# Arithmetic

#### Mac Radigan

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Arithmetic Preface

## Preface

for Ashton, Lyla, Neomi, Ruth, and Malakai

Arithmetic Copying

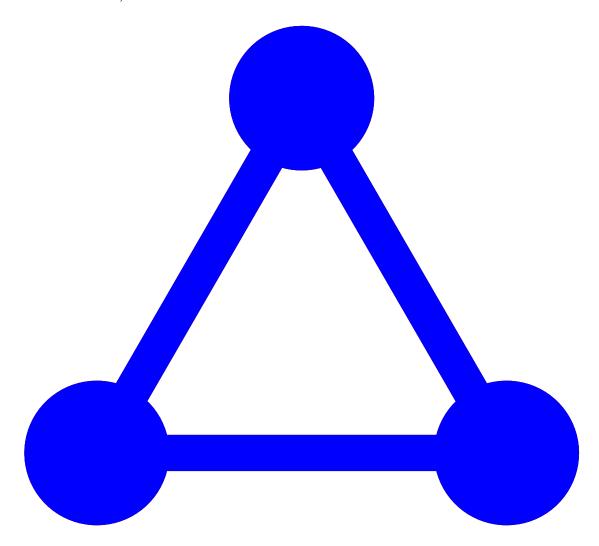
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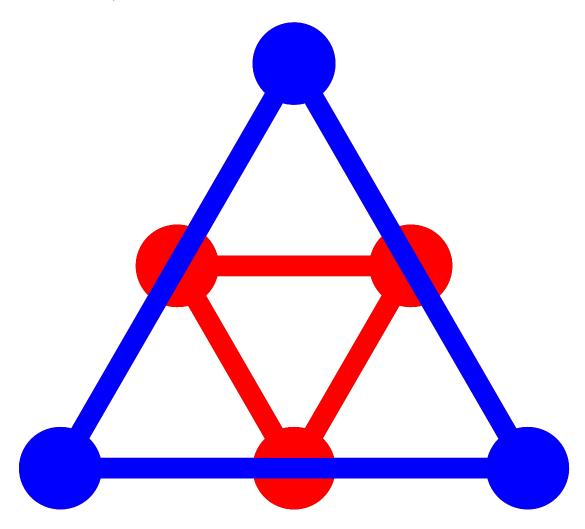
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Factor  $1 = 1 \times 1$ , factors 1-1



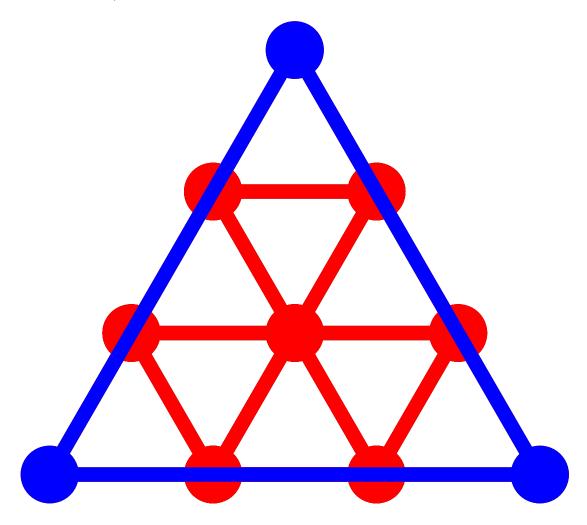
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Factor  $2 = 1 \times 2$ , factors 1-2



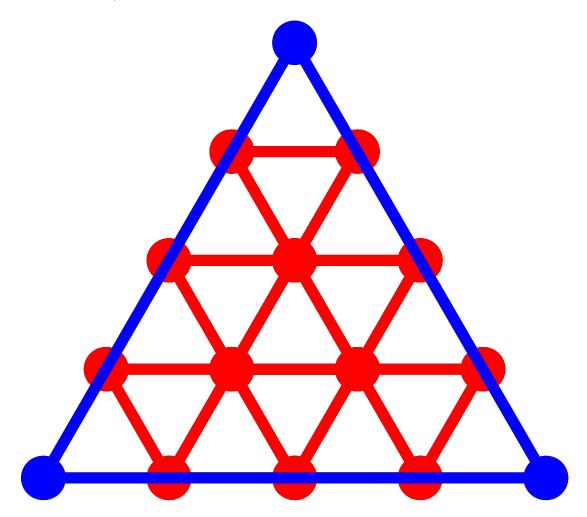
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Factor  $3 = 1 \times 3$ , factors 1-3

