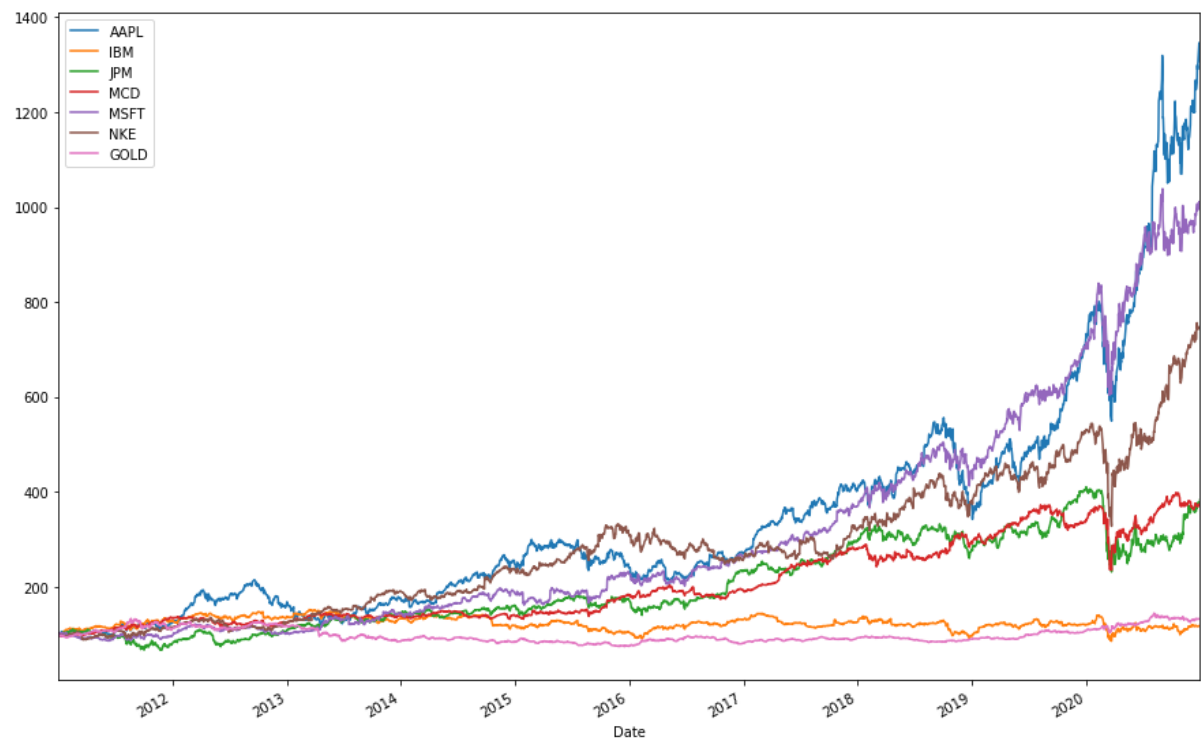
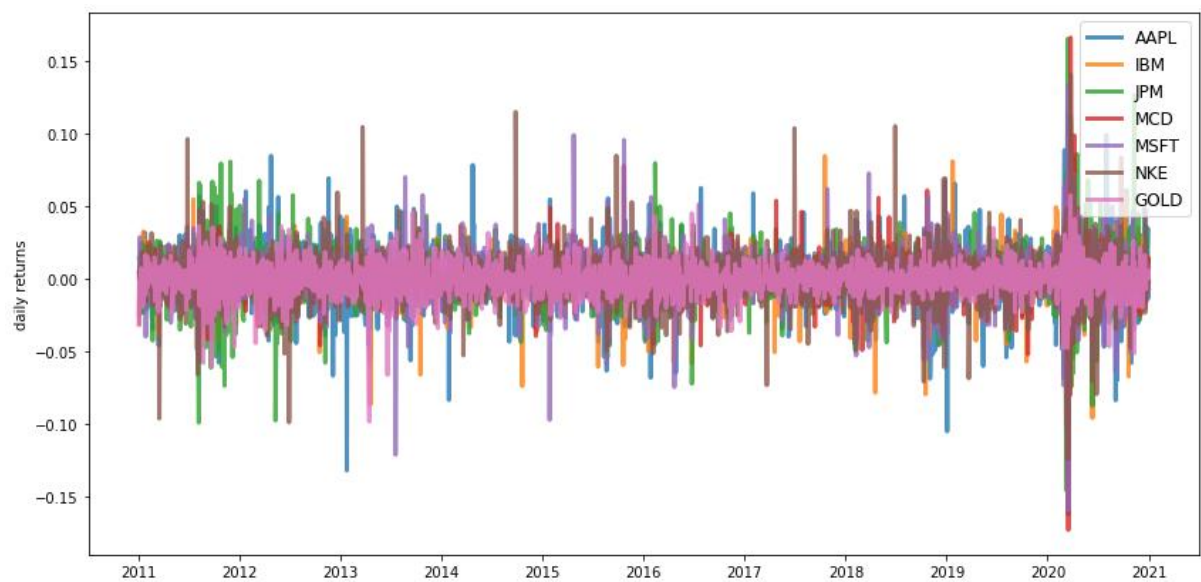


