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ME/CprE/ComS 557

Computer Graphics and Geometric Modeling

Light Sources

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- Attenuation
- Light Sources
 - Point Light
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 - Direct Light
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Light Source

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What we know so far:

Reflectance model for diffuse, specular, and ambient reflection

$$\text{Color} = \text{Specular} + \text{Diffuse} + \text{Ambient} + \text{Emissive}$$

But: a light source was considered as point (position in space)



Diffuse light/ reflection

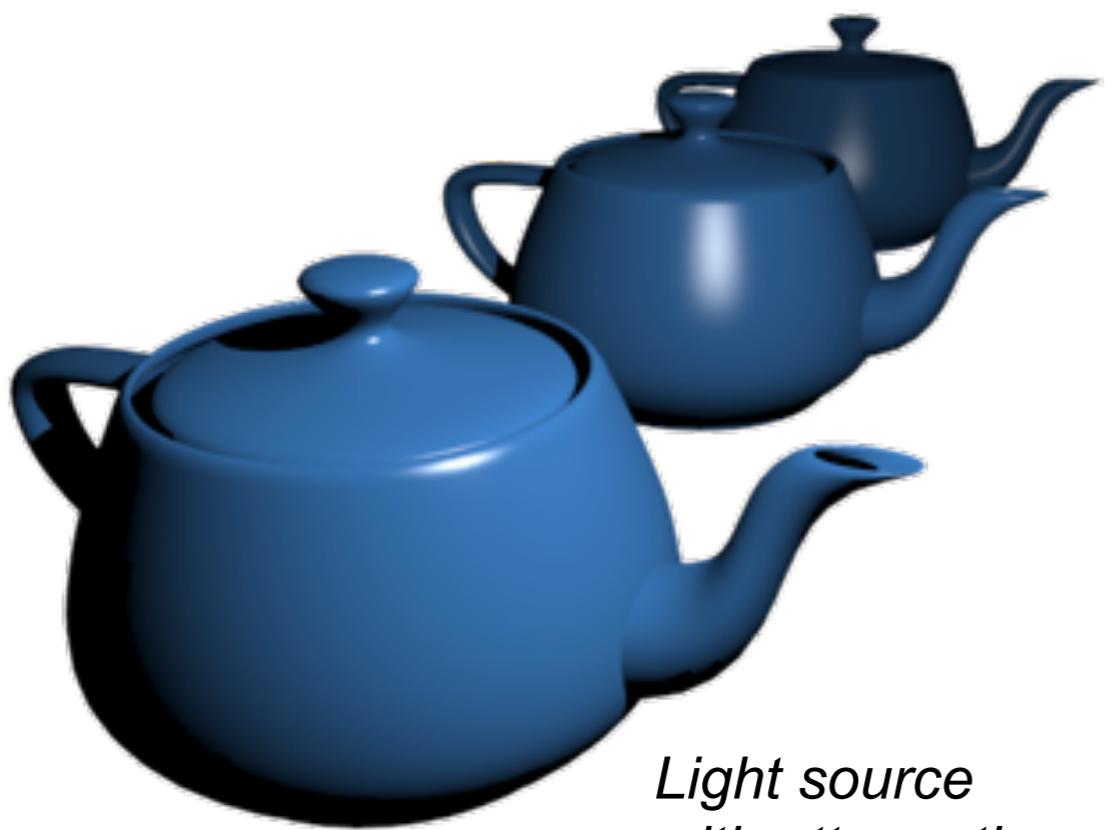


Diffuse + specular light / reflection

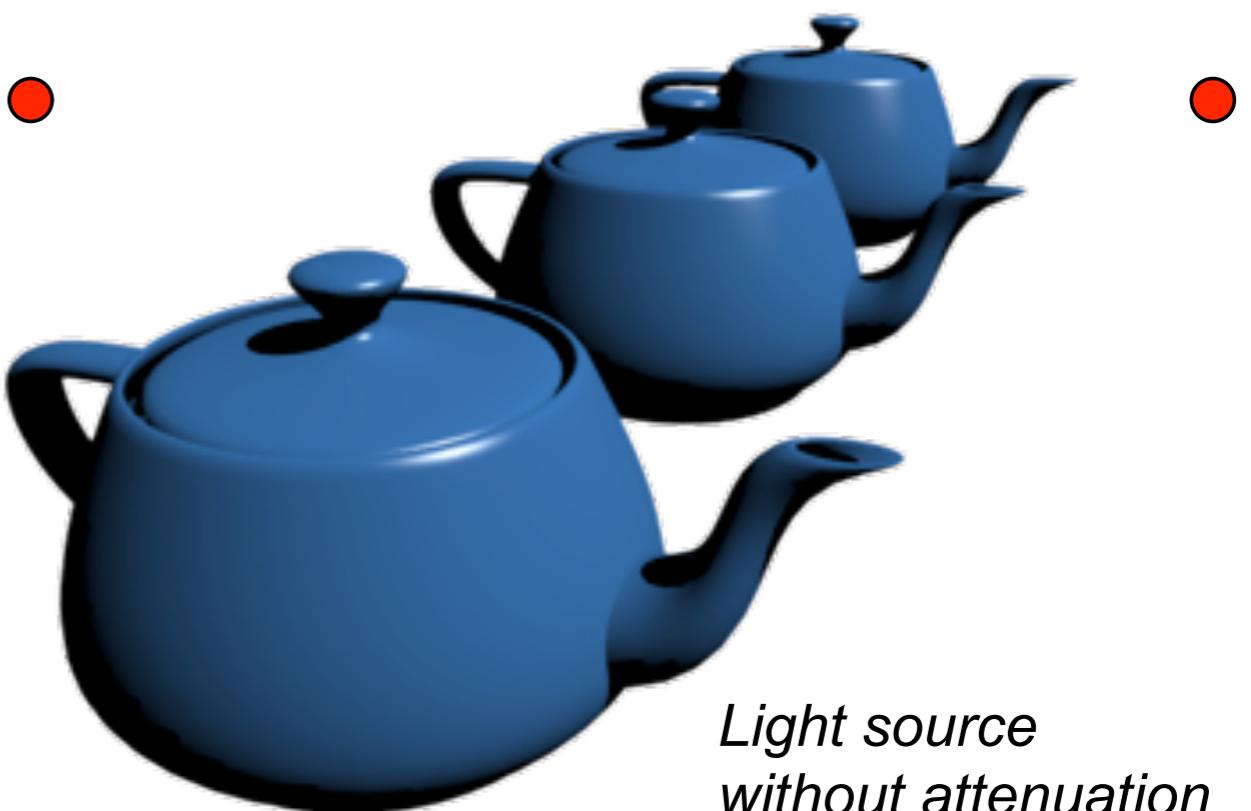
Attenuation

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Attenuation is the loss of light intensity over distance.
The greater the distance, the lower the intensity.



