Product $17 = 17 \times 1$

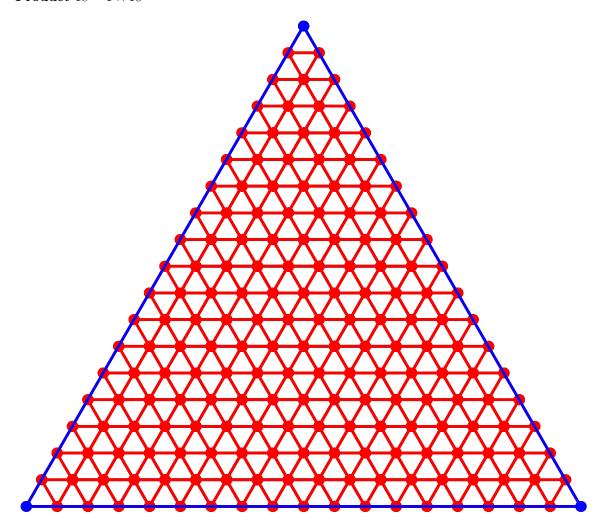


 $\textbf{Product}\ 17 = 1 \times 17$

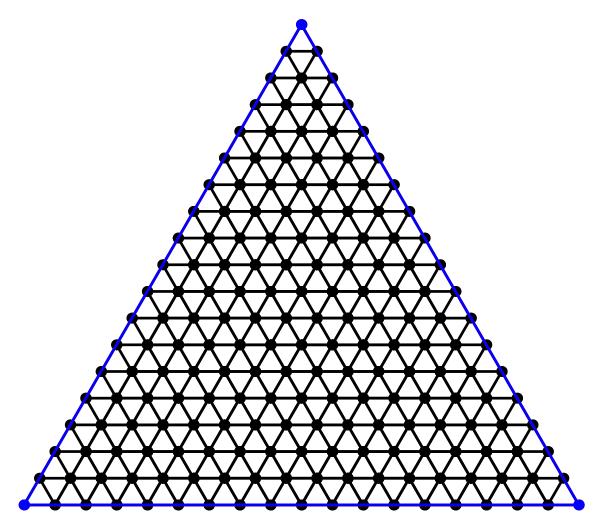


The Number 18

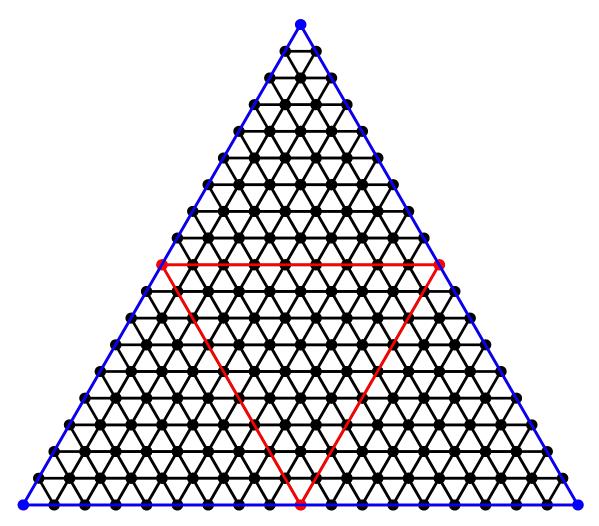
Product $18 = 1 \times 18$



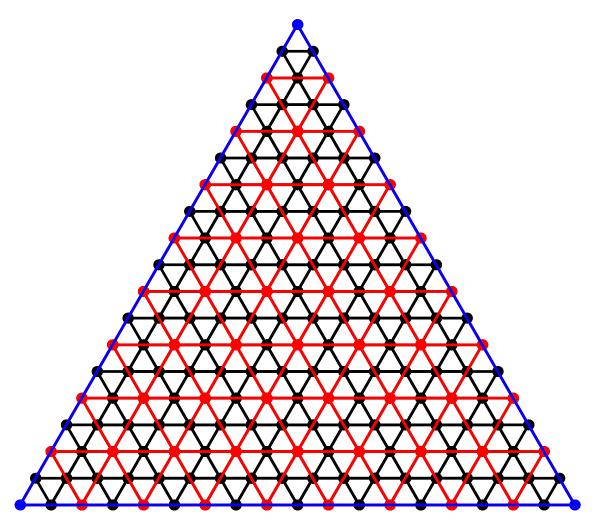