## Monte Carlo optimization

### Plot prices



### Plot returns



### Check metrics

Means:

AAPL 0.257426

IBM 0.016836

JPM 0.134468

MCD 0.132283

MSFT 0.230606

NKE 0.200816

GOLD 0.028618

Covariance:

	AAPL	IBM	JPM	MCD	MSFT	NKE	GOLD
AAPL	0.081177	0.027697	0.033939	0.021452	0.040876	0.029370	0.002107
IBM	0.027697	0.052320	0.036392	0.020267	0.030918	0.025687	0.000710
JPM	0.033939	0.036392	0.082852	0.026582	0.037617	0.035785	-0.003798
MCD	0.021452	0.020267	0.026582	0.038067	0.023809	0.024215	0.001155
MSFT	0.040876	0.030918	0.037617	0.023809	0.066118	0.030917	0.000554
NKE	0.029370	0.025687	0.035785	0.024215	0.030917	0.067818	-0.002378
GOLD	0.002107	0.000710	-0.003798	0.001155	0.000554	-0.002378	0.026868

Correlation:

	AAPL	IBM	JPM	MCD	MSFT	NKE	GOLD
AAPL	1.000000	0.424988	0.413843	0.385909	0.557949	0.395835	0.045110
IBM	0.424988	1.000000	0.552738	0.454138	0.525671	0.431237	0.018928
JPM	0.413843	0.552738	1.000000	0.473327	0.508242	0.477400	-0.080507
MCD	0.385909	0.454138	0.473327	1.000000	0.474567	0.476576	0.036122
MSFT	0.557949	0.525671	0.508242	0.474567	1.000000	0.461703	0.013139
NKE	0.395835	0.431237	0.477400	0.476576	0.461703	1.000000	-0.055711
GOLD	0.045110	0.018928	-0.080507	0.036122	0.013139	-0.055711	1.000000

Generate random weights:

```
array([0.22454855, 0.20413161, 0.04620425, 0.04290099, 0.13930751,  
       0.19058471, 0.15232238])
```

