association rules

November 25, 2024

1 Imports

```
[1]: ### IMPORTS ###

import numpy as np
import matplotlib.pyplot as plt
import pandas as pd
from tqdm import tqdm
```

2 Data Preprocessing

```
[2]: # load movie data
movies = pd.read_pickle('data/imdb/ml_movies_description.pkl')
movies.head()
```

```
[2]:
        movieId
                                title
                                                                             genres
                    Toy Story (1995)
                                       Adventure | Animation | Children | Comedy | Fantasy
              1
     1
              2
                      Jumanji (1995)
                                                        Adventure | Children | Fantasy
     2
                         Heat (1995)
              6
                                                              Action | Crime | Thriller
              8 Tom and Huck (1995)
     3
                                                                 Adventure | Children
              9 Sudden Death (1995)
                                                                             Action
        imdbId
                 tmdbId
                             id
                                                                         description
     0 114709
                862.0 114709 A cowboy doll is profoundly threatened and jea...
     1 113497
                 8844.0 113497 When two kids find and play a magical board ga...
     2 113277
                  949.0 113277 A group of high-end professional thieves start...
     3 112302 45325.0 112302 Two best friends witness a murder and embark o...
     4 114576
                 9091.0 114576 A former fireman takes on a group of terrorist...
```

```
[3]: # get a list of unique movie ids
movie_ids_imdb = movies['movieId'].unique()

# print the number of unique movie ids
print('Number of unique movie ids: ', len(movie_ids_imdb))
```