*Light source
with attenuation*

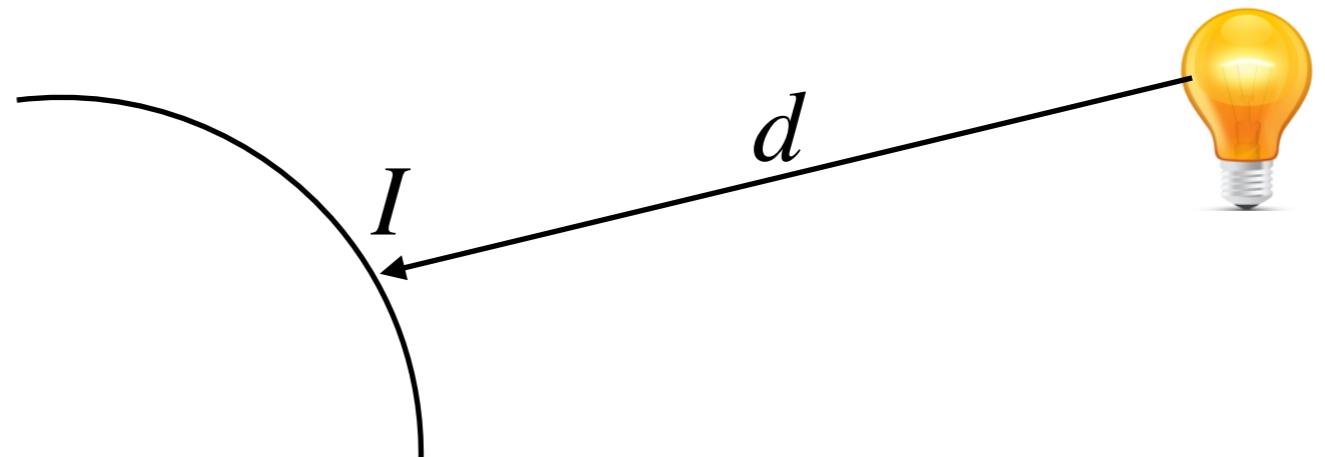


*Light source
without attenuation*

Attenuation

Physical attenuation is proportional to the inverse of the distance squared:

$$I \propto \frac{1}{d^2}$$



I: intensity

d: distance light source to surface

In computer graphics, we use a modified equation to

- avoid division by 0
- have better control to balance the light

$$a = \frac{1}{1 + k \cdot d^2}$$

a: attenuation factor

d: distance light source to surface

k: attenuation factor

Code Example

This code is part of the shader program spotlight.vs

First we calculate the attenuation parameter.

```
//attenuation  
float distanceToLight = length(light_position.xyz - surfacePostion.xyz);  
float attenuation = 1.0 / (1.0 + attenuationCoefficient * pow(distanceToLight, 2));
```

That is what we have so far.

```
// Calculate the linear color  
vec3 linearColor = out_ambient_color + out_diffuse_color + out_specular_color);
```

Now we replace it with:

```
// Calculate the linear color  
vec3 linearColor = out_ambient_color + attenuation * ( out_diffuse_color +  
out_specular_color);
```

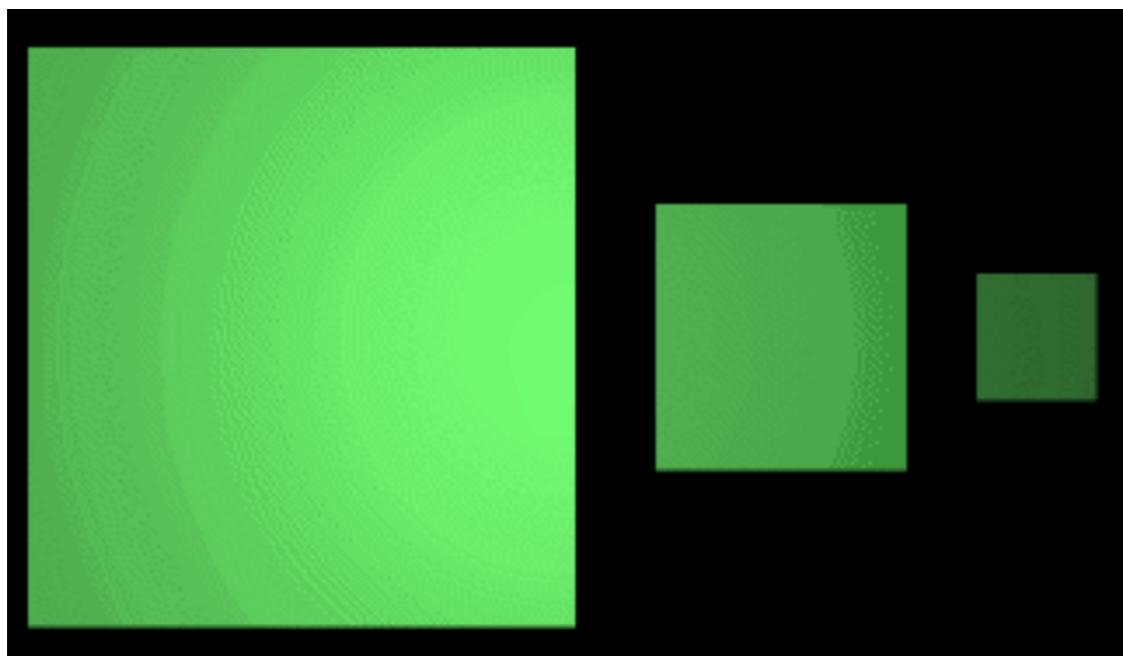
Sometimes....

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It does not work very well because the quadratic parameter is difficult to balance in order to find the right effect.

But we can move to a linear parameter or even to a combination of linear and quadratic attenuation.

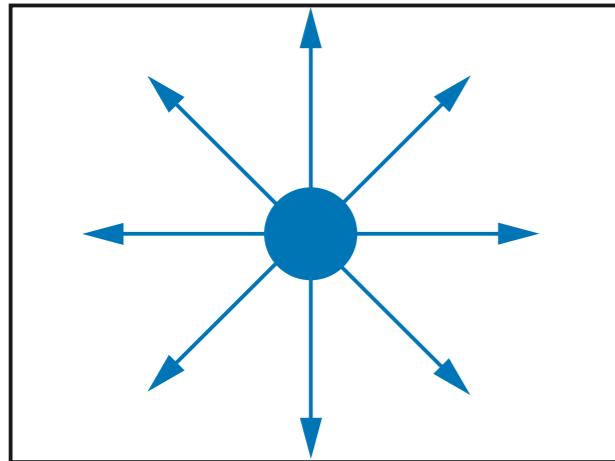
$$a = \frac{1}{1 + k_0 \cdot d + k_1 \cdot d^2}$$



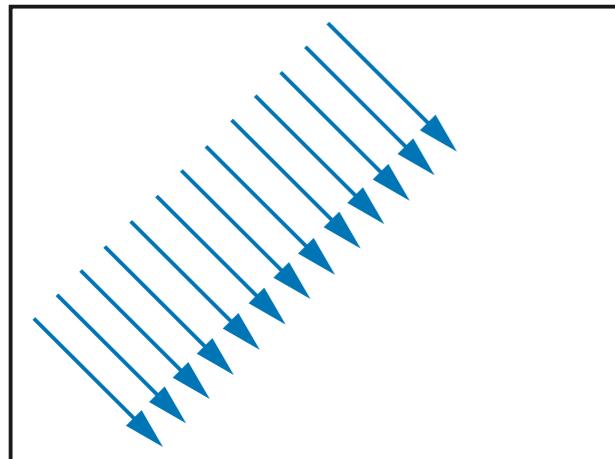
Linear attenuation is easier to balance

*a: attenuation factor
d: distance light source to surface
k₀: linear attenuation factor
k₁: quadratic attenuation factor*