$\textbf{Product} \ 18 = 18 \times 1$



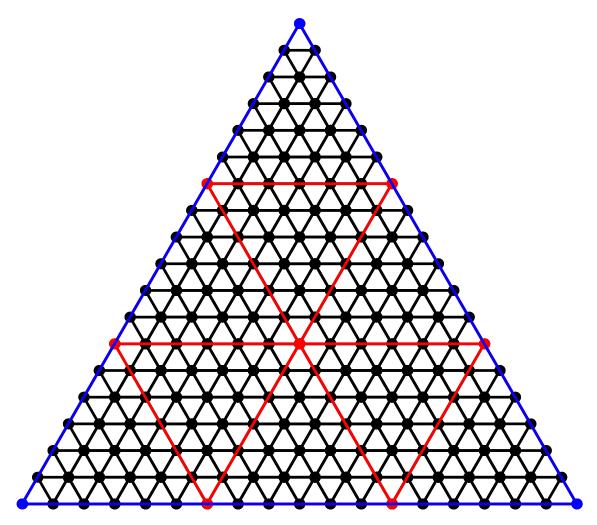
Product $18 = 9 \times 2$



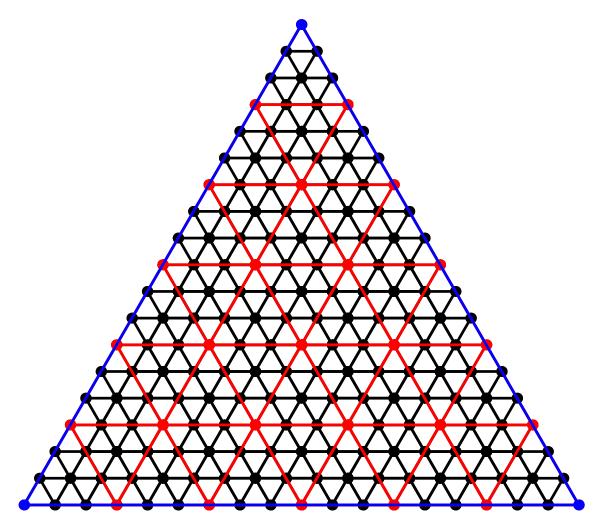
Product $18 = 2 \times 9$



Product $18 = 6 \times 3$

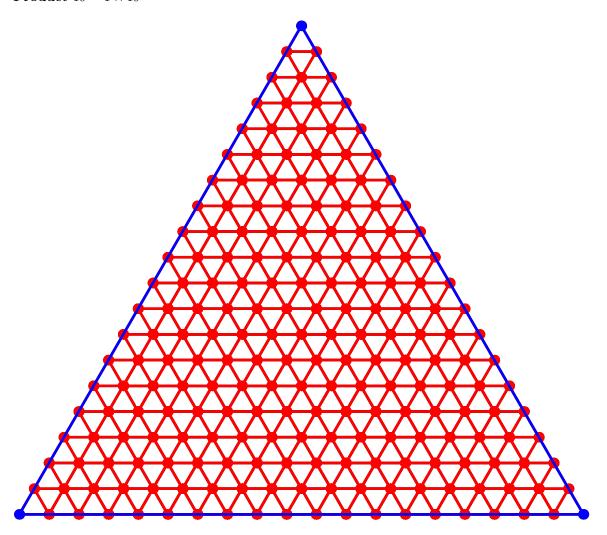


Product $18 = 3 \times 6$

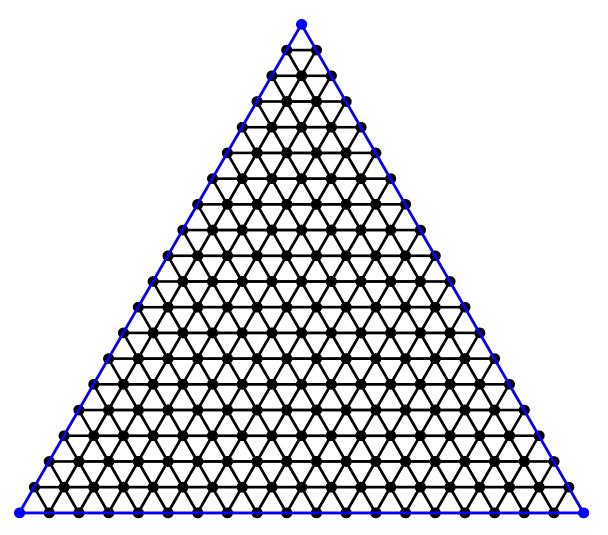