# calculate expected portfolio return from annualized return values

0.14788645952274218

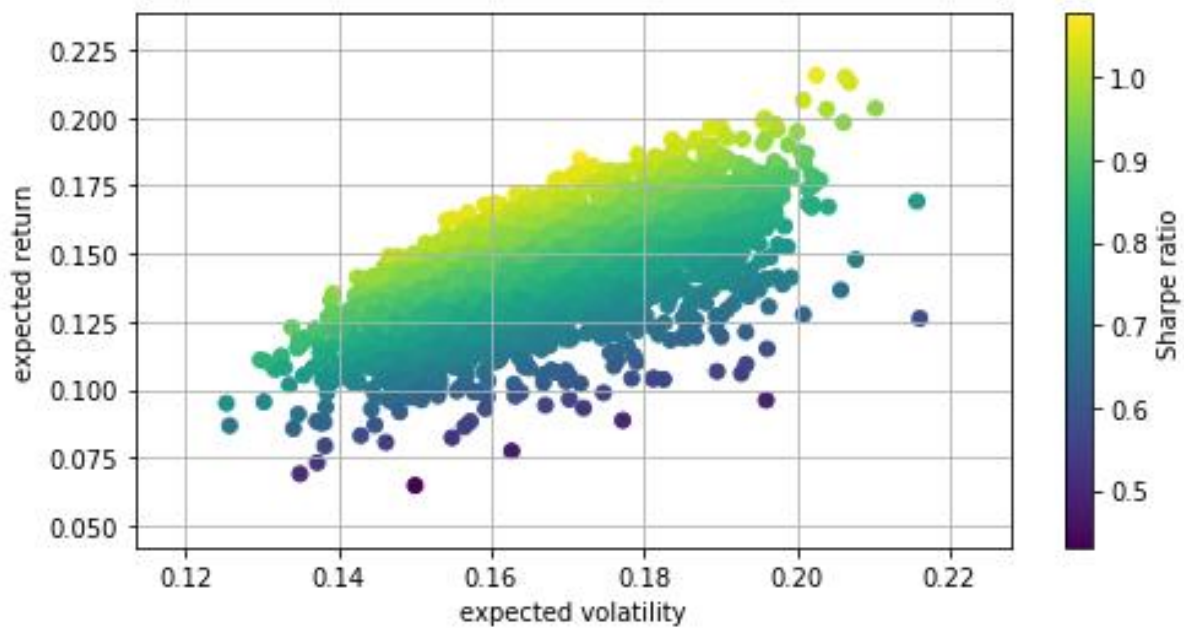
# calculate expected portfolio variance

```
0.027993858069324654
```

```
# calculate expected portfolio standard deviation
```

```
0.16731365177212723
```

```
# Plot the results from the simulation
```



```
noa * [1. / noa,] # initial guess of the weights - equal distribution
```

```
[0.14285714285714285,
```

```
0.14285714285714285,
```

```
0.14285714285714285,
```

```
0.14285714285714285,
```

```
0.14285714285714285,
```

```
0.14285714285714285,
```

```
0.14285714285714285]
```

```
# optimal portfolio composition results
```

```
array([0.274, 0. , 0. , 0.107, 0.253, 0.208, 0.158])
```

```
# calculate statistics
```

```
array([0.189, 0.174, 1.086])
```

```
# define a function that minimizes the variance
```

```
# absolute minimum variance portfolio results:
```

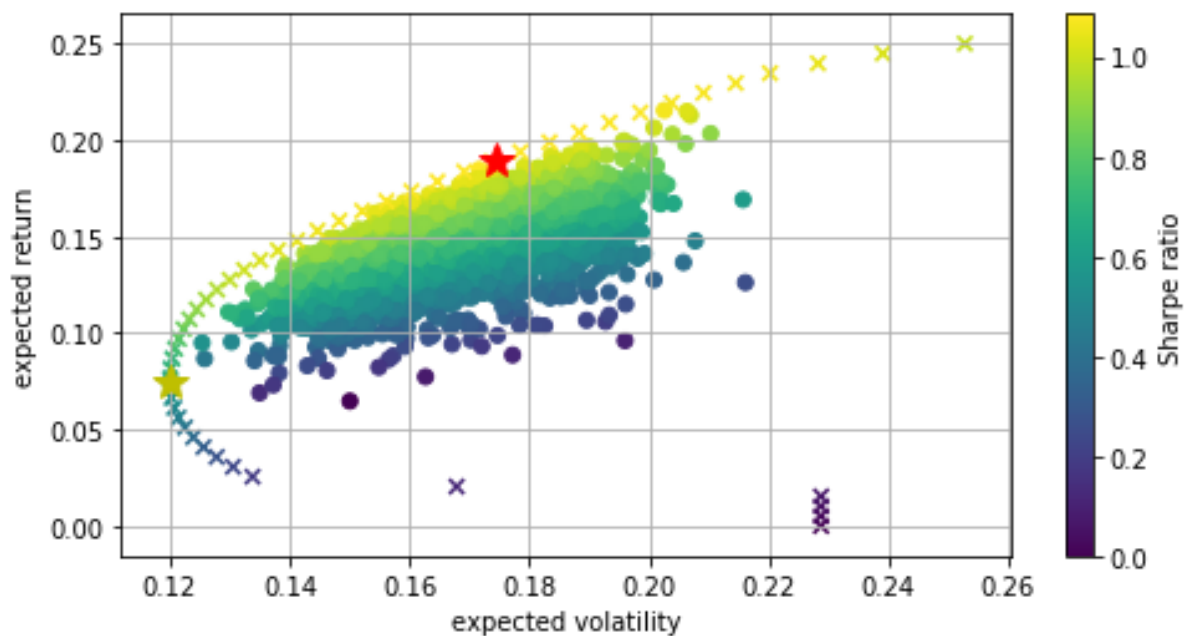
```
array([0.014, 0.108, 0.033, 0.211, 0.02 , 0.082, 0.531])
```

```
# calculate statistics
```

```
array([0.074, 0.12 , 0.619])
```

```
# Derive Efficient frontier
```

```
# Plot optimization results – тук всички редове след този коментар преди празния ред се изпълняват наведнъж, за да се начертае всичко на една графика
```



```
# Capital market line
```

