

The logo for ARLAB, featuring the letters "ARLAB" in a bold, red, sans-serif font.

ME/CprE/ComS 557

# Computer Graphics and Geometric Modeling

## Texture Mapping with OpenGL

October 15th, 2015

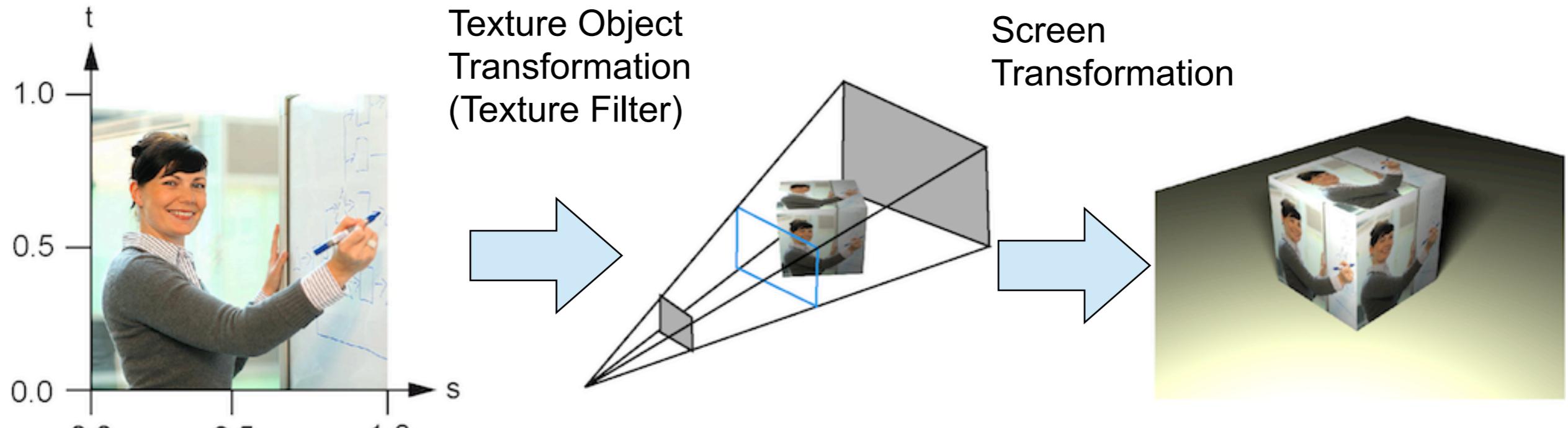
Rafael Radkowski

The Iowa State University logo, featuring the words "IOWA STATE UNIVERSITY" in a large, red, serif font, with "OF SCIENCE AND TECHNOLOGY" in a smaller, green, serif font below it.

# Content

- Texture Filter Reminder
- Bilateral Filter
- Midmaps
- Trilinear Filter

# The Texture Rendering Process



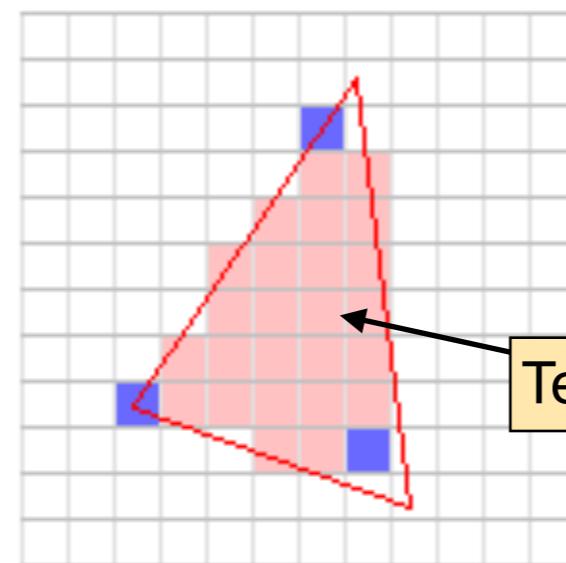
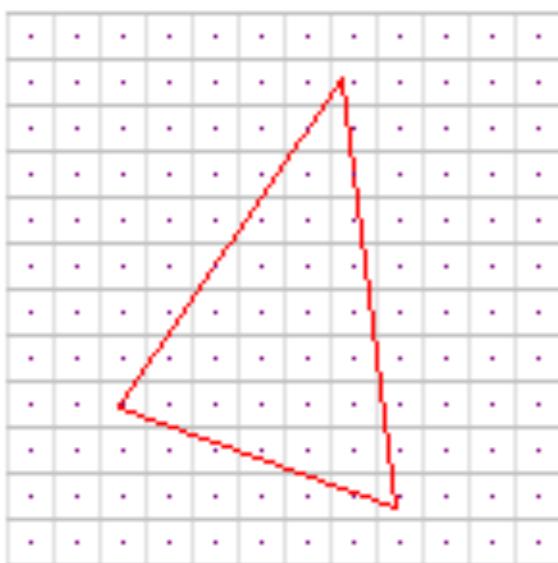
*Texture*

Texture Object  
Transformation  
(Texture Filter)

Screen  
Transformation

*Texture mapped to a object  
and perspective distorted*

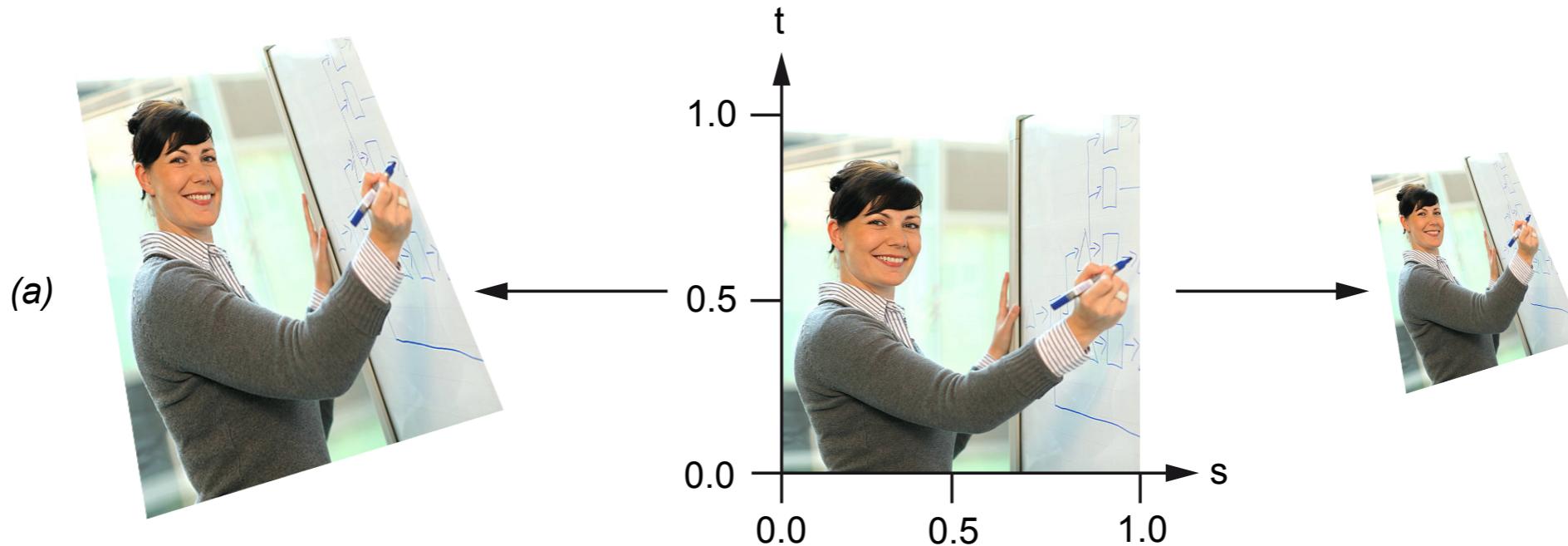
*The output on screen*



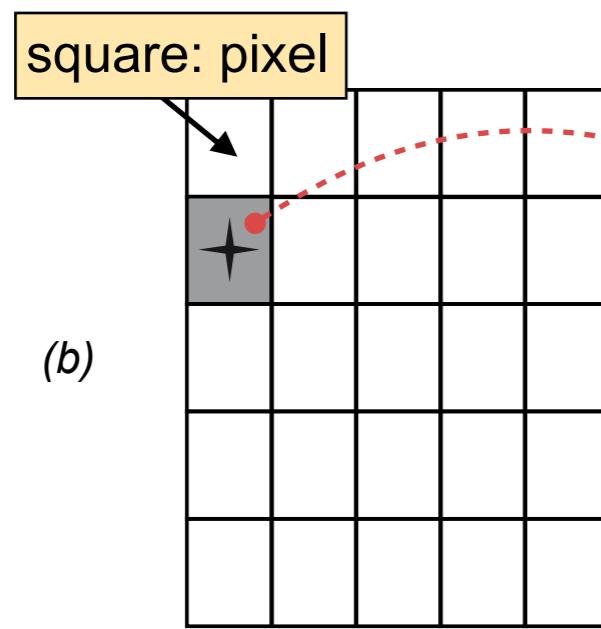
The graphics card must identify the correct color for each fragment (pixel) of a primitive.

**Texel color**

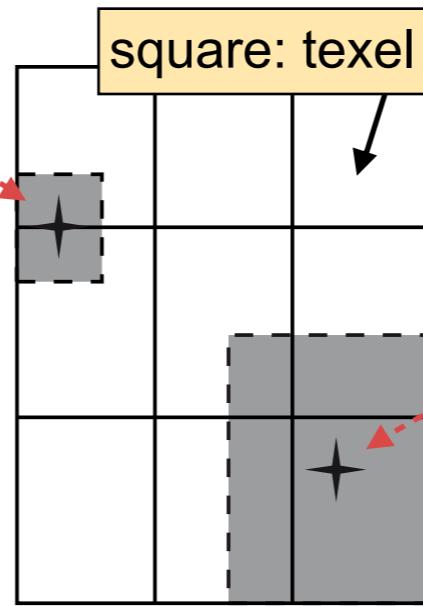
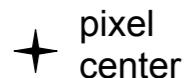
# Magnification & Minifying



