# Automated Checking of Implicit Assumptions on Textual Data

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#### Abstract

The abundance of data and increased reliance of data science programs in today's world gives rise to new opportunities in science and business. Due to the large and heterogeneous nature of the datasets used in data science applications, it had become increasingly important to develop new tools and techniques that will ease the process of data cleaning, that is finding and fixing erroneous values in data files.

# 1 Introduction

Today, we live in a world that produces tremendous amounts of data on a daily basis. The extensive use of social media websites and the digitization of traditional services such as banking, retail and publishing guarantees the existence of large datasets that are available to service providers. In addition to business, technological advancements have created an abundance of data in many fields of scientific research such as the genomic data created by efficient Deoxyribonucleic acid (DNA) sequencing or raw images of celestial bodies that are captured by modern telescopes [1].

This abundance of data, along with the rapid development in new data science techniques and methods to organize, analyze and detect patterns in large datasets, creates new and unique opportunities for experts in different domains. For example, it enables businesses to predict future customer behavior or medical researcher to associate the presence of a specific gene in the human DNA with susceptibility to certain diseases.

These advantages, however, are not achieved without challenges or difficulties. The datasets processed by data science algorithms are typically very large in size and could be obtained from various sources or maintained on different machines. For these reasons, they are likely to contain errors and inconsistencies.

In the field of data science, raw data, that is data as it is collected from the source and stored on some storage medium (e.g. database or cloud), is not usually usable as is. A recent survey among data scientists [2] shows them to cite "dirty data" as one of the most challenging aspects of their work. Dirty data, as defined in [3], is data that is wrong, missing or not represented according to a known standard such as non-standard representation of time and date.

Before feeding the data into a data science program, it must be cleansed and the erroneous values must be eliminated. Many tools have been introduced to achieve this goal.. [mention some data cleaning tools.]

In this thesis, we present an approach to detect incorrect input data with respect to a given data science program. Unlike the data-cleaning tools mentioned above, our method does not perform computations on the dataset directly. Instead, we design a static analysis that analyzes the source code of the program in order to find out the implicit assumptions that the program makes about the input data that it reads such that if these assumptions are violated the program will crash. These assumptions represent the pre-conditions that must

be satisfied so that the program runs without producing errors. Our analysis will compute an over-approximation of these pre-conditions. In other words, if there is a set of accepted values that will allow the program to run without raising an error, the set of values that our analysis computes will contain all the accepted values, but it might contain some extra values that will cause the program to raise errors. That is, the pre-conditions we compute are necessary but not sufficient for the program to terminate without crashing.

We then design an input checker that looks for values that violate the assumptions computed by the analysis. If that is the case, the wrong input values are flagged as errors so that the user can correct them. Our approach is advantageous in cases where the data cannot be shared with third parties to perform data cleaning. We implement our analysis and input checker for Python programs and integrate them into a tool that can be used directly by domain experts on their data.

```
sequence length: int = int(input())
2
     count a: int = 0
3
     count c: int = 0
     count g: int = 0
4
5
     count t: \mathbf{int} = 0
     for i in range (sequence length):
       base: str = input()
8
       if base = 'A':
         count a: int = count a + 1
9
       elif base == 'C':
10
         count c: int = count c + 1
11
       elif base == 'G':
12
13
         count_g: int = count_g + 1
       elif base == 'T':
14
15
         count_t: int = count_t + 1
16
       else:
17
         raise ValueError
```

Listing 1.1: Example of Assumptions on String Data

To elaborate further on what we aim to achieve in this thesis, let us examine the program in Listing 1. This program aims to read a DNA sequence and count the frequency of occurrence of each nucleotide. It first reads the length of the sequence (line 1), then since the only possible nucleotides in a DNA sequence are represented by the letters A, C, G and T, it sets a frequency counter for each of these nucleotides (lines 2-5). Then the program iterates through the sequence, reading one letter per line and incrementing the corresponding counter variable. If it encounters a letter that is neither A, C, G or T, it raises an exception because it assumes that, in an ideal scenario, no value in the input file will be outside this set of letters.

Our aim, thus, is not to perform computations on the input data based on the known fact that the human DNA contains only A, C, G and T bases and to cleanse the wrong values. Rather, we turn our attention to the program that will run on the data and try to answer the question: what does this program assume about its input data such that if those assumptions are not fulfilled, the program will raise an error? For our analysis to compute a successful overapproximation, it must always include the character 'A', 'C', 'G' and 'T' in the set of accepted values it produces. However, it may include some other values as well.

In section 1.1, we present the theoretical aspects upon which the work of this thesis is based. In section 2, we explain the design of our static analysis and its different components in more detail. In section 3, we give an overview of how our analysis and input checker were implemented and integrated into an IDE plug-in. We evaluate the work achieved in this thesis in section 4 and, finally, the conclusion and possible future work are to be found in section 5.

# 1.1 Theoretical Background

In this section we present the basic theoretical concepts which we use in our work.

#### 1.1.1 Static Analysis

Static analysis is the analysis of the source code of a program, without executing it, in order to infer some properties about the program's behaviour. Since it is generally impossible to infer with absolute certainty that a non-trivial property holds for all executions of a program, static analysis aims to approximate the behaviour of a program by analyzing a model of the program in all of its execution paths.

#### 1.1.2 Abstract Interpretation

The theory of Abstract Interpretation [5] is a general theory that allows for creating mathematically sound approximations of the behaviour of a program. It was created by Patrick Cousot and Radhia Cousot as a unifying framework for static analysis.

According to Abstract Interpretation, a program can have several semantics, that is several mathematical descriptions of its behaviour. The **concrete semantics** is the semantics that most closely resembles the real behaviour of the program. This is usually complex and computationally expensive to analyze. The **abstract semantics**, on the other hand, represents the semantics of the program with respect to some chosen property while abstracting away the irrelevant details. For example, the concrete semantics of a program can be the values which its numerical variables take, while an abstract semantics could be the signs of these variables. In this case, a statement such as "2 \* 3" can be abstracted as "(+) \* (-)".

In order to use Abstract Interpretation for static analysis, we must define an abstract domain that represents the states of the program according to the abstract semantics. An abstract domain must define an **element**, which is a computer representable object that represents the state of the program. As mentioned in the previous section, static analysis traverses all executions paths of the program. For this reasons, every abstract domain must define some operators in order to modify the current state according to the statements it encounters while traversing the paths of the program.

#### 1.2 Previous Work and Contribution

We build our approach on the work done in [4]. This work was focused on inferring assumptions on numerical values in terms of types, ranges and simple relations. They designed a type domain which we also use in this thesis and describe in section 2.3.1 and a simple relations domain to keep track of relations between numerical variables such as  $x \leq y$ . For ranges the used the well-known Interval Domain [5]. They also used a stack mechanism to store assumptions collected about the input values by the domains they employed.

Since we would like to analyze more evolved code examples that contain assumptions on both numerical and string values, such as Listing 1.1, we take a more generic approach to the problem in this thesis. We design our static analysis to be a generic framework which can employ any existing value domain to keep track of assumptions on the input data. This way, we can employ more powerful domains, for example the Octagon Domain which we use in this thesis, to keep track of relations between numerical variables and we can also keep track of assumptions on different types of variables, for instance numerical and string variables, at the same time. We also extend the stack mechanism used in [4] to be more generic and to keep track of assumptions from different domains simultaneously.

# 2 Static Analysis Design

In this section, we present a detailed description of our static analysis. In the next section we present the concrete semantics which we use in our analysis. In section 2.2, we describe our generic framework for inferring assumptions on input data as a top-level abstract domain. In section 2.3, we describe three abstract domains, namely the Type Domain (section 2.3.1), the Octagon Domain (section 2.3.2) and the Character Inclusion Domain (section 2.3.3), which we use to create the instance of our generic framework that we use to demonstrate how our technique works throughout this thesis and which we also used for our implementation.

## 2.1 Concrete Domain

To define our concrete domain, we first define the following sets:

- $\mathcal{L}$ : the set of all program points in the program being analyzed.
- S: the set of all possible string values.
- $\mathcal{V}$ : the set of all program variables.
- $\wp(\mathcal{V} \to \mathcal{S})$ : the set of environments mapping program variables to their possible values.
- $\wp(\mathcal{S})^*$ : the list of values read as input from one program point onwards.

We can then define our concrete domain as follows:

$$\mathcal{L} \to \wp(\mathcal{V} \to \mathcal{S}) \times \wp(\mathcal{S})^*$$

As indicated by the formula, our concrete domain maps a program point to a set of mappings of program variables to the values they are allowed to take and a list of input values which the program reads from this point onwards. Specifically, given a program, its concrete semantics is the set of values that its variables are allowed to take and the list of input values that it is allowed to read so that it terminates without errors.

# 2.2 The Assumption Abstract Domain

We use the theory of Abstract Interpretation [5] to design an abstract domain that over-approximates the concrete semantics defined in the previous section. In this context, over-approximation means that the constraints inferred by the analysis are necessary but not sufficient for the program to run without producing an error. If the input values violate those constraints, the program is guaranteed to produce an error. We guarantee an absence of false-positives. However, if the input values satisfy all the constraints, the program might still produce an error. Our static analysis works backwards by starting at the final state of the program and analyzing all the execution paths of the program till it reaches the initial state.

To examine the properties of our domain, let us consider the program in Listing 2, which performs the same operation as Listing 1, namely reading a DNA sequence and counting the frequency of every nucleotide, but on multiple sequences separated by a '.' or '#' character. On line 1, the number of sequences is read. Lines 3 and 4 assert that we have at least one sequence in the file. Another addition in Listing 2 is the check that the sequence length is not greater than some maximum length on lines 7 and 8.

There are multiple ways in which this program can produce an error. On line 1 if the value read cannot be cast to an integer, a error will be raised by Python. If the number of sequences is not positive (line 3), the length of each sequence is greater than the designated maximum sequence length, the sequence contains characters other than A, C, G and T (lines 15 through 24) or if the separator character is not a hash or a dot (line 26), the program raises a ValueError explicitly.