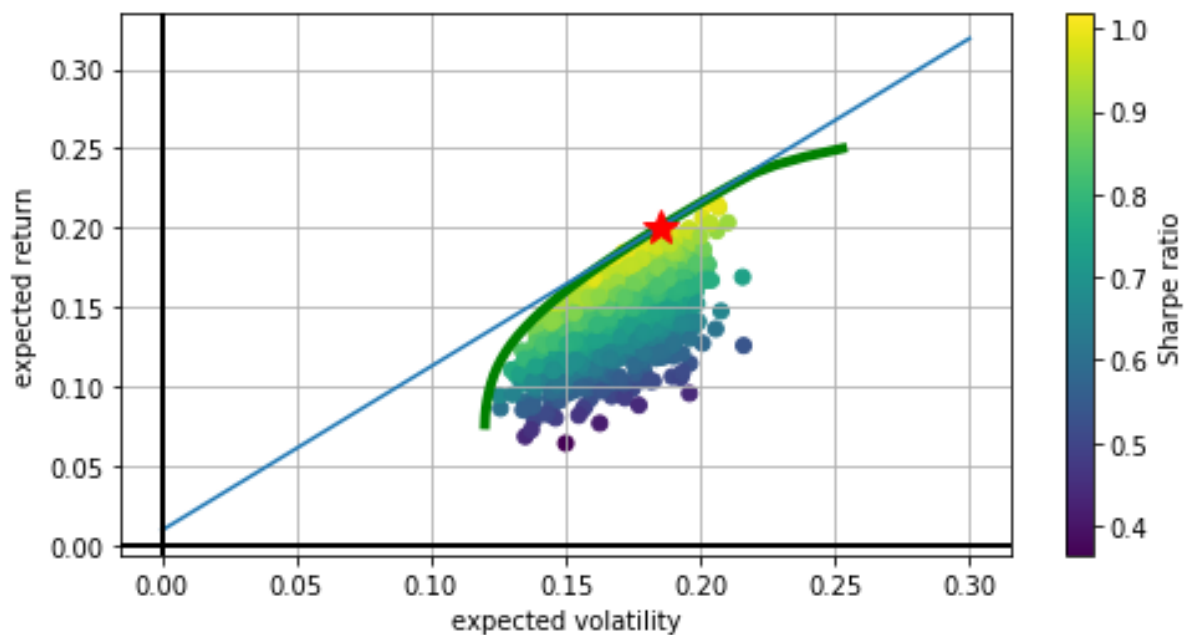
```
# results from the numerical optimization
```

```
array([0.01, 1.03062471, 0.18519155])
```

```
# equations' results
```

```
array([ 0., -0.,  0.])
```

```
# plot optimal portfolio – пак всички редове преди празния наведнъж
```



```
# optimal portfolio weights
```

```
# optimal portfolio weights print
```

