

## Laws of Logic

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|-----------------------------------------------------------------------------------------------------------------------------------------------|------------------------|
| 1. $\neg\neg p \leftrightarrow p$                                                                                                             | Law of Double Negation |
| 2. $\neg(p \vee q) \leftrightarrow \neg p \wedge \neg q$<br>$\neg(p \wedge q) \leftrightarrow \neg p \vee \neg q$                             | DeMorgan's Law         |
| 3. $p \vee q \leftrightarrow q \vee p$<br>$p \wedge q \leftrightarrow q \wedge p$                                                             | Commutative Laws       |
| 4. $p \vee (q \vee r) \leftrightarrow (p \vee q) \vee r$<br>$p \wedge (q \wedge r) \leftrightarrow (p \wedge q) \wedge r$                     | Associative Laws       |
| 5. $p \vee (q \wedge r) \leftrightarrow (p \vee q) \wedge (p \vee r)$<br>$p \wedge (q \vee r) \leftrightarrow (p \wedge q) \vee (p \wedge r)$ | Distributive Laws      |
| 6. $p \vee p \leftrightarrow p$<br>$p \wedge p \leftrightarrow p$                                                                             | Idempotent Laws        |
| 7. $p \vee F \leftrightarrow p$<br>$p \wedge T \leftrightarrow p$                                                                             | Identity Laws          |
| 8. $p \vee \neg p \leftrightarrow T$<br>$p \wedge \neg p \leftrightarrow F$                                                                   | Inverse Laws           |
| 9. $p \vee T \leftrightarrow T$<br>$p \wedge F \leftrightarrow F$                                                                             | Domination Laws        |
| 10. $p \vee (p \wedge q) \leftrightarrow p$<br>$p \wedge (p \vee q) \leftrightarrow p$                                                        | Absorption Laws        |
| 11. $(p \rightarrow q) \leftrightarrow (\bar{p} \vee q)$                                                                                      | Implication Identity   |
| 12. $(p \rightarrow q) \leftrightarrow (\bar{q} \rightarrow \bar{p})$                                                                         | Contrapositive         |

## Laws of Set Theory

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|---------------------------------------------------------------------------------------------------------|------------------------|
| 1. $\bar{\bar{A}} = A$                                                                                  | Law of Double Negation |
| 2. $\overline{A \cup B} = \bar{A} \cap \bar{B}$<br>$\overline{A \cap B} = \bar{A} \cup \bar{B}$         | DeMorgan's Laws        |
| 3. $A \cup B = B \cup A$<br>$A \cap B = B \cap A$                                                       | Commutative Laws       |
| 4. $A \cup (B \cup C) = (A \cup B) \cup C$<br>$A \cap (B \cap C) = (A \cap B) \cap C$                   | Associative Laws       |
| 5. $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$<br>$A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$ | Distributive Laws      |
| 6. $A \cup A = A$<br>$A \cap A = A$                                                                     | Idempotent Laws        |
| 7. $A \cup \emptyset = A$<br>$A \cap \mathcal{U} = A$                                                   | Identity Laws          |
| 8. $A \cup \bar{A} = \mathcal{U}$<br>$A \cap \bar{A} = \emptyset$                                       | Inverse Laws           |
| 9. $A \cup \mathcal{U} = \mathcal{U}$<br>$A \cap \emptyset = \emptyset$                                 | Domination Laws        |
| 10. $A \cup (A \cap B) = A$<br>$A \cap (A \cup B) = A$                                                  | Absorption Laws        |

## Rules of Inference

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|-----------------------------------------------------------------------------------------------------------------|------------------------------------|
| 1. $[p \wedge (p \rightarrow q)] \rightarrow q$                                                                 | Rule of Detachment (Modus Ponens)  |
| 2. $[(p \rightarrow q) \wedge (q \rightarrow r)] \rightarrow (p \rightarrow r)$                                 | Law of Syllogism                   |
| 3. $[(p \rightarrow q) \wedge \neg q] \rightarrow \neg p$                                                       | Modus Tollens                      |
| 4. $[(p) \wedge (q)] \rightarrow p \wedge q$                                                                    | Rule of Conjunction                |
| 5. $[(p \vee q) \wedge \neg p] \rightarrow q$                                                                   | Rule of Disjunctive Syllogism      |
| 6. $(\neg p \rightarrow F) \rightarrow p$                                                                       | Rule of Contradiction              |
| 7. $(p \wedge q) \rightarrow p$                                                                                 | Rule of Conjunctive Simplification |
| 8. $p \rightarrow (p \vee q)$                                                                                   | Rule of Disjunctive Amplification  |
| 9. $[(p \wedge q) \wedge [p \rightarrow (q \rightarrow r)]] \rightarrow r$                                      | Rule of Conditional Proof          |
| 10. $[(p \rightarrow r) \wedge (q \rightarrow r)] \rightarrow [(p \vee q) \rightarrow r]$                       | Rule for Proof by Cases            |
| 11. $[(p \rightarrow q) \wedge (r \rightarrow s) \wedge (p \vee r)] \rightarrow (q \vee s)$                     | Rule of the Constructive Dilemma   |
| 12. $[(p \rightarrow q) \wedge (r \rightarrow s) \wedge (\neg q \vee \neg s)] \rightarrow (\neg p \vee \neg r)$ | Rule of the Destructive Dilemma    |
| 13. $[(p \vee q) \wedge (\neg p \vee r)] \rightarrow (q \vee r)$                                                | Rule of Resolution                 |
| 14. $[p \rightarrow (q \wedge r)] \rightarrow [(p \rightarrow q) \wedge (p \rightarrow r)]$                     | Distributive Rule of Implication   |

## Sequence and Series Terms and Sums

Arithmetic Sequences:  $a_n = a_1 + (n - 1)d$ ,  $a_j = a_i + (j - i)d$ ,  $S_n = \frac{(a_1 + a_n)n}{2}$

Geometric Sequences:  $a_n = a_1 r^{n-1}$ ,  $a_j = a_i r^{j-i}$ ,  $S_n = \frac{a_1(1-r^n)}{1-r}$ ,  $r \neq 1$ ,  $S_\infty = \frac{a_1}{1-r}$ ,  $|r| < 1$

Sum Formulas:  $\sum_{i=1}^n c = cn$ ,  $\sum_{i=1}^n i = \frac{n(n+1)}{2}$ ,  $\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$ ,  $\sum_{i=1}^n i^3 = \frac{n^2(n+1)^2}{4}$