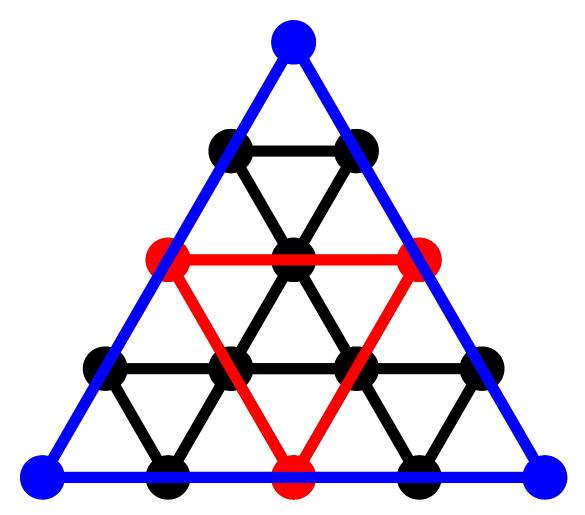


#### The Number 4

Factor  $4 = 1 \times 4$ , factors 1-4

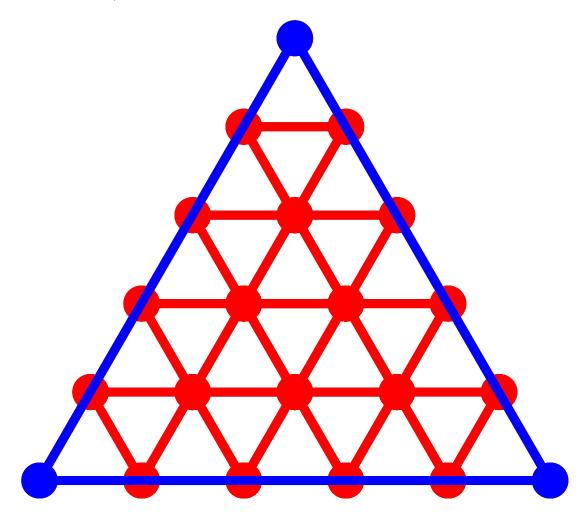


Factor  $4 = 2 \times 2$ , factors 2-2



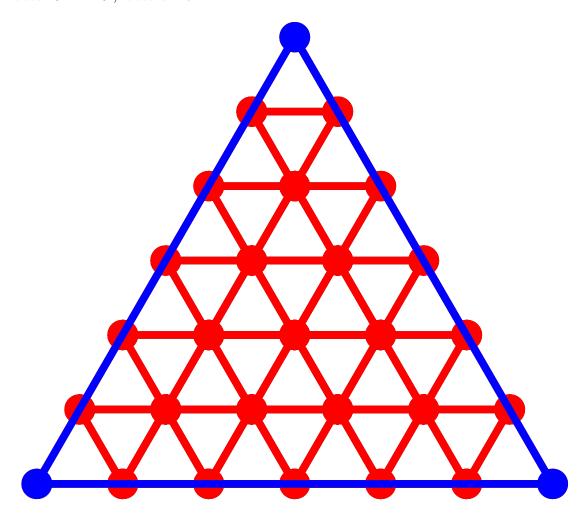
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Factor  $5 = 1 \times 5$  , factors 1-5

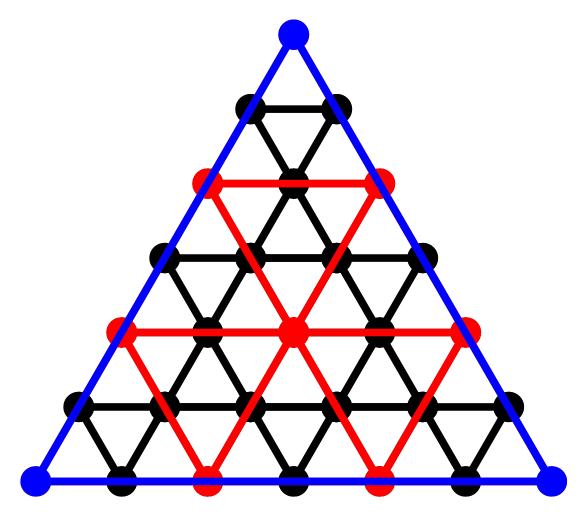


#### The Number 6

Factor  $6 = 1 \times 6$ , factors 1-6

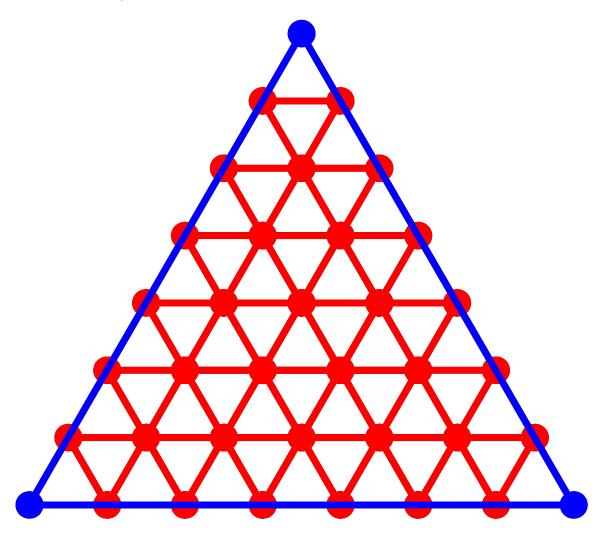


Factor  $6 = 2 \times 3$ , factors 2-3



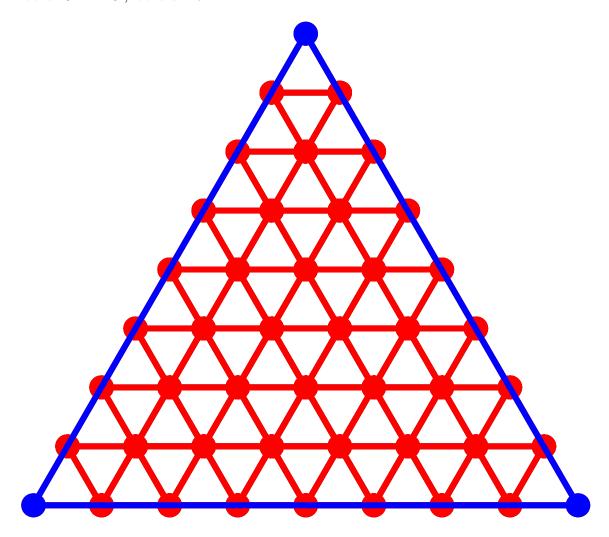
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Factor  $7 = 1 \times 7$ , factors 1-7

