

i.

$$\alpha = \frac{1}{2RC} = \frac{1}{2 \cdot R \cdot 1nF} = \frac{1}{2 \cdot R \cdot 1 \times 10^{-9}} = \frac{500000000}{R} \text{ rad/s}$$

$$\omega_0 = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{1.5\mu H \cdot 1nF}} = \frac{1}{\sqrt{1.5 \times 10^{-6} \cdot 1 \times 10^{-9}}} = 25819888.97 \text{ rad/s}$$

$$\zeta = \frac{\alpha}{\omega_0} = \frac{\frac{500000000}{R} \text{ rad/s}}{25819888.97 \text{ rad/s}} = \frac{19.36}{R}$$

The value of  $\zeta$  is dependent on  $R$ , therefore the system would be underdamped, critically damped, or overdamped at different values of  $R$ . In the given circuit,  $R = (R_1 \parallel R_2)$ .

ii.

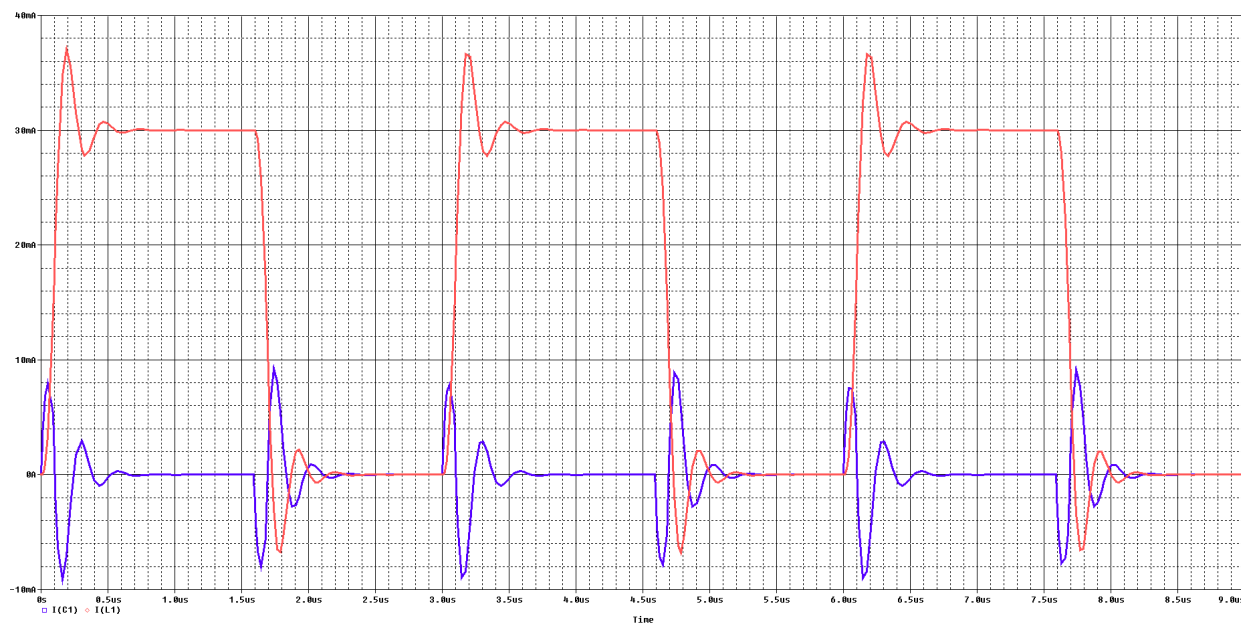
$$1 = \zeta = \frac{\frac{500000000}{R} \text{ rad/s}}{25819888.97 \text{ rad/s}} = \frac{19.36}{R}$$

$$1 = \frac{19.36}{R}$$

$$R = 19.36\Omega$$

$R = (R_1 \parallel R_2) = 19.36\Omega$ . Therefore  $2R = R_1 = R_2 = 38.72\Omega$ . The value of  $R_1 = R_2$  that results in the circuit being critically damped is  $38.72\Omega$ .

iii.



iv.



v. The phase difference in part ii is  $360 \cdot \frac{280ns}{3us} = 33.6$  or  $2\pi \text{ rad} \cdot \frac{280ns}{3us} = 0.59 \text{ rad}$ . The phase difference in part iii is  $360 \cdot \frac{140ns}{3us} = 16.8$  or  $2\pi \text{ rad} \cdot \frac{140ns}{3us} = 0.29 \text{ rad}$ .

vi.



vii.