**Texture Magnification Function**

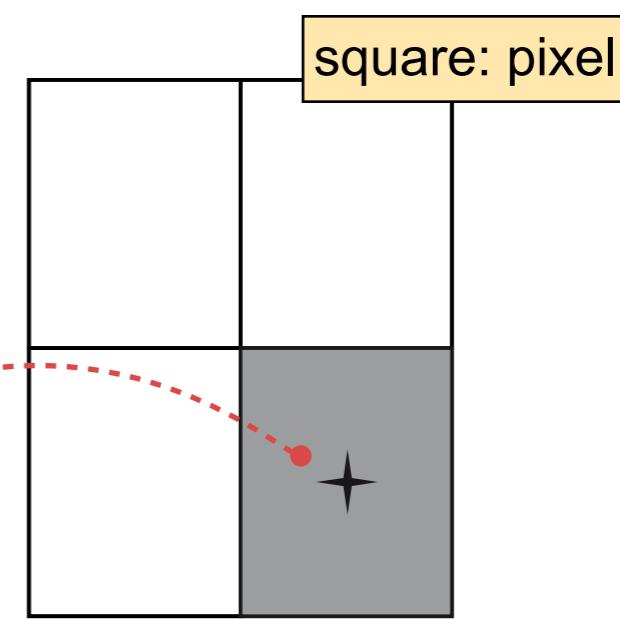


3D object is close to the camera and covers 25 pixels on screen



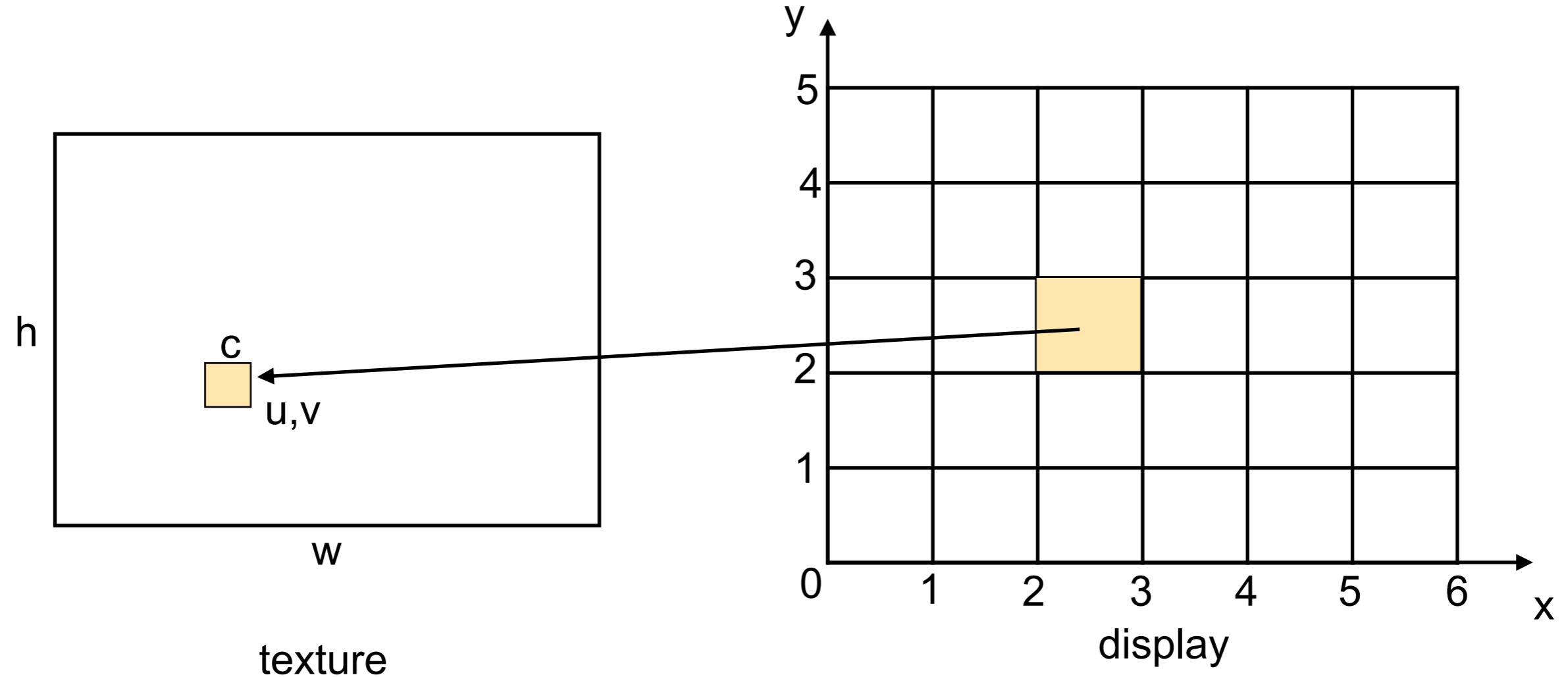
Texture

**Texture Minifying Function**



3D object is distant to camera and covers 4 pixels on screen

# Color selection

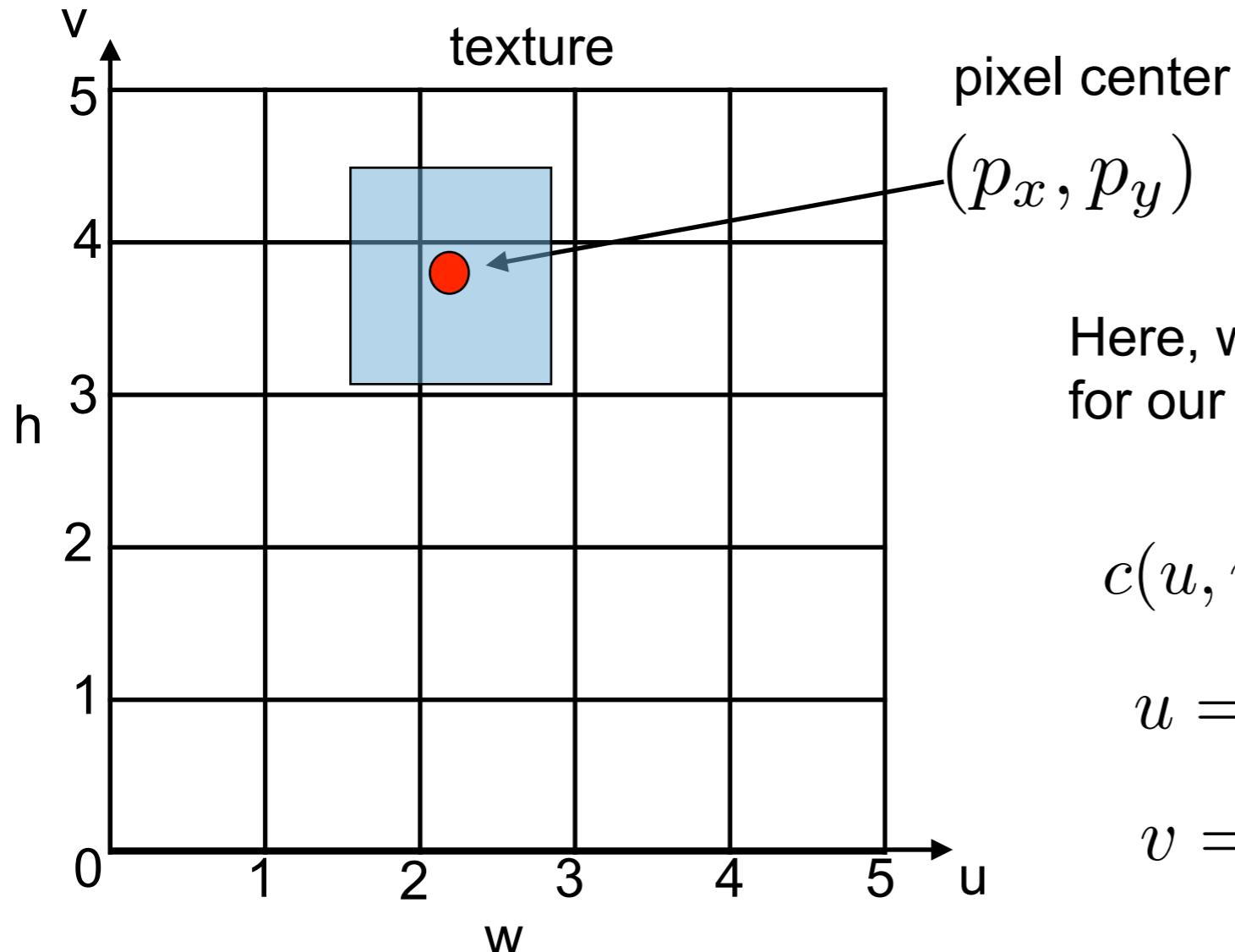


We need to find the color value  $c$  in the texture with size  $h$  and  $w$  in pixels, for fragment  $i, j$ .

$$v = \lfloor x \ w \rfloor \quad \text{and} \quad v = \lfloor y \ h \rfloor$$

$\lfloor x \rfloor$  is the *floor function*. it gives the highest inter value  $\leq x$

# Point Sampling / Nearest Neighbor



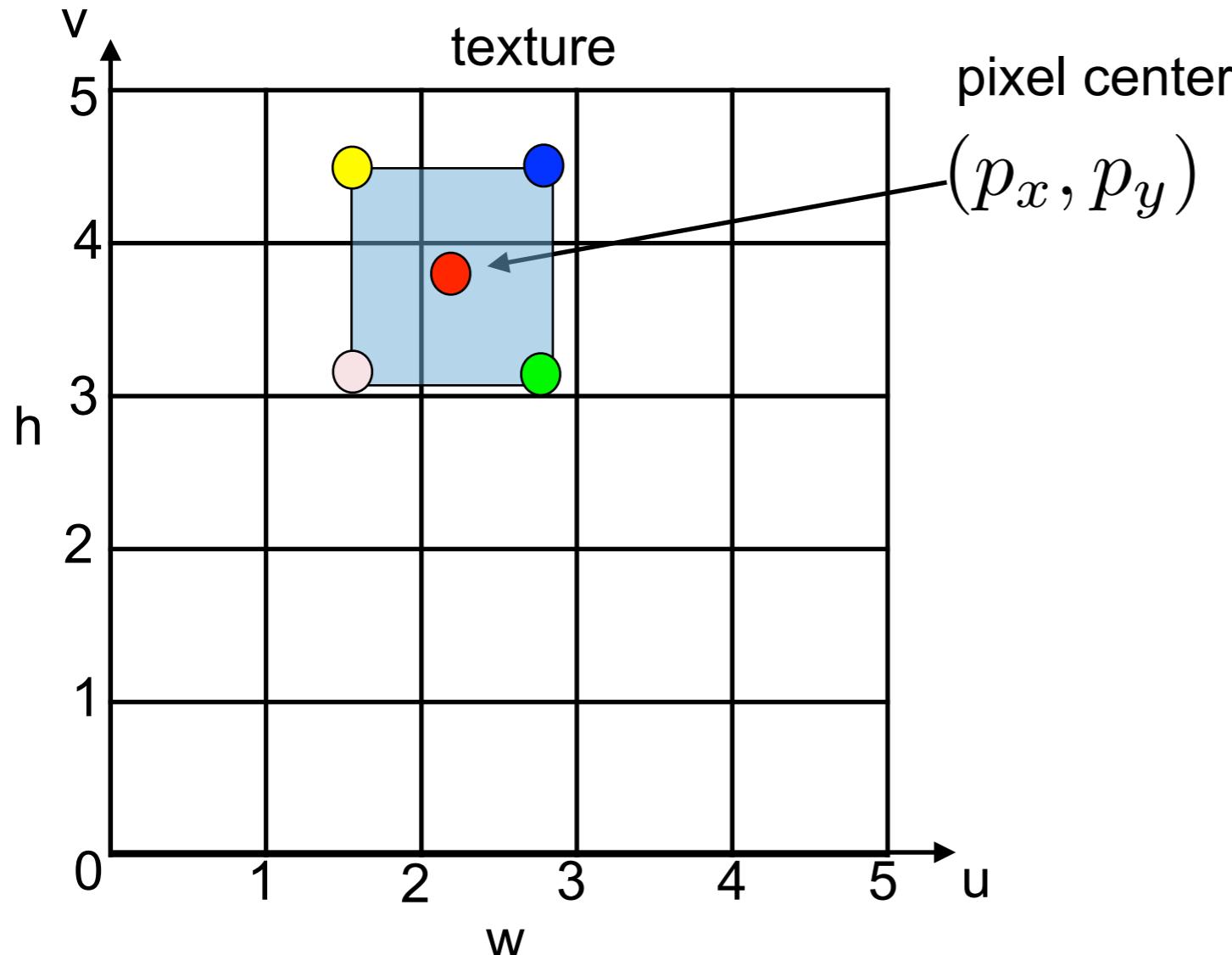
Here, we take the nearest color  $c$  for our vertex coordinate

