Classifiers

Store 1











3 out of 5

3/5 = .60 or 60%

Store 2











3 out of 10











3/10 = .30 or 30%

Outcomes

Predictors

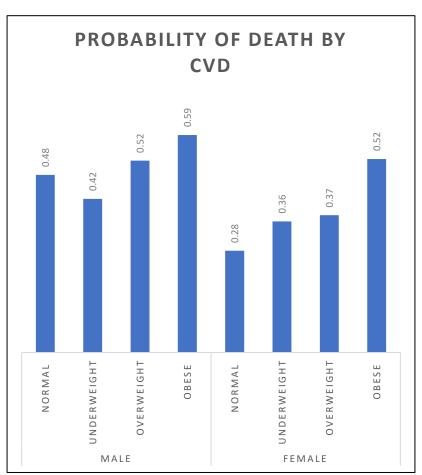
Grand Total

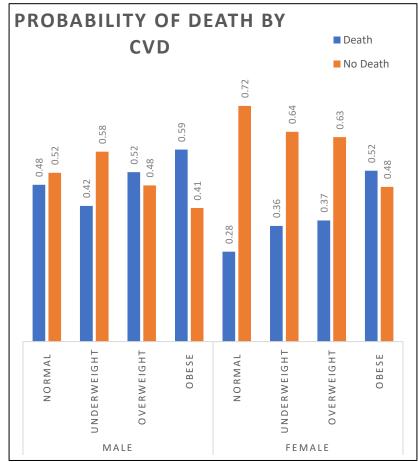
	Death
Male	0.51
Normal	0.48
Underweight	0.42
Overweight	0.52
Obese	0.59
Female	0.34
Normal	0.28
Underweight	0.36
Overweight	0.37
Obese	0.52
Grand Total	0.42

	Death b	Out	comes
		Death	No Death
	Male	0.51	0.49
	Normal	0.48	0.52
	Underweight	0.42	0.58
	Overweight	0.52	0.48
	Obese	0.59	0.41
/	Female	0.34	0.66
	Normal	0.28	0.72
	Underweight	0.36	0.64
	Overweight	0.37	0.63
	Obese	0.52	0.48

0.42

0.58





Equal-frequency binning

Equal-width binning

K-means clustering

- Equal-frequency binning
 - n-tiles
 - Medians, quartiles, quintiles, deciles, etc.
 - Equal representation across range
 - Parallels the original distribution
 - Good for model input
- Equal-width binning
- K-means clustering

Equal-frequency binning

- Equal-width binning
 - Each bin is the same size of the range (width)
 - Age, GPA, etc.
 - Convenient for interpretation
 - Must take care when determining the width
- K-means clustering

Equal-frequency binning

Equal-width binning

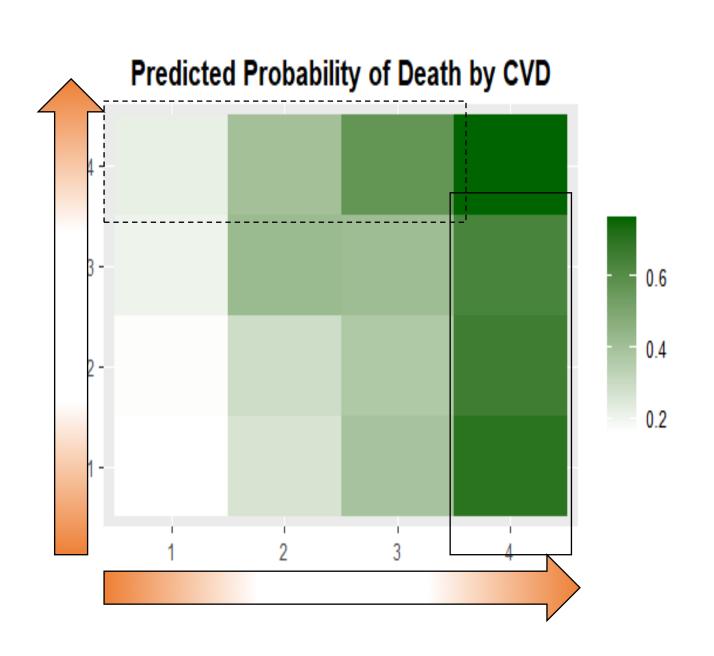
- K-means clustering
 - Each bin is determined Maximum Likelihood Optimization
 - Cases belong to the "closest mean"
 - Can identify useful profiles/typologies
 - Category labels must be interpreted post hoc and can be multidimensional

A Neat Trick

Outcome (binary) =
 Predictor1 (discretized) + Predictor2 (discretized)

Heatmap

- Plot the conditional probability of outcome
 - X-axis: Predictor1
 - Y-axis: Predictor 2
 - Color: Probability



What did we cover?