Number of unique movie ids: 51860

```
[4]: # load ratings
     ratings = pd.read_csv('data/ml-32m/ratings.csv')
     ratings.head()
[4]:
       userId movieId rating timestamp
            1
                           4.0 944249077
                    17
            1
                    25
                            1.0 944250228
     1
     2
            1
                    29
                            2.0 943230976
                     30
                            5.0 944249077
            1
            1
                     32
                            5.0 943228858
[5]: # get a list of unique user ids
     movie_ids_ml = ratings['movieId'].unique()
     # print the number of unique user ids
     print('Number of unique user ids: ', len(movie_ids_ml))
    Number of unique user ids: 84432
[6]: ### DATA PREPROCESSING ###
     # get the intersection of movie ids
     movie_ids = np.intersect1d(movie_ids_imdb, movie_ids_ml)
     print('Number of common movie ids: ', len(movie_ids))
     # filter the ratings data to contain only the common movie ids
     ratings = ratings[ratings['movieId'].isin(movie_ids)]
     # drop timestamp column
     ratings = ratings.drop('timestamp', axis=1)
     # print the number of ratings
     print('Number of ratings: ', len(ratings))
     # get the number of unique users
     user_ids = ratings['userId'].unique()
     # print the number of unique users
     print('Number of unique users: ', len(user_ids))
    Number of common movie ids: 49892
    Number of ratings: 25723135
    Number of unique users: 200947
[7]: # remove alle ratings for user 304, 6741 and 147001 for testing purposes
     ratings = ratings[~ratings['userId'].isin([304, 6741, 147001])]
```

```
[8]: ### CREATE LIKED MOVIES DATAFRAME ###
      # create a dataframe to only store ratings of 4 or 5
     liked_movies = ratings[ratings['rating'] >= 4]
      # print the number of liked movies
     print('Number of ratings 4 or 5: ', len(liked_movies))
     # print the number of unique users who liked movies
     print('Number of unique users who liked movies: ', len(liked_movies['userId'].

unique()))
      # print the number of unique movies that were liked
     print('Number of unique movies that were liked: ', len(liked movies['movieId'].

unique()))
     liked_movies.head()
     Number of ratings 4 or 5: 12781764
     Number of unique users who liked movies:
                                              200609
     Number of unique movies that were liked:
                                              33491
 [8]:
         userId movieId rating
              1
                      30
     4
              1
                      32
                             5.0
              1
                             5.0
                     111
     11
              1
                     166
                             5.0
     15
              1
                     260
                             5.0
     3 Exhaustive approach (not used)
 [9]: ### Create basket data ###
      # create a basket data
     baskets = liked_movies.groupby('userId')['movieId'].apply(list).
      →reset_index(name='basket')
     items = np.unique(np.concatenate(baskets['basket']))
[10]: len(baskets)
[10]: 200609
[11]: | # create a a DataFrame to hash items to integers
      #df_item hash = pd.DataFrame({'item': items, 'hashcode': range(len(items))}).
       ⇔set_index('item')
     df_item_hash = pd.DataFrame(range(len(items)), index=items,__
       df_item_hash.head()
```

```
[11]:
         hashcode
      1
                0
      2
                1
      6
                2
      8
                3
                4
[12]: # Count the occurrences of each item and store in an array
      ### SLOW ###
      #item_count_arr = np.zeros((len(items), 1))
      #for basket in tqdm(baskets['basket']):
           for item in basket:
               idx = df_item_hash.loc[item, 'hashcode']
      #
               item\ count\ arr[idx] += 1
      # Count the occurrences of each item and store in an array
      item_count_arr = np.zeros((len(items), 1))
      # Flatten the list of baskets and get the corresponding hashcodes
      flattened_baskets = np.concatenate(baskets['basket'].values)
      hashcodes = df_item_hash.loc[flattened_baskets, 'hashcode'].values
      # Use np.bincount to count occurrences of each hashcode
      item_count_arr[:len(np.bincount(hashcodes))] = np.bincount(hashcodes).
       \rightarrowreshape(-1, 1)
[13]: # find frequent items (items that appear in more than 0.5% of the baskets)
      freq_items = np.array([df_item_hash[df_item_hash['hashcode'] == x].index[0] for__
       →x in tqdm(np.where(item_count_arr > 0.1 * len(baskets))[0])])
      freq_items
                | 100/100 [00:00<00:00, 14229.07it/s]
     100%|
[13]: array([
                  1,
                          32,
                                  47,
                                          50,
                                                  110,
                                                          111,
                                                                  150,
                                                                          260,
                293,
                        296,
                                 364,
                                         377,
                                                 380,
                                                          457,
                                                                  480,
                                                                          527,
                541,
                        588,
                                 589,
                                         590,
                                                 593,
                                                          595,
                                                                  608,
                                                                          733,
                750,
                        780,
                                858,
                                         904,
                                                 912,
                                                          924,
                                                                 1036,
                                                                         1089,
                                                                 1206,
               1097,
                       1136,
                                1196,
                                        1197,
                                                1198,
                                                         1200,
                                                                         1208,
                       1213,
                                                                 1258,
               1210,
                                1214,
                                        1221,
                                                1222,
                                                         1240,
                                                                         1265,
               1270,
                       1291,
                                1527,
                                        1580,
                                                1617,
                                                         1732,
                                                                 2028,
                                                                         2324,
               2329,
                       2571,
                               2716,
                                        2762,
                                                2997,
                                                         3114,
                                                                 3147,
                                                                         3578,
               3996,
                       4011,
                                4226,
                                        4306,
                                                4878,
                                                         4886,
                                                                 4963,
                                                                         4993,
               4995,
                       5418,
                                5445,
                                        5618,
                                                5952,
                                                         5989,
                                                                 6016,
                                                                         6377,
               6539,
                       6874,
                                7153,
                                        7361,
                                                7438,
                                                         8961,
                                                                33794,
                                                                        44191,
              48516,
                      48780,
                               58559,
                                       59315,
                                               60069,
                                                        68157,
                                                                68954,
                                                                        74458,
                               99114, 109487])
                      91529,
              79132,
```

```
[14]: ### THIS IS SLOW ###
      ### hash the frequent items (starting from 1)
      #df_freq_item hash = pd.DataFrame(range(1,len(freq_items)+1), index=freq_items,__
       →columns=['hashcode'])
      # create a matrix to store the pair counts
      #pair_mat_hashed = np.zeros((len(freq_items)+1, len(freq_items)+1))
      #for b in tqdm(baskets['basket']):
           cand_list = [item for item in b if item in freq_items]
           if len(cand_list)<2:</pre>
      #
               continue
      #
          for idx, item1 in enumerate(cand_list):
      #
               for item2 in cand_list[idx+1:]:
                   i = df_freq_item_hash.loc[item1, 'hashcode']
                   j = df freq item hash.loc[item2, 'hashcode']
                   pair_mat_hashed[max(i,j),min(i,j)]+=1
      # pair_mat
      #pair_mat_hashed
[15]: # Create a matrix to store the pair counts
      pair_mat_hashed = np.zeros((len(freq_items)+1, len(freq_items)+1))
      # Create a dictionary for quick lookup of hashcodes
      df_freq_item_hash = pd.DataFrame(range(1,len(freq_items)+1), index=freq_items,__
       hashcode dict = df freq item hash['hashcode'].to dict()
      for b in tqdm(baskets['basket']):
          # Filter items in the basket to only those in hashcode_dict
          cand_list = [hashcode dict[item] for item in b if item in hashcode dict]
          if len(cand_list) < 2:</pre>
              continue
          # Convert cand_list to a numpy array
          cand_list = np.array(cand_list)
          # Get unique pairs of indices
          i_indices = np.maximum.outer(cand_list, cand_list)
          j_indices = np.minimum.outer(cand_list, cand_list)
          # Increment only unique pairs (i, j) where i > j
          unique_pairs = np.triu_indices_from(i_indices, k=1)
          pair_mat_hashed[i_indices[unique_pairs], j_indices[unique_pairs]] += 1
```

```
# Display the pair matrix
      pair_mat_hashed
                | 200609/200609 [00:03<00:00, 55619.26it/s]
     100%|
[15]: array([[
                  0.,
                           0.,
                                   0., ...,
                                              0.,
                                                       0.,
                                                               0.],
                  0.,
                           0.,
                                   0., ...,
                                              0.,
                                                      0.,
                                                               0.],
             [
                  0., 13780.,
                                   0., ...,
                                              0.,
                                                      0.,
                                                               0.],
                  0., 6572., 4285., ...,
             0.,
                                                               0.],
                  0., 6391., 5096., ..., 10369.,
             0.],
             Γ
                  0., 6995., 5332., ..., 11635., 12167.,
                                                               0.]])
[16]: # Get frequent pairs (pairs that appear in more than 0.05% of the baskets -
       \hookrightarrow support = 0.0005)
      # Extract frequent pairs that exceed support s2 (assume s2 = 0.02), and hash
       \hookrightarrow back.
      # Find indices where pair counts exceed the threshold
      pair_indices = np.where(pair_mat_hashed > 0.1 * len(baskets))
      # Extract frequent pairs and hash back
      freq_pairs = np.array([
          [df_freq_item_hash.index[x-1], df_freq_item_hash.index[y-1]]
          for x, y in zip(pair_indices[0], pair_indices[1])
      ])
      print('Number of frequent pairs: ', len(freq_pairs))
      # make this into a list of tuples
      freq_pairs = [tuple(x) for x in freq_pairs]
     Number of frequent pairs: 216
[17]: # calculate the support of each frequent pair
      pair_support = pair_mat_hashed[pair_indices] / len(baskets)
      # also calculate the confidence of each frequent pair (confidence = \sqcup
       ⇒support(pair) / support(item1))
[18]: # create a DataFrame to store the frequent pairs and their support
      df_freq_pairs = pd.DataFrame(freq_pairs, columns=['item1', 'item2'])
      df_freq_pairs['support'] = pair_support.flatten()
      # make one column called itemsets that contains the frequent pairs as tuples \Box
       →(frozen sets)
```

```
[18]: support itemsets
0 0.135672 (50, 47)
1 0.103016 (110, 47)
2 0.104726 (50, 110)
3 0.120329 (1, 260)
4 0.101685 (260, 47)
```