It is obvious from this example that we need to track information about both numerical values and string values if we are to compute the set of allowed input values to this program. For examples we need to ensure that the relation  $sequence\_length > max\_length$  holds and that the variable base has only the characters in the set  $\{'A', 'C', 'G', 'T'\}$ . This cannot be achieved by running a conventional static analysis using only one abstract domain.

```
number of sequences: int = int(input())
 2
     max length: int = int(input())
3
     if number of sequences \leq 0:
 4
       raise ValueError("Expecting at least one DNA sequence
     for s in range (number of sequences):
 5
 6
       sequence length: int = int(input())
 7
       if sequence_length > max_length:
 8
          raise ValueError
 9
       A count: int = 0
       C \text{ count: } \mathbf{int} = 0
10
       G \text{ count: } \mathbf{int} = 0
11
12
       T count: int = 0
```

```
for i in range (sequence length):
13
           base: str = input()
14
           if base = 'A':
15
             A count: int = A count + 1
16
           elif base == 'C':
17
             C \text{ count}: \text{ int } = C \text{ count } + 1
18
           elif base == 'G':
19
             G \text{ count: } \mathbf{int} = G \text{ count } + 1
20
           elif base = 'T':
21
22
             T \text{ count}: \mathbf{int} = T \text{ count} + 1
23
           else:
24
              raise ValueError
25
        separator: str = input()
        if separator = '.' or separator = '#':
26
27
           pass
28
        else:
           raise ValueError
29
```

Listing 2.1: Example of Assumptions on both String and Numerical Data

Our abstract domain, which we call the Assumption Domain, is a generic domain that allows for the approximation of multiple program properties simultaneously. It is parametrized by a list of abstract domains which are independent of one another. For each step of the analysis, the Assumption Domain invokes the corresponding operator or transformation on each domain independently. We define a SUBD to be a family of domains that can be used in our analysis. Any value domain can be a member of this family given that it define extra operators that are described in 2.2.1. The Assumption Domain uses these domains to keep track of assumptions on the values of program variables. For example, in the case of , we can use the Octagons Domain [6] to keep track of the relations between numerical variables such as  $sequence\_length \le max\_length$  and the Character Inclusion Domain [7] to keep track of the characters of the variable base.

Going back to Listing 2, if we trace a backward static analysis from line 24 to line 15 using the Character Inclusion Domain as a sub-domain, we will get that the variable base is allowed to contain only the characters 'A', 'C', 'G' and 'T'. When this variable is read as input on line 14, we need to store the assumption in some data structure. The same applies for the variable  $sequence\_length$ . Tracing the analysis backwards using the Octagon Domain will give us the constraint  $sequence\_length \le max\_length$ . On line 6, when the variable is read as input, this constraint must be stored in a way that preserves its order among other inputs that the program reads in the course of its execution. More specifically, we need a data structure in which the assumptions about  $sequence\_length$  appear before those about base. We also need a data structure that indicates how many times an input value is read. For example, it needs to show that the variable base is read  $sequence\_length$  number of times.

In our case, we choose this data structure to be a stack, in which every layer

represents a scope of the program. Whenever the analysis enters a new branch or a loop, a new layer is pushed onto the stack. Inside of this scope, whenever a variable is read as input, we store its constraints in the top layer of the stack. When exiting a branch or a loop, the top layer is popped from the stack and combined with the layer below it in such a way that the assumptions appear in the order in which the inputs are read. In the case of exiting a loop, we define a mechanism to indicate how many times a group of assumptions are repeater. This way, at the end of the analysis, the stack will contain all the assumptions on the input value of the program in the correct order. We define the stack with further detail in section 2.2.2.

Given the previously mentioned properties, we introduce our domain formally below.

We define STACK to be a set of all possible stacks which store assumptions on input values of the program.

We use the notation  $(X_i)_{i=1}^n$  throughout this thesis to indicate a list of length n.

We can define the Assumption Domain formally as follows:

$$D \equiv SUBD^n \times STACK$$

- An element  $d \in D = \{((S_i)_{i=1}^n, Q) | S_i \in SUBD \land Q \in STACK\}$ . Every element of this domain consists of a sequence of instances of sub-domains and a stack.
- A concretization function  $\gamma_D(d) = (\bigcap_{i=1}^n \gamma_{S_i}(S_i), \gamma_{STACK}(Q))$ . The concretization function gives a set of values that is a superset of the set of values allowed by the concrete domains. This applies to both the set of values that program variables are allowed to take, represented by the intersection of the concretization of the sub-domains, and the set of allowed input values, represented by the concretization of the stack.
- A partial order  $\sqsubseteq_D$  such that  $((S_{1,i})_{i=1}^n, Q_1) \sqsubseteq_D ((S_{2,i})_{i=1}^n, Q_2) \iff \bigwedge_{i=1}^n (S_{1i} \sqsubseteq_{S_i} S_{2i}) \land Q_1 \sqsubseteq_{STACK} Q_2$ . An element  $d_1$  of D is small than or equal to another element  $d_1$  if and only if  $d_1$  represents a set of allowed input values that is smaller than or equal the set allowed input values by  $d_2$ .
- A minimum element  $\perp_D = ((\perp_{S_i})_{i=1}^n, \perp_{STACK})$ . This elements represents a state where there are no possible input values that are acceptable by the program.
- A maximum element  $\top_D = ((\top_{S_i})_{i=1}^n, \top_{STACK})$ . This represents the set of all possible input value without any constraints.

- A join operator  $\sqcup_D$  such that  $((S_{1,i})_{i=1}^n,Q_1)\sqcup_D((S_{2,i})_{i=1}^n,Q_2)=(((S_{1,i}\sqcup_{S_i}S_{2,i})_{i=1}^n,Q_1\sqcup_{STACK}Q_2))$ . When joining two paths of the analysis, we must join the constraints computed by the analysis on both the program variables, by performing a pair-wise join on all the sub-domains and joining the two stacks  $Q_1$  and  $Q_2$ . The soundness of this operator follows from the soundness of the join operators of the sub-domains and the stack as follows:  $\gamma_D(((S_{1,i})_{i=1}^n,Q_1))\cup\gamma_D(((S_{2,i})_{i=1}^n,Q_2))=(\bigcap_{i=1}^n\gamma_{S_{1,i}}(S_{1,i}),\gamma_{STACK}(Q_1))\cup(\bigcap_{i=1}^n\gamma_{S_{2,i}}(S_{2,i}),\gamma_{STACK}(Q_2))$
- A meet operator  $\sqcap_D$  such that  $((S_{1,i})_{i=1}^n, Q_1) \sqcap_D ((S_{2,i})_{i=1}^n, Q_2) = (((S_{1,i} \sqcap_{S_i} S_{2,i})_{i=1}^n, Q_1 \sqcap_{STACK} Q_2))$ . Similar to the join, the meet operator is applied pair-wise to all sub-domains and the two stacks.
- A backward assignment operator  $[X := aexpr]((S_i)_{i=1}^n, Q) = (([X := aexpr](S_i))_{i=1}^n, [X := expr](Q))$ . The backward assignment operator is applied point-wise to every sub-domain and to the stack.
- A filter operator  $\llbracket bexpr \rrbracket ((S_i)_{i=1}^n, Q) = ((\llbracket bexpr \rrbracket (S_i))_{i=1}^n, \llbracket bexpr \rrbracket (Q))$ . The filter operator is applied element-wise to every sub-domain and to the stack.
- A widening operator  $\nabla_D$  such that  $((S_{1,i})_{i=1}^n, Q_1)\nabla_D((S_{2,i})_{i=1}^n, Q_2) = ((S_{1,i}\nabla_{S_i}S_{2,i}), Q_1\nabla_{STACK}Q_2)$ . Similar to the join and meet, widening is applied pair-wise between the sub-domains and the stack.

#### 2.2.1 Sub-domains

As mentioned in the previous section, our Assumption Domain can make use of any existing abstract domain in order to track assumptions on input data. However, in order for this setting to work effectively, we need to define some extra operators for existing abstract domains.

SUBD is the family of abstract domains which are capable of keeping track of constraints on variables. The variables are either program variables or special variables that represent an input value. An element  $F \in SUBD$  is an abstract domain whose concretization function  $\gamma_F$  operators  $\sqcup_F, \sqcap_F, \sqsubset_F, \nabla_F$ , backward assignment and filter are already defined.

The domains used in our analysis are required to define a special replacement operator  $\mathcal{R}_F(v, f, x)$  that, when an input value is read and stored in variable  $v \in \mathcal{V}$ , introduces some special variable x into element f of a relational domain F that denotes this input value and its relation to other variables. This newly introduced variable has to provide information on the order in which an input value was read with respect to other input values in the program. One possible definition for a replacement operator is to replace a variable that is read as input with a special variable  $l_i$  that represents the program point i at which it is read. In this case the operator is  $\mathcal{R}_F(v, f, l_i)$ .

If a program reads inputs from two different paths and these paths are to be joined at some point in the analysis, relational domain elements resulting from these two paths will contain different variables representing the inputs read on these paths. For this reason, we require the sub-domains to define a special operator  $\mathcal{U}(f_1, f_2)$  that unifies the environment of two elements of a relational domain. From the perspective of our analysis, we do not care about the particular variable that represents an input, but rather about the order in which these input are being read in their respective paths. The unification operator needs to ensure that the constraints on two input value read in the same order on two different paths can be joined successfully. An illustrative example on the replacement and unification operators can be found in section 2.3.2 where we refer to the Octagon Domain.

#### 2.2.2 The Stack

The stack used in our analysis follows the intuitive definition of a stack. It is composed of layers and defines push and pop operations. To introduce our stack, we need to define a set  $B = \{(l, (c_i)_{i=1}^n) \mid l \in \mathcal{L} \land \exists_{F_{in} \in SUBD_{in}} c \in F_{in}\} \cup \{\star\}$  which is either a sequence of constraints from any domain in SUBD associated with a specific program point or a constraint represented by  $\star$  which is an empty constraint and is used to indicate a lack of information on what constraints are placed on input values. For example, in Listing 2, an element  $(l7, (int, l7 \leq l2)) \in B$  would indicate that the value read from program point 7 is of type integer and is less than the value read form program point 2.

We then define the set of stack layers  $I = \{m \times (a_i)_{i=1}^k \mid m \in \mathbb{M} \land a_i \in I \cup B\}$  as a set of possibly repeated constraints on the input data, where  $\mathbb{M}$  is a set of multipliers that indicate how many time the constraints in the list are repeated. A multiplier is either an expression or an integer. For clarity, we express a list of constraints of length k that is repeated m times using the notation  $m \times (a_i)_{i=1}^k$ . We define a concretization function as well as join, meet and widening operators for the stack layers before we proceed to define them for the whole stack.

- A concretization function  $\gamma_I$  is defined recursively as follows:
  - $-\gamma_I(\star) = \mathcal{S}$ . An empty constraint indicates that the input value can be anything.
  - For  $(l,(c_i)_{i=1}^n) \in B$ ,  $\gamma_I((l,(c_i)_{i=1}^n)) = \gamma(c_1) \cap ... \cap \gamma(c_n)$ . A tuple of constraints associated with one program point concertizes to any value that satisfies all of the constraints of this tuple.
  - For  $m \times (a_i)_{i=1}^k \in I$ ,  $\gamma_I(m \times (a_i)_{i=1}^k) = [\gamma_I(a_1), ..., \gamma_I(a_k)]^m$ . To concertize a constraint in the set I, the concretization function is applied recursively to its list of constraints, then the result is repeated as many times as the value of its multiplier.
- A partial order  $\sqsubseteq_I$ :
  - For any  $b \in B$ ,  $b \sqsubseteq_I \star$ .

- For  $(l_1, (c_{1,i})_{i=1}^n), (l_2, (c_{2i})_{i=1}^n) \in B$ , the partial order is given by  $\bigwedge_{i=1}^n c_{1,i} \sqsubseteq_I c_{2,i}$ . We take the conjunction of the pair-wise order of the elements of the two tuples.
- For  $m \times (a_{1,i})_{i=1}^k$ ,  $m \times (a_{2,i})_{i=1}^k \in I$ , that is, two elements in I with the same multiplier and the same number of constraints, the order is given by  $\bigwedge_{i=1}^k a_{1,i} \sqsubseteq_I a_{2,i}$ .
- For two elements where one belongs to I and the other to B, we default to false.
- A maximum element  $\top_I \equiv 1 \times [\star]$ .
- A minimum element  $\perp_I$ .
- A join operator  $\sqcup_I$ :
  - For  $b \in B$ ,  $b \sqcup_I \star = \star$ 
    - For  $(l_1, (c_{1,i})_{i=1}^n), (l_2, (c_{2,i})_{i=1}^n) \in B$ , the join is given by  $(min(l_1, l_2), (c_{1,i} \sqcup c_{2,i})_{i=1}^n)$ . The soundness proof of this join follows from the soundness of the join operator of the individual domains as follows:  $\gamma_I((l_1, (c_{1i})_{i=1}^n)) \cup \gamma_I((l_2, (c_{2i})_{i=1}^n)) = (\gamma_I(c_{1,1}) \cap ... \cap \gamma_I(c_{1,n})) \cup (\gamma_I(c_{2,1}) \cap ... \cap \gamma_I(c_{2,n})) \subseteq \gamma_I(c_{1,1} \sqcup c_{2,1}) \cap ... \cap \gamma_I(c_{1,n} \sqcup c_{2,n}).$
    - For  $m \times (a_{1,i})_{i=1}^k$ ,  $m \times (a_{2,i})_{i=1}^k \in I$ , that is, two elements in I with the same multiplier and the same number of constraints, the join is given by  $m \times (a_{1,i} \sqcup a_{2,i})_{i=1}^k$ . The soundness can be proved as follows:  $[\gamma_I(a_{1,1}), ..., \gamma_I(a_{1,k})]^m \cup [\gamma_I(a_{2,1}), ..., \gamma_I(a_{2,k})]^m \subseteq [\gamma_I(a_{1,1} \sqcup a_{2,1}), ..., \gamma_I(a_{1,k} \sqcup a_{2,k})]^m$ .
  - For  $1 \times (a_{1,i})_{i=1}^{k_1}$ ,  $1 \times (a_{2,i})_{i=1}^{k_2} \in I$ , where  $k_1 \neq k_2$ , the join is given by  $m \times (a_{1,i} \sqcup a_{2,i})_{i=1}^{\min(k_1,k_2)} \oplus [\star]$ . When joining to elements from I with different constraint lengths, it is inevitable that we lose some information. The addition of the  $\star$  constraint is an indication that there is at least one input value for which we have no constraints and which can take any possible value. The soundness proof is somewhat similar to the previous point.  $[\gamma_I(a_{1,1}),...,\gamma_I(a_{1,k})] \cup [\gamma_I(a_{2,1}),...,\gamma_I(a_{2,k})] \subseteq [\gamma_I(a_{1,1} \sqcup a_{2,1}),...,\gamma_I(a_{1,k} \sqcup a_{2,k}),\mathcal{S}].$
- A meet operator returns the first element since it is not needed by the analysis for the set I.
- A backward assignment operator [X := aexpr] that is applied individually to constraints belonging to the set B.
- A widening operator  $\nabla_I \equiv \sqcup_I$ .
- A special replacement operator  $\mathcal{R}_I$  that is similar to the  $\mathcal{R}_F$  operator defined in the previous section:

- For  $(l,(c_i)_{i=1}^n) \in B$ , the replacement operator works as follows:

$$\mathcal{R}_I((l,(c_i)_{i=1}^n),v,l_1) = (l,(\mathcal{R}_F(c_i,v,l_1))_{i=1}^n)$$

The respective operator of each domain is applied to the constraint belonging to that domain.

- For elements of the set I:

$$\mathcal{R}_I(m \times (a_i)_{i=1}^k) = m \times (\mathcal{R}_I(a_i)_{i=1}^k)$$

The replacement operator is applied recursively to the constraints until it reaches an element of B, then it applies the  $\mathcal{R}_F$  operator.

- An insertion operator  $\mathcal{I}_I$  that is responsible for inserting new constraints or updating existing constraints on a stack layer:
  - For two elements  $(l, (c_{1,i})_{i=1}^n), (l, (c_{2,i})_{i=1}^n) \in B$  that are associated with the same program point, we update the existing constraint by joining the two:  $\mathcal{I}_I((l, (c_{1,i})_{i=1}^n), (l, (c_{2,i})_{i=1}^n)) = ((l, (c_{1,i})_{i=1}^n) \sqcup_I (l, (c_{2,i})_{i=1}^n)).$
  - For two elements  $m \times (a_{1,i})_{i=1}^{k1}, m \times (a_{2,i})_{i=1}^{k2} \in I$  where  $k1 \leq k2$  then it is required to update the existing constraints as follows:  $m \times (\mathcal{I}_I(a_{1,i},a_{2,i}))_{i=1}^{k1} \oplus (a_i)_{i=k1+1}^{k2}$ .
  - For all other cases, inserting  $b \in B \cup I$  in a stack layer  $m \times (a_i)_{i=1}^k$ :  $\mathcal{I}_I(m \times (a_i)_{i=1}^k, b) = m \times (b \oplus (a_i)_{i=1}^k)$ . The new constraint is prepended to the front of the list of existing constraints.

The stack is defined to be a sequence of layers:

$$q_0 \mid q_1 \mid \dots \mid q_{N-1} \mid q_N, q_i \in I$$

 $q_0$  is the bottom layer and  $q_N$  is the top layer. The PUSH operation of the stack is performed by adding a new empty layer  $1 \times [\ ]$  to the top of the stack whenever the analysis enters a new scope. The POP operation is performed on exiting a scope by merging the top two layers of the stack using the  $\mathcal{I}_I$  operator as follows:

$$POP(q_0 \mid q_1 \mid ... \mid q_{N-1} \mid q_N) = q_0 \mid q_1 \mid ... \mid \mathcal{I}_I(q_{N-1}, q_N)$$

The stack concretization function  $\gamma_{STACK}$  is defined as follows:  $\gamma_I(q_0) \mid \gamma_I(q_1) \mid ... \mid \gamma_I(q_N)$ . The binary operators join, meet, widening operators are applied pairwise to the layers of the stack. The backward assignment operator is applied to every layer of the stack.

# 2.3 An Instance of the Analysis

After designing an Assumption Domain in the previous section, we create an instance of this domain with several sub-domains for the purpose of this thesis. Here we introduce these sub-domains: the Type Domain, the Octagons Domain and the Character Inclusion Domain. We then trace an instance of the analysis instantiated with these three domains on a code example.

Similar to those defined in [8], we define an expression language that will be useful in defining substitution and filter algorithms for our sub-domains later in this section:

#### 2.3.1 The Type Domain

The Type Domain is used to keep track of types of variables. We define a type lattice T as per the Hass diagram below:



In section 2.1 we define  $\mathcal{S}$  to be the set of all possible strings. Here we define the sets  $\mathbb{F}, \mathbb{I}, \mathbb{B} \subseteq \mathcal{S}$  to be the sets of strings that can be interpreted as floating-point numbers, integers and booleans respectively. Then we define a concretization function  $\gamma_{\mathbf{T}}: \mathbf{T} \longrightarrow \mathcal{S}$  for the type lattice as follows:

$$\gamma_{\mathbf{T}}(String) = \mathcal{S}$$
 $\gamma_{\mathbf{T}}(Float) = \mathbb{F}$ 
 $\gamma_{\mathbf{T}}(Integer) = \mathbb{I}$ 

$$\gamma_{\mathbf{T}}(Boolean) = \mathbb{B}$$
$$\gamma_{\mathbf{T}}(\bot) = \phi$$

The operators  $\sqsubseteq_{\mathbf{T}}, \sqcup_{\mathbf{T}}, \sqcap_{\mathbf{T}}$  can be defined using the Hass diagram above.

We define arithmetic operations for the type lattice as follows:

$$t_1 + t_2 = \begin{cases} Integer & t_1 = Boolean \land t_2 = Boolean \\ String & t_1 = String \land t_2 = String \\ \bot_{\mathbf{T}} & (t_1 = String \land t_2 \neq String) \lor (t_1 \neq String \land t_2 = String) \\ t_1 \sqcup_{\mathbf{T}} t_2 & otherwise \end{cases}$$

$$t_1 - t_2 = \begin{cases} Integer & t_1 = Boolean \land t_2 = Boolean \\ \bot_{\mathbf{T}} & t_1 = String \lor t_2 = String \\ t_1 \sqcup_{\mathbf{T}} t_2 & otherwise \end{cases}$$

$$t_1 \times t_2 = \begin{cases} Integer & t_1 = Boolean \land t_2 = Boolean \\ \bot_{\mathbf{T}} & t_1 = String \land (t_2 = String \lor t_2 = Float) \\ \bot_{\mathbf{T}} & t_2 = String \land (t_1 = String \lor t_1 = Float) \\ t_1 \sqcup_{\mathbf{T}} t_2 & otherwise \end{cases}$$

$$t_1 \div t_2 = \left\{ egin{array}{ll} \bot_{\mathbf{T}} & t_1 = Boolean \lor t_2 = Boolean \ Float & otherwise \end{array} \right.$$

To define the Type Domain, we assume that a static type inference has already been run on the program and that it infers the most generic type for a variable in all execution paths of the program. Our Type Domain aims to track more fine-grained information about the types of variables. We assume that the function  $\mathsf{type}(v)$  returns the type of a variable according to the type inference. Then we proceed to define the Type Domain as follows:

$$\mathrm{TYP} \equiv \mathcal{V} \longrightarrow \mathbf{T}$$

- An element  $t \in \text{TYP} = \{v \to typ \mid v \in \mathcal{V} \land typ \in \mathbf{T}\}$ . An element of this domain maps a variable to an element of the type lattice.
- A concretization function  $\gamma_{TYP}$ :
  - We first define a function  $\gamma_c: (\mathcal{V} \to \wp(\mathcal{S})) \longrightarrow \wp(\mathcal{V} \to \mathcal{S})$ , which transforms a mapping from variable to multiple string values to multiple mappings from a variable to a string value.
  - We define an intermediate concretization function  $\gamma'_{\mathbf{TYP}}$ : TYP  $\longrightarrow$   $(\mathcal{V} \to \wp(\mathcal{S}))$  as follows:  $\gamma'_{\mathbf{TYP}}(f) = \lambda_x \cdot \gamma_{\mathbf{T}}(f(x))$ .
  - Finally, the concretization function of the Type Domain  $\gamma_{\text{TYP}}$ : TYP  $\longrightarrow \wp(\mathcal{V} \to \mathcal{S})$  as the chaining of the two previous functions:  $\gamma_c \circ \gamma'_{\text{TYP}}$ . It maps every variable to the possible values it can take according to its type.

- A partial order  $\sqsubseteq_{\text{TYP}}$ :  $t_1 \sqsubseteq_{\text{TYP}} t_2 \iff \forall_{v \in \mathcal{V}}(t_1(v) \sqsubseteq_{\mathbf{T}} t_2(v))$ . For an element of the domain to be smaller than the other, it has to the case that it maps every variable involved in the program to a smaller lattice element than it is mapped in the other element.
- A minimum element  $\perp_{\text{TYP}} = \lambda_x \cdot \perp_{\mathbf{T}}$ . It simply maps every variable to the least element of the type lattice. This represents a type error state.
- A maximum element T<sub>TYP</sub> = λ<sub>x</sub> · type(x). Since the type inference calculates the most generic type a variable can take, the maximum element of this domain maps every variable to the type computed for it by the type inference. If a variable has a type Float in the type inference, then this it the most generic it can have in all paths of the program and therefore we do not assign it to String but to Float.
- A join operator  $\sqcup_{\text{TYP}}$ :  $t_1 \sqcup_{\text{TYP}} t_2 = \lambda_x \cdot t_1(x) \sqcup_{\text{T}} t_2(x)$ . If variable is mapped to two different types in two different paths, then, when these paths are joined, we map the variable to the more *generic* type. That is, the type that is higher in the type lattice Hass diagram.
- A meet operator  $\sqcap_{\text{TYP}}$ :  $t_1 \sqcap_{\text{TYP}} t_2 = \lambda_x \cdot t_1(x) \sqcap_{\mathbf{T}} t_2(x)$ .
- A backward assignment operator  $[X := aexpr](t) = SUBS_{TYP}(t, X, aexpr)$  which is described in Algorithm 1. The substitution algorithm evaluates aexpr and all its sub-expressions and then refines the state t using this evaluation and the type of X.
- A filter operator [cond](t) = t. It does not affect the state.
- A widening operator  $\nabla_{\text{TYP}} \equiv \sqcup_{\text{TYP}}$ .

We note that since the Type Domain is a non-relational domain, a replacement operator  $\mathcal{R}_{TYP}$  and a unification operator  $\mathcal{U}_{TYP}$  return the state unchanged.

#### Algorithm 1 Substitution algorithm for Type Domain

```
\begin{aligned} & \text{function SUBS}_{\text{TYP}}(t, \ x, \ aexpr) \\ & value \leftarrow t(x) \\ & t(x) \leftarrow \text{type}(x) \\ & eval \leftarrow empty \ map \\ & eval \leftarrow \text{EVAL}_{\text{TYP}}(aexpr, eval) \\ & \text{REFINE}_{\text{TYP}}(aexpr, eval, eval[x] \sqcap_{\mathbf{T}} value, t) \\ & \textbf{return} \ t \end{aligned}
```

#### Algorithm 2 Expression evaluation for Type Domain

```
function EVAL<sub>TYP</sub>(expr, eval)

if expr is a literal then

eval[expr] \leftarrow type of literal

return eval

if expr \in \mathcal{V} then

eval[expr] \leftarrow type(v)

return eval

if expr = expr1 \diamond expr2 where \diamond \in \{+, -, \times, \div\} then

eval[expr] \leftarrow EVAL<sub>TYP</sub>(expr1) \diamond EVAL<sub>TYP</sub>(expr2)

return eval
```

#### Algorithm 3 Expression refinement for Type Domain

```
function REFINE<sub>TYP</sub> (expr, eval, value, t)

if expr is a literal then

return t

if expr \in \mathcal{V} then

t(x) \leftarrow eval[expr] \sqcap_{\mathbf{T}} value

return t

if expr = expr1 \diamond expr2 where \diamond \in \{+, -, \times, \div\} then

value \leftarrow eval[expr] \sqcap_{\mathbf{T}} value

refine1 \leftarrow \text{REFINE}_{\text{TYP}}(expr1, eval, value, t)

refine2 \leftarrow \text{REFINE}_{\text{TYP}}(expr2, eval, value, refine1)

return refine2
```

#### 2.3.2 The Octagon Domain

The Octagon Domain was introduced by Antoine Miné in [6] as a numerical relational domain that can keep track of relations the form  $\pm X \pm Y \geq c$  where X and Y are program variables. We use the Octagon Domain in our analysis in order to keep track of relations between variables such as  $sequence\_length \leq max \ length$  in Listing 2.1.

As explained in section 2.2.1, in order for an existing domain to work with our analysis framework, it needs to define a *replacement* operator that, whenever an input is read, introduces a new variable to denote this input and the constraints and relations associated with it before it is stored in the stack. In the same section, we also explain the need to define a unification operator to address the problem of inconsistent environments arising from introducing new variables into our analysis.

```
1 x: int = input()
2 if x > 10:
3 y: int = int(input())
4 if y + x <= 10:
```

Listing 2.2: Example of Unification

We define a replacement operator  $\mathcal{R}_O(o, v, l_i)$  for the Octagon Domain, where o is an octagon, v is the variable that is being read as input and  $l_i$  is the program point at which the input is being read. The operator works by first adding the variable  $l_i$  to the octagon. This variable has no constraints associated with it at first. Then, assuming the Octagons Domain defines a backward assignment operator, we perform the substitution  $[v := l_i]_O$ . Thus, v is replaced by  $l_i$  in all the constraints of the octagon and v becomes top.

We define the unification operator  $\mathcal{U}_O(o_1, o_2)$  where both  $o_1$  and  $o_2$  are octagons. The operator is applied before every join, meet or widening operation in the analysis. We assume every element of the Octagon Domain keeps a list of its variables in the order in which they were added during the analysis. For every variable  $l_i$  in  $o_1$  and  $l_j$  in  $o_2$ , that have the same order in the respective variable lists, if j < i, we replace  $l_i$  with  $l_j$  in  $o_1$ . That is, when we have two variables that represent inputs read in the same order in two different paths in the analysis, we replace the variable that represents a later program point, with a variable that represents an earlier program point. After this step, if there are variables in  $o_2$  which are not in  $o_1$ , they are added to  $o_1$ . Note that in this case the operator is asymmetric and needs to be called twice,  $\mathcal{U}_O(o_1, o_2)$  and  $\mathcal{U}_O(o_2, o_1)$ , before every join, meet and widening.

To illustrate the replacement and unification operators we introduce Listing 2.2. In the then-branch of the if-statement, we read a variable y and assert the condition y + x > 10. In the else-branch, we read a variable z and enforce the condition z + x > 20. If we trace a backward analysis on this program and employing the  $\mathcal{R}_O$  we defined earlier in this section, then in the then-branch, we get  $\mathcal{R}_O(\{y+x>10\},y,l_3)=\{l3+x>10\}$  and similarly in the else-branch we get the relation  $\{l_7+x>20\}$ . A join needs to be performed on these two elements at the head of the if-statement. Since our analysis treats  $l_3$  and  $l_7$  as different variables, without the unification operator, the join will yield top.

As mentioned earlier, our analysis does not care about the specific variables representing input values, but rather about the order in which they occur in the list of input values which the program reads in their respective paths. In this example, we only care that after reading x we read another variable whose summation to x had to be greater than 20, otherwise the program will crash. Therefore, for the purpose of our analysis,  $l_3$  and  $l_7$  should be treated as the same variable when joining the two paths at the head of the if-condition since both of them are read second in their respective paths. We call the unification operator once as follows:  $\mathcal{U}_O(\{l_3+x>10\},\{l_7+x>20\})=\{l_3+x>10\}$  and then another time switching the operands as follows:  $\mathcal{U}_O(\{l_7+x>20\},\{l_3+x>10\})$ 

10}) = { $l_3 + x > 20$ }. Then a join can be performed between { $l_3 + x > 10$ } and { $l_3 + x > 20$ } which will give us  $l_3 + x > 20$ .

#### 2.3.3 The Character Inclusion Domain

The Character Inclusion Domain, as defined in [7], is an abstract domain that maps a string into two sets: a set of characters that are certainly included in the string and another set of characters that may be included in the string. For a finite alphabet A, we define a character inclusion lattice as follows:

- An element  $c \in CI = \{(C, M) : C, M \in \wp(A) \land C \subseteq M\} \cup \bot_{CI}$ . This can be understood as an abstraction of a string which certainly contains all the characters in C and is only allowed to contain characters in M.
- A concretization function  $\gamma_{CI}$ :  $\langle CI, \sqsubseteq_{CI} \rangle \longrightarrow \langle A^*, \subseteq \rangle$  such that  $\gamma_{CI}((C,M)) = \{x \mid x \in A^* \land \mathtt{char}(x) \supseteq C \land \mathtt{char}(x) \subseteq M\}$ , where  $\mathtt{char}(x)$  is a function that returns the set of all characters in a string x. An element (C,M) concertizes to the set of all string which contain all the characters in C and which do not contain any characters outside M.
- A partial order:  $(C_1, M_1) \sqsubseteq_{CI} (C_2, M_2) \iff (C_1 \supseteq C_2, M_1 \subseteq M_2)$ . This order indicates that the fewer the certainly included characters and the more the maybe included characters, the more strings we represent. For example the element  $(\{a\}, \{a, b\})$  concertizes to  $\{a, aa, ab, aaa, aab, ...\}$  while the element  $(\emptyset, \{a, b\})$  concertizes to  $\{\varepsilon, a, b, aa, ab, bb, ...\}$ . The restriction of having a in the certainly included set makes the values  $\{\varepsilon, b, bb, bbb, ...\}$  disappear from the concretization.
- A least element  $\perp_{CI}$  which represents a failure state.
- A greatest element  $\top_{CI} = (\emptyset, A)$  which represents a string that can contain any combination of characters from the alphabet.
- A join operator:  $(C_1,M_1)\sqcup_{CI}(C_2,M_2)=(C_1\cap C_2,M_1\cup M_2).$  The soundness of this operator can be stated as follows:  $\{x\mid x\in A^*\wedge \operatorname{char}(x)\supseteq C_1\wedge \operatorname{char}(x)\subseteq M_1\}\cup \{x\mid x\in A^*\wedge \operatorname{char}(x)\supseteq C_2\wedge \operatorname{char}(x)\subseteq M_2\}\subseteq \{x\mid x\in A^*\wedge \operatorname{char}(x)\supseteq C_1\cap C_2\wedge \operatorname{char}(x)\subseteq M_1\cup M_2\} \iff \gamma_{CI}((C_1,M_1))\cup \gamma_{CI}((C_2,M_2))\subseteq \gamma_{CI}((C_1,M_1)\sqcup_{CI}(C_2,M_2)).$  If we have two elements  $(\{a,b\},\{a,b,c\})$  and  $(\{a\},\{a,b,d\})$  that we would like to join, then we can only say that the resulting element will *certainly* contain the character a (the intersection of C sets), but it may contain any of the characters a, b, c or d (the union of the two M sets).
- A meet operator:  $(C_1, M_1) \sqcap_{CI}(C_2, M_2) = (C_1 \cup C_2, M_1 \cap M_2) \cup \bot_{CI}$ . The bottom is to account for cases when  $C_1 \cup C_2 \not\subseteq M_1 \cap M_2$ . The soundness of this operator can be stated as follows:  $\{x \mid x \in A^* \wedge \operatorname{char}(x) \supseteq C_1 \wedge \operatorname{char}(x) \subseteq M_1\} \cap \{x \mid x \in A^* \wedge \operatorname{char}(x) \supseteq C_2 \wedge \operatorname{char}(x) \subseteq M_2\} \subseteq \{x \mid x \in A^* \wedge \operatorname{char}(x) \supseteq C_1 \cup C_2 \wedge \operatorname{char}(x) \subseteq M_1 \cap M_2 \cap M_$

 $M_2$   $\iff \gamma_{CI}((C_1, M_1)) \cap \gamma_{CI}((C_2, M_2)) \subseteq \gamma_{CI}((C_1, M_1) \cap_{CI} (C_2, M_2)).$  The meet works in the opposite way to the join. If we have two elements  $(\{a, b\}, \{a, b, c\})$  and  $(\{a\}, \{a, b, d\})$  which we would like to meet, we can say that the resulting element will *certainly* contain both a and b (the union of the two C sets) and that it may contain only a and b (the intersection of the two M set) as well.

- A concatenation operator:  $((C_1, M_1) +_{CI} (C_2, M_2)) = ((C_1 \cup M_1), (C_2 \cup M_2))$ . When concatenating two string, the resulting string will *certainly* that characters that are certainly included in both strings and *may* contain the characters that may be included in both strings as well.
- A widening operator  $\nabla_{CI} \equiv \sqcup_{CI}$ . The widening operator is the same as the join.

Then we define the Character Inclusion Domain as a mapping from variables to elements of the character inclusion lattice as follows:

$$CHAR \equiv \mathcal{V} \longrightarrow CI$$

- An element  $c \in CHAR = \{v \longrightarrow ci \mid v \in \mathcal{V} \land ci \in CI\}$ . Every element in the Character Inclusion Domain maps a variable to an element in the character inclusion lattice.
- A concretization function  $\gamma_{\text{CHAR}}$ :
  - We first define a function  $\gamma_c: (\mathcal{V} \to \wp(\mathcal{S})) \longrightarrow \wp(\mathcal{V} \to \mathcal{S})$ , which transforms a mapping from variable to multiple string values to multiple mappings from a variable to a string value.
  - We define an intermediate concretization function  $\gamma'_{\text{CHAR}}$ : CHAR  $\longrightarrow$   $(\mathcal{V} \to \wp(\mathcal{S}))$  as follows:  $\gamma'_{\text{CHAR}}(f) = \lambda_x \cdot \gamma_{CI}(f(x))$ .
  - Finally, we define the concretization function of the Character Inclusion Domain  $\gamma_{\text{CHAR}}: \text{CHAR} \longrightarrow \wp(\mathcal{V} \to \mathcal{S})$  as the chaining of the two previous functions:  $\gamma_c \circ \gamma'_{\text{CHAR}}$ .
- A partial order  $\sqsubseteq_{\text{CHAR}}$ :  $c_1 \sqsubseteq_{\text{CHAR}} c_2 \iff \forall_{v \in \mathcal{V}} (c_1(v) \sqsubseteq_{CI} c_2(v))$ .
- A minimum element  $\perp_{\text{CHAR}} = \lambda_x \cdot \perp_{CI}$ . Every variable is mapped to the smallest element in the character inclusion lattice.
- A maximum element  $\top_{\text{CHAR}} = \lambda_x \cdot \top_{CI}$ . Every variable is mapped to the biggest element of the character inclusion lattice.
- A join operator  $\sqcup_{\text{CHAR}}$ :  $c_1 \sqcup_{\text{CHAR}} c_2 = \lambda_x \cdot c_1(x) \sqcup_{CI} c_2(x)$  which maps a variable to the joining of the two lattice elements to which it was mapped in  $c_1$  and  $c_2$ .
- A meet operator  $\sqcap_{\text{TYP}}$ :  $c_1 \sqcap_{\text{CHAR}} c_2 = \lambda_x \cdot c_1(x) \sqcap_{CI} c_2(x)$  which maps a variable to the meet of the two lattice elements to which it was mapped in  $c_1$  and  $c_2$ .

- A backward assignment operator  $[X := aexpr](c) = SUBS_{CHAR}(c, X, aexpr)$  which is described in Algorithm 4. It evaluates aexpr and all its sub-expressions and refine the state c with the values computed in this evaluation and the value to which X was mapped before the assignment is invoked. Meanwhile, X becomes top.
- A filter operator  $[\![cond]\!](c) = \text{FILTER}_{\text{CHAR}}(cond, c)$  which is described in Algorithm 5.
- A widening operator  $\nabla_{\text{CHAR}} \equiv \sqcup_{\text{CHAR}}$  which is equivalent to the join.

As is the case for the Type Domain, the replacement operator  $\mathcal{R}_{CHAR}$  and a unification operator  $\mathcal{U}_{CHAR}$  do not produce any changes on the state since this domain is non-relational.

#### Algorithm 4 Substitution algorithm for Character Inclusion Domain

```
function SUBS<sub>CHAR</sub>(c, x, aexpr)

value \leftarrow c(x)

c(x) \leftarrow \top_{CI}

eval \leftarrow emtpy \ map

eval \leftarrow \text{EVAL}_{\text{CHAR}}(aexpr, eval, c)

REFINE<sub>CHAR</sub>(aexpr, eval, eval[x] \sqcap_{CI} value, c)

return \ c
```

#### Algorithm 5 Filter algorithm for Character Inclusion Domain

```
function FILTER<sub>CHAR</sub> (cond, c)
    if cond = (cond1 \land cond2) then
         c1 \leftarrow \text{FILTER}_{\text{CHAR}}(cond1, c)
         c2 \leftarrow \text{FILTER}_{\text{CHAR}}(cond2, c)
         return c1 \sqcap_{\text{CHAR}} c2
    else if cond = (cond1 \lor cond2) then
         c1 \leftarrow \text{FILTER}_{\text{CHAR}}(cond1, c)
         c2 \leftarrow \text{FILTER}_{\text{CHAR}}(cond2, c)
         return c1 \sqcup_{\text{CHAR}} c2
    else if cond = (expr1 == expr2) then
         eval1 \leftarrow empty\ map
         eval1 \leftarrow \text{EVAL}_{\text{CHAR}}(expr1, eval1, c)
         eval2 \leftarrow empty\ map
         eval2 \leftarrow \text{EVAL}_{\text{CHAR}}(expr2, eval2, c)
         REFINE_{CHAR}(expr1, eval1, eval1[expr1], c)
         REFINE_{CHAR}(expr2, eval2, eval2[expr2], c)
    return c
```

#### Algorithm 6 Expression evaluation for Character Inclusion Domain

```
function EVAL<sub>CHAR</sub>(expr, eval, c)

if expr is a literal then

eval[expr] \leftarrow (\operatorname{char}(x), \operatorname{char}(x))

return eval

if expr \in \mathcal{V} then

eval[expr] \leftarrow c(expr)

return eval

if expr = expr1 + expr2 then

eval[expr] \leftarrow \text{EVAL}_{\text{CHAR}}(expr1) +_{CI} \text{EVAL}_{\text{CHAR}}(expr2)

return eval
```

#### Algorithm 7 Expression refinement for Character Inclusion Domain

```
function REFINE_{CHAR}(expr, eval, (C, M), c) 

if expr is a literal then 

return c 

if expr \in \mathcal{V} then 

c(x) \leftarrow eval[expr] \sqcap_{CI} (C, M) 

return c 

if expr = expr1 + expr2 then 

(C, M) \leftarrow eval[expr] \sqcap_{CI} (C, M) 

refine1 \leftarrow \text{REFINE}_{\text{TYP}}(expr1, eval, (\emptyset, M), c) 

refine2 \leftarrow \text{REFINE}_{\text{TYPE}}(expr2, eval, (\emptyset, M), refine1) 

return refine2
```

# 3 Implementation

We implemented our static analysis and input checker in Python as an extension to the Lyra project [9]. We then implemented a plug-in for IntelliJ IDEA that enables the user to use the analysis and checker as a tool. The plug-in implementation is in Java.

We implement the Assumption Domain described in section 2.2 in a class we call AssumptionState. The AssumptionState class has a list of sub-states which represents the sub-domains in the Assumption Domain. The Type Domain already exists as part of Lyra. We implemented separate classes for the Octagon and Character Inclusion domains. For the Octagon domain, we used the Python interface of the ETH Library for Numerical Analysis (ELINA) [10]. We added extra logic in order to translate the Lyra representation of expressions and conditions into a representation that is compatible with ELINA and also to implement the replacement and unification operators mentioned in section 2.3.2. The Character Inclusion domain is implemented as described in section 2.3.3 with the addition of support for built-in python functions that perform checks on the characters included in a string such as isalpha(), isalnum(), isdecimal(), isdigit(), islower() and isupper().

Every one of the sub-states keeps track of all program variables. If a variable belongs to a type that the domain cannot handle, then its value will always be top in this domain. Therefore, an integer variable will always be mapped to top in the Character Inclusion Domain and a string variable will never have any constraints on it in the Octagon Domain. We require all sub-states to define functions that convert their constraints into JSON object and parse them back from JSON object. We also require every sub-state to implement an input-checking function that, given a input value read from a file, is able to tell whether this value satisfies the constraints that the sub-state represents or not.

The class InputStack also has the stack described in section 2.2.2 which implemented as an extension to the already existing Stack interface in Lyra. We define the pop and push operators for it as well as the structure of individual stack layers. The stack layer is implemented in the class InputLattice which represents a list of possibly repeated constraints on the input data (see the set I in section 2.2.2) and defines a mechanism for recording assumptions on the top layer as well as for joining lists of assumptions from different paths of the analysis.

Our implementation follows a hierarchy similar to that used in [4]. We

implement an AssumptionController class which acts as the entry point for our tool and takes as input the path to a Python code file and an input data file. This class controls three other classes that are in the layer right below it in the hierarchy: AssumptionAnalysis which extends the Lyra Runner class, JSONHandler and InputChecker. The AnalysisAnalysis class is responsible for running a backward static analysis on a given Python program. The JSONHandler class is responsible for writing the assumptions resulting from the analysis into a JSON file and later reading them back from the JSON file. The InputChecker runs a checking algorithm an a given input file and produces a list of errors present in the file.

The analysis starts with an instance of the AssumptionState class set to top and traverses the program paths backward calling the appropriate functions from the class at every step. The final result of the analysis is stored in the stack of the final state and it is of type InputLattice. When the analysis terminates, the controller retrieves the result and passes it to the JSONHandler class which writes the assumptions into JSON file by calling the functions defined in every sub-state. For subsequent runs of the controller, it checks if the code of the program has been modified and if it has not been modified, it does not run the analysis again but calls the JSONH and ler to read the assumptions for that program from the existing JSON file and convert them back into an Input Lattice object. The assumptions are then passed to the Input Checker class along with the input file which is required to be checked for errors. The InputChecker traverses the input file line by line and checks the value in every line against the corresponding assumption by calling the input-checking functions defined in every sub-state. It produces a dictionary which maps a line number in the input file to a Checker Error object which contains an appropriate error message describing how the value on this line violates an assumption.

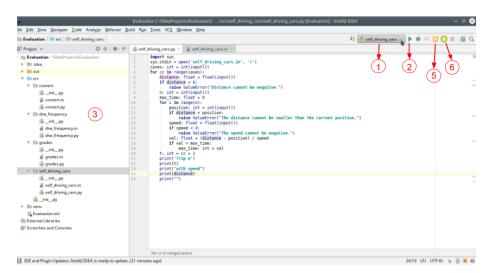


Figure 3.1: Screenshot of the IntelliJ IDEA Interface with the Plug-in

We implement a plug-in for IntelliJ IDEA that allows a user to run our analysis and input checker. The decision to implement such a plug-in was based on feedback received from participants in the user study conducted in [4]. The interface which is presented to the user is shown in Figure 3.1. To run the tool on a specific Python program, we must create a run configuration for it and select it from the drop-down menu labeled 1 in the figure. Using the green button labeled 6 we can choose which input data file to check. Then we can run the tool via the button labeled 5 in the figure. The lines which contain errors in the input file will be underlined in red and when the user hovers them with the mouse, an error message will appear. In addition to that, a pop-up message will always appear at the bottom of the screen indicating the location and error message of the first error value in the file. This functionality was added to guide the user step by step in fixing the errors in the file from top to bottom. If the tool cannot detect any more errors in the file, a green pop-up appears at the bottom of the screen indicating so.

# 4 Evaluation

In this section we present the evaluation of the work done in this thesis. In section 4.1, we present methodology and result of a user study we conducted in order to evaluate the usability of our tool. In section 4.2, we present an evaluation of the static analysis we defined in section 2.

# 4.1 User Study

We conducted a user study to evaluate the usability of the tool we developed. We asked ten users, five who have a background in computer science and five who study or work in other fields, to use our tool and give us feedback on how helpful they find it. The methodology of the user study is presented in the next section and the results are presented in section 4.1.2.

## 4.1.1 Methodology

In our user study, we asked our users to do two experiments. For every experiment we presented the user with a programs, accompanied by an input data file which contains some errors that will cause the program to crash, and asked them to try to fix the errors in the data file so that the program runs without crashing. For one experiment they were asked to do this without any help and for the other they were asked to do this with the help of our tool. In the sections below we describe the programs and the input data we use and the procedure of the two experiments.

#### **Programs and Input Data**

We used four programs in our user study. The programs 'Grades' (Listing 4.1) and 'Self-Driving Cars' (Listing 4.3) are taken from the user study conducted in [4]. The programs 'Convert' (Listing) and 'DNA Frequency' we obtained from the online sources [cite] and [cite] respectively. The code of the programs so that it can be handled by our analysis. For example, we removed statements that contain lists and function call. We also added new statement which provide more interesting assumptions on these input data. We constructed the input datasets to contain an average of eight errors per file. The errors we added

can be classified into two main types: errors which appear as a result of typing mistakes, such as the number **6.5**, which represents a grade, being typed as **6..5** on line 32 in Listing 4.2, and errors which result from some garbage values being printed in the data file due to, for example, the conversion of data from one format to another such as the value **G**, which represents a DNA base, being printed as ..**G** on line 6 in Listing 4.8.

#### Experiments

As mentioned earlier, we asked every participant in our user study to do two experiments, one after the other. In both experiments the user was presented with a Python program and a text file containing some input data which has errors that will cause the program to crash. They were asked to not change the code of the program but to change the input data, only adding or modifying lines without deleting them, such that the program runs without crashing. The users were presented with an online form that walked them through the experiments step by step. Before starting the experiments, the users were asked to answer some general questions in the form indicating their age, field of study, current occupation and their level of familiarity with programming on five-point Likert scale ranging from 1 to 5.

In both experiments, the form explained to them the task that they are required to perform and then asked them to choose one of the four programs based on their month of birth to ensure some randomness in the experiment. They were handed a sheet of paper containing a brief description of the task the program tries to achieve. In the experiment without the tool, they were given instructions on how to run a Python program in IntelliJ IDEA, while in the experiments with the tool, they were given instructions on how to run the tool and what kind of error messages they should expect to see. Then we allowed the user to work on the problem for eight minutes each. Both the form and the problem descriptions are shown in the appendix.

After every task, we asked the users to answer some questions in the form. For both experiments we asked if they had been able to fix the errors in the input data and how many minutes they spent on this task. For the experiment with the tool, we added a question about whether or not they were able to run the program without raising any errors. This is to account for the cases were the user was able to fix all the errors detected by the tool, but the tool failed to flag some erroneous data due to imprecision in the analysis.

These questions were followed by a group of questions on a five-point Likert scale in which the options were: Strongly Disagree, Disagree, Neutral, Agree, Strongly Agree. In both experiments, we asked how frustrated the users felt trying to solve the problems and how understandable they found the error messages printed by the program in the first experiment and displayed by the tool in the second experiment. We added two more questions in the second experiment asking them to rate how user-friendly they found the tool and whether they would rather fix the errors in a data file with or without the help of the

tool.

At the end of the form there were two open-ended questions that aimed to get feedback from the users in their own words. The first questions asked the users what they liked about the tool and the second questions asked them to suggest improvements that they think should be added to the tool. The form as well as the descriptions of the problems can be found in the appendix.

#### 4.1.2 Results

In this section we present some statistics that we gathered from our user study along with some insights that can guide future work on this project.

The ages of the participants ranges from 19 to 31 with an average of 23.4. Five participants have backgrounds in computer science (one user used the term "informatics" in the form), while two participants have backgrounds in physics, two in environmental engineering and one in mathematics. Six of our participants are bachelor's students, two are master's students, one participant is a postdoctoral researcher and one is a teaching assistant. When asked to rate their familiarity with programming, the majority of participants who rated their experience 4 or above, as expected, have a background in computer science. More details can be seen in Figure 4.1. In all the figures in which we distinguish between computer science and non-computer science participants we label the former as "CS" and the later as "non-CS".

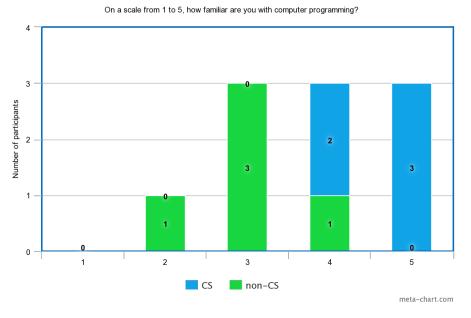


Figure 4.1: Self-rating programming experience

We found that in the experiment without the tool, only one participant was

able to fix all the errors in the input file successfully and it took them 5 and a half minutes. That participant studies computer science and they had rated their familiarity with programming 4 on the five-point scale. All other participants had at least one error in their data files when the assigned 8 minutes of the experiment were over.

In the second experiment with the tool, 9 out of 10 participants were able to fix all the errors detected by the tool within the 8 minutes of the experiment. The participant who was not able to do so had only one error left in their file at the end of the 8 minutes. They were from a computer science background and had rated their familiarity with programming 5 on the five-point scale. The time (in minutes) taken by each participant is shown in Figure [add figure]. We note that, on average, participants without computer science backgrounds took 4.9 minutes, while those with computer science background took 5.7 minutes. We noticed that some participants with computer science background first tried to solve the problem themselves without the help of the tool, while most participants with no background in computer science focused on understanding the error messages of the tool and fixing the input value which they pointed out. The user who could not fix all the errors in the file in the assigned 8 minutes had spent some time trying to solve the problem by examining the code and matching it to the input data. This is a possible explanation for why participants with no background in computer science took less time on average to solve the problem with the tool.

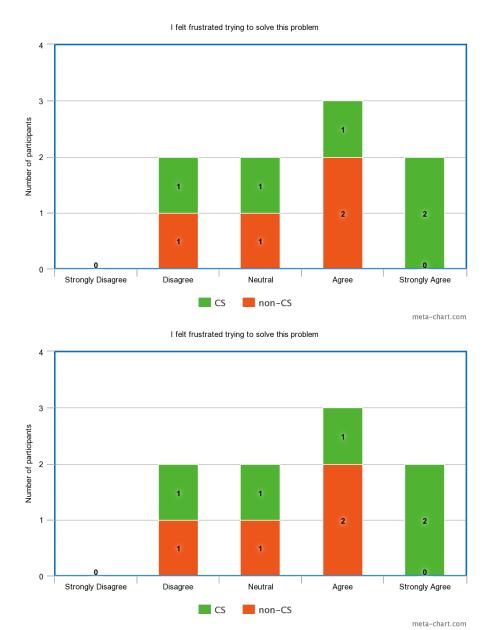


Figure 4.2: Measure of frustration

The plots in Figure 4.2 show that 6 users reported some level of frustration trying to fix errors in the data without the help of our tool, while only one user reported some level of frustration trying to achieve the same goal with the help of the tool. This, as we expected, shows that our tool created an improvement

in the overall debugging experience of the users. An interesting result was that the number of Computer Science participants who felt frustrated trying to debug the data without the help of our tool was less than then the number of non-Computer Science users who felt frustrated performing the same task. A possible explanation for this result is that, as we noticed during the experiments, participants with experience in Computer Science had the expectation that they would be able to examine the code and fix the errors in the data somewhat easily because of their familiarity with programming, unlike non-Computer Science participants who had already expected the task to be challenging.

When asked to state what they liked about the tool, users mentioned that it gave clear and detailed error messages that appeared in the data file and, therefore, they did not have to examine the code to find out the errors in the data. Some of the suggestions that users made to improve the tool was to make it faster and to print the error messages in the console and to highlight which line of code was the source of the error instead of just highlighting the error in the data file.

From the previous results, we conclude that a tool that guides users through data debugging is a useful tool and helps the users achieve their goals in less time and with less frustration. Some future improvements would be to enhance the performance such that the tool is faster, to introduce an error console in which the users can read the errors all at once without having to scan the data file looking for marked errors and to mark the code lines at which the errors occur instead of just marking the input data lines.

```
subject: str = input()
 1
2
    homeworks: int = int(input())
     students: int = int(input())
3
     for i in range(students):
4
      id: str = input()
5
      sum: float = 0
6
7
      \max: float = 0
       for j in range(homeworks):
8
9
         grade: float = float(input())
10
         best: float = float(input())
         if grade < 0 or grade > best:
11
12
         raise ValueError
13
         sum: float = sum + grade
         \max: float = \max + best
14
15
       average: float = sum / max * 100.0;
16
       print("Student ID:")
17
       print(id)
18
       print("Average homework grade:")
19
20
       print (average)
       grade: float = float(input())
21
22
       best: float = float(input())
```

```
23 if grade < 0 or grade > best:
24 raise ValueError
25 final_grade: float = grade / best * 100.0
26 print("Final test grade:")
27 print(final_grade)
```

Listing 4.1: Code for Program 'Grades'

```
1
     CS 101: Introduction to Computer Science
2
3
     4
     34 - 8342
4
5
     9
6
     10
7
     12
8
     12
9
     11
10
     10
11
     45
12
     50
     34 - 14002
13
14
     6
15
     10
16
     13
17
     12
18
     -9
19
     10
20
     51
21
     50
22
     31 - 1234
23
     5.5
24
     10
25
     9
26
     12
27
     10#
28
     10
29
     -43
     50
30
     34 - 2373
31
32
     6..5
33
     10
34
     11
35
     12
     7
36
     10
37
38
     48
```

Listing 4.2: Input Data for 'Grades'

```
2 | cases: int = int(input())
3 for case in range (cases):
    distance: float = float(input())
     if distance < 0:
5
       raise ValueError("Distance cannot be negative.")
6
7
    n: int = int(input())
    \max: float = 0
8
9
    for i in range(n):
10
       position: int = int(input())
       if \ \ distance \ < \ position:
11
         raise ValueError("Distance cannot be smaller than
12
      the current position.")
      speed: float = float(input())
13
       if speed < 0:
14
         raise ValueError("Speed cannot be negative.")
15
       val: float = (distance - position) / speed
16
17
       if val > max:
        \max: int = val
18
19
     t: int = case + 1
    print("Trip:")
20
21
    print(t)
22
    print("with speed")
    print(distance / max)
```

Listing 4.3: Code for Program 'Self-Driving Cars'

```
4
 1
 2
      10.5
 3
      3
 4
      4
 5
      40
 6
      6
 7
      45.5
 8
      12
 9
      50
10
      120
11
      5>>
12
      25 \mathrm{km}
13
      90
14
      45
15
      99 \text{km/h}
16
      -57
```

```
-123
17
     76
18
     130
19
20
     1200
21
     140
22
     50
23
     2
24
     60
25
     120
26
     30
27
     112
     200
28
     2
29
30
     100
     120
31
     170
32
```

Listing 4.4: Input Data for 'Self-Driving Cars

```
1 | \text{items}: \text{int} = \text{int}(\text{input}())
2 | \mathbf{if} | \text{ items} = 0:
     raise ValueError
3
4 for i in range(items):
     name: str = input()
5
     weight: float = int(input())
 6
     if weight \leq 0:
 7
8
       raise ValueError
     unit: str = input()
9
10
     if unit = 'pounds' or unit = 'lb' or unit = 'lbs':
       weight: float = weight * 453.592 * 1e-3
11
12
     elif unit = 'ounces' or unit = 'oz' or unit = 'oz.':
       weight: float = weight * 28.35 * 1e-3
13
14
     elif unit = 'grams' or unit = 'gms' or unit = 'g':
15
       weight: float = weight * 1e-3
16
     elif unit = 'kilograms' or unit = 'kilo' or unit = '
      kg ':
17
       pass
     else:
18
       raise ValueError
19
     \mathbf{print}\,(\,{\tt "Item}:\ {\tt "}\ +\ {\tt name}\,)
20
     print("weight:")
21
22
     print(weight)
23
     print("kg")
```

Listing 4.5: Code Program 'Convert'

```
10#
1
2
     earphones
3
     300
4
    gramx
5
    stereo set
6
7
    kg
    camera tripod
8
9
    1@
10
    qounds
11
     trolly suitcase
12
     30
13
    lbs
    laptop lenovo 5070
14
15
16
    laptop lenovo thinkpad
17
    2>>
18
19
    pounds
20
    12x envelope
21
    35
22
    gm.
    bic blue pens 4-piece set
23
24
     125
25
    grams
26
    travel compass
27
28
    grams
29
    vacuum cleaner
    2#0
30
31
```

Listing 4.6: Input Data for 'Convert'

```
sequences: int = int(input())
1
2
    if sequences < 1:
      raise ValueError("Expecting at least one DNA sequence
3
    for s in range (sequences):
4
      length: int = int(input())
5
6
      a: int = 0
7
      c: int = 0
      g: int = 0
8
      t: int = 0
10
      for i in range(length):
```

```
base: str = input()
11
         if base == 'A':
12
         a: int = a + 1
13
         elif base == 'C':
14
15
         c: int = c + 1
16
         elif base == 'G':
17
         g: int = g + 1
         elif base == 'T':
18
         t: int = t + 1
19
20
         else:
21
         raise ValueError
22
       separator: str = input()
23
       if separator = '.' or separator = '\#':
24
       else:
25
         raise ValueError
26
       print("Frequency of A nucleotide:")
27
28
       print("Frequency of C nucleotide:")
29
30
       print(c)
       print("Frequency of G nucleotide:")
31
32
       print(g)
       print("Frequency of T nucleotide:")
33
34
       \mathbf{print}(t)
       CG content: float = (c + g) / (a + t + c + g) * 100.0
35
       print("CG content: ")
36
       print(CG content)
37
       print("%")
38
```

Listing 4.7: Code for Program 'DNA Frequency'

```
3..
 1
 2
       10
 3
       Α
       O
 4
       \mathbf{C}
 5
        . . G
 6
       G
       Χ
 8
 9
       Τ
       Α
10
       \mathbf{C}
11
12
       G
13
       #
14
       15
15
       \mathbf{C}
```

```
G_{0}
16
        Τ
17
18
        Α
        \mathbf{C}
19
20
        &C*
        G
21
        Т
22
        O
23
24
        G
25
        Α
        \mathbf{C}
26
        T))
27
        G
28
        Τ
29
30
        5
31
32
        Α
33
        \mathbf{C}
        Т
34
```

Listing 4.8: Input Data for 'DNA Frequency'

### 4.2 Evaluation of the Static Analysis

We evaluated our static analysis using 25 code examples, including slightly varied versions of Listings 4.1, 4.3, 4.5, 4.7 which were used in our user study, and an example which we took from [4]. The other examples we constructed ourselves in order to test various aspects of our analysis.

#### 4.2.1 Methodology

Our aim was to measure both the soundness and the precision of our analysis. For every code example, we examined the assumptions inferred by the analysis on each of its inputs and compared it to assumptions that we had computed manually to see whether it was sound and precise or not. The results are shown in table 4.1. The column "Inputs" counts the number of input values read in each program. We consider all of the assumptions associated with a single input value to be one assumption. If one domain computes an unsound assumption on an input value, then the whole assumption on this input value is considered unsound and not counted in the "Sound" column in our table and, similarly, if one domain computes an imprecise assumption on an input value, then the whole assumption is considered imprecise and counted in the "Imprecise" column.

We added the column "Source of imprecision" to gain more insights on how to tune the precision of our analysis and what improvements could be introduced in future work to gain higher precision. The first three sub-columns "OCT", "CHAR" and "TYP" count the number of inputs for which the assumption of the Octagon, Character Inclusion and Type domains were imprecise, respectively. The fourth sub-column "Design" counts imprecision resulting from limitations in the design of our analysis such as loss of precision due to joins. One imprecise assumption can be counted in more than one of these sub-columns if it has more than one cause. If, for example, both the Type and Octagon domains computed imprecise assumptions on the same input value, then we add one in both the "OCT" and "TYP" columns.

#### 4.2.2 Results

Table 4.1 shows that we counted 73 inputs in all of our examples and that the analysis was sound for all of them, meaning that it did not compute any assumptions that would cause a correct input value to be flagged as an error. There were 29 imprecisions, meaning that for 29 inputs, we could find at least one input value that satisfies the assumptions inferred by our analysis that would still cause the program to crash.

The Character Inclusion Domain was the least precise domain with 16 imprecise assumptions. We noticed that in 13 of these cases, the loss of precision was due to its inability to distinguish the order or frequency of characters in a string. For example, in our running example in Listing 2.1, it infers the assumption  $(\phi, \{'A', T', C', G'\})$  for the variable base. A string such as "AATC" would satisfy this assumption, but it would still cause the program to raise an error on runtime. The remaining instances of imprecision were caused by the fact that in our implementation of boolean functions such as <code>isalpha()</code>, we infer an assumption such as  $(\phi, \{'a', b', c', ...\})$  with a "certainly" set that is empty, which causes the empty string to satisfy this assumption, while in fact <code>isalpha("")</code> evaluates to false.

The Octagon Domain was imprecise in 7 cases. In 2 cases, the imprecision was due to its inability to detect inequality constraints such as  $n \neq 0$ . There were three cases in which the constraints were non-octagonal such as a+b < c. The remaining two cases information was lost by joining two branches. The Type Domain was imprecise in 4 cases, all of which were because of joining two branches.

There were 4 imprecisions due to the limitations in the design of our analysis and the fact that if we join two branches and one of them has more input values than the other, we lose some information on the branch with more inputs. We discuss the possibility to overcome this limitation when we discuss future work in section 5.

It is evident from our results that, although the our analysis has some limitations, a significant improvement in precision can be achieved either by using more domains in our analysis or by replacing the domains we have used with more powerful domains. For example, if we add the Sign Domain to our analysis, we can capture the 2 assumptions of the form  $n \neq 0$  which the Octagon Domain misses. The Polyhedra Domain can also capture the 3 constraints of the form a+b < c which the Octagon Domain cannot capture. If we replace

Table 4.1: Results of Static Analysis Evaluation

Program name	Inputs	Sound	Imprecise	Source	e of impre	ecision	
		ı	ı				
				OCT	CHAR	TYP	Design
$if\_condition.py$	2	2	0	0	0	0	0
add.py	2	2	0	0	0	0	0
cast.py	1	1	0	0	0	0	0
assume 1.py	1	1	1	0	1	0	0
basic.py	1	1	1	0	1	0	0
concatenation.py	2	2	2	0	2	0	0
merge.py	3	3	1	0	0	1	1
must.py	1	1	1	0	1	0	0
substitution.py	3	3	3	0	3	0	0
cars.py	5	5	1	1	0	0	0
convert.py	4	4	2	1	1	0	0
dna-l.py	5	5	2	0	2	0	0
food.py	5	5	1	0	0	1	0
grades.py	8	8	1	0	1	0	0
lost.py	3	3	1	0	0	0	1
$str\_func.py$	2	2	2	0	2	0	0
triangle area.py	3	3	3	3	0	0	0
type_mix.py	4	4	1	0	1	0	0
unification.py	3	3	2	2	0	1	0
123.py	2	2	0	0	0	0	0
branch.py	3	3	1	0	0	1	0
filter.py	1	1	0	0	0	0	0
five.py	3	3	1	0	1	0	0
loop.py	3	3	2	0	0	0	2
merge2.py	3	3	0	0	0	0	0
			I				I
$\mathbf{SUM}$	73	73	29	7	16	4	4

the Character Inclusion Domain with the String Set Domain described in 2.3.3, which keeps track of sets of strings instead of just characters in a string, then for example in Listing 2.1, we can say that *base* can be only one of exactly four possible values 'A', 'T', 'C' or 'G', which achieves a significant increase in precision.

5 Conclusion and Future Work

## A Appendix

### **Lyra Checker Evaluation**

Thank you for agreeing to take part in the user study of my bachelor's project.

* R6	equired						
1.	What is your age? *						
2.	What is your field of study	? *					
3.	What is your current occup	ation?					
	Bachelor's student						
	Master's student						
	PhD student						
	Other:						
4.	On a scale from 1 to 5, how Mark only one oval.			ou with			ramming? *
		1	2	3	4	5	
	I have never programmed before						I have a strong programmer background

### **Experiment I: Fixing input data**

In this experiment you are presented with a Python program that reads some input data from a file and does some computations on them. Some of the input data is wrong and will cause the program to raise some errors.

We would like you to try to fix the input data so that the program runs without raising errors. You can assume that the program is correct. Please do NOT modify it.

### Choose a program to run

To ensure some randomization to the experiment, please choose a program to run based on your month of birth:

January-March: convert April-June: dna\_frequency July-September: grades

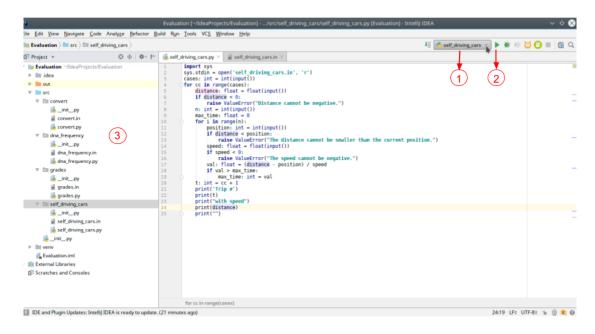
October-December: self driving cars

5. Please select which problem you chose. * Mark only one oval.	
convert	
dna_frequency	
grades	
self_driving_cars	

# For the experiment to be successful, please read the instructions till the end of this page and the problem descriptions on paper carefully:

- 1- You will be using IntelliJ IDEA for this experiment. Each program is in a folder along with its input file. For example, the program convert.py reads input from the file <u>convert.in</u>. They both exist in the folder named "convert". You can view the input file data or program code by double-clicking them in the section Labeled 3 in the picture below.
- 2- To run a program, select its name form the drop down menu (Labeled 1) and click the Run button (Labeled 2).
- 3- You are given 8 minutes to try to correct as many errors as possible in the input data file of your chosen program.

IMPORTANT NOTE: You are allowed to look at the program code, but not to modify it. You can only add, or modify the lines of the input file, but not delete any of them completely.



### Please tell me when you are ready to start.

### Please answer these questions after finishing the task:

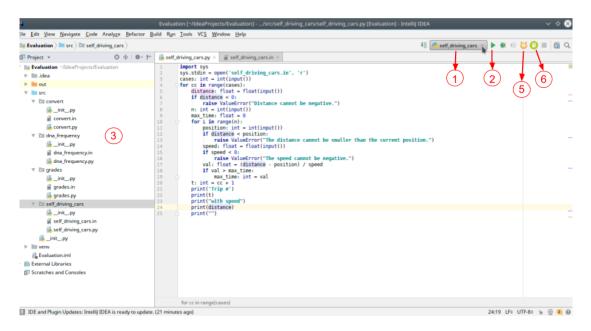
6. How many minutes did this experiment take?

Yes						
No						
	ow much you a	agree w	ith the	e follo	owing	
tements:						
I felt frustrated	trying to solve this pr	oblem *				
Mark only one o						
	Strongly disagree	Disagree	Neutral	Agree	Strongly Agree	
Rate						
The errors mes	sages printed by the p	orogram he	elped me	identify	what was wrong w	/ith
Mark only one o	val per row.					
	Strongly disagree	Disagree	Neutral	Agree	Strongly Agree	
Rate periment l	I: Fixing input	data wi	th Lyra	a Che	ecker	help
Rate  periment I experiment is site wrong values	I: Fixing input of milar to the previous on	data wi	th Lyra	a Che	ecker	help
Periment I experiment is site wrong values	I: Fixing input ( milar to the previous on in the input file.  Dgram to run  e a program to run base driving_cars	data wir e. But now	th Lyra	a Che	ecker	help
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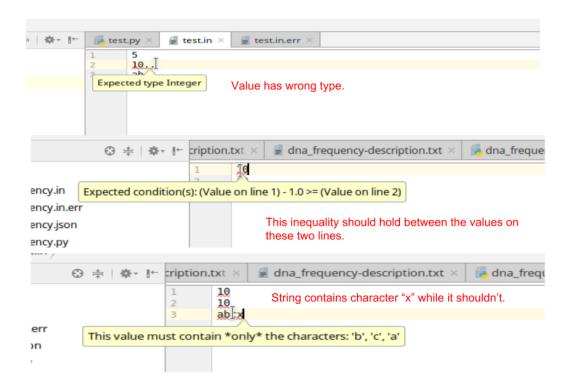
# For the experiment to be successful, please read the instructions till the end of this page and the problem descriptions on paper carefully:

- 1- Choose the program from the drop-down menu labeled 1 in the picture below.
- 2- Choose the corresponding input file using the green button labeled 6.
- 3- Click the Lyra icon labeled 5 to run the tool and wait a few seconds.
- 4- Examine the error messages and try to fix the errors in the file. Note that the error messages will not be updated automatically once you change the data. You have to run the tool again to update them.
- 5- Repeat steps 3 and 4 until there are no more errors in the file.

IMPORTANT NOTE: You are allowed to look at the program code, but not to modify it. You can only add, or modify the lines of the input file, but not delete any of them completely.



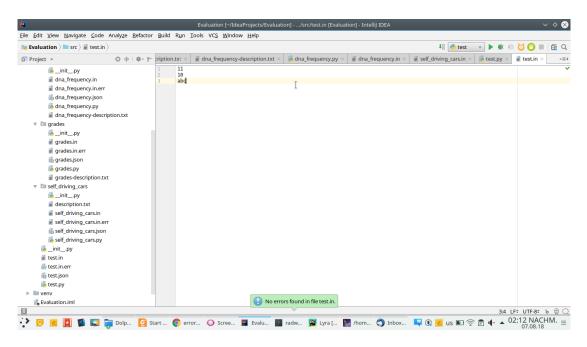
Wrong values are underlined in red in the input file. Hover over the red line to see the error message.



### The tool will show a pop-up indicating the first error in the file



When the tool cannot detect any more errors in your input file, it will display a message in a green pop-up like the image below.



Please tell me when you're ready to start the second experiment.

Please answer these questions after finishing the task:

11. How many minut take? *	es did this experime	ents				
12. Were you able to Mark only one ove		he input fil	e? *			
Yes No						
13. Were you able to Mark only one ove		thout raisir	ng en erro	or? *		
Yes						
O No						
Please rate hostatements:	ow much you	agree w	ith the	e follo	owing	
14. I felt frustrated to Mark only one ove		oblem *				
	Strongly disagree	Disagree	Neutral	Agree	Strongly Agree	
Rate						

Strongly disagree Disagree Neutral Agree Strongly Agree Rate	I found it easy to run the tool and understand its output *  Mark only one oval per row.  Strongly disagree Disagree Neutral Agree Strongly Agree  Rate Disagree Neutral Agree Strongly Agree  Rate Disagree Neutral Agree Strongly Agree  Mark only one oval per row.  Strongly disagree Disagree Neutral Agree Strongly Agree  Rate Disagree Neutral Agree Strongly Agree		Strongly disagree	Disagree	Neutral	Agree	Strongly Agree
Strongly disagree Disagree Neutral Agree Strongly Agree Rate	Rate  I would prefer to fix errors in the input data using the tool than using program of messages only *  Mark only one oval per row.  Strongly disagree Disagree Neutral Agree Strongly Agree Rate  Pineral questions  What did you like about this tool? *	Rate					
Rate    would prefer to fix errors in the input data using the tool than using program of messages only *   Mark only one oval per row.     Strongly disagree   Disagree   Neutral   Agree   Strongly Agree     Rate	Rate  I would prefer to fix errors in the input data using the tool than using program of messages only *  Mark only one oval per row.  Strongly disagree Disagree Neutral Agree Strongly Agree  Rate  Peral questions  What did you like about this tool? *	=	ral per row.		-		Our of Access
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Mark only one oval per row.  Strongly disagree Disagree Neutral Agree Strongly Agree  Rate  Netral questions  What did you like about this tool? *	Mark only one oval per row.  Strongly disagree Disagree Neutral Agree Strongly Agree  Rate  Netral questions  What did you like about this tool? *	Rate					
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What did you like about this tool? *	What did you like about this tool? *				Neutrai	Agree	Strongly Agree
		neral ques	tions		Neutral	Agree	Strongly Agree

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