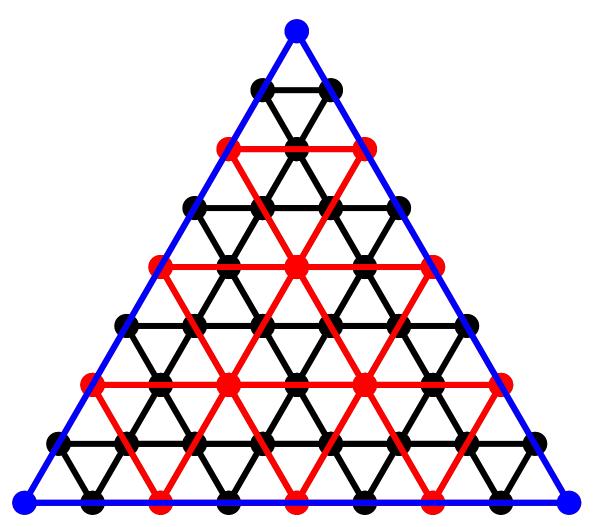


#### The Number 8

Factor  $8 = 1 \times 8$ , factors 1-8

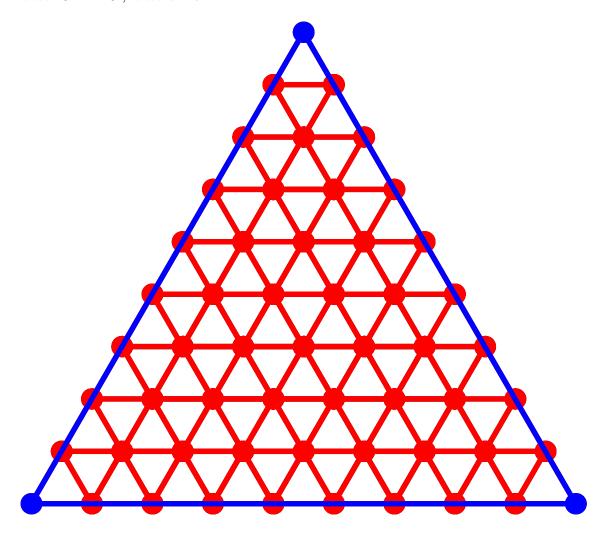


Factor  $8 = 2 \times 4$ , factors 2-4

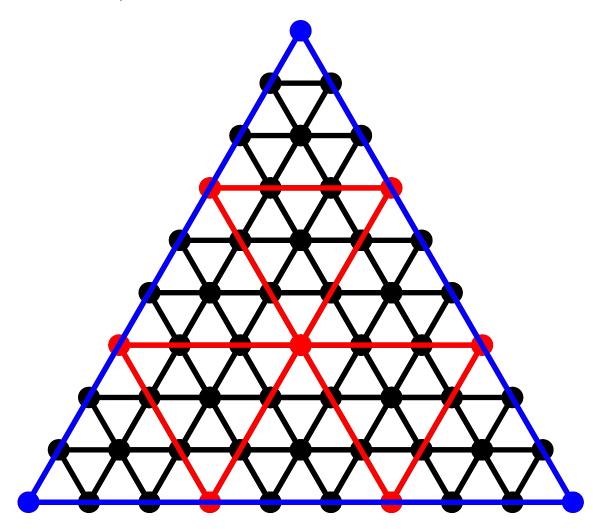


#### The Number 9

Factor  $9 = 1 \times 9$ , factors 1-9

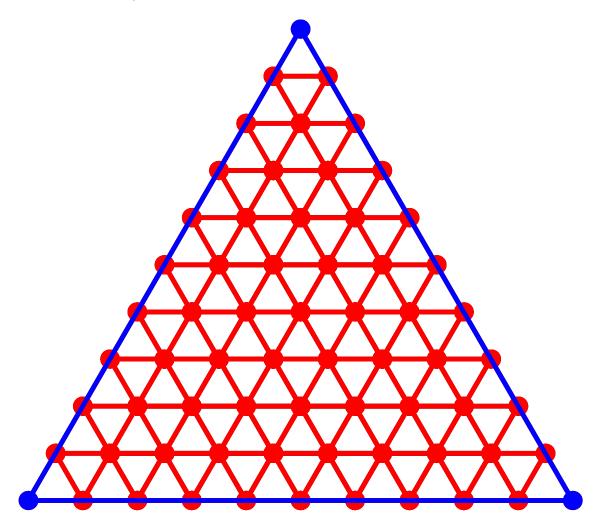


Factor  $9 = 3 \times 3$ , factors 3-3

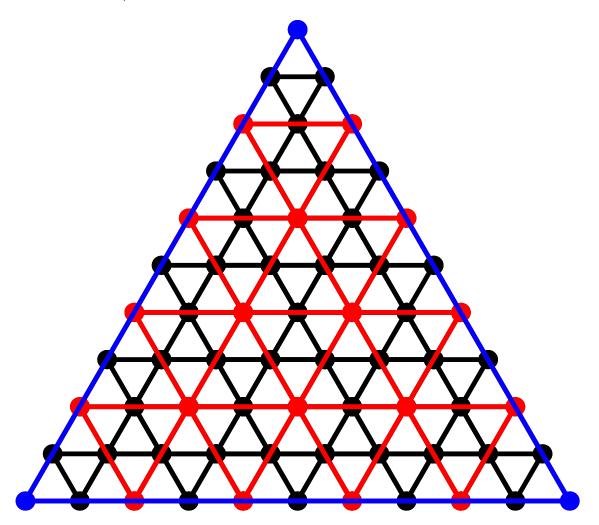


#### The Number 10

Factor  $10 = 1 \times 10$ , factors 1-10

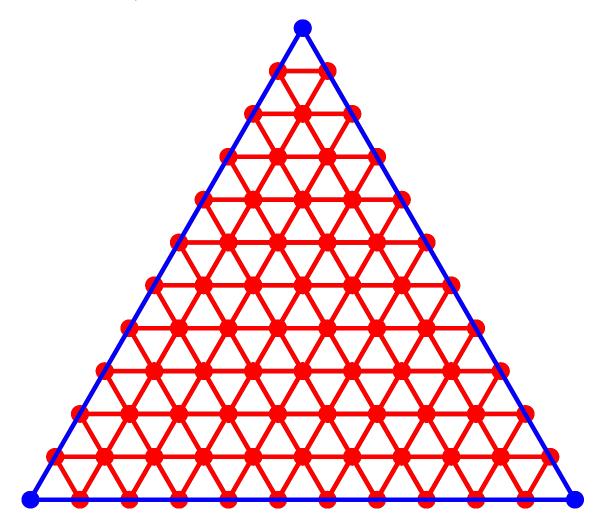


Factor  $10 = 2 \times 5$ , factors 2-5



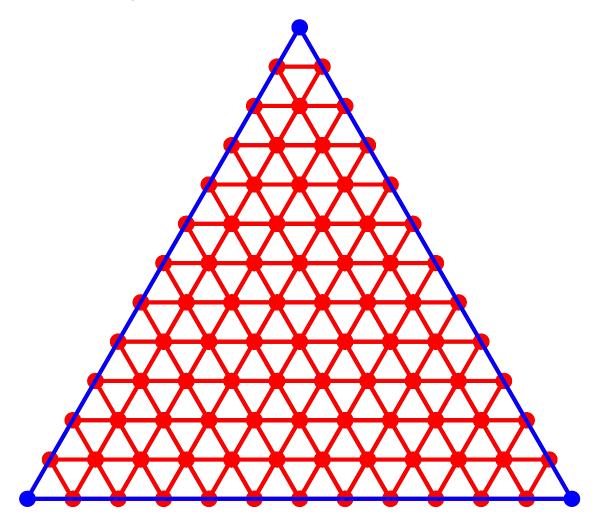