4 Association Rule Mining w. A-priori Algorithm

```
[19]: ### ASSOCIATION RULE MINING WITH APRIORI ###
from mlxtend.preprocessing import TransactionEncoder
from mlxtend.frequent_patterns import apriori, association_rules
```

4.1 Find Transactions

```
[20]: df_subset = liked_movies
    transactions = df_subset.groupby('userId')['movieId'].apply(list).values

# Use TransactionEncoder to convert the data into a binary matrix
    te = TransactionEncoder()
    te_ary = te.fit(transactions).transform(transactions)
    binary_df = pd.DataFrame(te_ary, columns=te.columns_)
```

4.2 Find Frequent Itemsets

4.2.1 Using Minimum Support Threshold of 0.2

```
Frequent Itemsets (with more than one element):
```

```
support itemsets
0 0.226894 (1)
1 0.237975 (47)
2 0.276025 (50)
```

```
4
         0.318321
                           (260)
     5
         0.385706
                           (296)
     6
         0.208525
                           (480)
     7
         0.295635
                           (527)
     8
         0.235533
                           (589)
     9
         0.351694
                           (593)
     10 0.220598
                           (608)
     11 0.272894
                           (858)
     12 0.275681
                          (1196)
     13 0.253284
                          (1198)
     14 0.238334
                          (1210)
     15 0.211356
                          (1270)
     16 0.211561
                          (2028)
     17 0.358648
                          (2571)
     18 0.205679
                          (4226)
     19 0.272126
                          (4993)
     20 0.248533
                          (5952)
     21 0.250183
                          (7153)
     22 0.230089
                         (58559)
     23 0.220204
                         (79132)
     24 0.229815
                     (1196, 260)
                     (1210, 260)
     25 0.200156
                      (296, 593)
     26 0.222119
     27 0.219970 (5952, 4993)
     28 0.218071
                    (4993, 7153)
                   (5952, 7153)
     29 0.212493
[22]: frequent_itemsets_2['length'] = frequent_itemsets_2['itemsets'].apply(lambda x:___
       \rightarrowlen(x))
      len(frequent_itemsets_2)
[22]: 30
     Generating Association Rules
[23]: # Generate association rules
      rules_apriori_2 = association_rules(frequent_itemsets_2, metric="confidence",_
       min_threshold=0.5, num_itemsets=len(transactions))
[24]: rules_apriori_2
[24]:
         antecedents consequents
                                   antecedent support consequent support
                                                                             support \
              (1196)
                            (260)
                                             0.275681
                                                                  0.318321 0.229815
      1
               (260)
                           (1196)
                                             0.318321
                                                                  0.275681 0.229815
      2
              (1210)
                            (260)
                                             0.238334
                                                                  0.318321 0.200156
      3
               (260)
                           (1210)
                                             0.318321
                                                                  0.238334 0.200156
      4
               (296)
                           (593)
                                             0.385706
                                                                  0.351694 0.222119
```