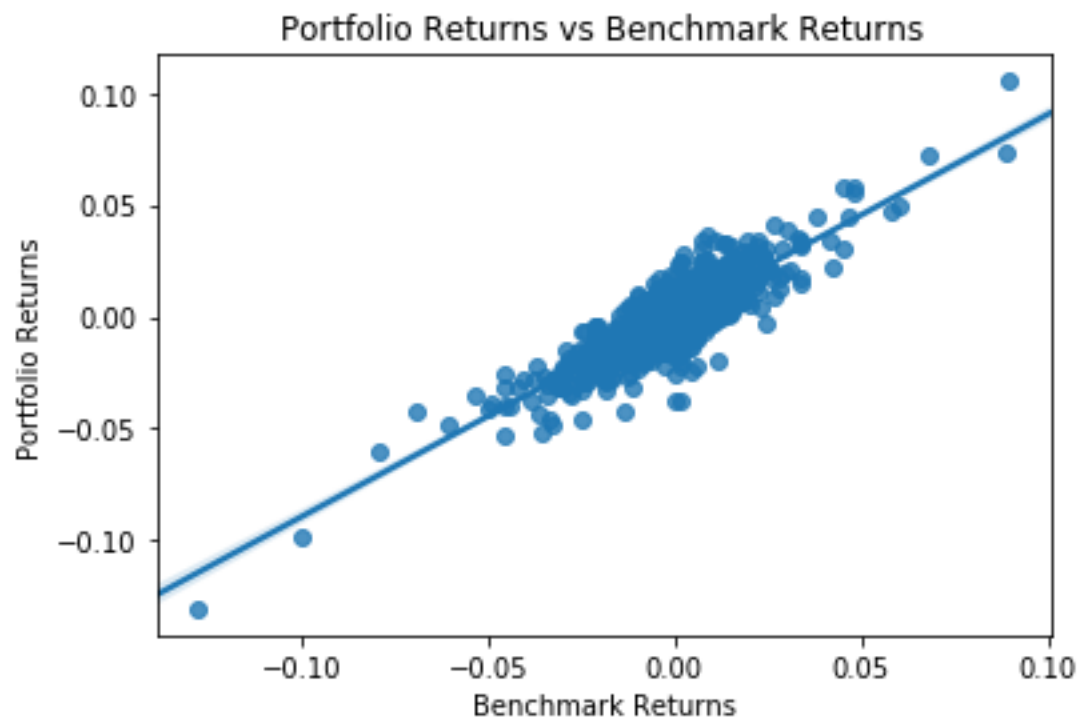
```
array([0.302, 0., 0., 0.09, 0.277, 0.22, 0.111])
```

```
# Check statistics
```

```
array([0.20088233, 0.18521005, 1.08461893])
```

```
# Alpha and Beta
```

```
# plot optimal portfolio returns vs benchmark returns – всички редове до празния се изпълняват наведнъж
```



```
# print beta
```