The Number 19

Product $19 = 1 \times 19$

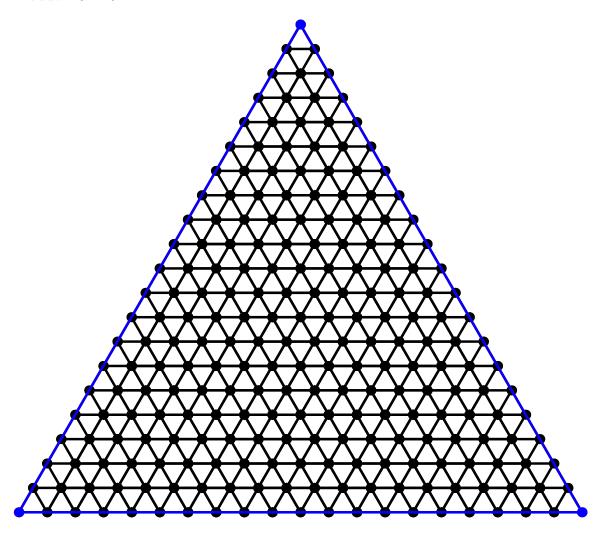


$\textbf{Product} \ 19 = 19 \times 1$

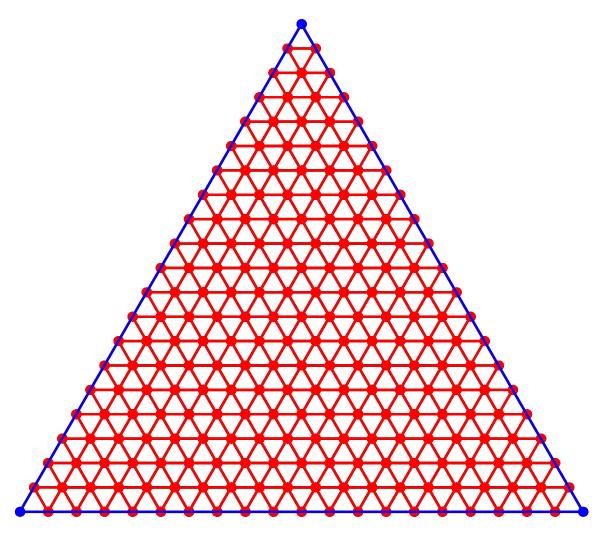


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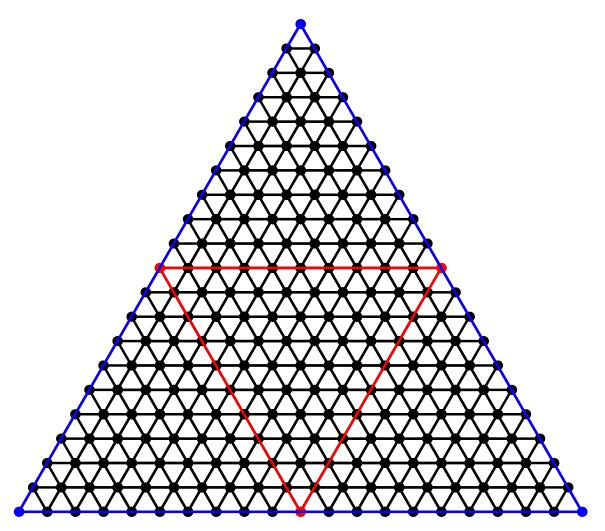
Product $20 = 20 \times 1$