$$c(u, v) = c_{x,y} \text{ with}$$

$$u = \lfloor p_x \, w \rfloor$$

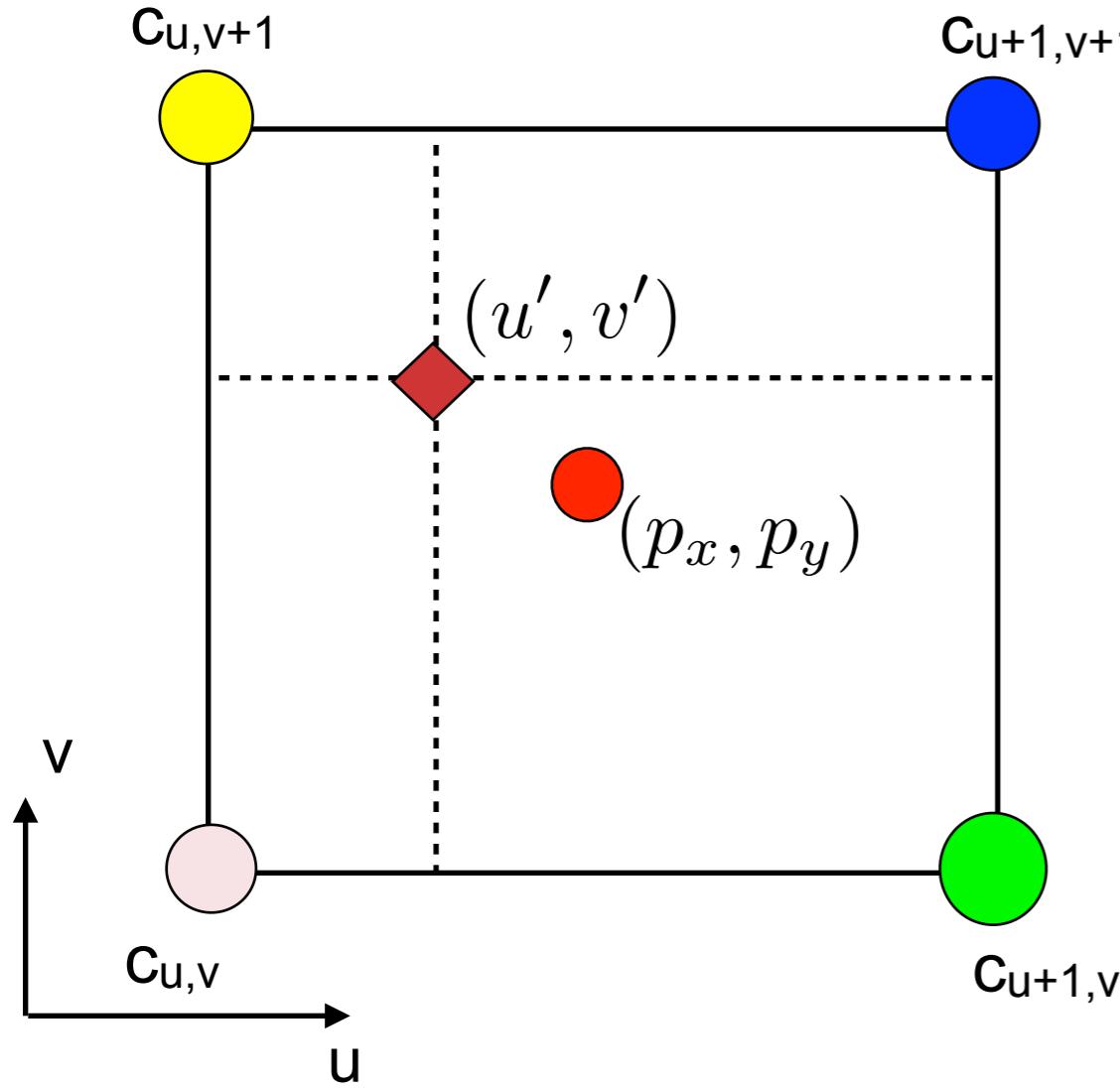
$$v = \lfloor p_y \, h \rfloor$$

# Bilinear Interpolation



Bilinear interpolation is an extension of linear interpolation. The key idea is to perform linear interpolation first in one direction, and then again in the other direction.

# Bilinear Interpolation



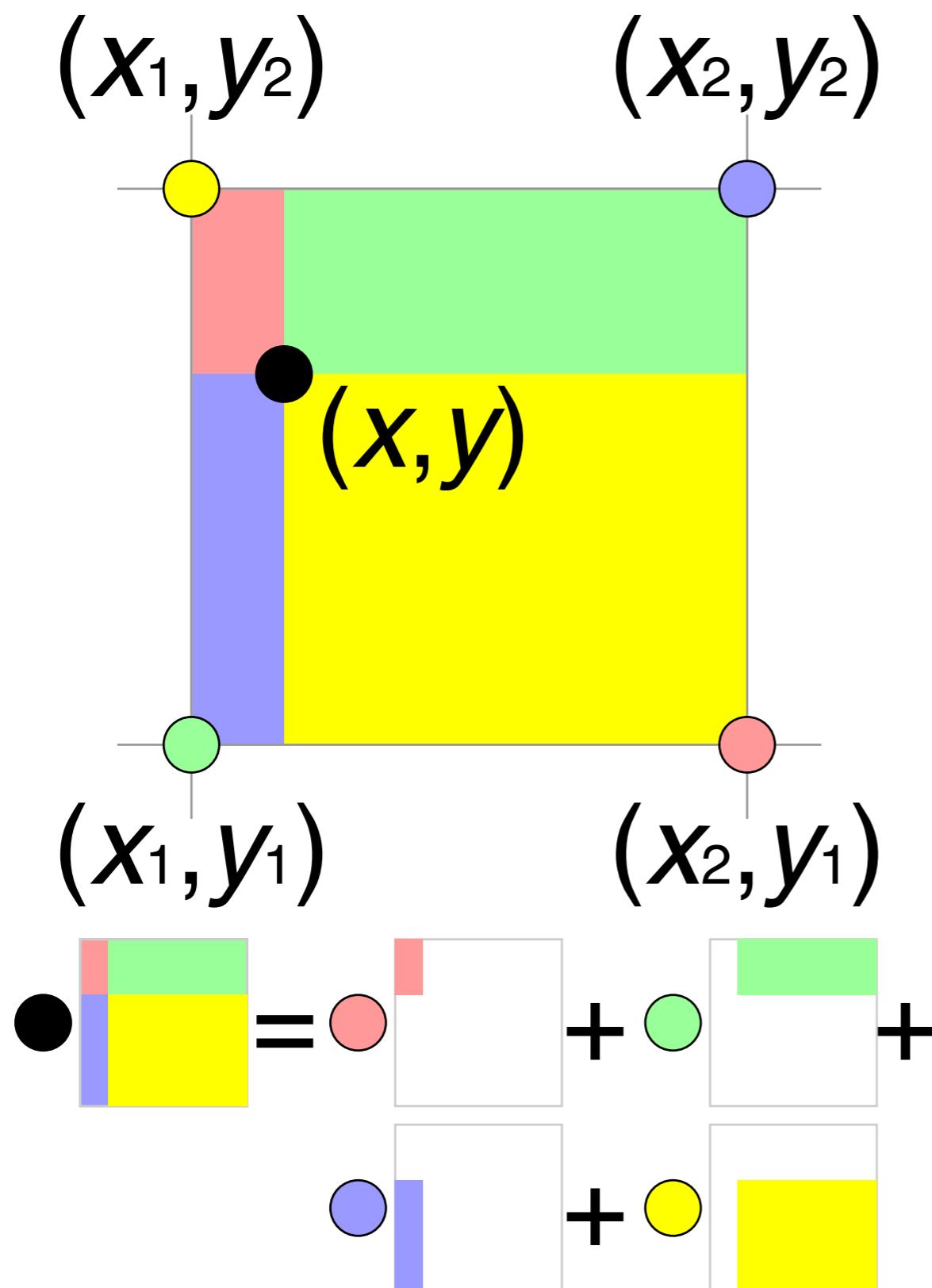
Relative position - range 0 to 1 - within four adjacent texel positions

$$(u', v') = (p_x - \lfloor p_x \rfloor, p_y - \lfloor p_y \rfloor)$$

Color value

$$\begin{aligned} c_{x,y} = & (1 - u')(1 - v')c_{u,v} \\ & + u'(1 - v')v_{u+1,v} \\ & + (1 - u')v'c_{u,v+1} \\ & + u'v'c_{u+1,v+1} \end{aligned}$$

- The "opposite" color has more weight
- Note, all fragments add up to 1.



## Bilinear Interpolation

# Limitations



Bilinear filtering is rather accurate until the scaling of the texture gets below half or above double the original size of the texture - that is, if the texture was 256 pixels in each direction, scaling it to below 128 or above 512 pixels can make the texture look bad, because of missing pixels or too much smoothness.

# MipMap-Filter

*multum in parvo, meaning "much in little"*



2048 x 2048



Original  
texture

1024 x 1024



Pre-calculated images  
down to 2 x 2 pixels.