3

0.239411

(110)

```
5
               (593)
                          (296)
                                           0.351694
                                                               0.385706 0.222119
     6
                          (4993)
                                                               0.272126 0.219970
              (5952)
                                           0.248533
     7
              (4993)
                          (5952)
                                           0.272126
                                                               0.248533 0.219970
     8
              (4993)
                          (7153)
                                           0.272126
                                                               0.250183 0.218071
     9
              (7153)
                         (4993)
                                           0.250183
                                                               0.272126 0.218071
     10
              (5952)
                          (7153)
                                           0.248533
                                                               0.250183 0.212493
                          (5952)
                                           0.250183
                                                               0.248533 0.212493
     11
              (7153)
         confidence
                         lift representativity leverage conviction \
           0.833629 2.618833
                                            1.0 0.142060
                                                             4.097336
     0
     1
           0.721961 2.618833
                                            1.0 0.142060
                                                             2.605102
     2
           0.839810 2.638251
                                            1.0 0.124289
                                                             4.255445
     3
           0.628786 2.638251
                                            1.0 0.124289
                                                             2.051822
     4
           0.575876 1.637435
                                            1.0 0.086468
                                                             1.528577
     5
                                            1.0 0.086468
           0.631568 1.637435
                                                             1.667320
     6
           0.885074 3.252436
                                            1.0 0.152338
                                                             6.333390
     7
           0.808338 3.252436
                                            1.0 0.152338
                                                             3.920799
     8
           0.801359 3.203090
                                            1.0 0.149990
                                                             3.774737
     9
           0.871645 3.203090
                                            1.0 0.149990
                                                             5.670793
     10
           0.854988 3.417448
                                            1.0 0.150314
                                                             5.170728
           0.849349 3.417448
                                            1.0 0.150314
                                                             4.988145
     11
         zhangs_metric
                         jaccard certainty kulczynski
                                               0.777795
              0.853422 0.631038
     0
                                   0.755939
     1
              0.906805 0.631038
                                   0.616138
                                               0.777795
     2
              0.815267 0.561447
                                   0.765007
                                               0.734298
     3
              0.910928 0.561447
                                   0.512628
                                               0.734298
     4
              0.633717 0.431063
                                   0.345797
                                               0.603722
     5
              0.600471 0.431063
                                   0.400235
                                               0.603722
     6
              0.921582 0.731553
                                   0.842107
                                               0.846706
     7
              0.951454 0.731553
                                   0.744950
                                               0.846706
     8
              0.944946 0.716776
                                   0.735081
                                               0.836502
     9
              0.917293 0.716776
                                   0.823658
                                               0.836502
     10
              0.941338 0.742402
                                   0.806604
                                               0.852169
              0.943409 0.742402
                                   0.799525
                                               0.852169
[25]: # find all unique movie ids in antecedents and consequents
     unique_ante = np.unique(np.concatenate(rules_apriori_2['antecedents'].
       →apply(list)))
     unique_cons = np.unique(np.concatenate(rules_apriori_2['consequents'].
       →apply(list)))
      #print(len(unique_ante), len(unique_cons))
      # find the union of unique movie ids in antecedents and consequents
     unique_movies = np.unique(np.concatenate([unique_ante, unique_cons]))
```

```
# print the unique movie ids and names
      print(unique_movies)
      print(movies[movies['movieId'].isin(unique_movies)][['movieId', 'title']])
     [ 260 296 593 1196 1210 4993 5952 7153]
           movieId
                                                                  title
     163
               260
                             Star Wars: Episode IV - A New Hope (1977)
               296
                                                   Pulp Fiction (1994)
     182
     373
               593
                                      Silence of the Lambs, The (1991)
     743
              1196 Star Wars: Episode V - The Empire Strikes Back...
     755
                    Star Wars: Episode VI - Return of the Jedi (1983)
     3366
              4993 Lord of the Rings: The Fellowship of the Ring,...
     4031
              5952
                        Lord of the Rings: The Two Towers, The (2002)
              7153 Lord of the Rings: The Return of the King, The...
     4831
           Using Minimum Support Threshold of 0.15
[26]: # frequent itemsets
      min_support = 0.15
      frequent_itemsets_15 = apriori(binary_df, min_support=min_support,_u

use_colnames=True)

      print("Frequent Itemsets (with more than one element):")
      print(frequent_itemsets_15)
     Frequent Itemsets (with more than one element):
          support
                              itemsets
     0
         0.226894
                                   (1)
         0.184767
                                  (32)
     1
     2
         0.237975
                                  (47)
     3
         0.276025
                                  (50)
     4
         0.239411
                                 (110)
     73 0.172988
                   (1210, 260, 1196)
     74 0.155427
                    (1196, 2571, 260)
     75 0.153612 (5952, 4993, 2571)
     76 0.152595 (7153, 4993, 2571)
     77 0.198810 (5952, 4993, 7153)
     [78 rows x 2 columns]
[27]: frequent_itemsets_15['length'] = frequent_itemsets_15['itemsets'].apply(lambda_
       \rightarrow x: len(x))
      len(frequent_itemsets_15)
```