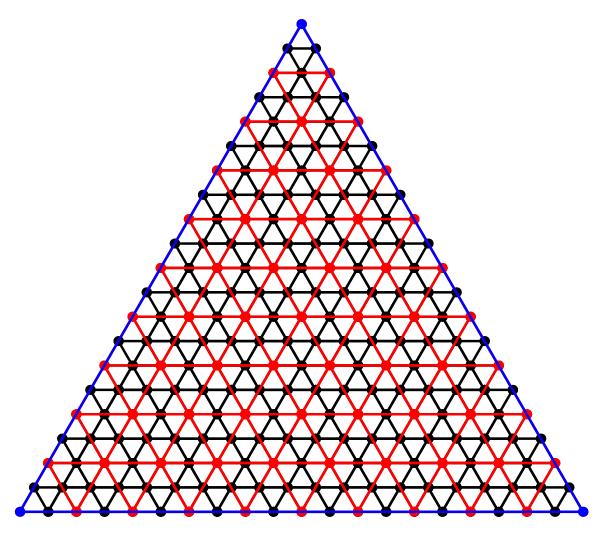
 $\textbf{Product} \ 20 = 1 \times 20$



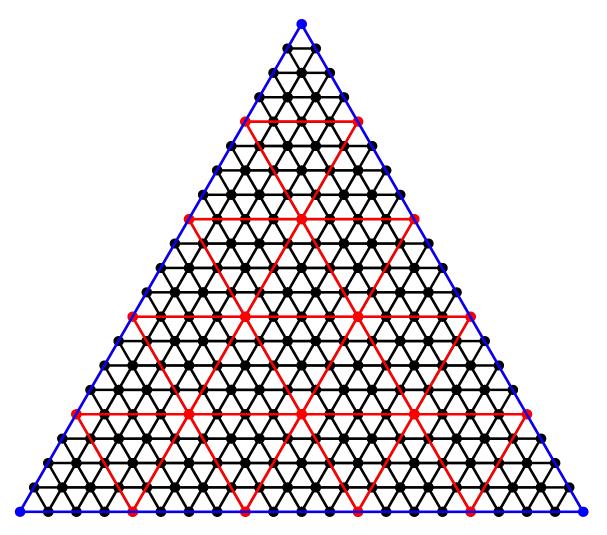
$\textbf{Product} \ 20 = 10 \times 2$



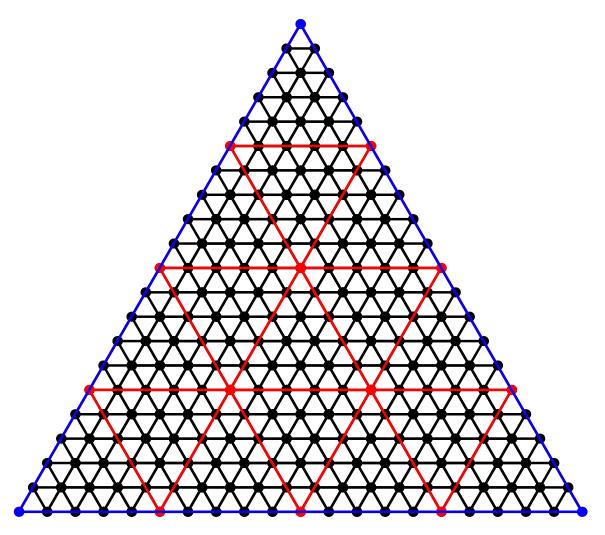
Product $20 = 2 \times 10$



 $\textbf{Product} \ 20 = 4 \times 5$

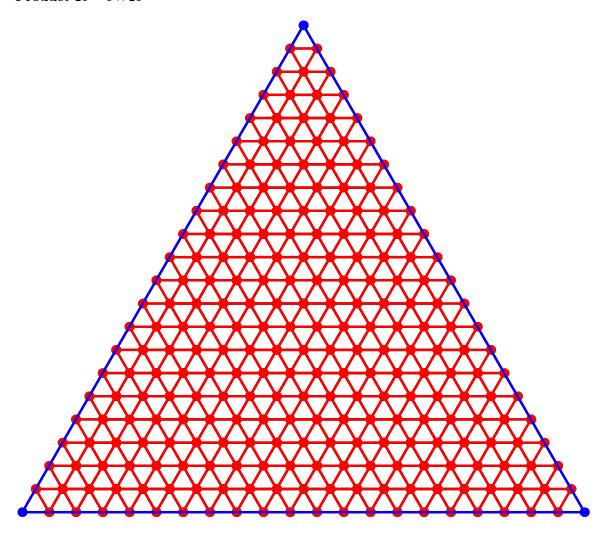


 $\textbf{Product} \ 20 = 5 \times 4$

