

HW3

3. Construct a cfl for $L = \{ w \text{ in } \{a, b, c\}^* \mid \text{no}_a(w) = \text{no}_b(w) \pmod{4} \}$, where $\text{no}_a(w)$ denotes number of symbols 'a' in the sentence sequence 'w'

$S \rightarrow abc \mid abeasbc \mid a b S c \mid a T b c \mid a b T c$

$T \rightarrow bac \mid b S a c \mid b a S c \mid b T a c$

$\Rightarrow h = 1..5$

$S_0 \rightarrow abc \mid a S_h b c \mid a b S_h c \mid a S_h b S_h c$

$S_1 \rightarrow acb \mid a S_h c b \mid a c S_h b \mid a S_h c S_h b$

$S_2 \rightarrow bac \mid b S_h a c \mid b c S_h a \mid b S_h c S_h a$

$S_3 \rightarrow bac \mid b S_h a c \mid b a S_h c \mid b S_h a S_h c$

$S_4 \rightarrow cab \mid c S_h a b \mid c a S_h b \mid c S_h a S_h b$

$S_5 \rightarrow cba \mid c S_h b a \mid c b S_h a \mid c S_h b S_h a$

$m, m, h \mid h = m + m'$