Generating association rules

[27]: 78

```
rules_apriori_15 = association_rules(frequent_itemsets_15, metric="confidence",_

→min_threshold=0.5, num_itemsets=len(transactions))
[29]: rules_apriori_15
[29]:
           antecedents
                          consequents
                                        antecedent support
                                                              consequent support
      0
                   (47)
                                 (296)
                                                   0.237975
                                                                        0.385706
      1
                   (47)
                                 (593)
                                                   0.237975
                                                                        0.351694
      2
                   (50)
                                 (296)
                                                   0.276025
                                                                        0.385706
      3
                   (50)
                                 (593)
                                                   0.276025
                                                                        0.351694
      4
                 (1196)
                                 (260)
                                                   0.275681
                                                                        0.318321
      63
          (5952, 7153)
                                (4993)
                                                   0.212493
                                                                        0.272126
      64
          (4993, 7153)
                                                   0.218071
                                                                        0.248533
                                (5952)
                         (4993, 7153)
      65
                 (5952)
                                                   0.248533
                                                                        0.218071
                         (5952, 7153)
      66
                 (4993)
                                                   0.272126
                                                                        0.212493
      67
                         (5952, 4993)
                                                   0.250183
                                                                        0.219970
                 (7153)
                                            representativity
                     confidence
                                                               leverage
                                                                          conviction
           support
                                      lift
          0.169589
                       0.712631
                                  1.847604
                                                               0.077800
                                                                            2.137650
      0
                                                          1.0
      1
          0.157814
                       0.663155 1.885601
                                                          1.0 0.074120
                                                                            1.924639
      2
                                                          1.0
          0.188102
                       0.681469
                                  1.766812
                                                               0.081638
                                                                            1.928525
      3
          0.165182
                       0.598432
                                  1.701571
                                                          1.0
                                                               0.068106
                                                                            1.614438
      4
          0.229815
                       0.833629
                                  2.618833
                                                          1.0
                                                               0.142060
                                                                            4.097336
      . .
      63
          0.198810
                       0.935606
                                 3.438129
                                                          1.0
                                                               0.140985
                                                                           11.303387
      64
          0.198810
                       0.911674
                                 3.668218
                                                          1.0 0.144612
                                                                            8.507872
      65
          0.198810
                       0.799932
                                 3.668218
                                                          1.0
                                                               0.144612
                                                                            3.908313
                                                          1.0
          0.198810
                       0.730578
                                  3.438129
                                                               0.140985
                                                                            2.922953
      66
          0.198810
                       0.794656
                                 3.612563
                                                          1.0 0.143777
                                                                            3.798653
      67
          zhangs_metric
                           jaccard
                                     certainty
                                               kulczynski
                                                   0.576158
      0
               0.602026
                         0.373467
                                      0.532197
      1
               0.616338
                          0.365434
                                      0.480422
                                                   0.555941
      2
                          0.397152
               0.599480
                                      0.481469
                                                   0.584576
      3
               0.569505
                          0.357122
                                      0.380589
                                                   0.534054
      4
               0.853422
                          0.631038
                                      0.755939
                                                   0.777795
      63
               0.900492
                          0.695601
                                      0.911531
                                                   0.833092
      64
               0.930248
                          0.742396
                                      0.882462
                                                   0.855803
      65
               0.967958
                          0.742396
                                      0.744135
                                                   0.855803
               0.974268
                          0.695601
                                      0.657880
      66
                                                   0.833092
                                      0.736749
      67
               0.964487
                          0.732685
                                                   0.849229
```

[68 rows x 14 columns]

[28]: # Generate association rules

```
[30]: # find all unique movie ids in antecedents and consequents
      unique_ante = np.unique(np.concatenate(rules_apriori_15['antecedents'].
       →apply(list)))
      unique cons = np.unique(np.concatenate(rules apriori 15['consequents'].
       →apply(list)))
      #print(len(unique_ante), len(unique_cons))
      # find the union of unique movie ids in antecedents and consequents
      unique_movies = np.unique(np.concatenate([unique_ante, unique_cons]))
      # print the unique movie ids and names
      print(unique movies, len(unique movies))
      print(movies[movies['movieId'].isin(unique_movies)][['movieId', 'title']])
     Γ 47
             50 260
                      296
                           527
                                 593 608 858 1196 1198 1210 1221 2571 4993
      5952 7153] 16
           movieId
                                                                 title
     31
                47
                                           Seven (a.k.a. Se7en) (1995)
     33
                50
                                            Usual Suspects, The (1995)
                            Star Wars: Episode IV - A New Hope (1977)
     163
               260
     182
               296
                                                   Pulp Fiction (1994)
                                               Schindler's List (1993)
     334
               527
     373
               593
                                      Silence of the Lambs, The (1991)
     382
               608
                                                          Fargo (1996)
     528
               858
                                                 Godfather, The (1972)
     743
              1196 Star Wars: Episode V - The Empire Strikes Back...
              1198 Raiders of the Lost Ark (Indiana Jones and the...
     745
              1210 Star Wars: Episode VI - Return of the Jedi (1983)
     755
                                        Godfather: Part II, The (1974)
     766
              1221
                                                    Matrix, The (1999)
     1656
              2571
     3366
              4993 Lord of the Rings: The Fellowship of the Ring,...
                        Lord of the Rings: The Two Towers, The (2002)
     4031
              5952
     4831
              7153 Lord of the Rings: The Return of the King, The...
     4.2.3 Using Minimum Support Threshold of 0.1
[31]: # frequent itemsets
      min_support = 0.1
      frequent_itemsets_1 = apriori(binary_df, min_support=min_support,__

use_colnames=True)

      print("Frequent Itemsets (with more than one element):")
      print(frequent_itemsets_1)
     Frequent Itemsets (with more than one element):
                                      itemsets
           support
```

(1)

(32)