#### The Number 11

Factor  $11 = 1 \times 11$ , factors 1-11

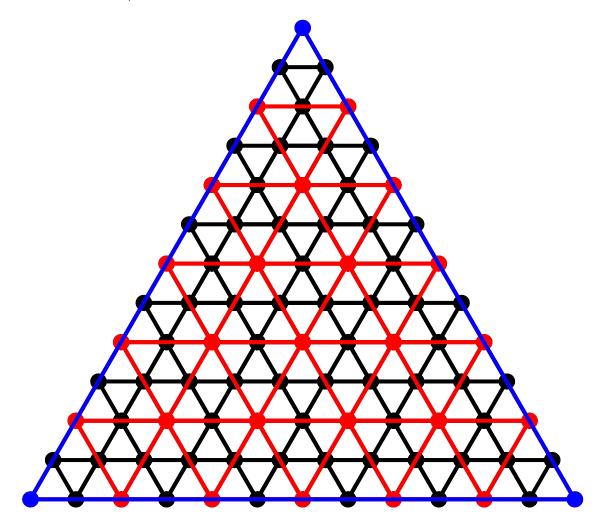


#### The Number 12

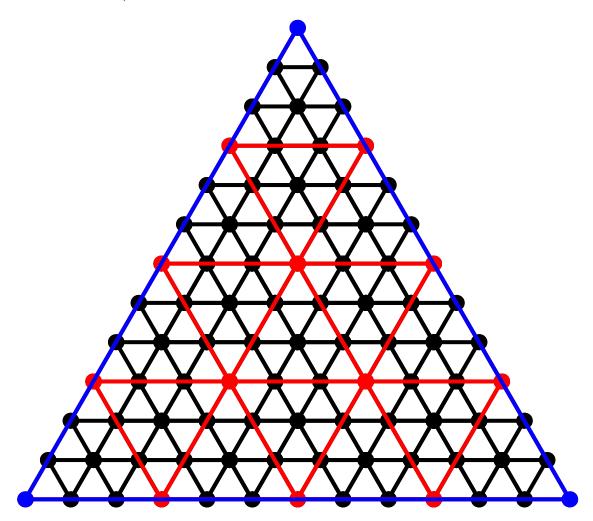
Factor  $12 = 1 \times 12$ , factors 1-12



Factor  $12 = 2 \times 6$ , factors 2-6

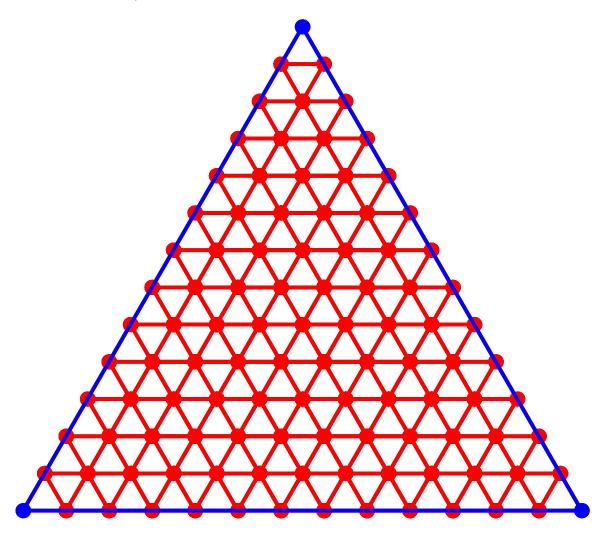


Factor  $12 = 3 \times 4$ , factors 3-4



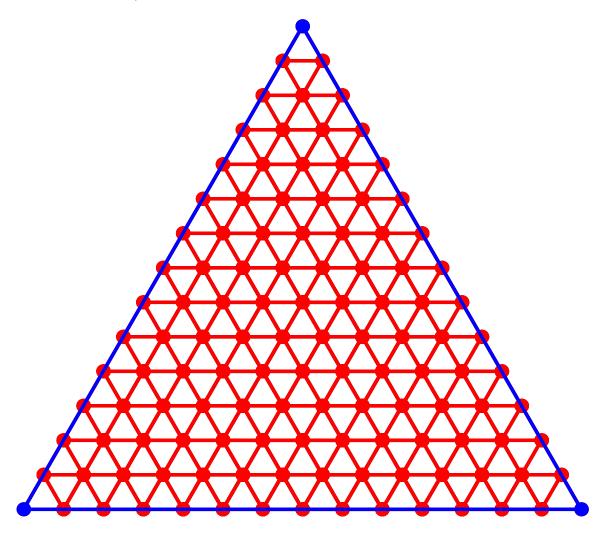
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Factor  $13 = 1 \times 13$ , factors 1-13

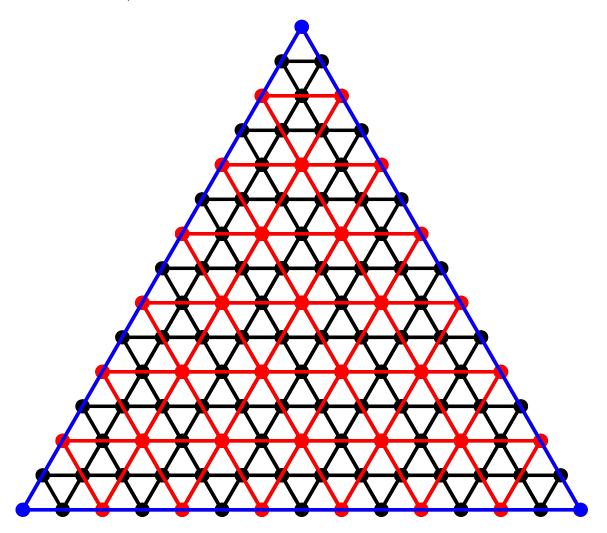


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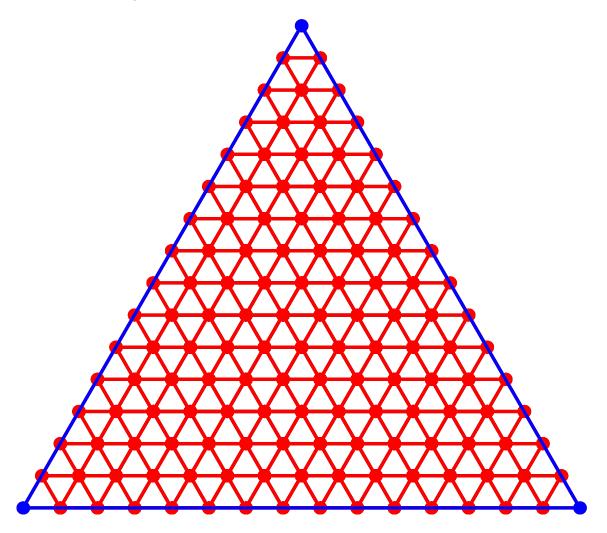


