

Minimum Absolute Slice Problem Description

A non-empty zero-indexed array A of N integers is given. A pair of integers (P, Q) , such that $0 \leq P \leq Q < N$, is called a slice of array A . The sum of a slice (P, Q) is the total of $A[P] + A[P+1] + \dots + A[Q]$. A min abs slice is a slice whose absolute sum is minimal.

For example, array A such that:

- $A[0] = 2$
- $A[1] = -4$
- $A[2] = 6$
- $A[3] = -3$
- $A[4] = 9$

contains the following slices, among others:

- $(0, 1)$, whose absolute sum = $|2 + (-4)| = 2$
- $(0, 2)$, whose absolute sum = $|2 + (-4) + 6| = 4$
- $(0, 3)$, whose absolute sum = $|2 + (-4) + 6 + (-3)| = 1$
- $(1, 3)$, whose absolute sum = $|(-4) + 6 + (-3)| = 1$
- $(1, 4)$, whose absolute sum = $|(-4) + 6 + (-3) + 9| = 8$
- $(4, 4)$, whose absolute sum = $|9| = 9$

Both slices $(0, 3)$ and $(1, 3)$ are min abs slices and their absolute sum equals 1.

Write a function:

int solution(int A[], int N);

that, given a non-empty zero-indexed array A consisting of N integers, returns the absolute sum of min abs slice.

For example, given:

- $A[0] = 2$
- $A[1] = -4$
- $A[2] = 6$
- $A[3] = -3$
- $A[4] = 9$

the function should return 1, as explained above.

Assume that:

- N is an integer within the range $[1..100,000]$;
- each element of array A is an integer within the range $[-10,000..10,000]$.

Complexity:

- expected worst-case time complexity is $O(N \log(N))$;
- expected worst-case space complexity is $O(N)$, beyond input storage (not counting the storage required for input arguments).

Elements of input arrays can be modified.