- Conditional Mean as a Classifier
 - Probability scores ← Discrete Predictors
- Discretizing Continuous Variables
 - Equal-frequency binning
 - Equal-width binning
 - K-means clustering
- Next up:
 - Assessing the conditional mean as a classifier
 - Does the model work well as a Classifier

Classifiers

Evaluating Classifiers: Sensitivity and Specificity

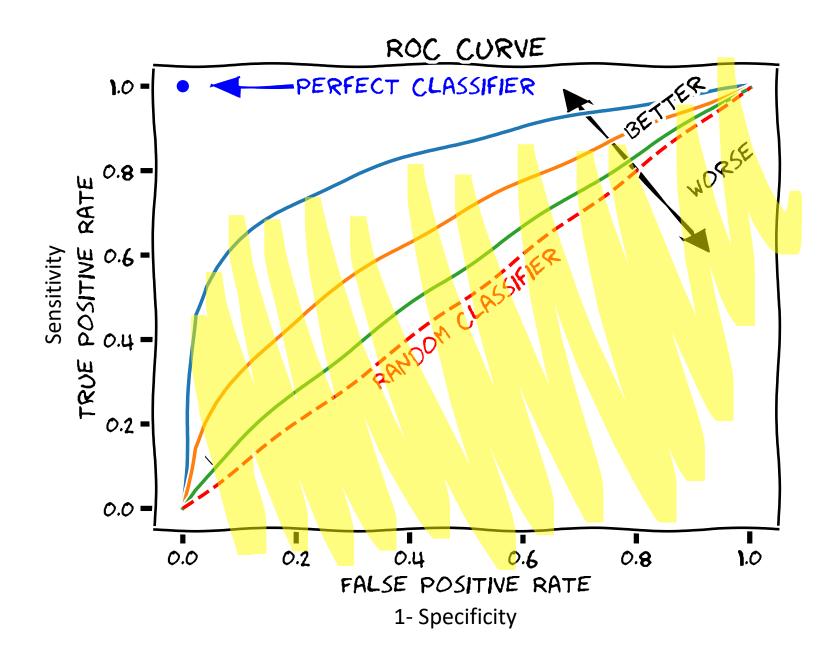


	Reality									Acc	Sen	Spe	
	R	В	R	В	R	В	R	В	R	В	_	_	_
Model 1	R	R	R	R	R	R	R	R	R	R	0.50	1.00	0.00
Model 2	В	В	В	В	В	В	В	В	В	В	0.50	0.00	1.00
Model 3	R	В	В	R	R	R	В	R	R	В	0.50	0.60	0.40

Sensitivity or Specificity?

Depends...

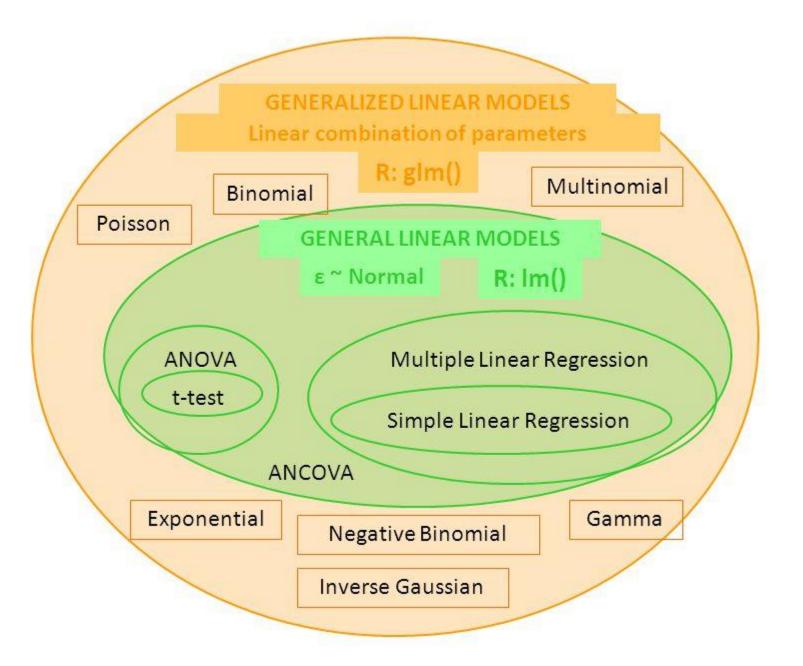
- Costs of False Positive
 - Squander resources
- Costs of False Negative
 - Miss opportunities
- Trade-offs
 - Numbersense Chapter



