Design and Analysis of Algorithms Graphs 3: Depth-First Search

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3.3.3

For all nodes u,v, either [pre[u], post[u]] is completely within [pre[v], post[v]], or the other way around, or there is no overlap. Why? pre[u] to post[u] is the time u is on the stack.

This is because each [pre[u],post[u]] is completely within [pre[v],post[v]] because only unexplored nodes are added to the stack. So, when a node is added to the stack (u), all of the nodes for (v) will be discovered before the stack is emptied and returns to u. This is because v cannot be added to the exploration of u.The name depth-first sort of implies this, too. If we start at a node (u), we search as deep as we can before returning to u, so any v searches will take less time than u.

3.3.5

What is the running time of DFS?

The running time of DFS is O(N)

It appears that the running time is O(N), or or O(E), since we call explore on depending on the size of the Edges. Each edge is explored 1 time!