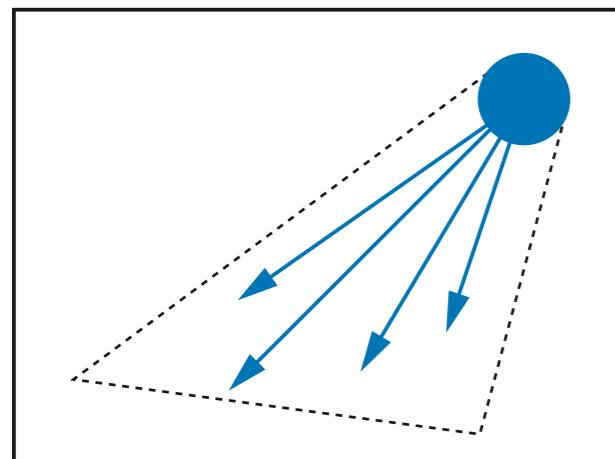
Light Sources



Point Light: a directed light source that emits light equally into all directions. The intensity of light decrease constantly with increasing distance between light source and surface. A candle light is an example.



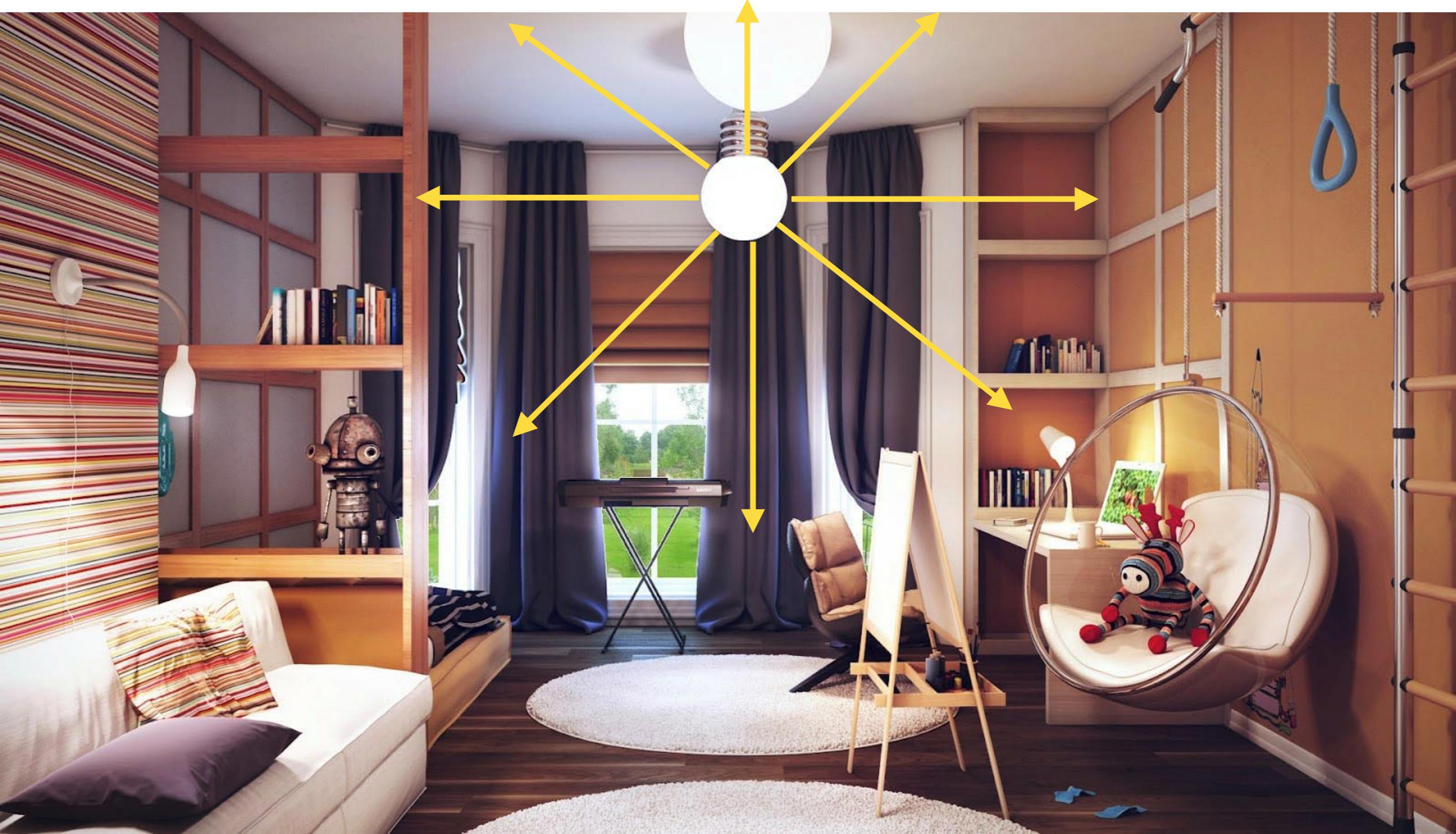
Directed Light: light that is emitted from a distant light source. Thus, all light rays run parallel. The distance between light source and surface has no effect on the intensity. The sun is an example.



Spotlight: is a point light which emits light only within a limited angle. The intensity of light decrease with increasing distance to the surface and to the edges of the spot. It can be used to simulate a flashlight.