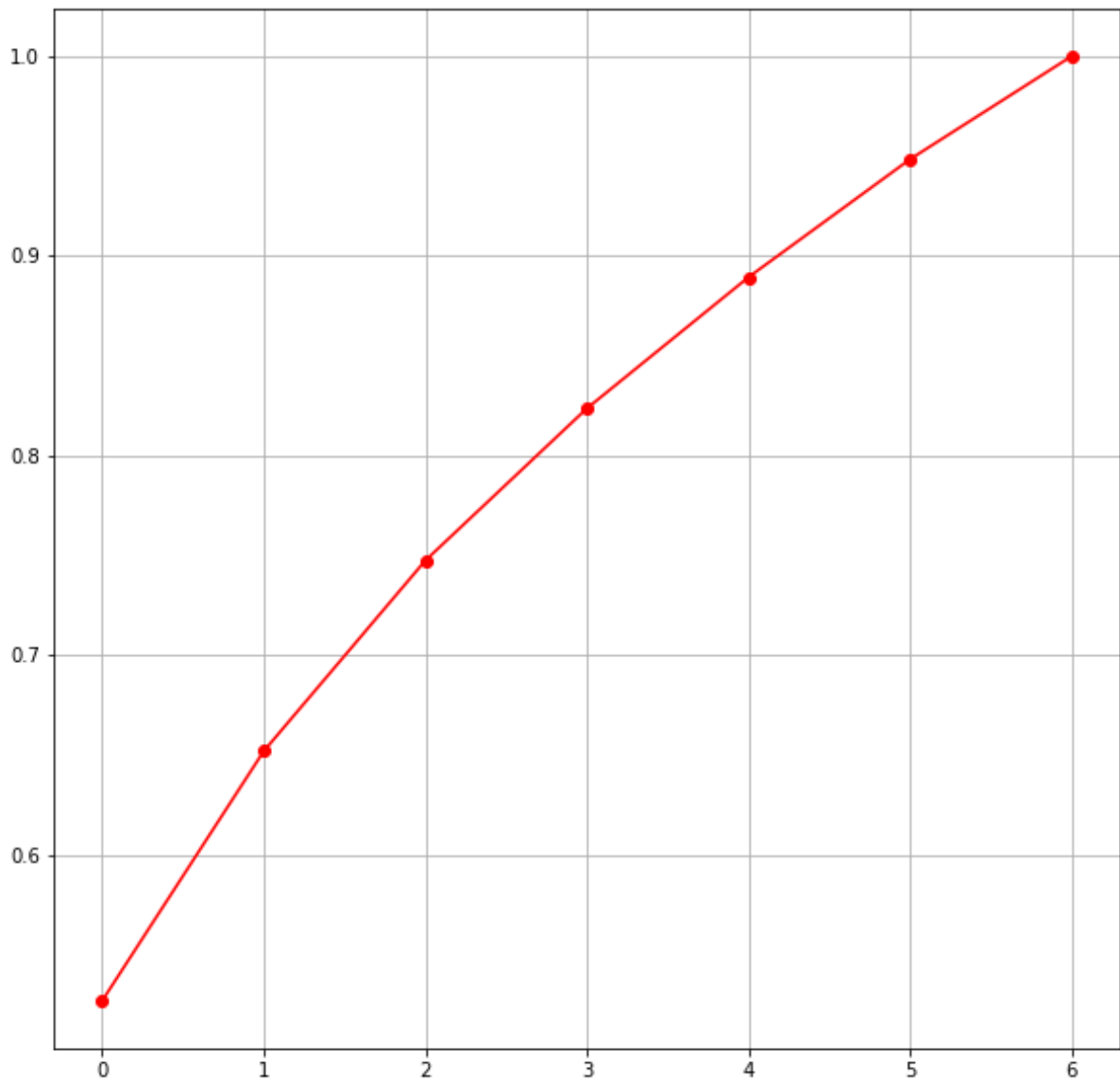
```
0.9016
```

```
# print alpha
```

```
0.00041
```

```
##### PCA part #####
```

```
# find optimal number of components
```