512 x 512



256 x 256



128 x 128



64 x 64



(0)

(1)

(2)

(3)

(4) (5)

Filtering for minification is expensive, and different areas must be averaged depending on the amount of minification

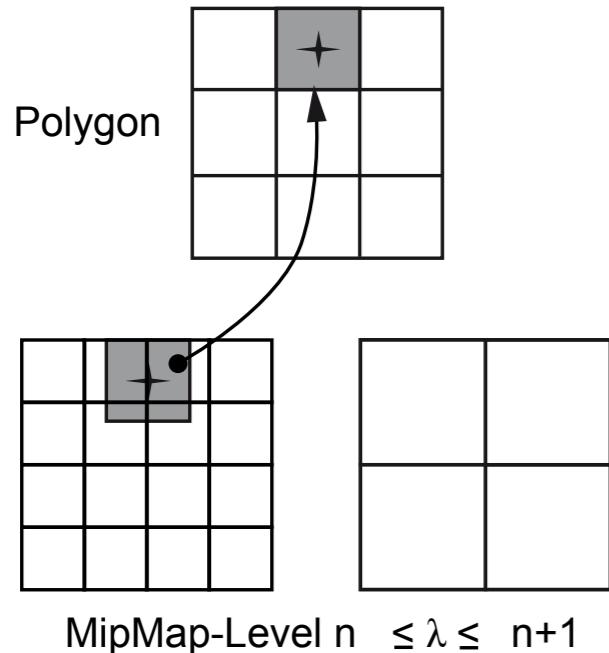
MipMap-Approach

- Prefilter different texture images at different resolutions
- For each screen pixel, choose texture that has an appropriate size

# MipMap-Minifying Filter

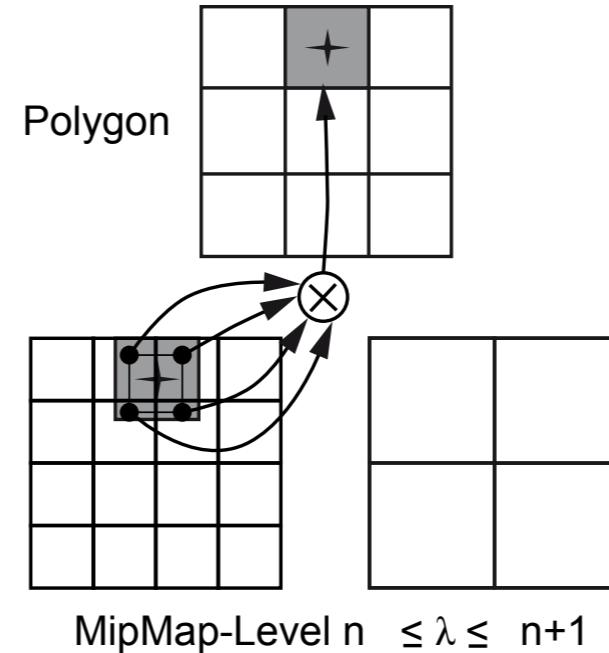


**Point Sampling**



`GL_NEAREST_MIPMAP_NEAREST*`

**Bilineare Filter**



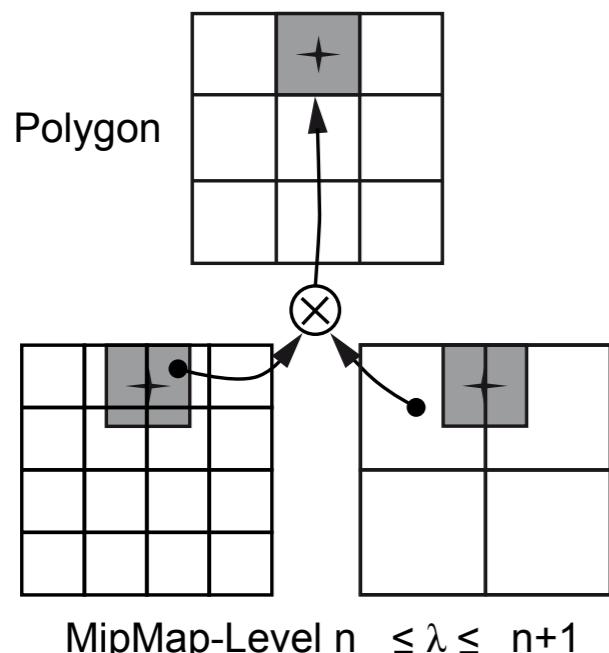
`GL_LINEAR_MIPMAP_NEAREST`

**Calculating the MipMap Level:**

$$\lambda = \log_2(\max(\frac{1}{\rho_x}, \frac{1}{\rho_y}))$$

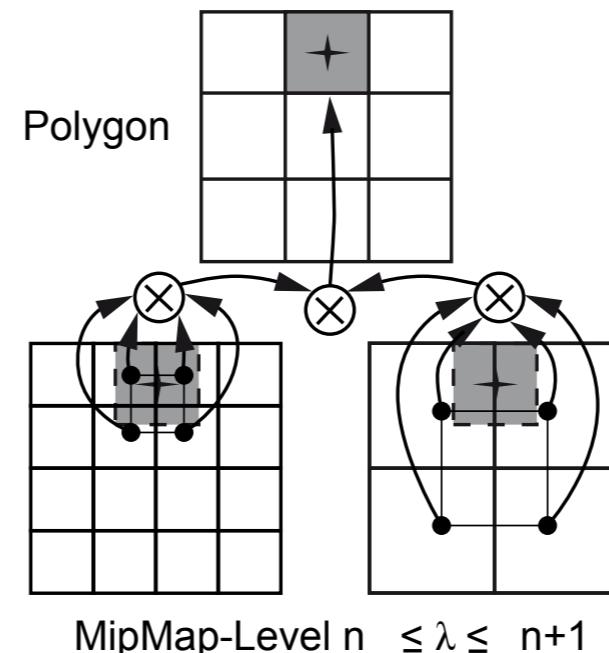
$\rho_x, \rho_y$  : Scaling factors, provided by the graphics card.

**Trilineare Filter**



`GL_NEAREST_MIPMAP_LINEAR`

**Trilineare Filter**



`GL_LINEAR_MIPMAP_LINEAR`

# Calculating the MidMap Level



The level depends on a scale factor  $\rho(x, y)$  and the level-of-detail parameter  $\lambda(x, y)$ , defined as

$$\lambda_{base}(x, y) = \log_2[\rho(x, y)]$$

with

$$\rho = \max \left\{ \sqrt{\left( \frac{\partial u}{\partial x} \right)^2 + \left( \frac{\partial v}{\partial x} \right)^2 + \left( \frac{\partial w}{\partial x} \right)^2}, \sqrt{\left( \frac{\partial u}{\partial y} \right)^2 + \left( \frac{\partial v}{\partial y} \right)^2 + \left( \frac{\partial w}{\partial y} \right)^2} \right\}$$

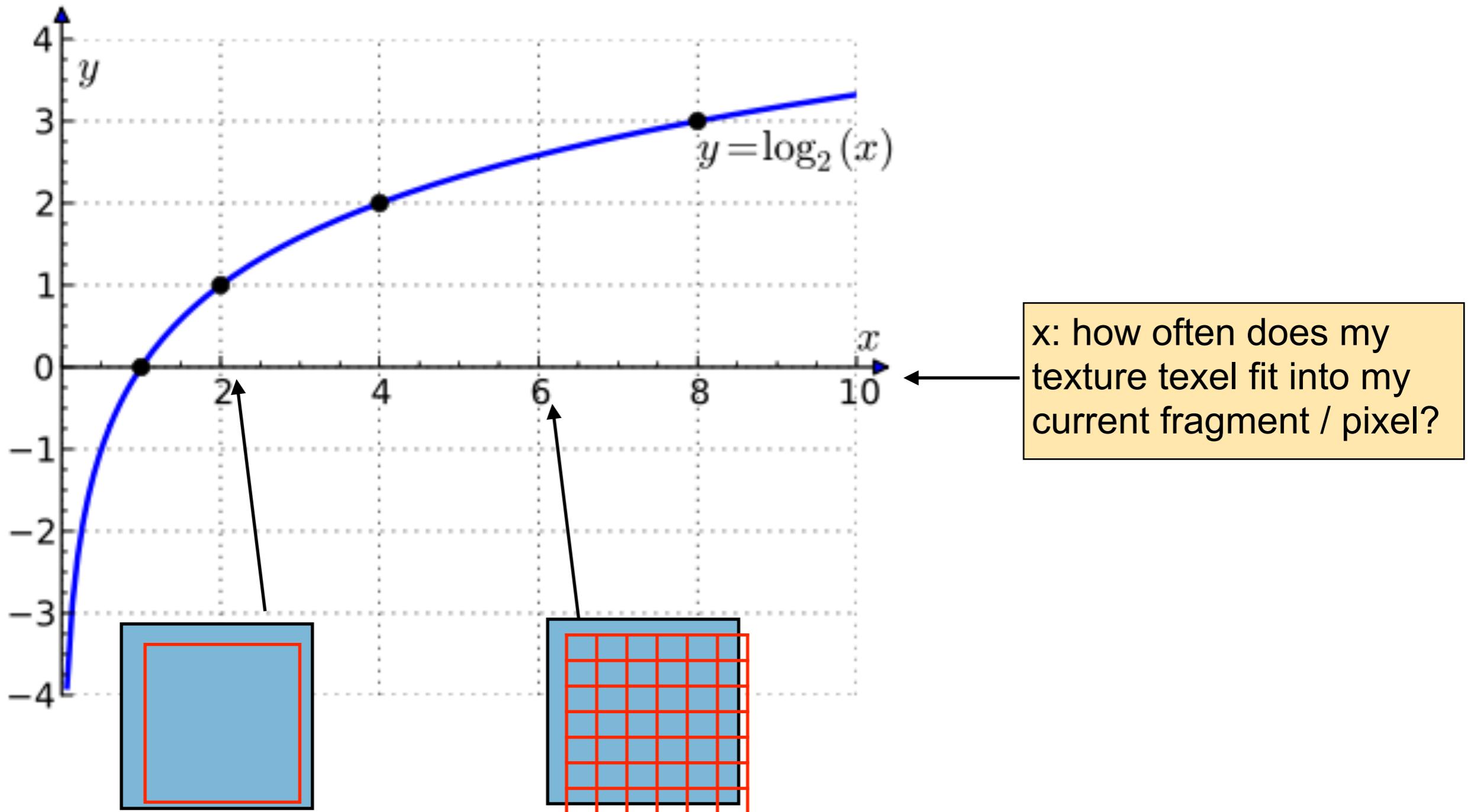
where  $\partial u / \partial x$  indicates the derivative of  $u$  with respect to window  $x$ , and similarly for the other derivatives. For a line, the formula is

$$\rho = \sqrt{\left( \frac{\partial u}{\partial x} \Delta x + \frac{\partial u}{\partial y} \Delta y \right)^2 + \left( \frac{\partial v}{\partial x} \Delta x + \frac{\partial v}{\partial y} \Delta y \right)^2 + \left( \frac{\partial w}{\partial x} \Delta x + \frac{\partial w}{\partial y} \Delta y \right)^2} / l,$$

where  $\Delta x = x_2 - x_1$  and  $\Delta y = y_2 - y_1$  with  $(x_1, y_1)$  and  $(x_2, y_2)$  being the segment's window coordinate endpoints and  $l = \sqrt{\Delta x^2 + \Delta y^2}$ .