Point Light Source

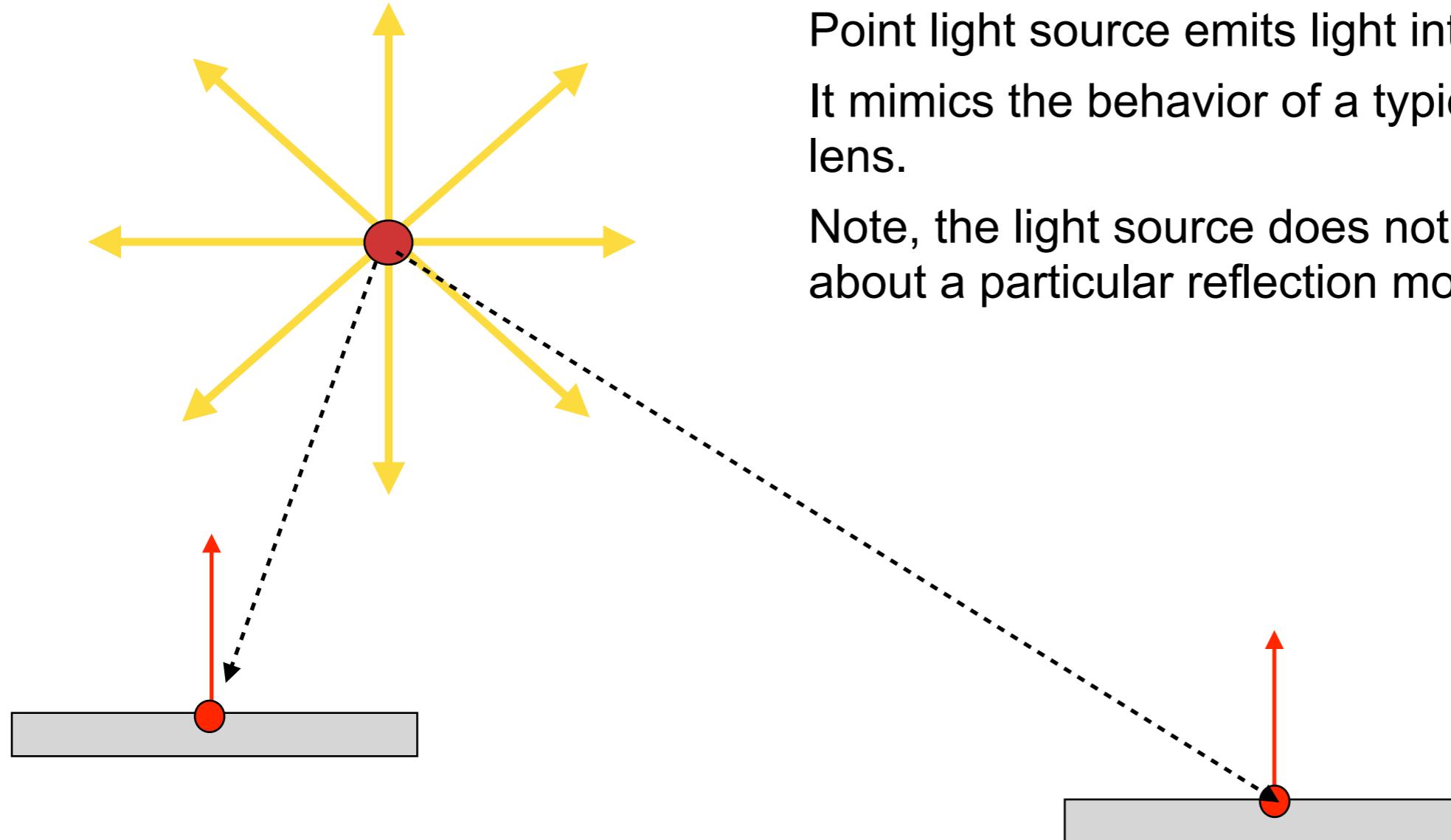
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from: www.home-designing.com

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Point Light Source



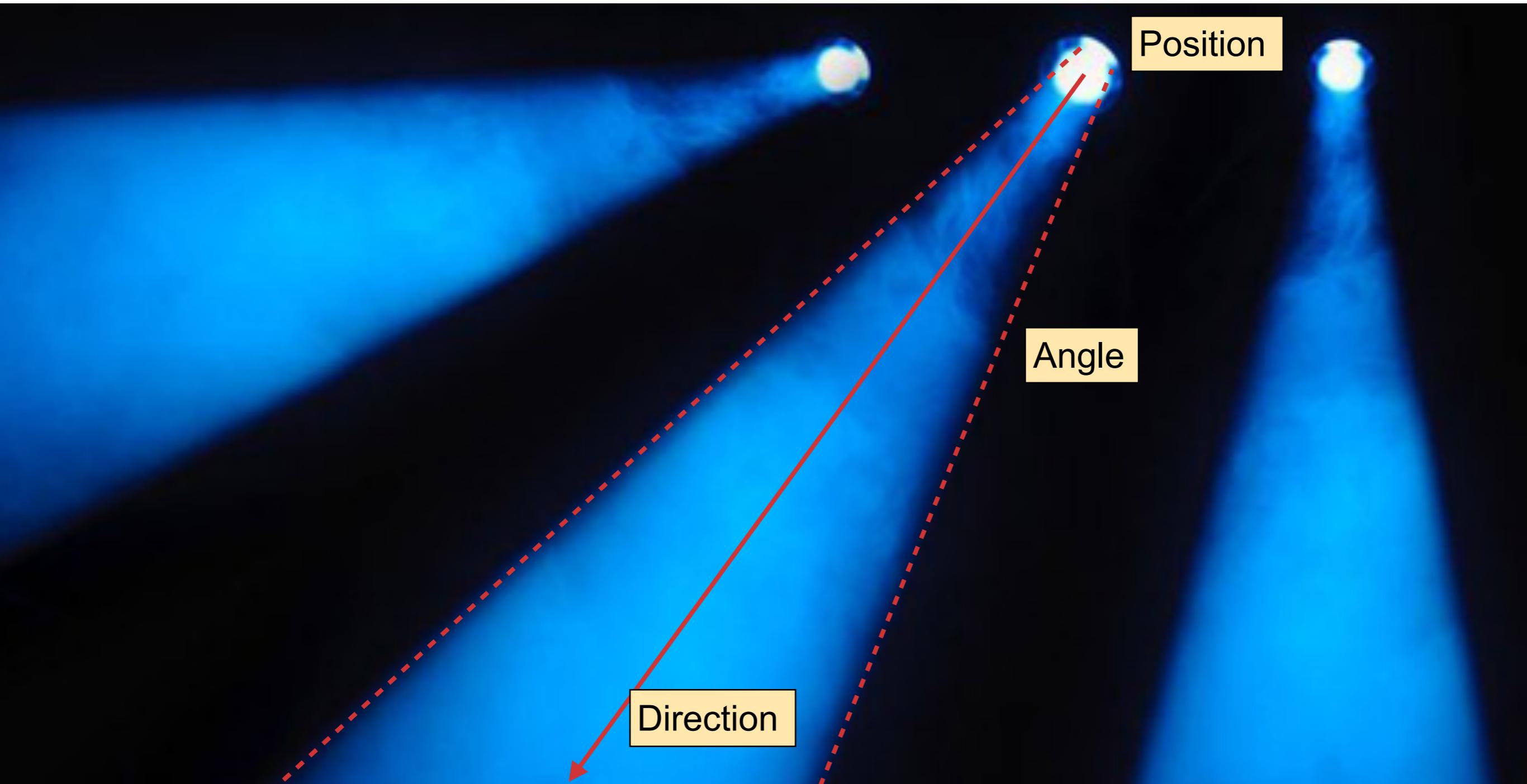
Point light source emits light into all directions.
It mimics the behavior of a typical light without lens.
Note, the light source does not tell one anything about a particular reflection model.