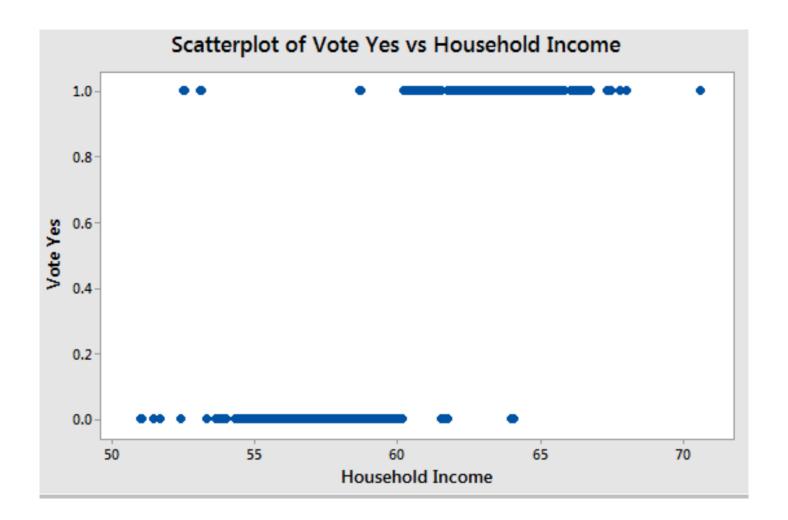
Classifiers

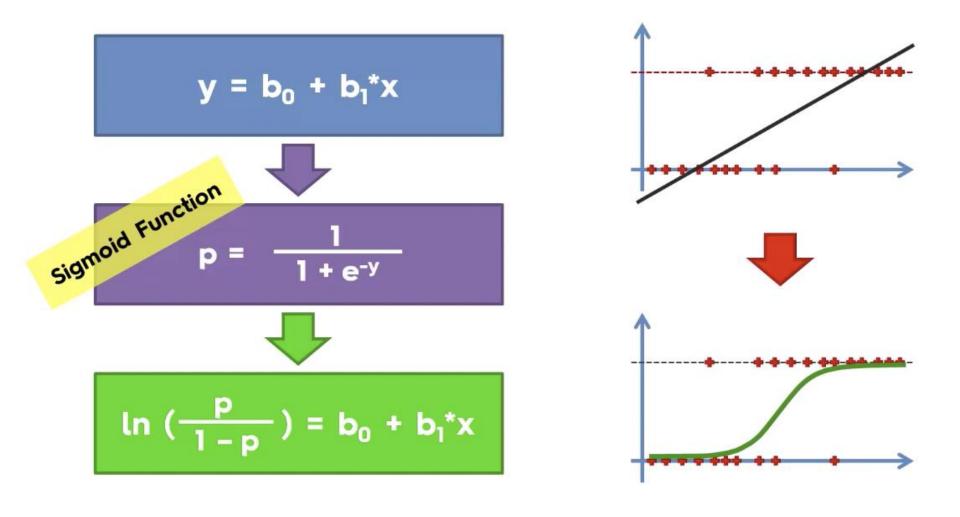
Logistic Regression as a Classifier

What is Logistic Regression?



https://images.slideplayer.com/15/4659936/slides/slide_3.jpg





https://www.vebuso.com/2020/02/linear-to-logistic-regression-explained-step-by-step/

Coefficients:

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 '' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 5734.6 on 4220 degrees of freedom Residual deviance: 5035.5 on 4216 degrees of freedom (19 observations deleted due to missingness)
AIC: 5045.5

Logistic Regression Coefficients

- Log-odds or the natural log of the odds (AKA logit)
- Difficult to interpret.
- We can "exponentiate" logits to create odds ratios (ORs)
 - Easier to understand
 - OR = 1 (no effect)
 - OR < 1 (decrease in odds of outcome=1)
 - OR > 1 (increase in odds of outcome=1)

Interpreting an Odds Ratio

Odds Ratio (OR)

- Ratio of two values of X (Predictor) that are one unit apart
- Categorical Predictors: OR reflects the odds of the Predictor=1 category vs. the Predictor=0 category on the Outcome=1 category
- Continuous Predictors: OR reflects the increase/decrease in odds of the Outcome for a one unit increase in the Predictor

Categorical Example

OR reflects the odds of the Predictor=1 category vs. the Predictor=0 category on the Outcome=1 category

- Predictor = bmicat_X1 (0=Underweight, **1=Underweight**)
- Outcome = Died via CVD (1) vs. did not die via CVD (0)
- bmicat_X1 OR = $e^{0.16434} = 1.18$
- Interpretation: The odds of dying via CVD (Outcome=1) are 1.18 times larger for those who were Underweight according to the BMI (Predictor=1) (compared to those who were Normal according to the BMI), holding all other variables in the model constant.

Continuous Example

OR reflects the increase/decrease in odds of the Outcome for a one unit increase in the Predictor

- Predictor = Age
- Outcome = Died via CVD (1) vs. did not die via CVD (0)
- Age OR = $e^{0.09858} = 1.10$
- Interpretation: The odds of dying via CVD (Outcome=1) are 1.10 larger for each additional year of life, all else being equal.