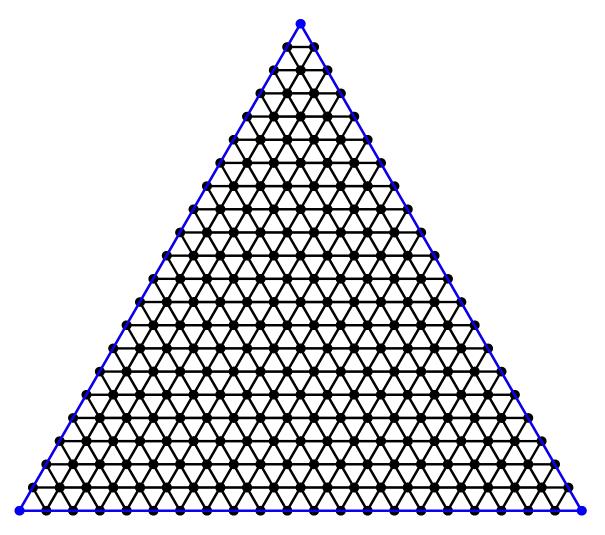


The Number 21

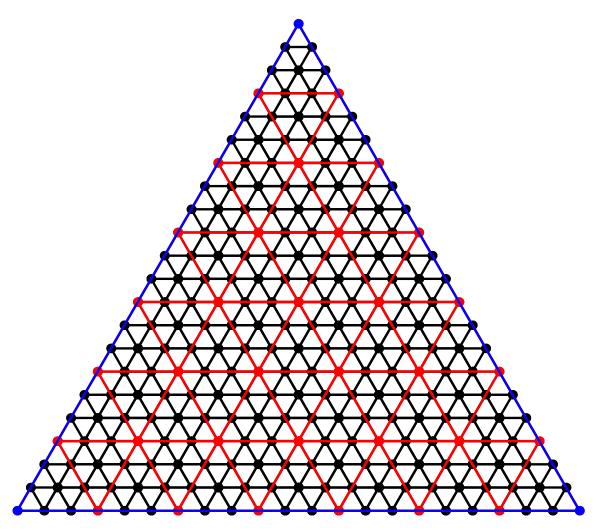
Product $21 = 1 \times 21$



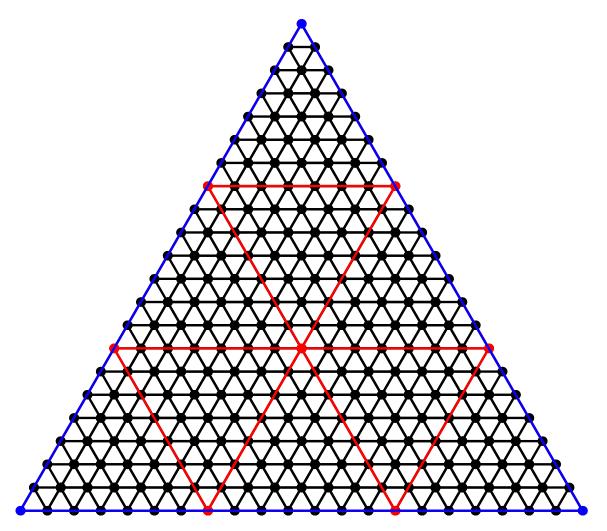
$\textbf{Product}\ 21 = 21 \times 1$



Product $21 = 3 \times 7$

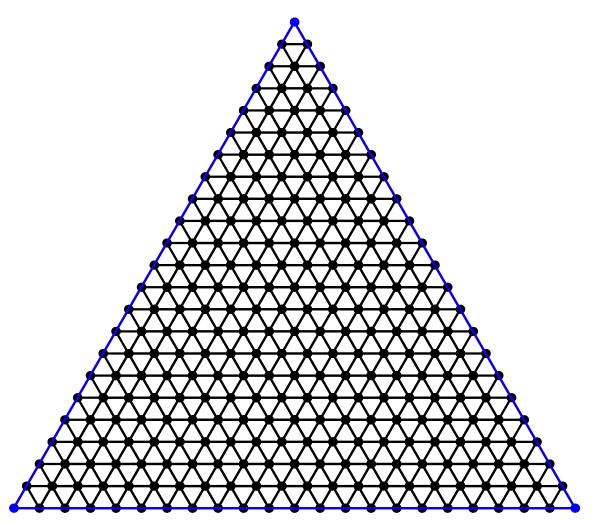


 $\textbf{Product}\ 21 = 7 \times 3$

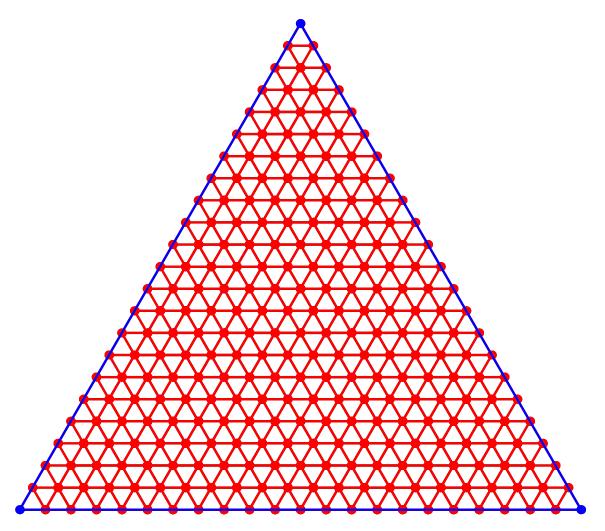


