

Assignment 4

Prove or disprove that the given solution is correct in each of the problems 1-6 below.

1. p. 69, problem 1a
2. p. 73, problem 1a
3. p. 81, problem 3
4. p. 81, problem 4
5. p. 81, problem 6
6. p. 87, problem 4a
7. In the vector space  $L(R^2)$ , let  $T$  be the transformation defined by

$$T \begin{pmatrix} a & b \\ c & d \end{pmatrix} = \begin{pmatrix} a & b \\ c - 3a & d - 3b \end{pmatrix}$$

- a. Is  $T$  linear?
- b. Does there exist a 2x2 matrix  $A$  such that  $AB = T(B)$  for all 2x2 matrices  $B$ ?
- c. Does there exist a 2x2 matrix  $A$  such that  $BA = T(B)$  for all 2x2 matrices  $B$ ?
8. p. 88, problem 6(a).
9. p. 97, problem 3 for  $n=2$ .
10. p. 97, problem 4 for  $n=2$ .