0

1

0.226894

0.184767

```
2
          0.237975
                                          (47)
     3
          0.276025
                                          (50)
     4
          0.239411
                                         (110)
     . .
                      (5952, 4993, 260, 7153)
     394 0.114147
     395
          0.103804
                      (296, 4993, 5952, 7153)
     396
          0.110778
                      (5952, 4993, 1196, 7153)
                      (5952, 7153, 4993, 2571)
     397
          0.140617
     398 0.105962 (5952, 4993, 7153, 58559)
     [399 rows x 2 columns]
[32]: frequent itemsets 1['length'] = frequent itemsets 1['itemsets'].apply(lambda x:___
       \rightarrowlen(x))
      len(frequent_itemsets_1)
[32]: 399
     Generating association rules
[33]: # Generate association rules
      rules_apriori_1 = association_rules(frequent_itemsets_1, metric="confidence",_
       min_threshold=0.5, num_itemsets=len(transactions))
[56]: print(len(rules_apriori_1))
      rules_apriori_1.head()
     507
[56]:
        antecedents consequents antecedent support consequent support
                                                                           support \
                (1)
                          (260)
                                           0.226894
                                                                0.318321 0.120329
      1
               (32)
                          (296)
                                           0.184767
                                                                0.385706 0.122726
      2
               (32)
                          (593)
                                           0.184767
                                                                0.351694
                                                                          0.104985
      3
               (47)
                           (50)
                                           0.237975
                                                                0.276025
                                                                          0.135672
      4
               (47)
                          (296)
                                           0.237975
                                                                0.385706 0.169589
         confidence
                         lift representativity leverage conviction \
      0
           0.530329 1.666022
                                            1.0 0.048104
                                                              1.451398
      1
           0.664221 1.722092
                                            1.0 0.051460
                                                              1.829458
                                                              1.501412
      2
           0.568203 1.615616
                                            1.0 0.040004
      3
           0.570109 2.065429
                                             1.0 0.069985
                                                              1.684091
           0.712631 1.847604
                                            1.0 0.077800
                                                              2.137650
         zhangs_metric
                         jaccard certainty kulczynski
      0
              0.517093 0.283202
                                   0.311009
                                               0.454170
              0.514345 0.274098
                                   0.453390
                                               0.491204
      1
      2
              0.467402 0.243317
                                   0.333961
                                               0.433358
      3
              0.676932 0.358609
                                   0.406208
                                               0.530815
```

```
4
              0.602026 0.373467
                                   0.532197
                                                0.576158
[35]: # find all unique movie ids in antecedents and consequents
      unique_ante = np.unique(np.concatenate(rules_apriori_1['antecedents'].
       →apply(list)))
      unique_cons = np.unique(np.concatenate(rules_apriori_1['consequents'].
       →apply(list)))
      #print(len(unique ante), len(unique cons))
      # find the union of unique movie ids in antecedents and consequents
      unique_movies = np.unique(np.concatenate([unique_ante, unique_cons]))
      # print the unique movie ids and names
     print(len(unique_movies))
     print(movies[movies['movieId'].isin(unique_movies)][['movieId', 'title']])
     49
            movieId
                                                                   title
     0
                                                       Toy Story (1995)
                  1
                              Twelve Monkeys (a.k.a. 12 Monkeys) (1995)
     20
                 32
                                            Seven (a.k.a. Se7en) (1995)
     31
                 47
                                             Usual Suspects, The (1995)
     33
                 50
     71
                                                      Braveheart (1995)
                110
     72
                111
                                                     Taxi Driver (1976)
     91
                150
                                                       Apollo 13 (1995)
```

```
778
          1240
                                             Terminator, The (1984)
802
          1270
                                          Back to the Future (1985)
                         Indiana Jones and the Last Crusade (1989)
819
          1291
1262
          2028
                                         Saving Private Ryan (1998)
                                          American History X (1998)
1477
          2329
                                                 Matrix, The (1999)
1656
          2571
1783
          2762
                                            Sixth Sense, The (1999)
                                                   Gladiator (2000)
2338
          3578
2817
          4226
                                                     Memento (2000)
2860
          4306
                                                       Shrek (2001)
          4993
                Lord of the Rings: The Fellowship of the Ring,...
3366
4031
          5952
                     Lord of the Rings: The Two Towers, The (2002)
4649
          6874
                                           Kill Bill: Vol. 1 (2003)
                Lord of the Rings: The Return of the King, The...
4831
          7153
          7361
                      Eternal Sunshine of the Spotless Mind (2004)
4961
5006
          7438
                                           Kill Bill: Vol. 2 (2004)
6858
         33794
                                               Batman Begins (2005)
                                            Dark Knight, The (2008)
8368
         58559
10097
         79132
                                                   Inception (2010)
                                                Interstellar (2014)
13780
        109487
```

4.2.4 Using Minimum Support Threshold of 0.05

THIS DID NOT WORK

```
[36]: # frequent itemsets

#min_support = 0.05

#frequent_itemsets_05 = apriori(binary_df, min_support=min_support, u)

ouse_colnames=True)

#print("Frequent Itemsets (with more than one element):")

#print(frequent_itemsets_05)
```