The Number 22

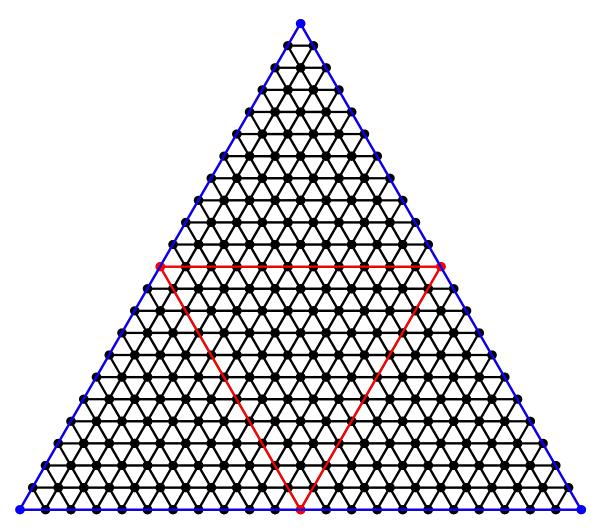
Product $22 = 22 \times 1$



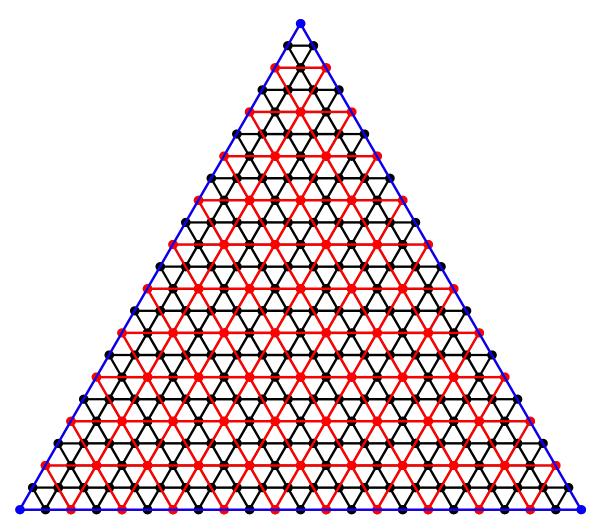
 $\textbf{Product}\ 22 = 1 \times 22$



$\textbf{Product}\ 22 = 11 \times 2$

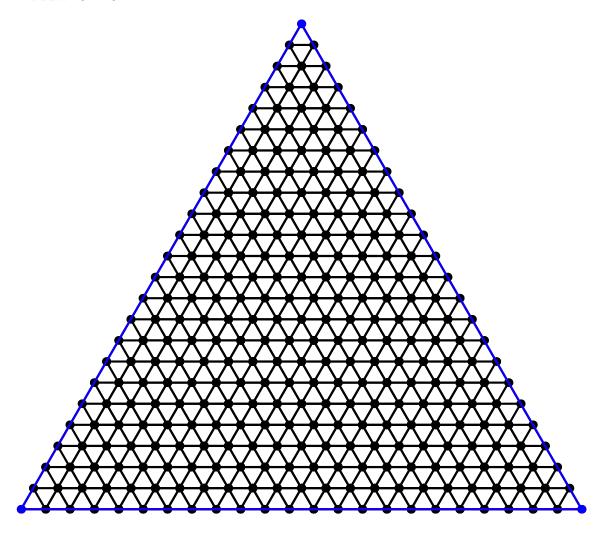


 $\textbf{Product}\ 22 = 2 \times 11$

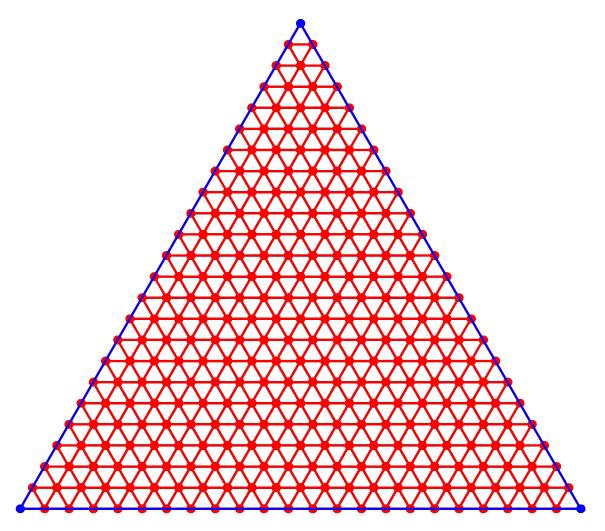


The Number 23

Product $23 = 23 \times 1$