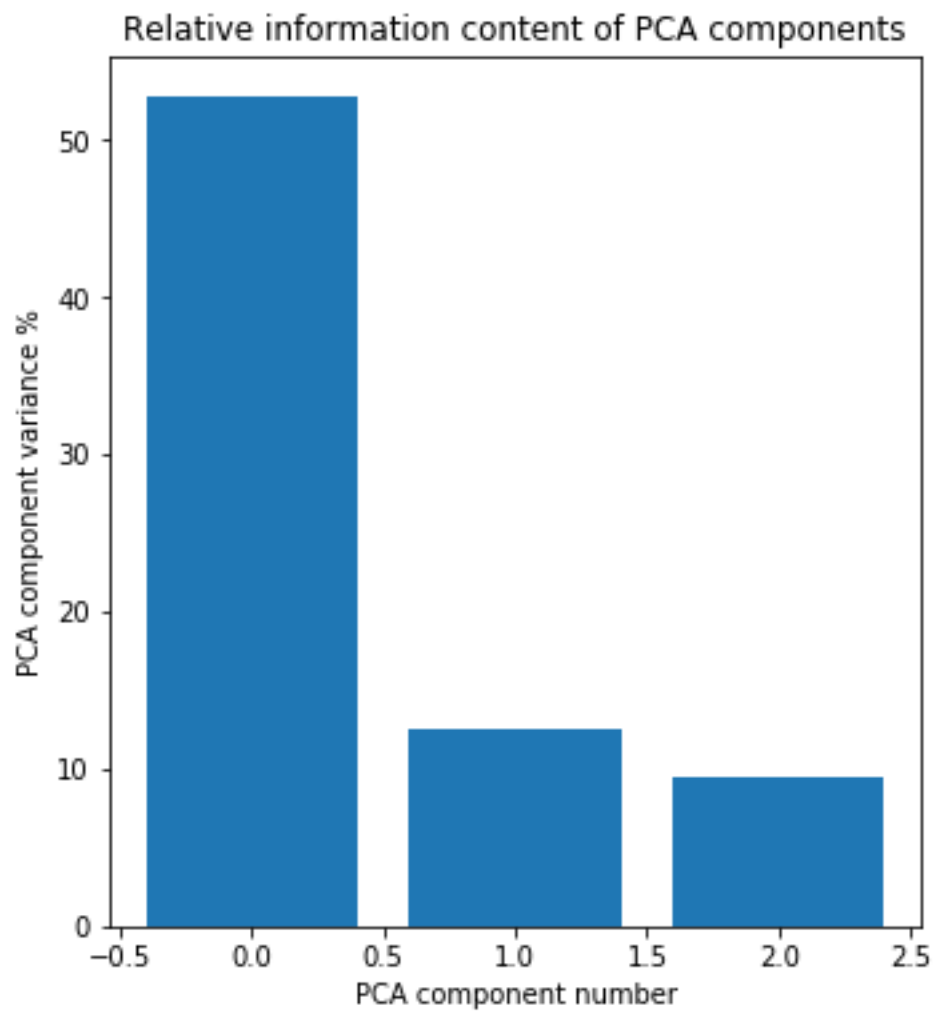
# PCA with 3 components

explained variance ratio (first three components): 0.7473709517414355

# explained variance by each component

array([0.52689465, 0.12502717, 0.09544913])