4.3 Association Rule Evaluation

```
[37]: # load ratings
ratings = pd.read_csv('data/ml-32m/ratings.csv')
ratings.head()
```

```
[37]:
         userId movieId rating timestamp
                             4.0 944249077
      0
              1
                      17
      1
              1
                      25
                             1.0 944250228
      2
              1
                      29
                             2.0 943230976
      3
                      30
                             5.0 944249077
              1
              1
                      32
                             5.0 943228858
```

```
[38]: # get a list of unique user ids
movie_ids_ml = ratings['movieId'].unique()
```

```
print('Number of unique user ids: ', len(movie_ids_ml))
     Number of unique user ids: 84432
[39]: ### DATA PREPROCESSING ###
      # get the intersection of movie ids
      movie_ids = np.intersect1d(movie_ids_imdb, movie_ids_ml)
      print('Number of common movie ids: ', len(movie_ids))
      # filter the ratings data to contain only the common movie ids
      ratings = ratings[ratings['movieId'].isin(movie_ids)]
      # drop timestamp column
      ratings = ratings.drop('timestamp', axis=1)
      # print the number of ratings
      print('Number of ratings: ', len(ratings))
      # get the number of unique users
      user_ids = ratings['userId'].unique()
      # print the number of unique users
      print('Number of unique users: ', len(user_ids))
     Number of common movie ids: 49892
     Number of ratings: 25723135
     Number of unique users: 200947
[40]: # get only the ratings for user 304, 6741 and 147001
      test_ratings = ratings[ratings['userId'].isin([304, 6741, 147001])]
[41]: def eval_rules(user_id, rules):
          # get the test ratings for the user
          test_user = test_ratings[test_ratings['userId'] == user_id]
          # get num ratings
          num_ratings = len(test_user)
          print('Number of ratings for user', user_id, ':', num_ratings)
          # using the rules, check if any of the antecedents are in the test ratings
          # if they are, check if the consequents are also in the test ratings
          # if both are and both are rated higher than 4, increment perfect \mu
       \hookrightarrow classification
          perfect_recommendation = 0
          perfect_rule = []
          # if both are rated higher than 3.5, increment good classification
```

print the number of unique user ids

```
good_recommendation = 0
  good_rule = []
  # if both are and only one is rated higher than 4, increment bad_{\sqcup}
\hookrightarrow classification
  bad_recommendation = 0
  bad rule = []
  for idx, row in rules.iterrows():
      if row['antecedents'].issubset(test_user['movieId']) and__
→row['consequents'].issubset(test_user['movieId']):
           if test_user[test_user['movieId'].
sisin(row['antecedents'])]['rating'].values[0] >= 4 and

¬test_user[test_user['movieId'].isin(row['consequents'])]['rating'].values[0]

⇒>= 4:
               if [row['consequents'], row['antecedents']] in perfect_rule:
               perfect_recommendation += 1
               # append string "item1 -> item2" to good_rule
               perfect_rule.append([row['antecedents'], row['consequents']])
           elif test_user[test_user['movieId'].
⇔isin(row['antecedents'])]['rating'].values[0] >= 3.5 and □

¬test_user[test_user['movieId'].isin(row['consequents'])]['rating'].values[0]

⇒>= 3.5:
               if [row['consequents'], row['antecedents']] in good_rule:
                   continue
               good_recommendation += 1
               # append string "item1 -> item2" to good_rule
               good_rule.append([row['antecedents'], row['consequents']])
           elif test_user[test_user['movieId'].
⇔isin(row['antecedents'])]['rating'].values[0] >= 3.5 and_□

¬test_user[test_user['movieId'].isin(row['consequents'])]['rating'].values[0]

if [row['consequents'], row['antecedents']] in bad_rule:
                   continue
               bad recommendation += 1
               # append string "item1 -> item2" to bad_rule
               bad_rule.append([row['antecedents'], row['consequents']])
           else:
               pass
  # it might be the case that rules go both ways, so we need to check for
→that as well
```

```
return perfect_recommendation, good_recommendation, bad_recommendation,_u
→perfect_rule, good_rule, bad_rule
```

Rule Evaluation for Minimum Support = 0.2

```
[46]: # evaluate the rules for user 304 with a support of 0.2
      perfect_recommendation, good_recommendation, bad_recommendation, perfect_rule, ⊔
       ⇒good rule, bad rule = eval rules(304, rules apriori 2)
      print('Perfect recommendation:', perfect_recommendation)
      print('Good recommendation:', good_recommendation)
      print('Bad recommendation:', bad_recommendation)
      # evaluate the rules for user 6741 with a support of 0.2
      perfect_recommendation, good_recommendation, bad_recommendation, perfect_rule,_
       ⇒good_rule, bad_rule = eval_rules(6741, rules_apriori_2)
      print('Perfect recommendation:', perfect_recommendation)
      print('Good recommendation:', good_recommendation)
      print('Bad recommendation:', bad_recommendation)
      # evaluate the rules for user 147001 with a support of 0.2
      perfect recommendation, good recommendation, bad recommendation, perfect rule,
       ⇒good_rule, bad_rule = eval_rules(147001, rules_apriori_2)
      print('Perfect recommendation:', perfect_recommendation)
      print('Good recommendation:', good_recommendation)
      print('Bad recommendation:', bad_recommendation)
     Number of ratings for user 304: 168
     Perfect recommendation: 1
     Good recommendation: 0
     Bad recommendation: 0
     Number of ratings for user 6741: 336
     Perfect recommendation: 5
     Good recommendation: 0
     Bad recommendation: 0
     Number of ratings for user 147001 : 223
     Perfect recommendation: 3
     Good recommendation: 1
     Bad recommendation: 0
     Rule Evaluation for Minimum Support = 0.15
[49]: # evaluate the rules for user 304 with a support of 0.15
      perfect_recommendation, good_recommendation, bad_recommendation, perfect_rule,_
       ⇒good_rule, bad_rule = eval_rules(304, rules_apriori_15)
```