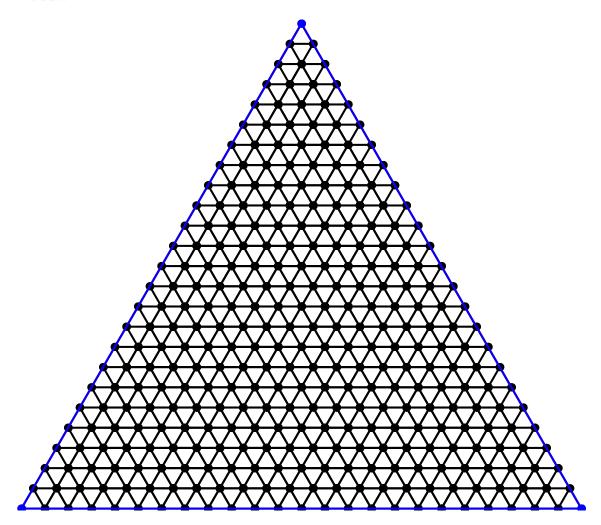


Product $23 = 1 \times 23$

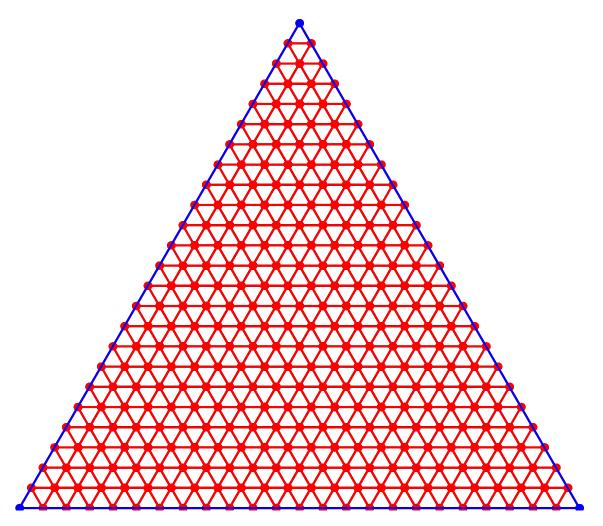


The Number 24

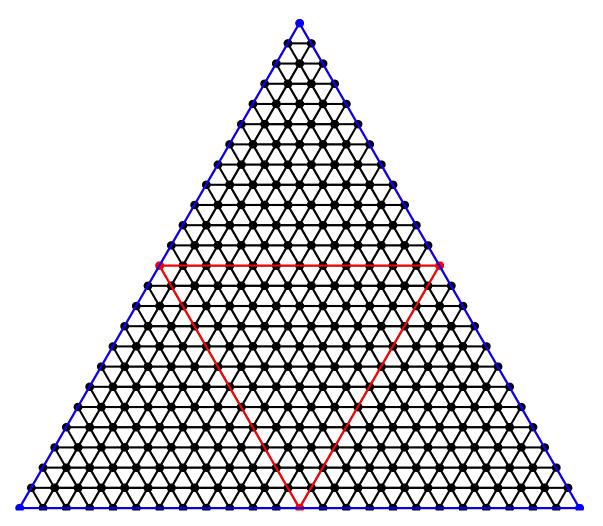
Product $24 = 24 \times 1$



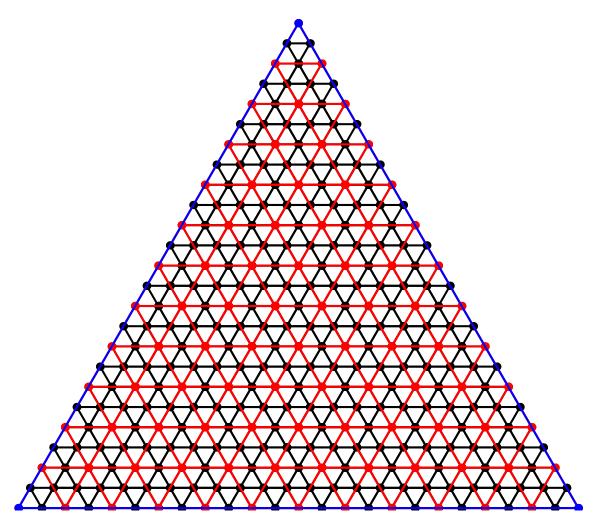
 $\textbf{Product} \ 24 = 1 \times 24$



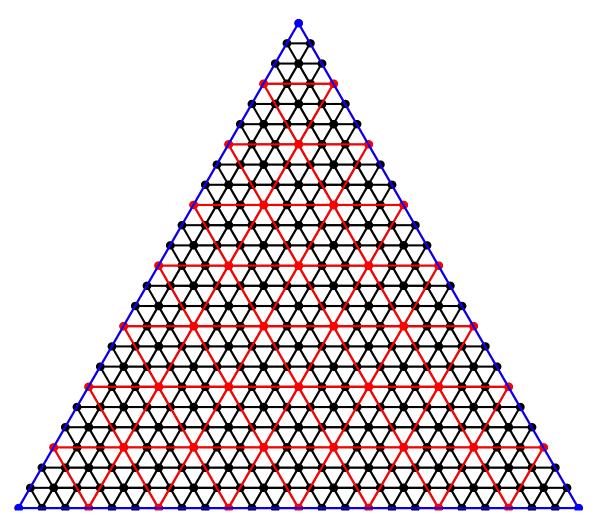
$\textbf{Product} \ 24 = 12 \times 2$