# Binary Logarithm

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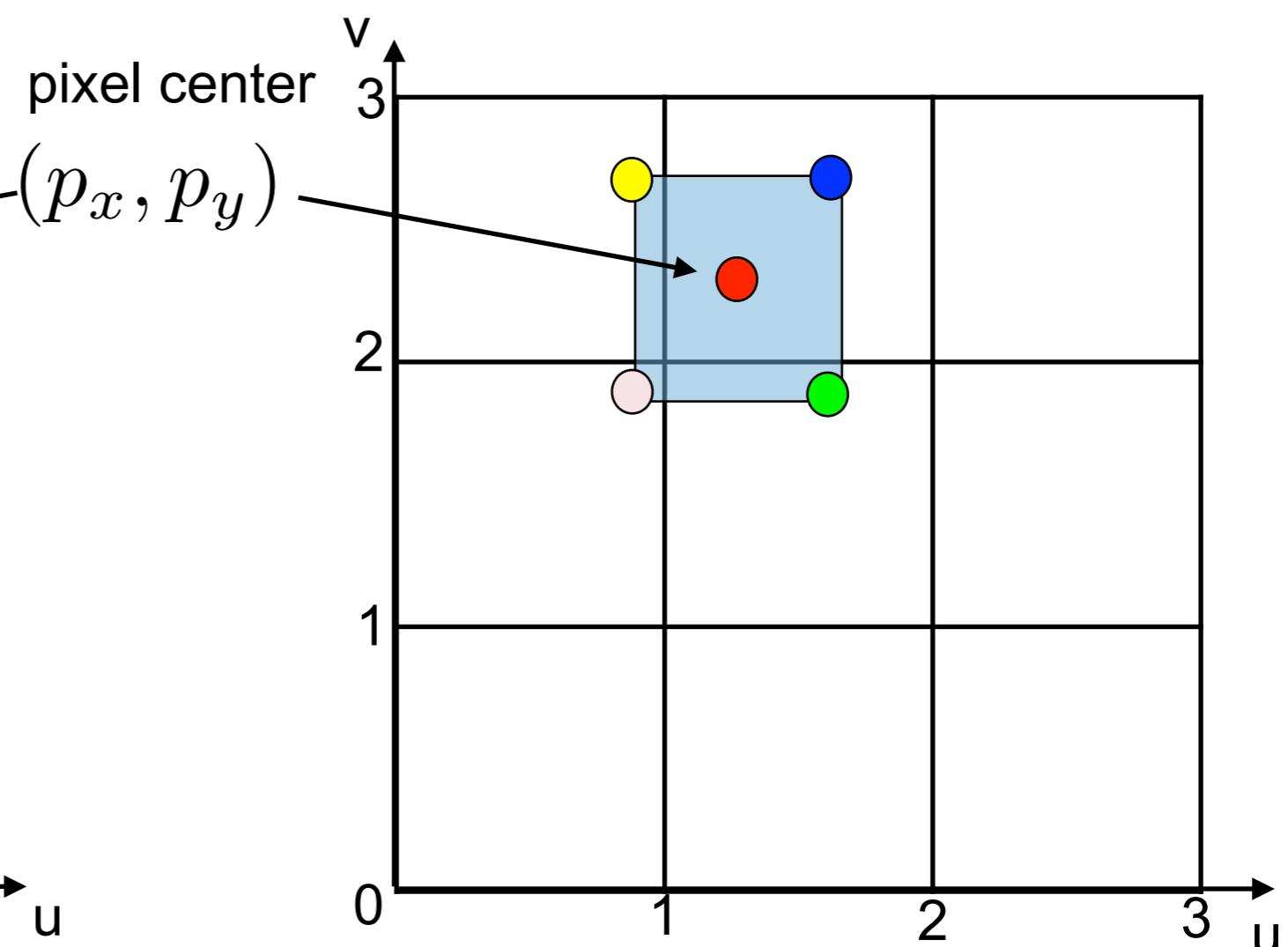
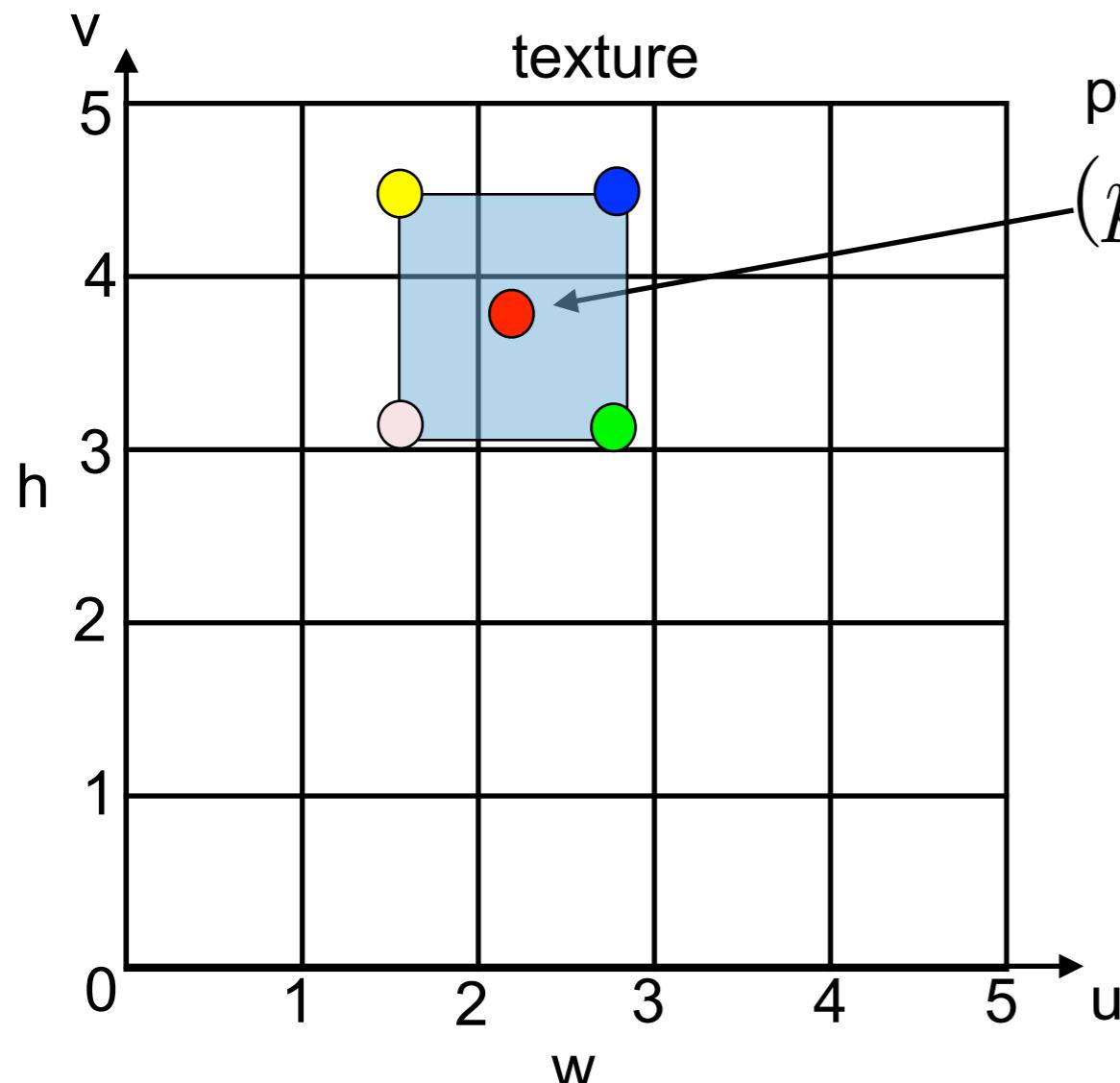


red: texel

blue: fragment

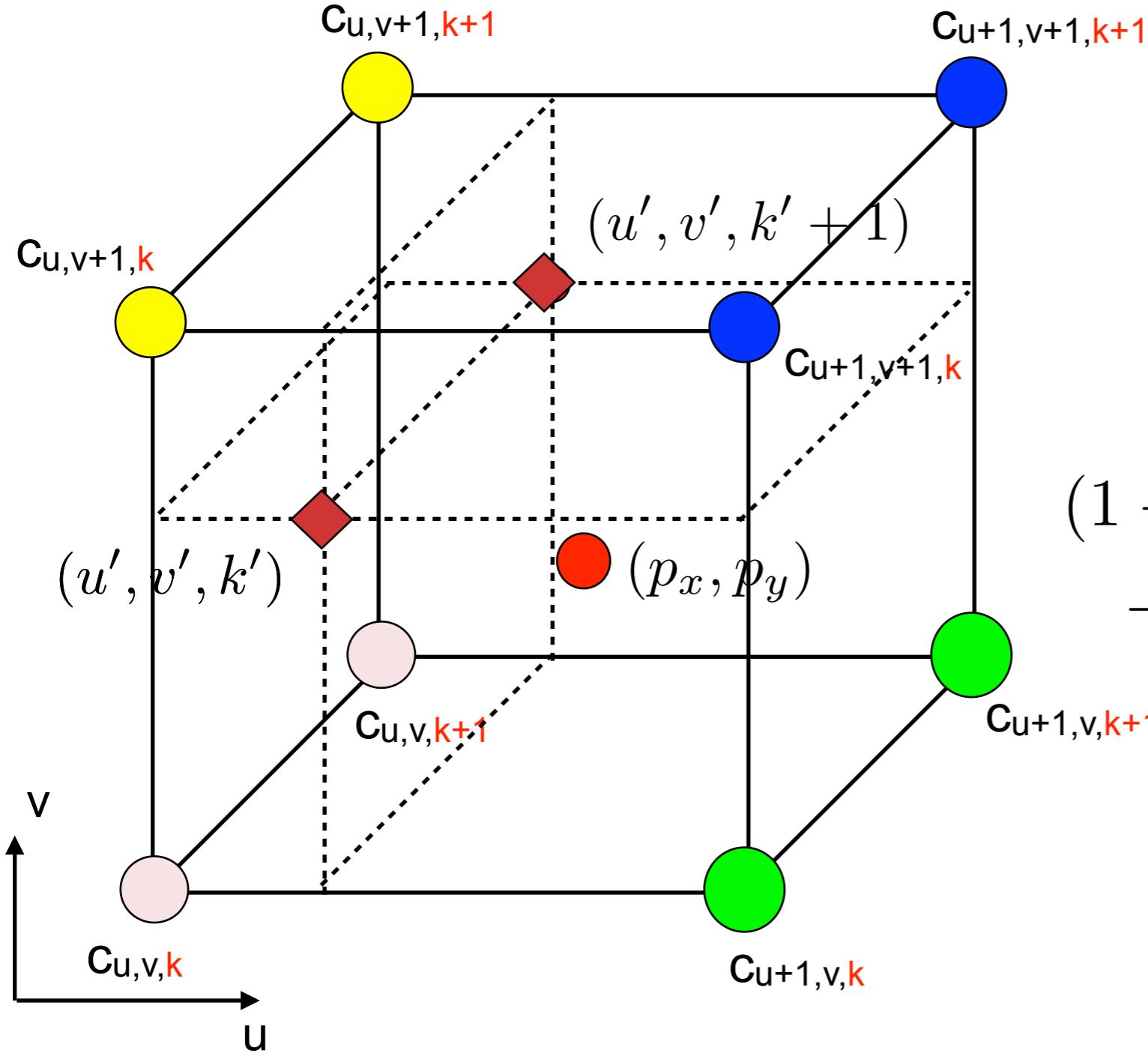
# Trilinear Interpolation (Bicubic Interpolation)