Factor  $14 = 2 \times 7$ , factors 2-7

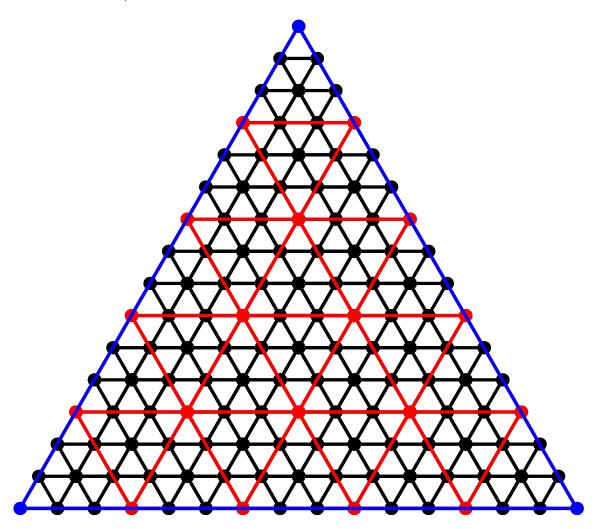


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Factor  $15 = 1 \times 15$ , factors 1-15

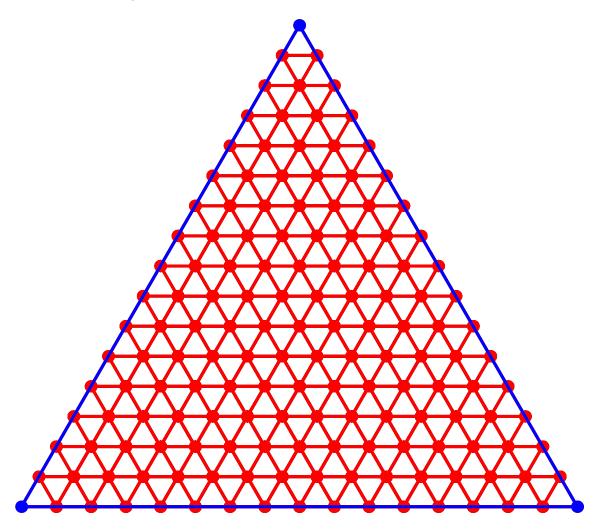


Factor  $15 = 3 \times 5$ , factors 3-5

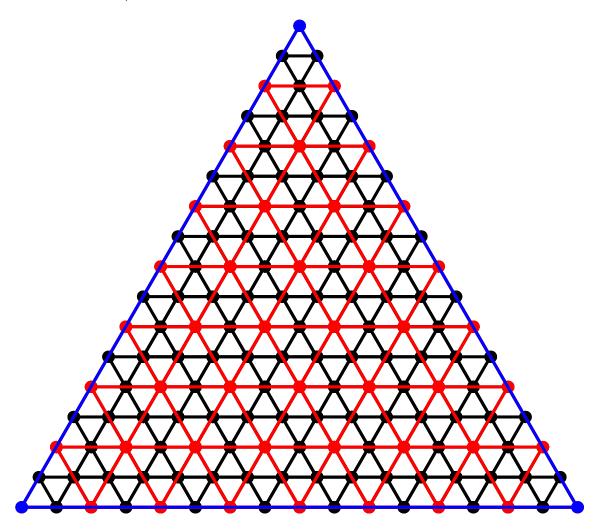


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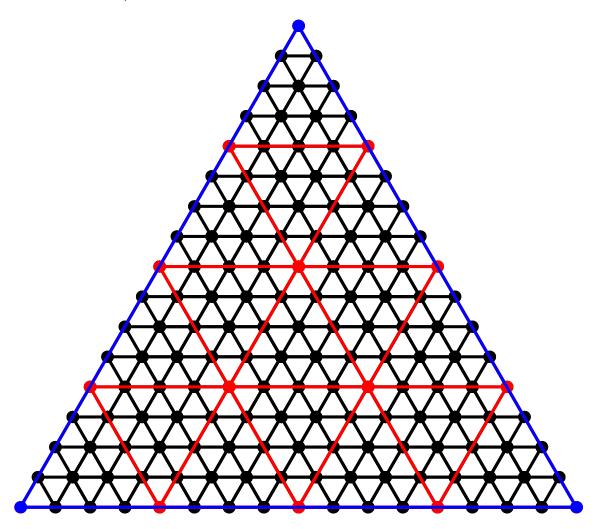
Factor  $16 = 1 \times 16$ , factors 1-16



