

# Math 122B Homework 1

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## 1 Problem 1

Let  $P(z)$  denote a polynomial of degree  $d \geq 1$ . Define

$$M(r) = \sup_{|z|=r} |P(z)|, \quad r > 0$$

Show that both functions

$$r \mapsto M(r), \quad r \mapsto -r^{-d}M(r)$$

are strictly increasing

**Proof.**

□

## 2 Problem 2

Compute the integral

$$\int_{|z|=3} \sin\left(\frac{1}{z}\right) dz$$

**Proof.**

□

## 3 Problem 3

(Correct statement). Let  $n$  be a positive integer and let  $f(z)$  be an entire function satisfying the inequality  $|f(z)| > |z|^n$ , for  $|z| > 1$ . Prove that  $f$  is a polynomial

**Proof.**

□