ARLAB



# Trilinear Interpolation (Bicubic Interpolation)

ARLAB

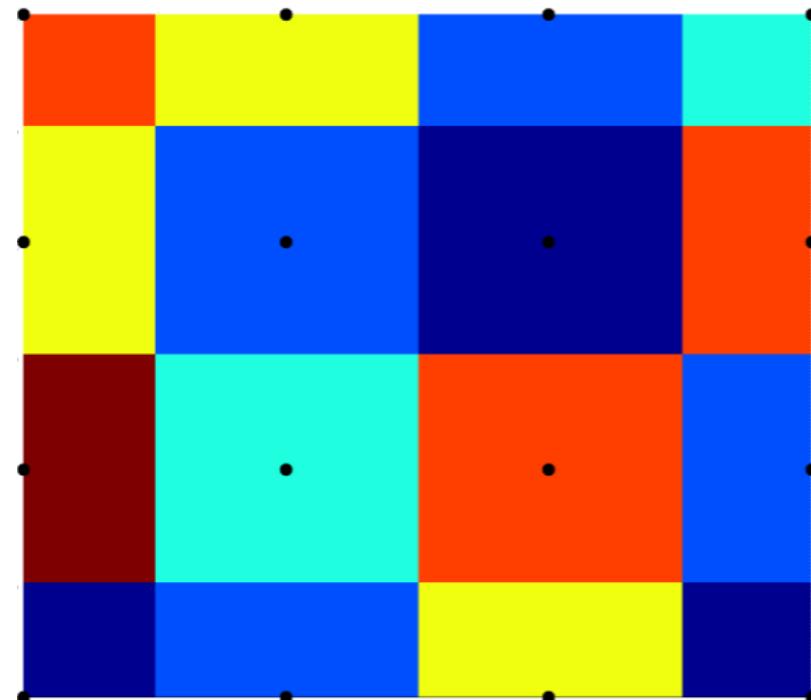


Mathematical representation:  
we add an additional  
component  $k$ .

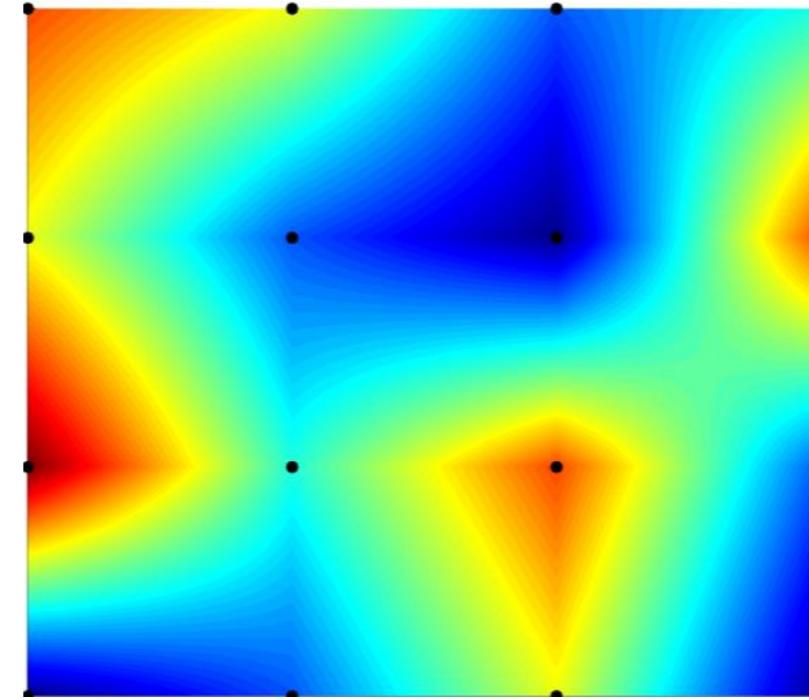
$$\begin{aligned} c_{x,y} = c(u, v, k) = \\ (1 - u')(1 - v')(1 - k')c_{u,v,k} \\ + u'(1 - v')(1 - k)v_{u+1,v,k} \\ + \dots \end{aligned}$$

# Example

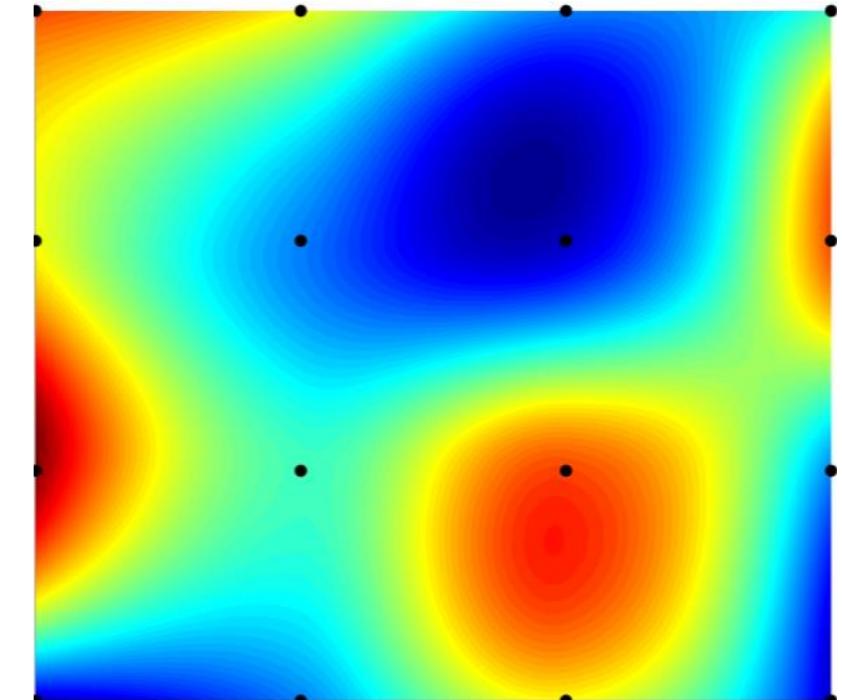
ARLAB



nearest texel

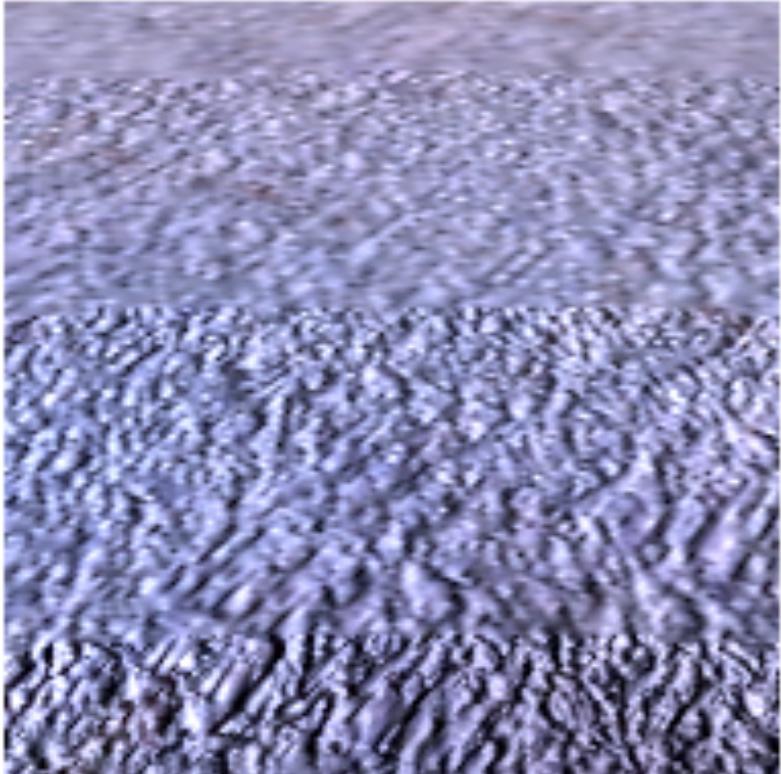


bilinear interpolation  
(weighted average  
of 2x2 texels)

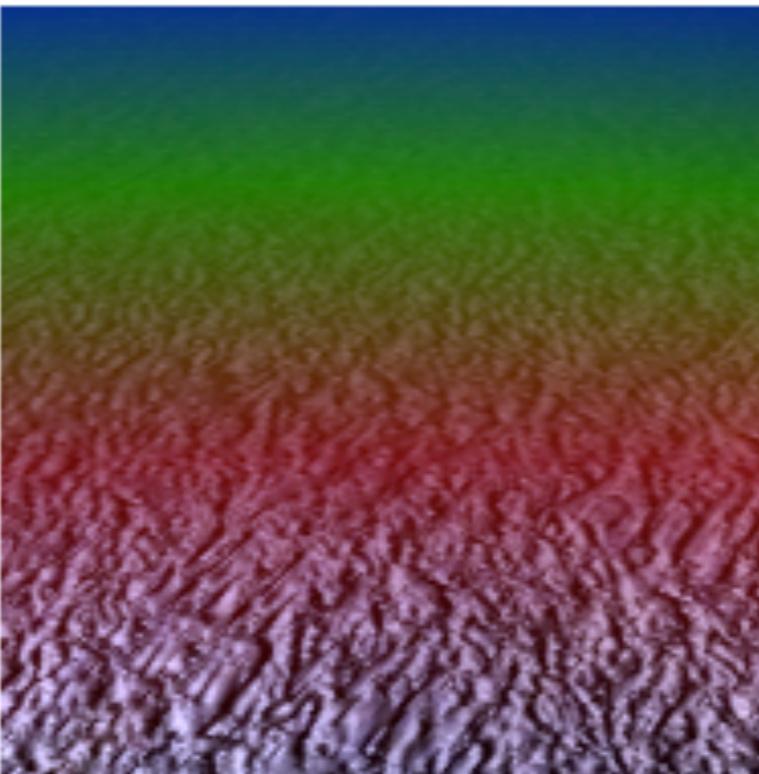
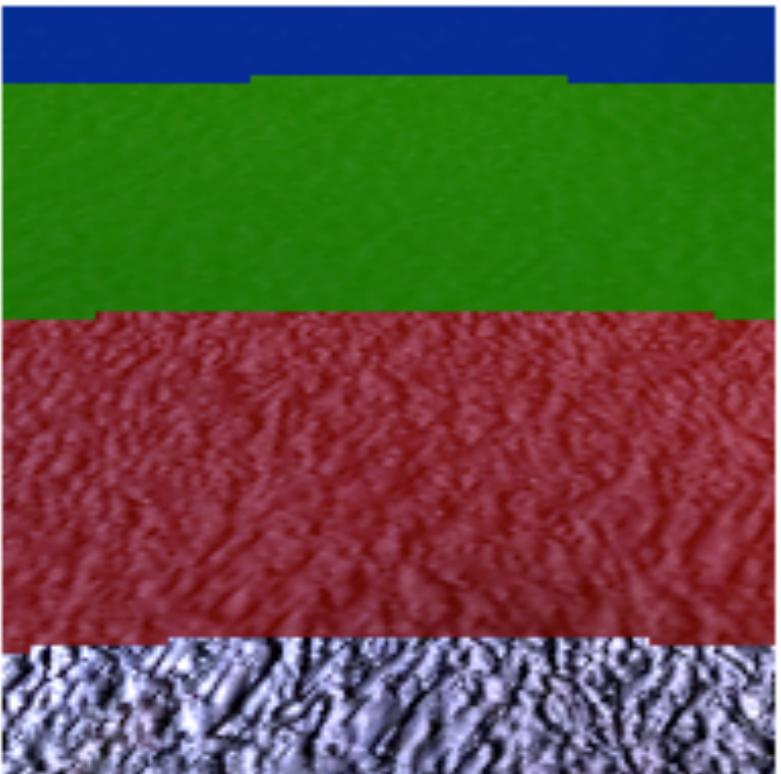


trilinear or bicubic  
interpolation (weighted  
average of 2x2 texels)