Factor  $16 = 2 \times 8$ , factors 2-8

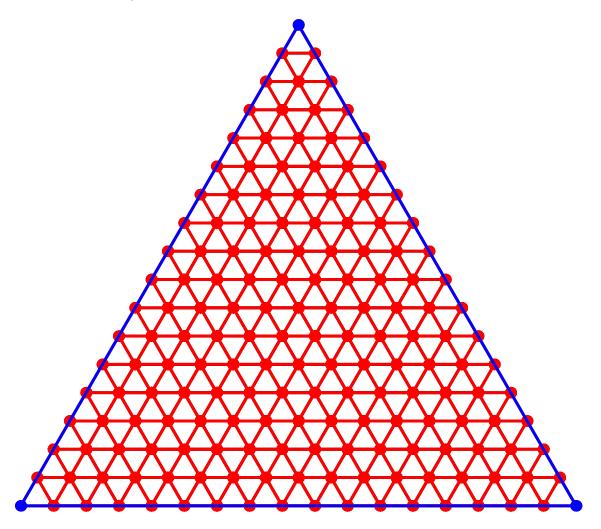


Factor  $16 = 4 \times 4$ , factors 4-4



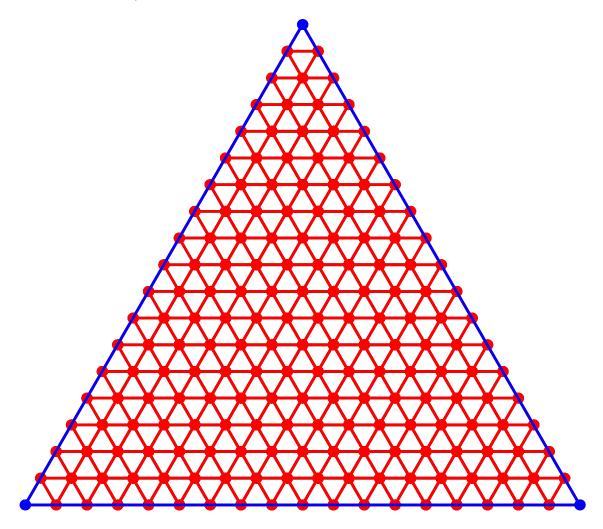
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Factor  $17 = 1 \times 17$ , factors 1-17

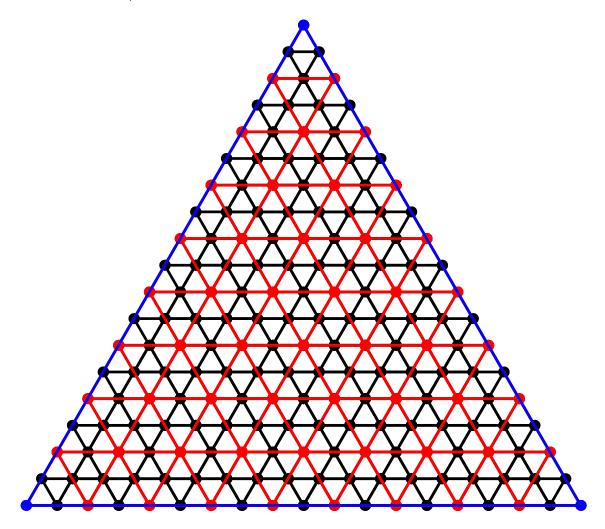


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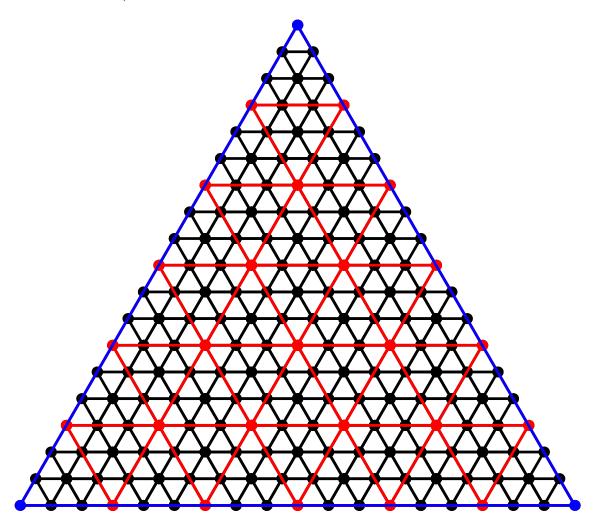
Factor  $18 = 1 \times 18$ , factors 1-18



Factor  $18 = 2 \times 9$ , factors 2-9

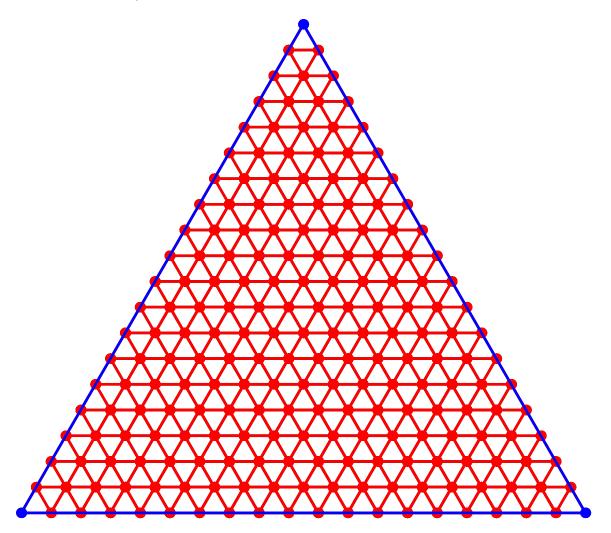


Factor  $18 = 3 \times 6$ , factors 3-6



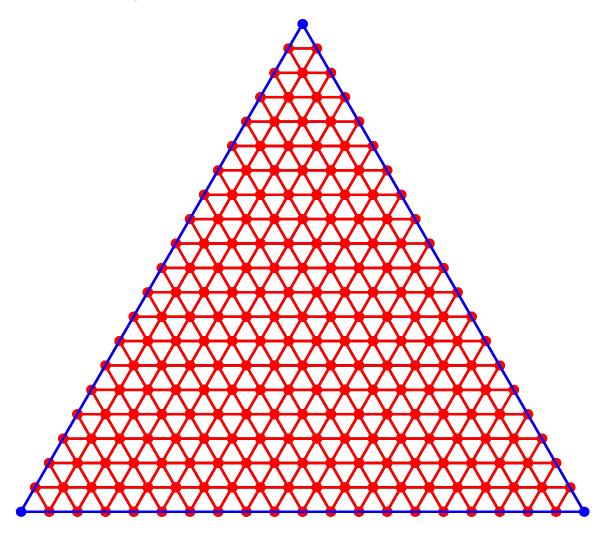
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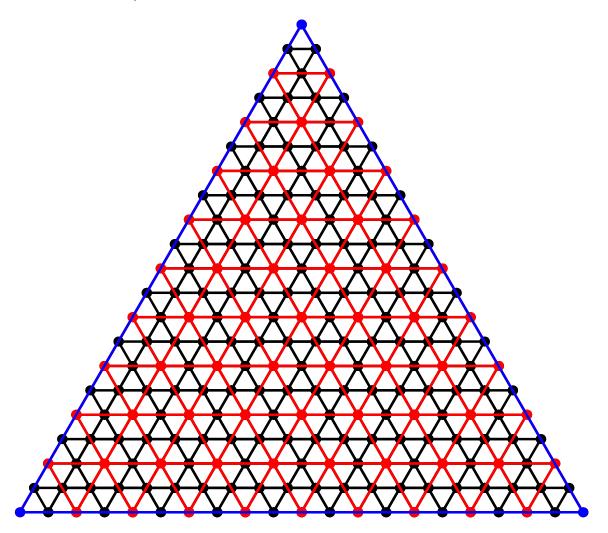


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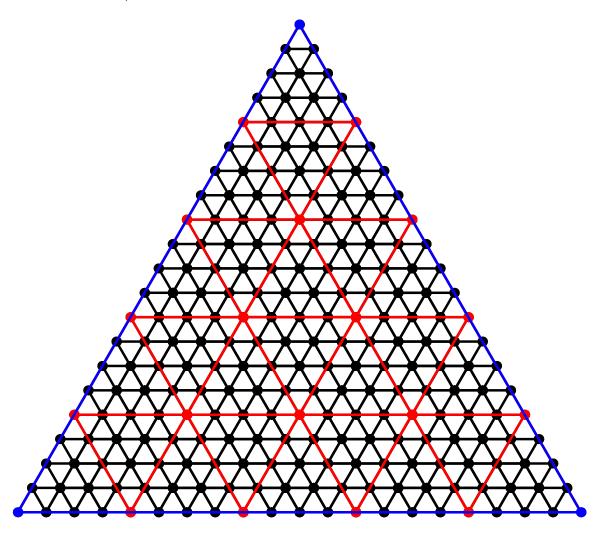
Factor  $20 = 1 \times 20$ , factors 1-20



Factor  $20 = 2 \times 10$ , factors 2-10

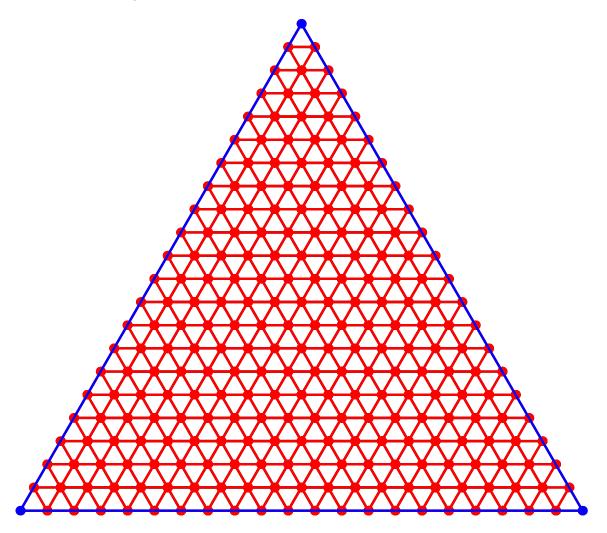


Factor  $20 = 4 \times 5$ , factors 4-5

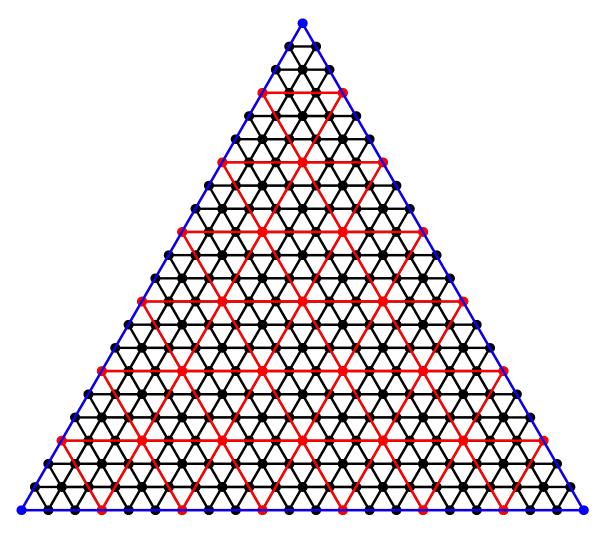


## The Number 21

Factor  $21 = 1 \times 21$ , factors 1-21

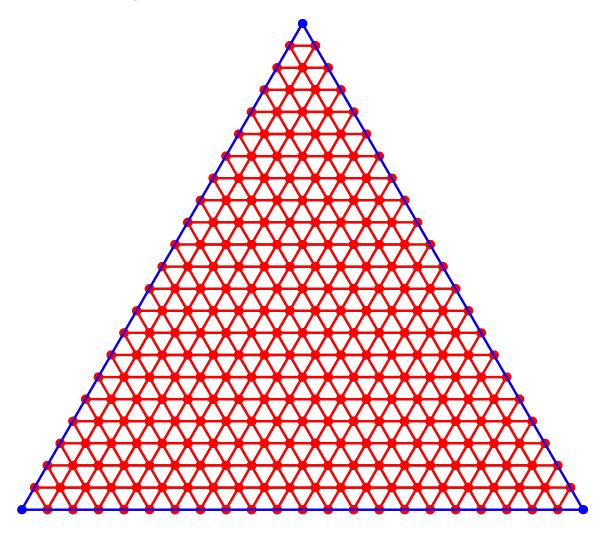


Factor  $21 = 3 \times 7$ , factors 3-7

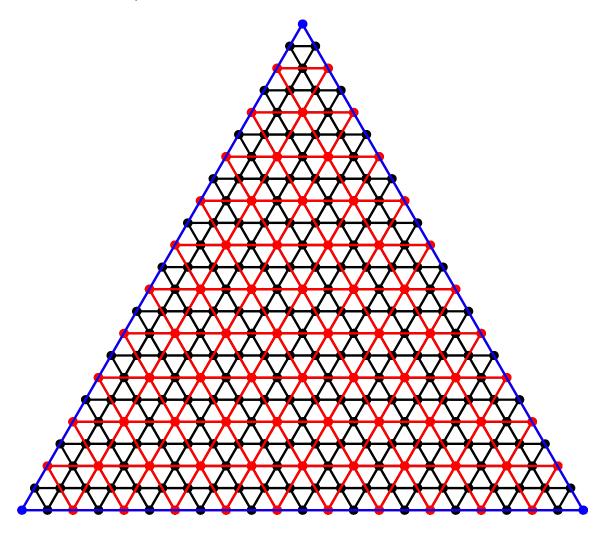


## The Number 22

Factor  $22 = 1 \times 22$ , factors 1-22

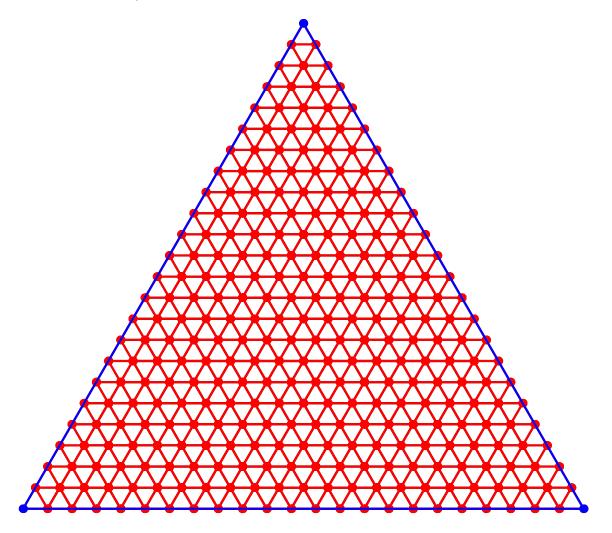


Factor  $22 = 2 \times 11$ , factors 2-11



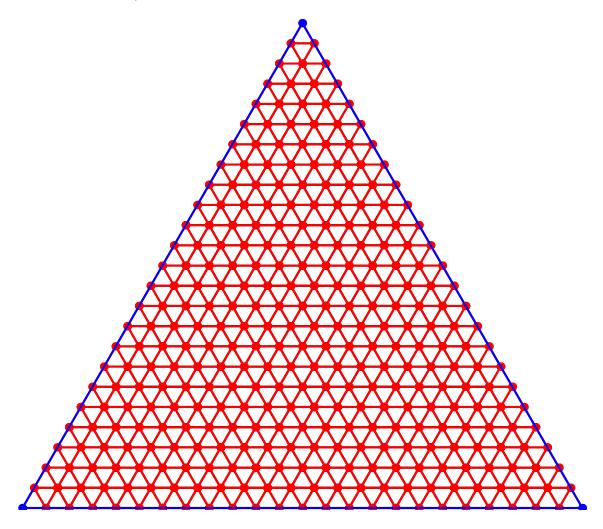
## The Number 23

Factor  $23 = 1 \times 23$ , factors 1-23

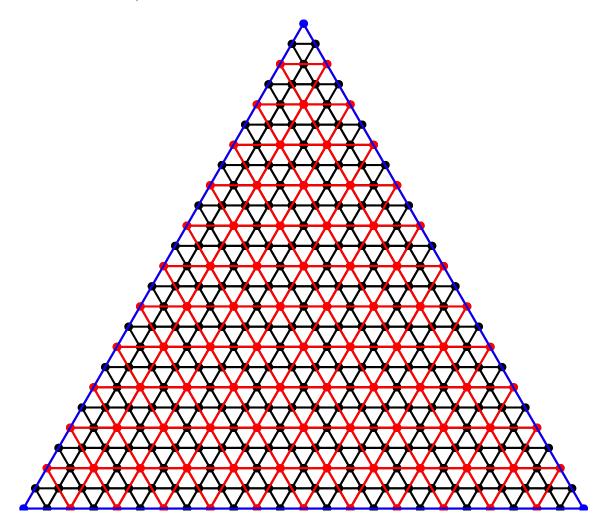


## The Number 24

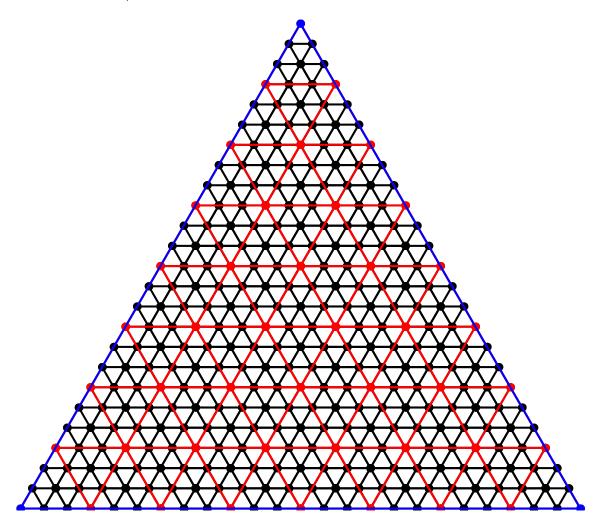
Factor  $24 = 1 \times 24$ , factors 1-24



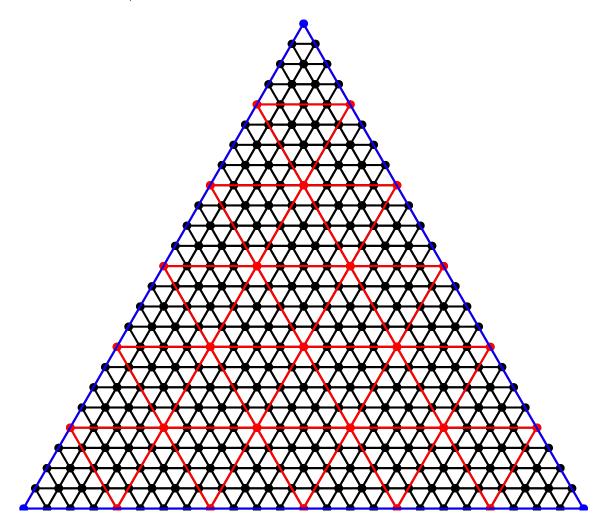
Factor  $24 = 2 \times 12$ , factors **2-12** 



Factor  $24 = 3 \times 8$ , factors 3-8



Factor  $24 = 4 \times 6$ , factors 4-6



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