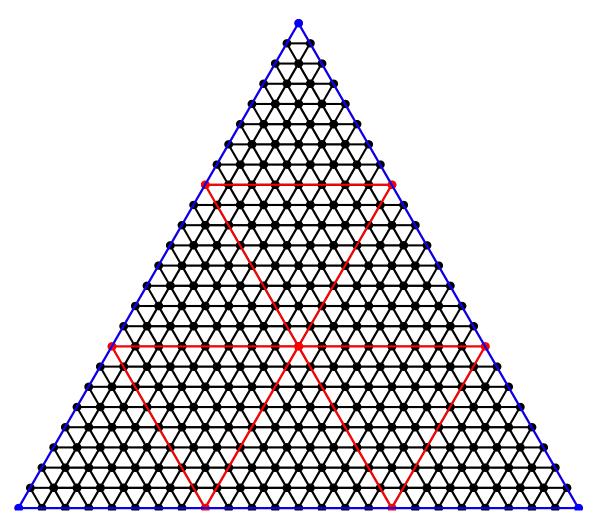
 $\textbf{Product} \ 24 = 2 \times 12$



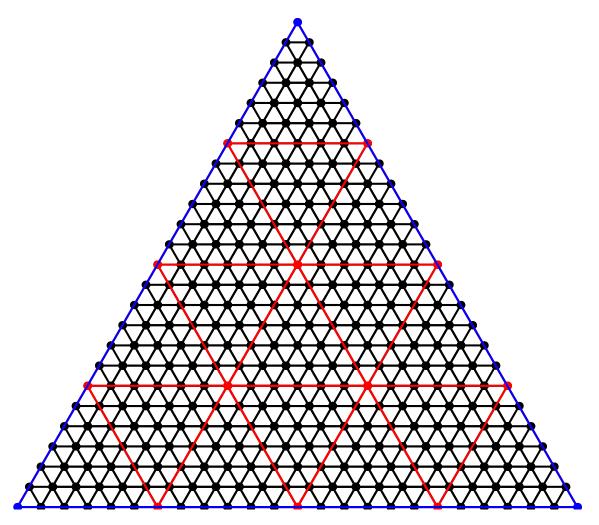
Product $24 = 3 \times 8$



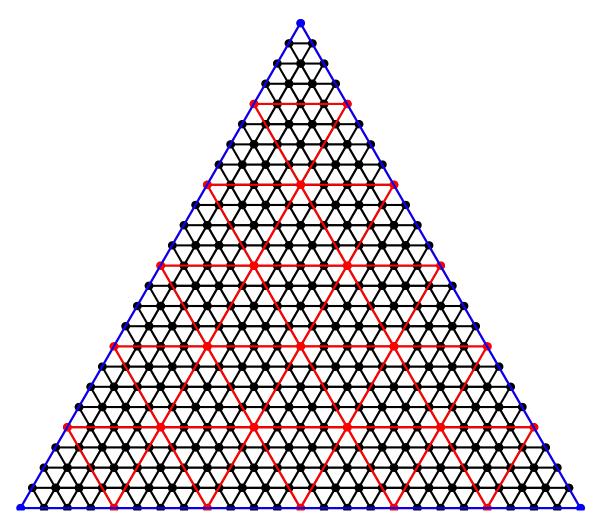
Product $24 = 8 \times 3$



Product $24 = 6 \times 4$



 $\textbf{Product}\ 24 = 4 \times 6$



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