# Bilinear vs. Trilinear



Difference between a Bilinear (left) and a Trilinear (right) filter



Difference between a Bilinear (left) and a Trilinear (right) filter visualized in false colors. Each color represents a different MipMap level



# Filter with OpenGL and GLSL

# Fragment Shader Program

## Nearest Neighbor



This is the regular texture shader code

```
#version 410 core

uniform sampler2D tex; //this is the texture

in vec2 pass_TexCoord; //this is the texture coord
in vec4 pass_Color;
out vec4 color;

void main(void)
{
    // This function finds the color component for each texture coordinate.
    vec4 tex_color = texture(tex, pass_TexCoord);

    // This mixes the background color with the texture color.
    // The GLSL shader code replaces the former environment. It is now up to us
    // to figure out how we like to blend a texture with the background color.
    color = pass_Color + tex_color;
}
```

# Fragment Shader Program

## Bilateral Filter



```
#version 410 core

uniform sampler2D tex; //this is the texture

in vec2 pass_TexCoord; //this is the texture coord
in vec4 pass_Color;
out vec4 color;

void main(void)
{
    // This function finds the color component for each texture coordinate.
    vec4 tex_color = texture2DBilinear(tex, pass_TexCoord);

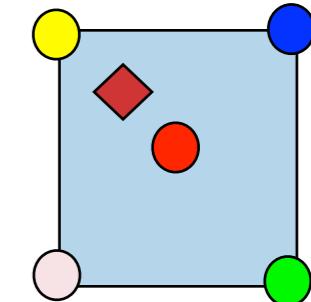
    // This mixes the background color with the texture color.
    // The GLSL shader code replaces the former environment. It is now up to us
    // to figure out how we like to blend a texture with the background color.
    color = pass_Color + tex_color;
}
```

# Fragment Shader Program

## Bilateral Filter

ARLAB

Texture is a square texture



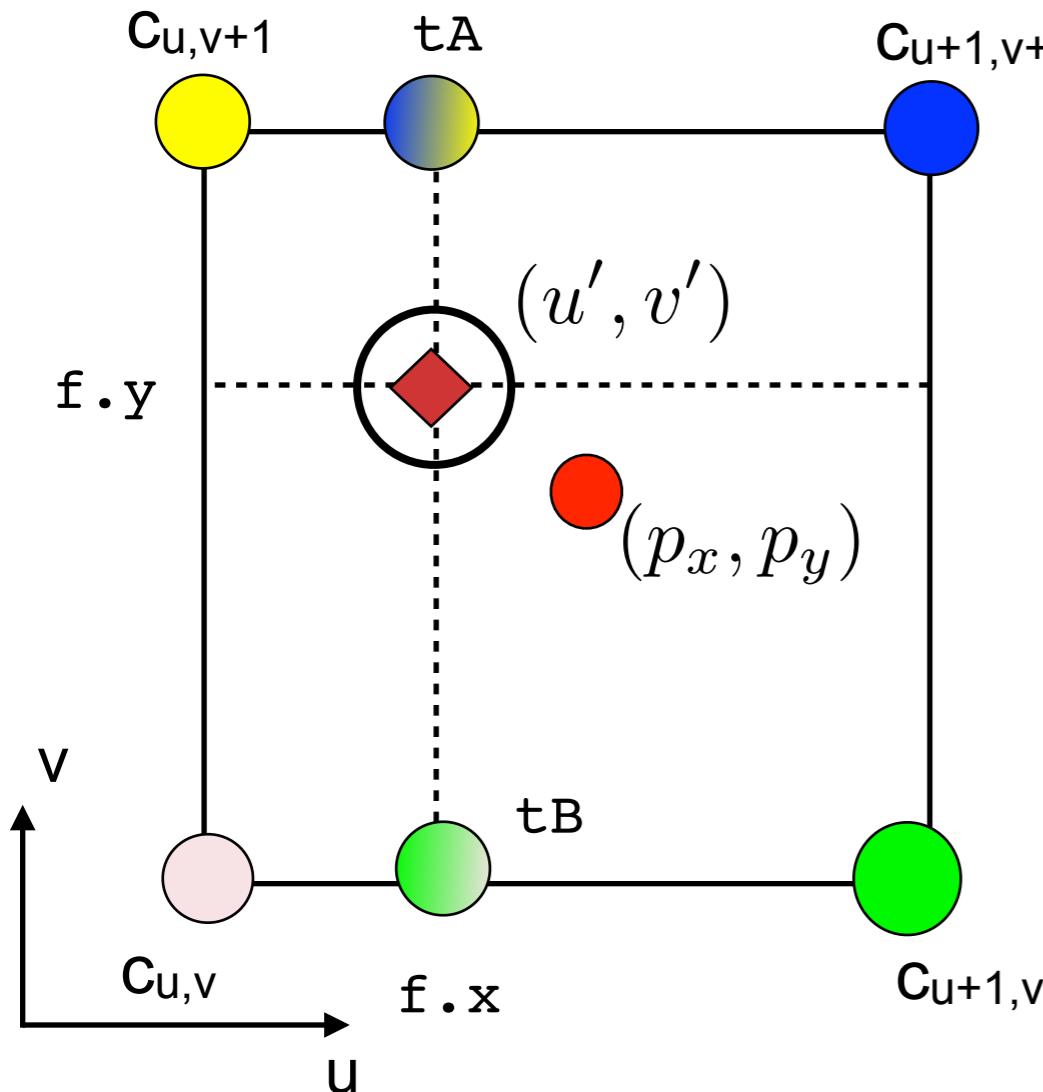
```
const float textureSize = 512.0; //size of the texture  
const float texelSize = 1.0 / textureSize; //size of one texel
```

```
vec4 texture2DBilinear( sampler2D textureSampler, vec2 uv )  
{  
    vec4 tl = texture(textureSampler, uv);  
    vec4 tr = texture(textureSampler, uv + vec2(texelSize, 0));  
    vec4 bl = texture(textureSampler, uv + vec2(0, texelSize));  
    vec4 br = texture(textureSampler, uv + vec2(texelSize , texelSize));  
  
    vec2 f = fract( uv.xy * textureSize ); // the decimal part  
    vec4 tA = mix( tl, tr, f.x ); // interpolate the red dot in the image  
    vec4 tB = mix( bl, br, f.x ); // interpolate the blue dot in the image  
    return mix( tA, tB, f.y ); // interpolate the green dot in the image  
}
```

# Fragment Shader Program Bilateral Filter

ARLAB

The mathematical theory differs a little from the computational process. However, the output is equal



- ◆ `vec2 f = fract( uv.xy * textureSize );`
- `vec4 tA = mix( tl, tr, f.x );`
- `vec4 tB = mix( bl, br, f.x );`
- `return mix( tA, tB, f.y );`

# fract / mix



compute the fractional part of the argument

```
genType fract( genType x);
```

### Parameters:

- x - Specify the value to evaluate.

linearly interpolate between two values

```
genType mix( genType x, genType y, float a);
```

### Parameters

- x - Specify the start of the range in which to interpolate.
- y - Specify the end of the range in which to interpolate.
- a - Specify the value to use to interpolate between x and y.

# Midmaps in GLSL

Calculate the Midmap level in your fragment shader code.

Two steps:

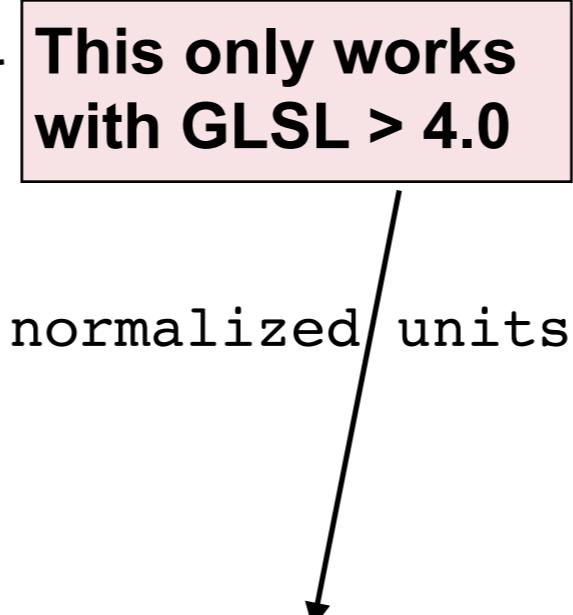
1. We need to find the correct midmap level
2. Fetch the nearest texture color

```
#version 400
uniform sampler2D myTexture;
in vec2 textureCoord; // in normalized units
out vec4 fragColor;

void main()
{
    float mipmapLevel = textureQueryLod(myTexture, textureCoord).x;

    fragColor = textureLod(myTexture, textureCoord, mipmapLevel);
}
```

**This only works with GLSL > 4.0**



# textureQueryLod



compute the level-of-detail that would be used to sample from a texture

```
vec2 textureQueryLod( gsampler2D sampler, vec2 P );
```

## Parameters:

sampler - Specifies the sampler to which the texture whose level-of-detail will be queried is bound

P - Specifies the texture coordinates at which the level-of-detail will be queried.