Another way to report

 (OR - 1) X 100 = percent increase if positive, or decrease if negative, (over reference category of Predictor) in odds of outcome (Outcome)

Categorical Example

- Predictor = bmicat_X1 (0=Underweight, **1=Underweight**)
- Outcome = Died via CVD (1) vs. did not die via CVD (0)
- bmicat_X1 OR = $e^{0.16434} = 1.18$
- $(1.18 1) \times 100 = 0.18 \times 100 = 18\%$
- For those who were Underweight according to the BMI
 (Predictor=1) (compared to those who were Normal
 according to the BMI), the odds of dying via CVD
 (Outcome=1) increased by 18%, all else being equal.

Continuous Example

- Predictor = Age
- Outcome = **Died via CVD (1)** vs. did not die via CVD (0)
- Age OR = $e^{0.09858} = 1.10$
- $(1.10 1) \times 100 = 0.10 \times 100 = 10\%$
- For each additional year of life (1 unit increase on Predictor), the odds of dying via CVD (Outcome=1) increase by 10%, all else being equal.

Now for the intercept

- Linear Regression
 - Value of Outcome when all Predictors equal zero.
- Logistic Regression
 - Probability when all Predictors equal zero.
 - Baseline Probability

$$\frac{(e^{Intercept})}{(1+e^{Intercept})} = Base Probability$$

Baseline probability

$$\frac{\left(e^{-5.47823}\right)}{\left(1+e^{-5.47823}\right)}$$

$$\frac{0.00417}{\left(1+0.00417\right)}$$

The predicted probability that someone will die from CVD is .42% when *Age* is zero and they are *Normal according to the BMI* (*Underweight* is zero, *Overweight* is zero, and *Obese* is zero).

= 0.0042

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Coefficients:
```

$$e^{Coefficient} = Odds Ratio$$

$$\frac{(e^{Intercept})}{(1+e^{Intercept})} = Base Probability$$

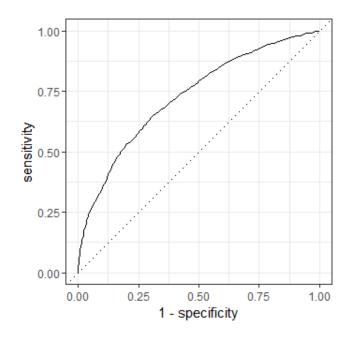
Characteristic	OR1	95% CI1	p-value
(Intercept)	0.00	0.00, 0.01	<0.001
AGE	1.10	1.09, 1.11	<0.001
bmicat_X1	1.18	0.64, 2.12	0.6
bmicat_X2	1.32	1.14, 1.52	<0.001
bmicat_X3	1.98	1.61, 2.45	<0.001

¹OR = Odds Ratio, CI = Confidence Interval

Model Assessment

- Several possible metrics
 - Loglikelihood (LL); Negative loglikelihood (-LL, deviance);
 Akaike information criterion (AIC); Bayesian information criterion (BIC); Brier score (analogous to RMSE^2)
 - Accuracy, Sensitivity, Specificity, ROC-AUC

	Estimate
Accuracy	0.68
Sensitivity	0.54
Specificity	0.78
AUC	0.73



	Reality									Acc	Sen	Spe	
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Model 3	R	В	В	R	R	R	В	R	R	В	0.50	0.60	0.40

	Reality						Acc	Sen	Spe				
	R	В	R	В	R	В	R	В	R	В	_	_	_
Model 1	R	R	R	R	R	R	R	R	R	R	0.50	1.00	0.00
Model 2	В	В	В	В	В	В	В	В	В	В	0.50	0.00	1.00
Model 3	R	В	В	R	R	R	В	R	R	В	0.50	0.60	0.40

		Rec		
	Model 1	R	В	
Prediction	R	5	5	
Pred	В	0	0)	
		5	5	Total = 10

Accuracy =
$$5+0/10 = 0.50$$

Sensitivity =
$$5/5 = 1.00$$

Specificity =
$$0/5 = 0.00$$

False Pos =
$$5/5 = 1.00$$

False Neg =
$$0/5 = 0.00$$

		Rea		
	Model 1	R	В	
Prediction	R	5	5	
Predi	В	0	0	
		5	5	Total = 10

Accuracy =
$$5+0/10 = 0.50$$

Sensitivity = $5/5 = 1.00$
Specificity = $0/5 = 0.00$

		Rea		
	Model 1	R	В	
Prediction	R	0	0	
	В	5	5	
		5	5	Total = 10

Accuracy =
$$0+5/10 = 0.50$$

Sensitivity = $0/5 = 0.00$
Specificity = $5/5 = 1.00$

Accuracy =
$$3+2/10 = .50$$

Sensitivity = $3/5 = 0.60$
Specificity = $2/5 = 0.40$