print('Perfect recommendation:', perfect_recommendation)

```
print('Good recommendation:', good_recommendation)
      print('Bad recommendation:', bad_recommendation)
      # evaluate the rules for user 6741 with a support of 0.15
      perfect_recommendation, good_recommendation, bad_recommendation, perfect_rule,_
       ⇒good_rule, bad_rule = eval_rules(6741, rules_apriori_15)
      print('Perfect recommendation:', perfect_recommendation)
      print('Good recommendation:', good_recommendation)
      print('Bad recommendation:', bad_recommendation)
      # evaluate the rules for user 147001 with a support of 0.15
      perfect_recommendation, good_recommendation, bad_recommendation, perfect_rule,_
       ⇒good_rule, bad_rule = eval_rules(147001, rules_apriori_15)
      print('Perfect recommendation:', perfect_recommendation)
      print('Good recommendation:', good_recommendation)
      print('Bad recommendation:', bad_recommendation)
     Number of ratings for user 304: 168
     Perfect recommendation: 6
     Good recommendation: 7
     Bad recommendation: 0
     Number of ratings for user 6741: 336
     Perfect recommendation: 23
     Good recommendation: 1
     Bad recommendation: 13
     Number of ratings for user 147001 : 223
     Perfect recommendation: 18
     Good recommendation: 2
     Bad recommendation: 1
     Rule Evaluation for Minimum Support = 0.1
[50]: # evaluate the rules for user 304 with a support of 0.1
      perfect_recommendation, good_recommendation, bad_recommendation, perfect_rule,_

¬good_rule, bad_rule = eval_rules(304, rules_apriori_1)

      print('Perfect recommendation:', perfect_recommendation)
      print('Good recommendation:', good_recommendation)
      print('Bad recommendation:', bad_recommendation)
      # evaluate the rules for user 6741 with a support of 0.1
      perfect_recommendation, good_recommendation, bad_recommendation, perfect_rule,_

¬good_rule, bad_rule = eval_rules(6741, rules_apriori_1)
```

```
print('Perfect recommendation:', perfect_recommendation)
             print('Good recommendation:', good_recommendation)
             print('Bad recommendation:', bad_recommendation)
             # evaluate the rules for user 147001 with a support of 0.1
             perfect_recommendation, good_recommendation, bad_recommendation, perfect_rule,_

¬good_rule, bad_rule = eval_rules(147001, rules_apriori_1)

             print('Perfect recommendation:', perfect_recommendation)
             print('Good recommendation:', good_recommendation)
             print('Bad recommendation:', bad_recommendation)
           Number of ratings for user 304: 168
           Perfect recommendation: 29
           Good recommendation: 76
           Bad recommendation: 0
           Number of ratings for user 6741: 336
           Perfect recommendation: 240
           Good recommendation: 16
           Bad recommendation: 55
           Number of ratings for user 147001 : 223
           Perfect recommendation: 105
           Good recommendation: 24
           Bad recommendation: 5
            Further Tests for User 6741
[53]: # evaluate the rules for user 6741 with a support of 0.1
             perfect_recommendation, good_recommendation, bad_recommendation, perfect_rule,_
                →good_rule, bad_rule = eval_rules(6741, rules_apriori_1)
             print('Perfect recommendation:', perfect_recommendation)
             print('Good recommendation:', good_recommendation)
             print('Bad recommendation:', bad_recommendation)
             # go through the bad rules and print movie names
             for rule in bad rule[:5]:
                     print(f"Antecedent :{movies[movies['movieId'].isin(rule[0])][['movieId',_
               ititle']]}, consequent: {movies[movies['movieId'].isin(rule[1])][['movieId', المالة ا

        'title']]}")

           Number of ratings for user 6741: 336
           Perfect recommendation: 240
           Good recommendation: 16
           Bad recommendation: 55
           Antecedent :
                                              movieId
                              47 Seven (a.k.a. Se7en) (1995), consequent:
                                                                                                                                              movieId
           title
            1656
                               2571 Matrix, The (1999)
```

Antecedent : movieId title

33 50 Usual Suspects, The (1995), consequent: movieId

title

1656 2571 Matrix, The (1999)

Antecedent: movieId title 163 260 Star Wars: Episode IV - A New Hope (1977), consequent:

movieId title

1656 2571 Matrix, The (1999)

Antecedent: movieId title

369 589 Terminator 2: Judgment Day (1991), consequent: movieId

title

1656 2571 Matrix, The (1999)

Antecedent : movieId title

528 858 Godfather, The (1972), consequent: movieId

title

1656 2571 Matrix, The (1999)

[]: