Convex Optimization notes

Mac Radigan

Convex Optimization

Infeasible Start Newton Method

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Algorithm 1 Infeasible Start Newton Method
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\begin{aligned} & \textbf{given} x \in f, \nu, \epsilon < 0, \alpha \in \left(0, \frac{1}{2}\right), \beta \in (0, 1) \\ & \textbf{repeat} \\ & 1. \text{ compute primal and dual Newton steps } \Delta x_{NT} \text{ and } \Delta \nu_{NT} \\ & 2. \text{ backtracking line search on } \|r\|_2 \\ & t := 1 \\ & \textbf{while } \|r\left(x + t\Delta x_{NT}, \nu + t\Delta \nu_{NT}\right)\|_2 > (1 - \alpha t) \|r\left(x, \nu\right)\|_2 \  \, \textbf{do} \\ & t := \beta t \\ & \textbf{end while} \\ & 3. \text{ update } x := x + t\Delta x_{NT} \text{ and } \nu := \nu + t\Delta \nu_{NT} \\ & \textbf{until } Ax = b \textbf{and } \|r\left(x, \nu\right)\| \leq \epsilon \end{aligned}
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