# textureLod

Perform a texture lookup with explicit level-of-detail

```
gvec4 textureLod( gsampler2D sampler, vec2 P, float lod);
```

## Parameters:

- sampler - Specifies the sampler to which the texture from which texels will be retrieved is bound.
- P - Specifies the texture coordinates at which texture will be sampled.
- lod - Specifies the explicit level-of-detail

# Midmaps in GLSL



Version 3: we need to calculate the midmap level on our own.

```
#version 330

uniform sampler2D myTexture;
in vec2 textureCoord; // in normalized units
out vec4 fragColor;

float mip_map_level(in vec2 texture_coordinate) // in texel units
{
    vec2 dx_vtc          = dFdx(texture_coordinate);
    vec2 dy_vtc          = dFdy(texture_coordinate);
    float delta_max_sqr = max(dot(dx_vtc, dx_vtc), dot(dy_vtc, dy_vtc));
    float mml = 0.5 * log2(delta_max_sqr);
    return max( 0, mml );
}

void main()
{
    // convert texture coordinates to texel units before calling mip_map_level
    float mipmapLevel = mip_map_level(textureCoord * textureSize(myTexture, 0));

    fragColor = textureLod(myTexture, textureCoord, mipmapLevel);
}
```

# dFdx, dFdy

Return the partial derivative of an argument with respect to x or y

```
genType dFdx( genType p);  
genType dFdy( genType p);
```

## Parameters

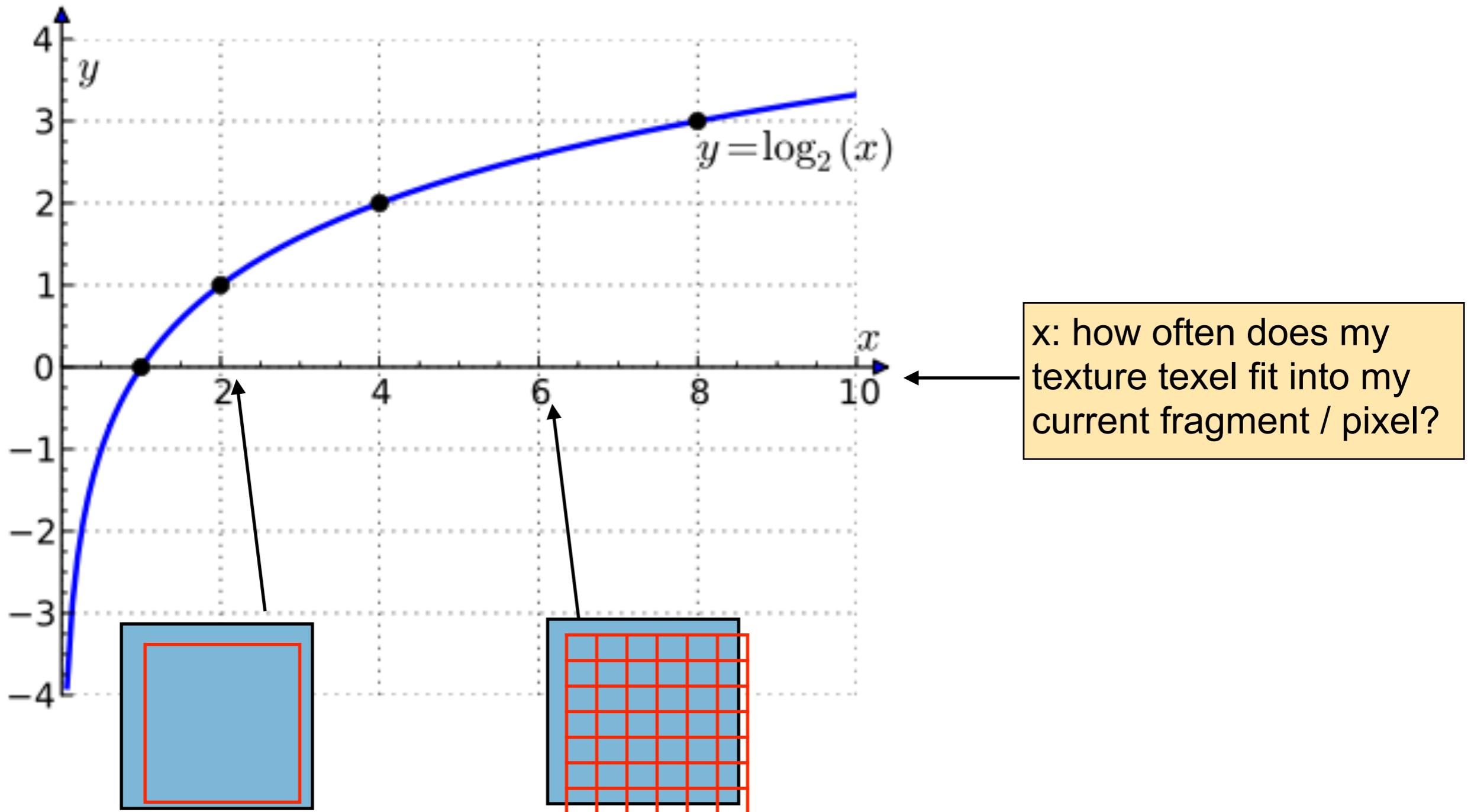
- p - Specifies the expression of which to take the partial derivative.

*Available only in the fragment shader*

$$p_{ux} = \frac{\partial u}{\partial x}, \quad p_{vx} = \frac{\partial v}{\partial x}$$
$$p_{uy} = \frac{\partial u}{\partial y}, \quad p_{vy} = \frac{\partial v}{\partial y}$$

# Binary Logarithm

ARLAB



red: texel

blue: fragment

# Trilinear / Cubic Filter



```
vec4 TrilinearFilter(sampler2D texture, vec2 texcoord, vec2 texscale)
{
    float fx = fract(texcoord.x);
    float fy = fract(texcoord.y);
    texcoord.x -= fx;
    texcoord.y -= fy;

    vec4 xcubic = cubic(fx);
    vec4 ycubic = cubic(fy);

    vec4 c = vec4(texcoord.x - 0.5, texcoord.x + 1.5, texcoord.y -
                  0.5, texcoord.y + 1.5);
    vec4 s = vec4(xcubic.x + xcubic.y, xcubic.z + xcubic.w, ycubic.x +
                  ycubic.y, ycubic.z + ycubic.w);
    vec4 offset = c + vec4(xcubic.y, xcubic.w, ycubic.y, ycubic.w) / s;

    vec4 sample0 = texture2D(texture, vec2(offset.x, offset.z) * texscale);
    vec4 sample1 = texture2D(texture, vec2(offset.y, offset.z) * texscale);
    vec4 sample2 = texture2D(texture, vec2(offset.x, offset.w) * texscale);
    vec4 sample3 = texture2D(texture, vec2(offset.y, offset.w) * texscale);

    float sx = s.x / (s.x + s.y);
    float sy = s.z / (s.z + s.w);

    return mix(
        mix(sample3, sample2, sx),
        mix(sample1, sample0, sx), sy);
}
```

# Building Midmaps



```
// Change the parameters of your texture units.  
  
glTexParameterf( GL_TEXTURE_2D, GL_TEXTURE_MIN_FILTER,GL_NEAREST );  
glTexParameterf( GL_TEXTURE_2D, GL_TEXTURE_MAG_FILTER,GL_LINEAR );  
glTexParameterf( GL_TEXTURE_2D, GL_TEXTURE_WRAP_S,GL_REPEAT );  
glTexParameterf( GL_TEXTURE_2D, GL_TEXTURE_WRAP_T,GL_REPEAT );  
  
// Create a texture and load it to your graphics hardware. This  
// texture is automatically associated with texture 0 and the texture  
// variable "texture" / the active texture.  
  
if(channels == 3)  
    glTexImage2D(GL_TEXTURE_2D, 0, GL_RGB, width, height, 0, GL_BGR,  
    GL_UNSIGNED_BYTE, data);  
else if(channels == 4)  
    glTexImage2D(GL_TEXTURE_2D, 0, GL_RGBA, width, height, 0, GL_BGRA,  
    GL_UNSIGNED_BYTE, data);
```

Midmap

# Building Midmaps

```
// Change the parameters of your texture units.  
glTexParameteri( GL_TEXTURE_2D, GL_TEXTURE_MIN_FILTER,GL_NEAREST );  
glTexParameteri( GL_TEXTURE_2D, GL_TEXTURE_MAG_FILTER,GL_LINEAR );  
glTexParameteri( GL_TEXTURE_2D, GL_TEXTURE_WRAP_S,GL_CLAMP_TO_EDGE );  
glTexParameteri( GL_TEXTURE_2D, GL_TEXTURE_WRAP_T,GL_CLAMP_TO_EDGE );
```

You do not need these filters anymore

```
// Create a texture and load it to your graphics hardware. This  
texture is automatically associated with texture 0 and the texture  
variable "texture" / the active texture.  
  
if(channels == 3){  
    glTexImage2D(GL_TEXTURE_2D, 0, GL_RGB, width, height, 0, GL_BGR,  
    GL_UNSIGNED_BYTE, data_0);  
    glTexImage2D(GL_TEXTURE_2D, 1, GL_RGB, width, height, 0, GL_BGR,  
    GL_UNSIGNED_BYTE, data_1);  
}  
  
else if(channels == 4)  
    glTexImage2D(GL_TEXTURE_2D, 0, GL_RGBA, width, height, 0, GL_BGRA,  
    GL_UNSIGNED_BYTE, data);
```

Midmap level: load images with different resolutions and add your midmap levels manually

# Building Midmaps

```
*****
```

```
//Create a midmap texture pyramid and load it to the graphics hardware.
```

```
gluBuild2DMipmaps( GL_TEXTURE_2D, 3, width, height, GL_RGB,  
GL_UNSIGNED_BYTE, data );
```

2048 x 2048

Load a big image



1024 x 1024



The highest level is

$$\log_2(\max(width, height))$$

It takes half of the size for all other textures until the size is 1x1

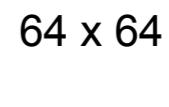
512 x 512



256 x 256



128 x 128



64 x 64

1x1

(11)

(10)

(9)

(8) (7) (6)

(0)

# MidMaps in OpenGL



gluBuild2DMipmaps builds a series of prefiltered two-dimensional texture maps of decreasing resolutions called a mipmap

**GLint gluBuild2DMipmaps(GLenum target, GLint components, GLsizei height, GLenum format, GLenum type, const void \* data);**

This function  
replaces glTexture2D

## Parameters:

- target: Specifies the target texture. Must be GL\_TEXTURE\_2D.
- internalFormat: Specifies the number of color components in the texture. Must be 1, 2, 3, or 4.
- width, height: Specifies the width and height, respectively, of the texture image.
- format: Specifies the format of the pixel data. Must be one of: GL\_COLOR\_INDEX, GL\_RED, GL\_GREEN, GL\_BLUE, GL\_ALPHA, GL\_RGB, GL\_RGBA, GL\_LUMINANCE, and GL\_LUMINANCE\_ALPHA.
- type: Specifies the data type for data. Must be one of: GL\_UNSIGNED\_BYTE, GL\_BYTE, GL\_BITMAP, GL\_UNSIGNED\_SHORT, GL\_SHORT, GL\_UNSIGNED\_INT, GL\_INT, or GL\_FLOAT.
- data: Specifies a pointer to the image data in memory.

# Thank you!

## Questions

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