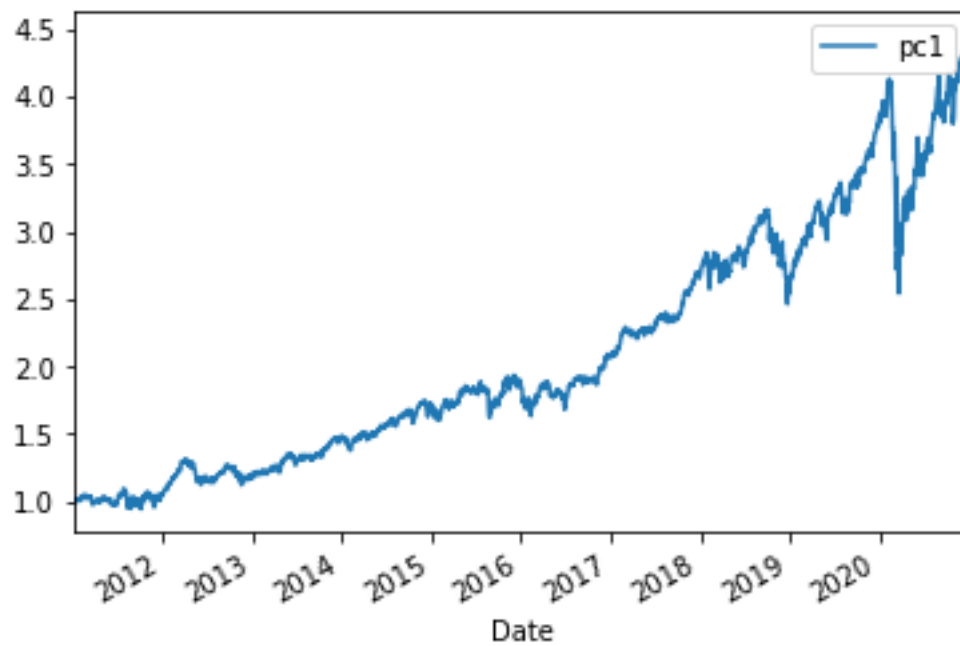
# plot information content



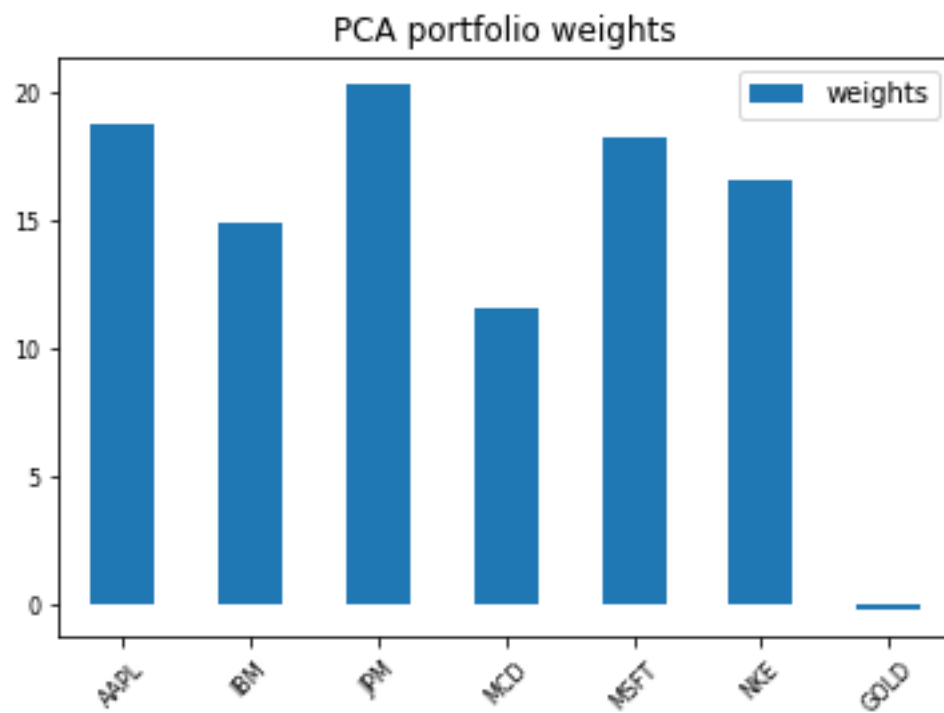
#plot PC portfolio vs market



PC portfolio vs Market



# portfolio weights



weights

AAPL 18.741815

IBM 14.896949

JPM 20.321120

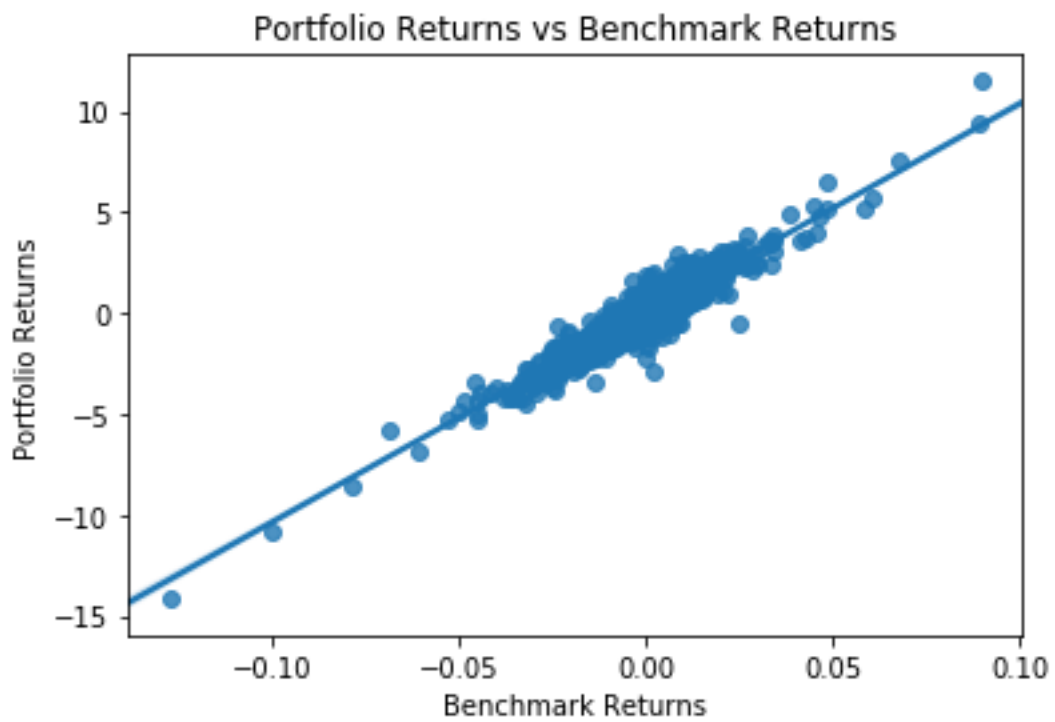
MCD 11.500847

MSFT 18.191867

NKE 16.572417

GOLD -0.225014 = 0

# plot optimal portfolio returns vs benchmark returns



The portfolio beta is 103.6358

The portfolio alpha is 0.02231