Described by:

- position
- intensity
- color
- attenuation

Spot Light Source

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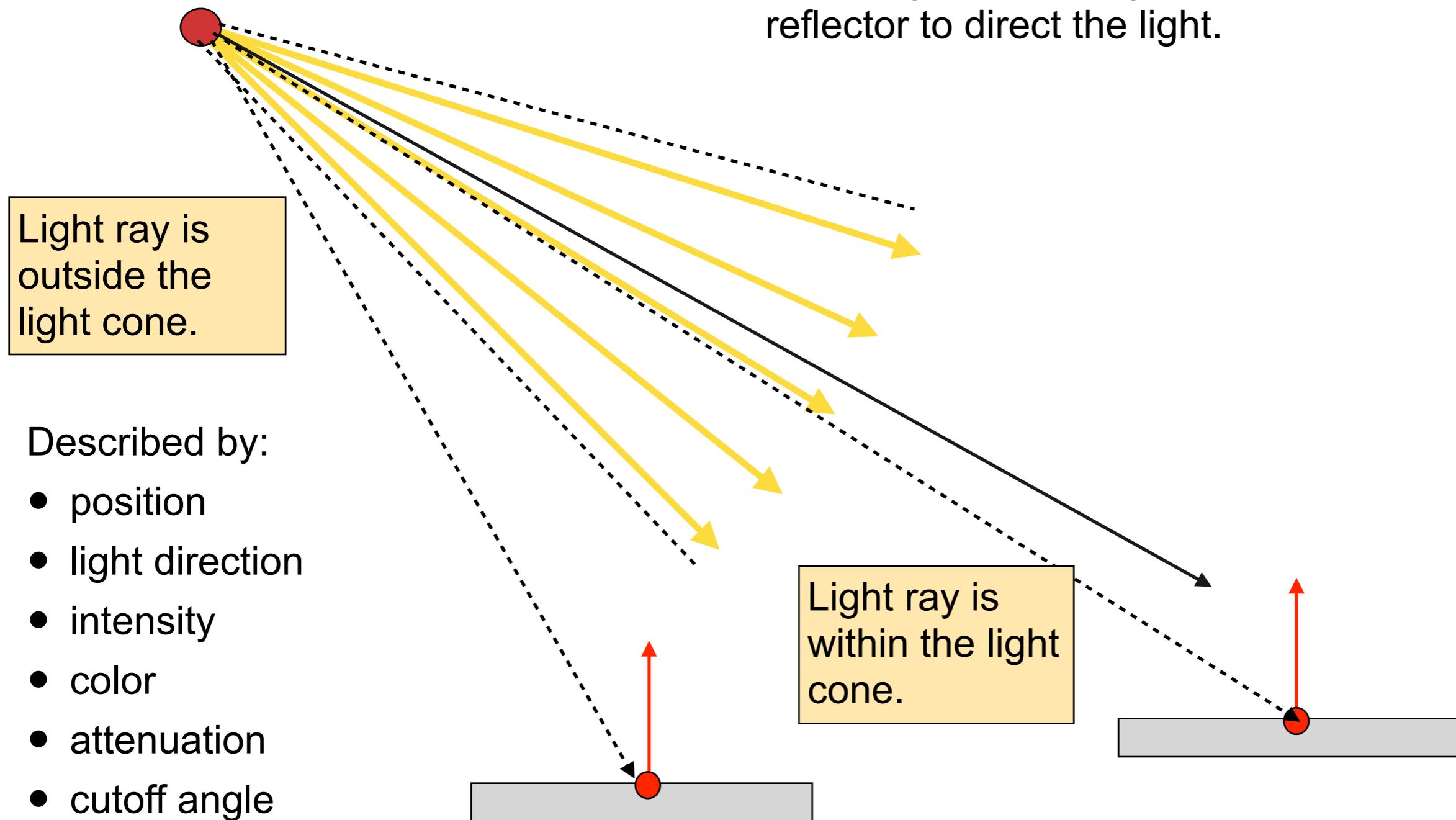


from: www.centrestageleeds.com

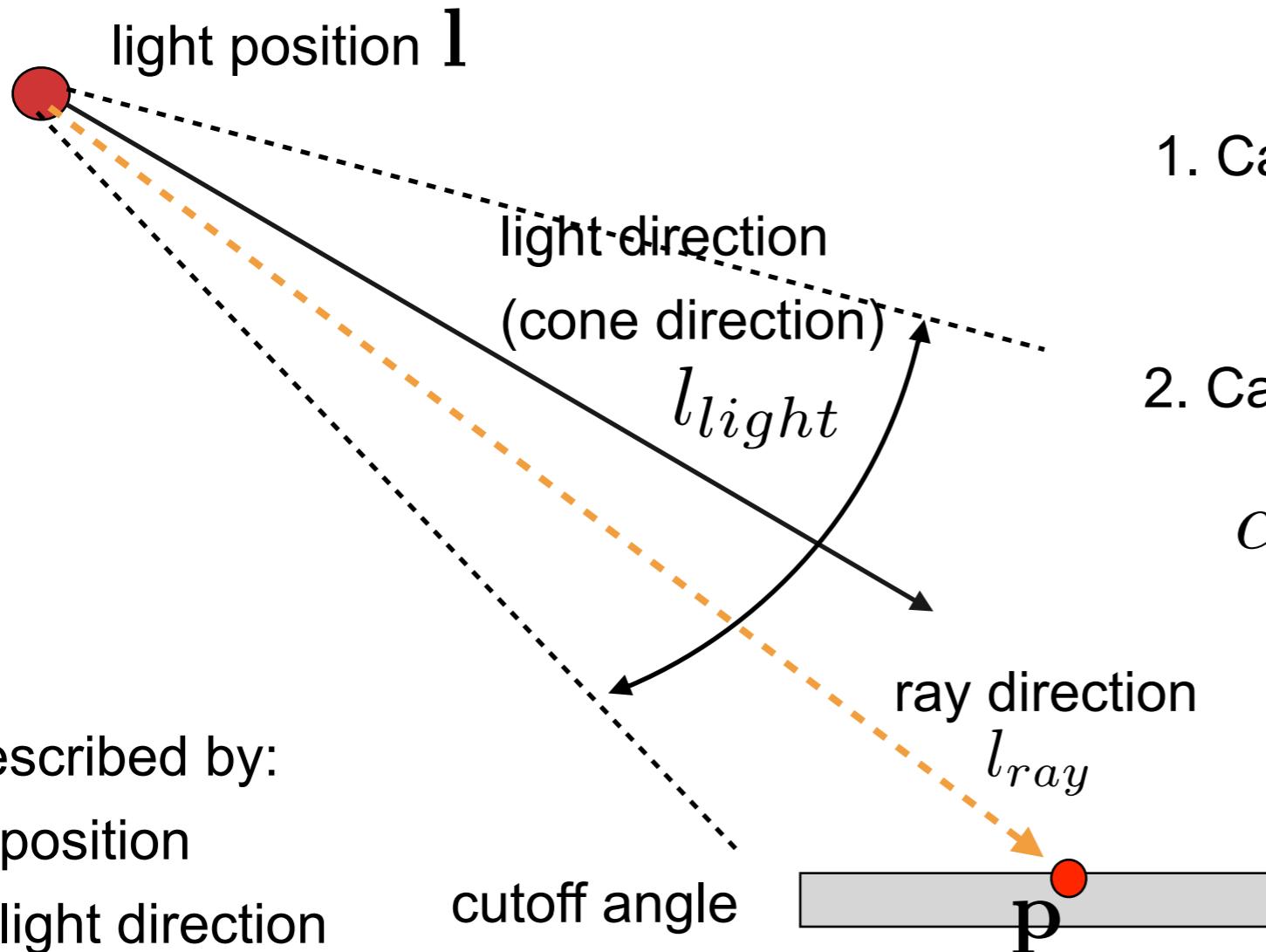
Spotlight

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A spot light mimics light sources with a reflector to direct the light.



Spotlight Calculation



Described by:

- position
- light direction
- intensity
- color
- attenuation
- cutoff angle

1. Calculate the light ray direction:

$$l_{ray} = p - l$$

2. Calculate the angle:

$$\alpha = \cos(l_{ray} \cdot l_{light})^{-1}$$

3. Check whether the angle is inside the cone:

$$if(\alpha > \text{cutoff angle}) a = 0.0$$

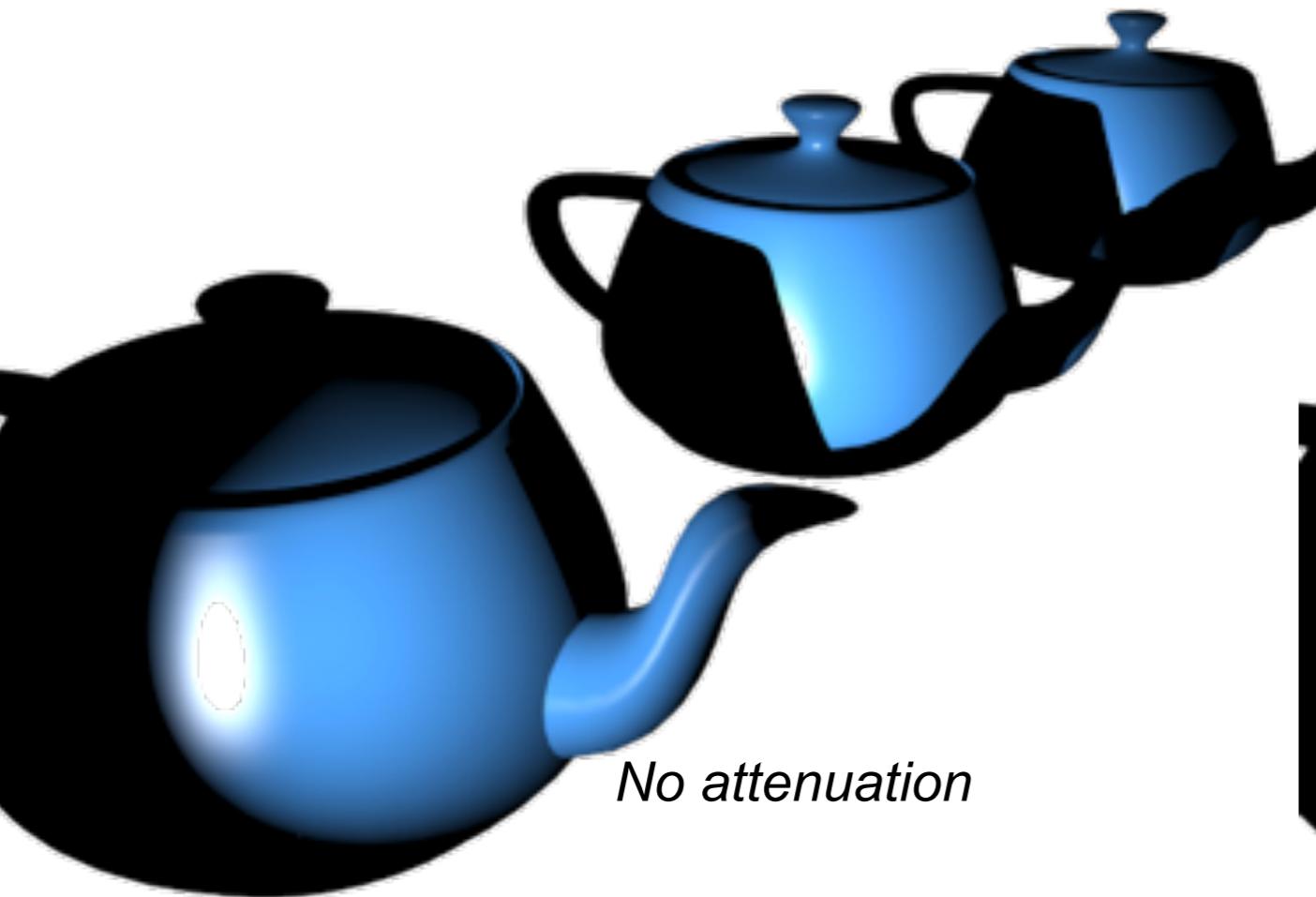
Code Example



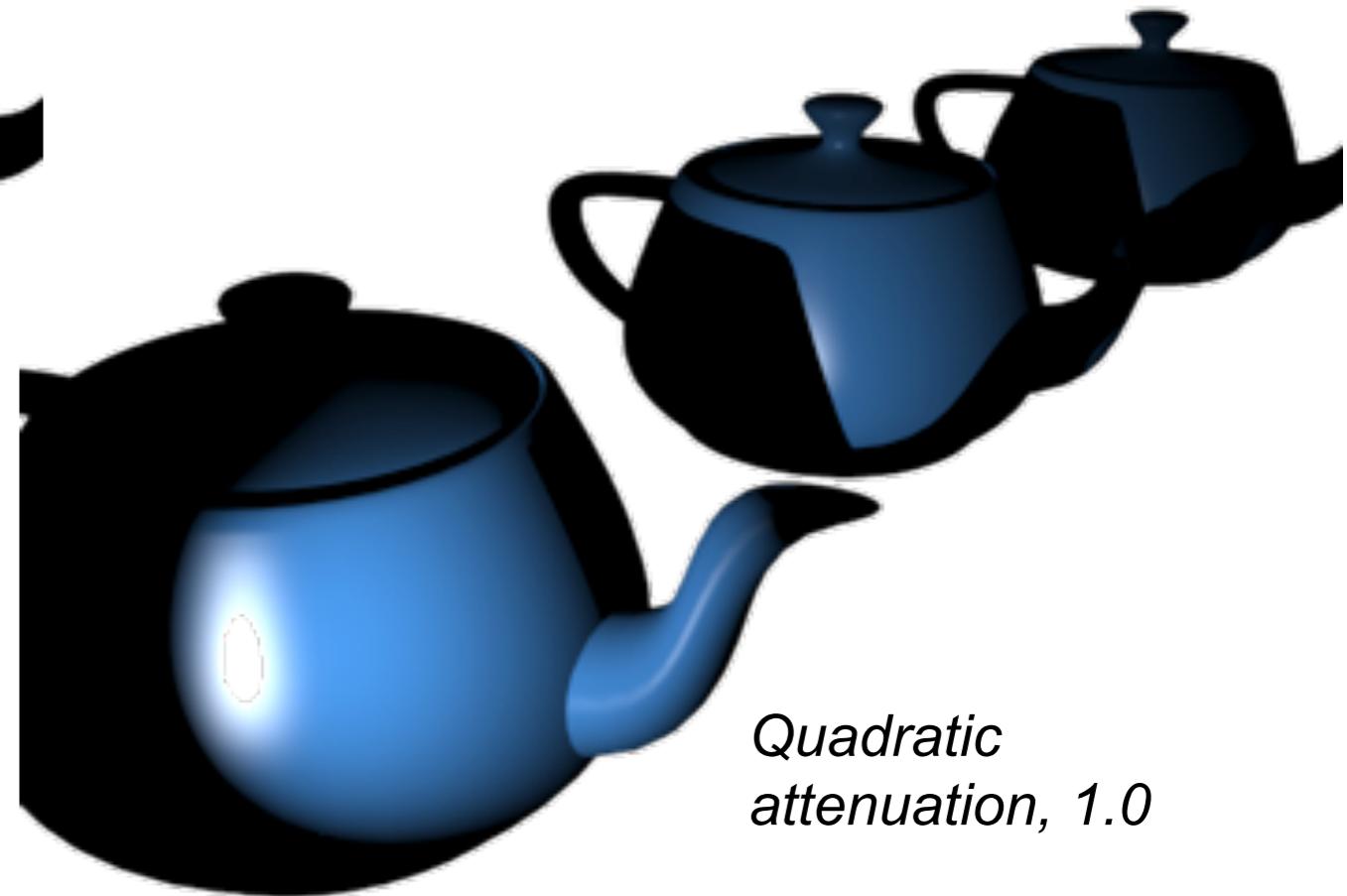
```
//////////////////////////////  
/////  
// Spotlight  
// 1. Normalize the cone direction  
vec3 cone_direction_norm = normalize(cone_direction);  
  
// 2. Calculate the ray direction.  
vec3 ray_direction = -surface_to_light.xyz;  
  
// 3. Calculate the angle between light and surface using the dot product again.  
// To simplify our understanding, we use the degrees  
float light_to_surface_angle =  
    degrees(acos(dot(ray_direction, cone_direction_norm)));  
  
// 4. Last, we compare the angle with the current direction and  
// reduce the attenuation to 0.0 if the light is outside the angle.  
if(light_to_surface_angle > cone_angle){  
    attenuation = 0.0;  
}
```

Spot Light – Attenuation

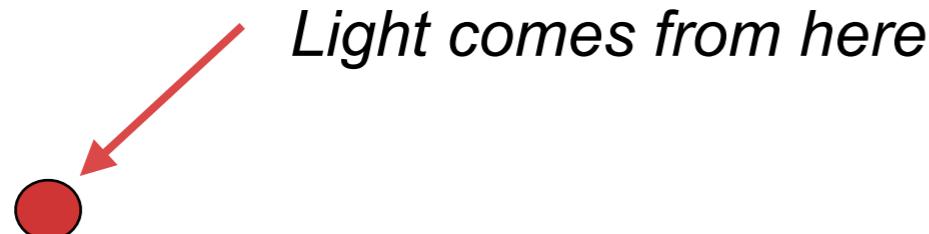
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No attenuation

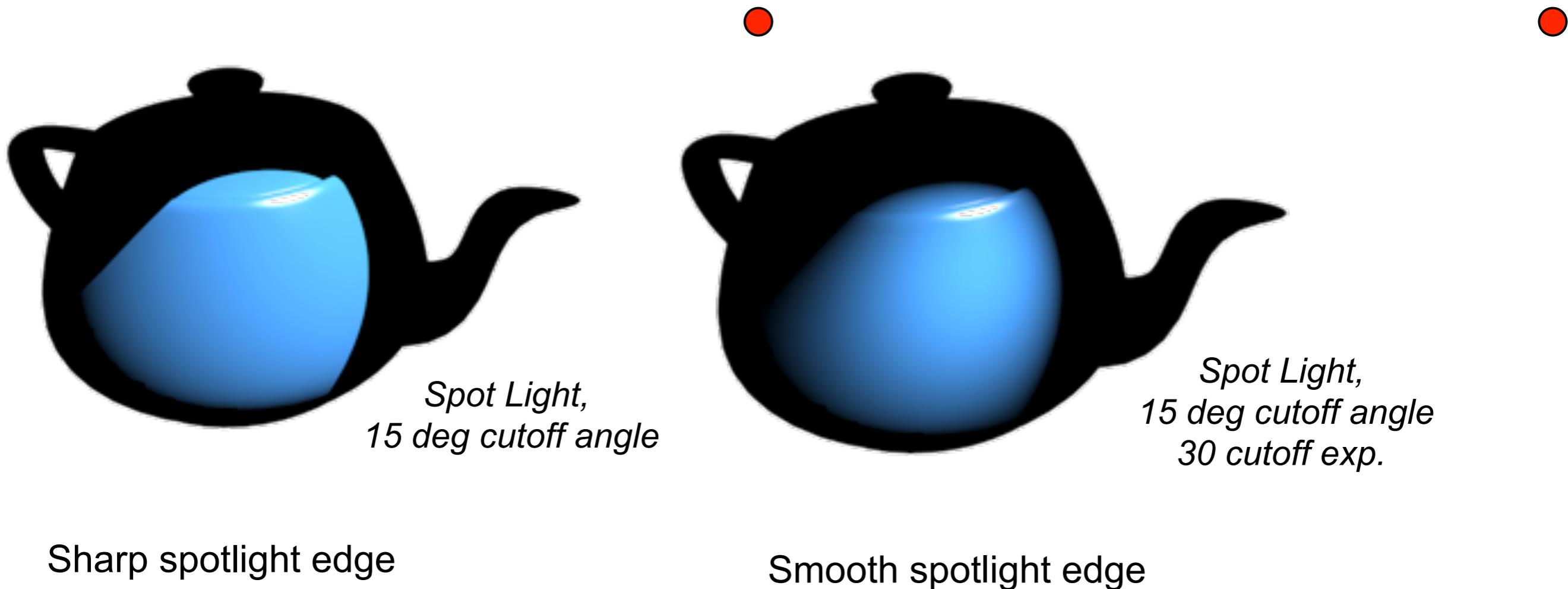


*Quadratic
attenuation, 1.0*



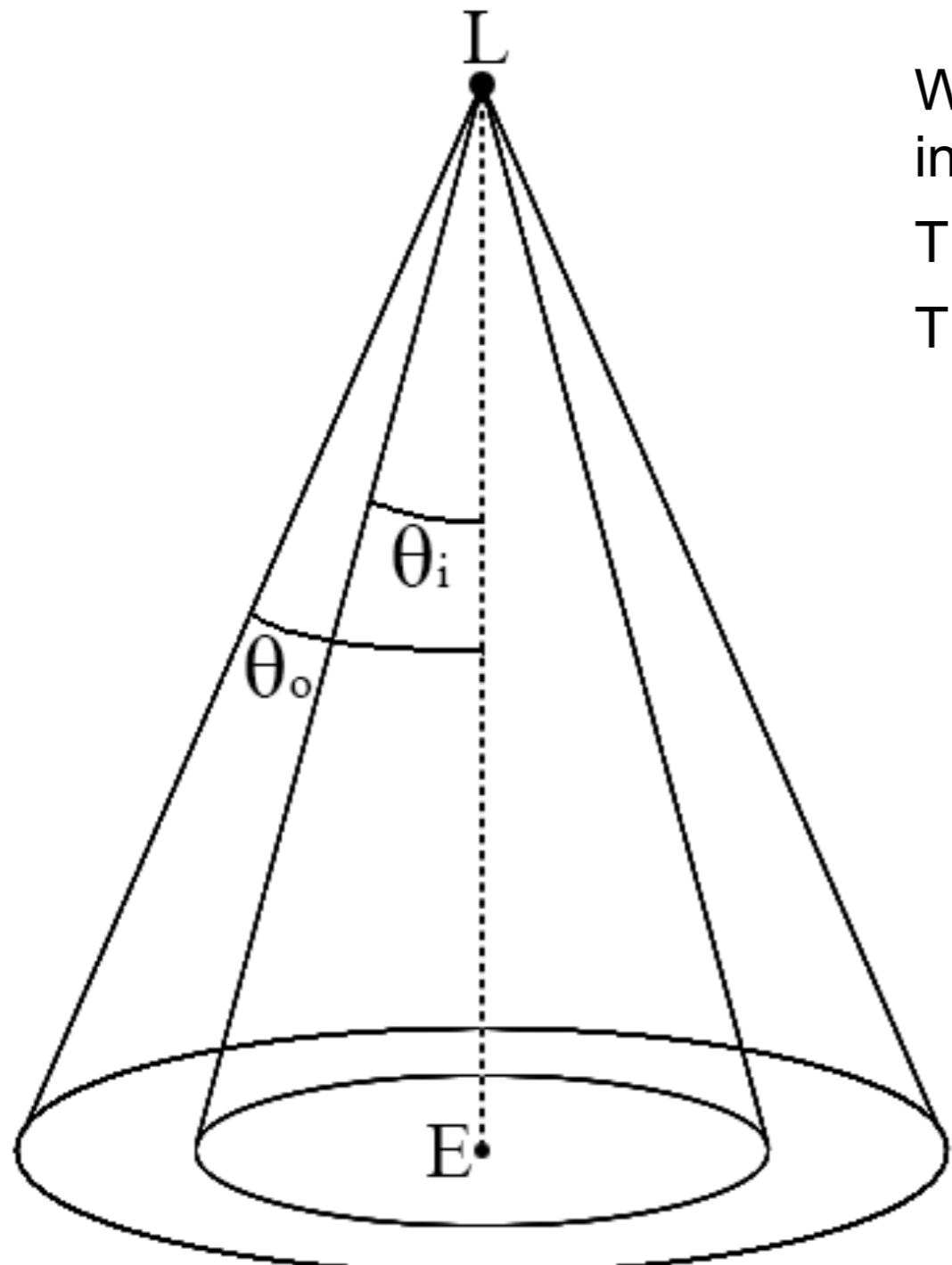
Smooth Spot Light

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Smooth Spotlight

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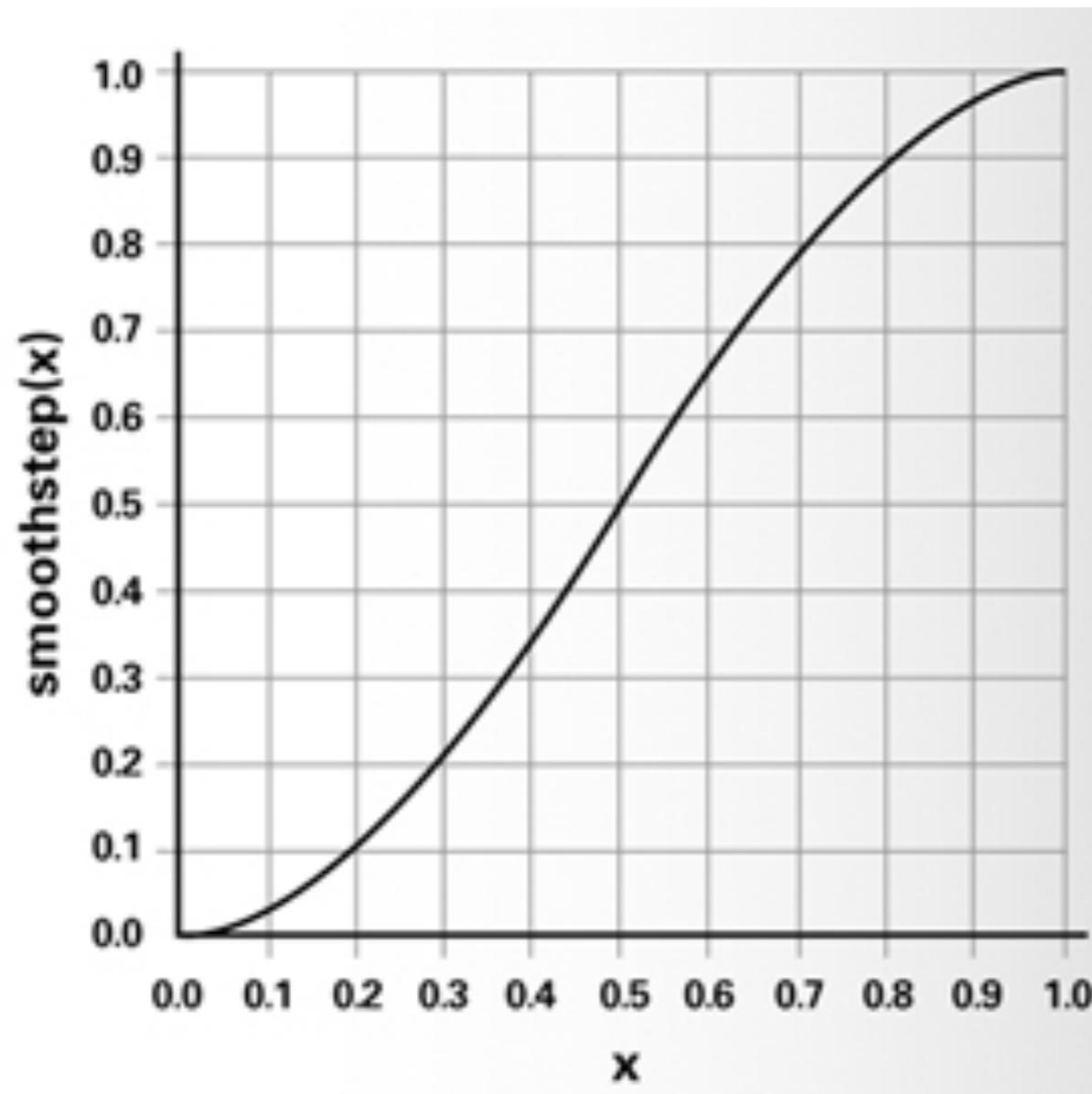
We work with two spotlight cones and interpolate between both of them.

The inner circle is the hard spotlight.

The outer circle is the soft spotlight.

Smooth Spotlight

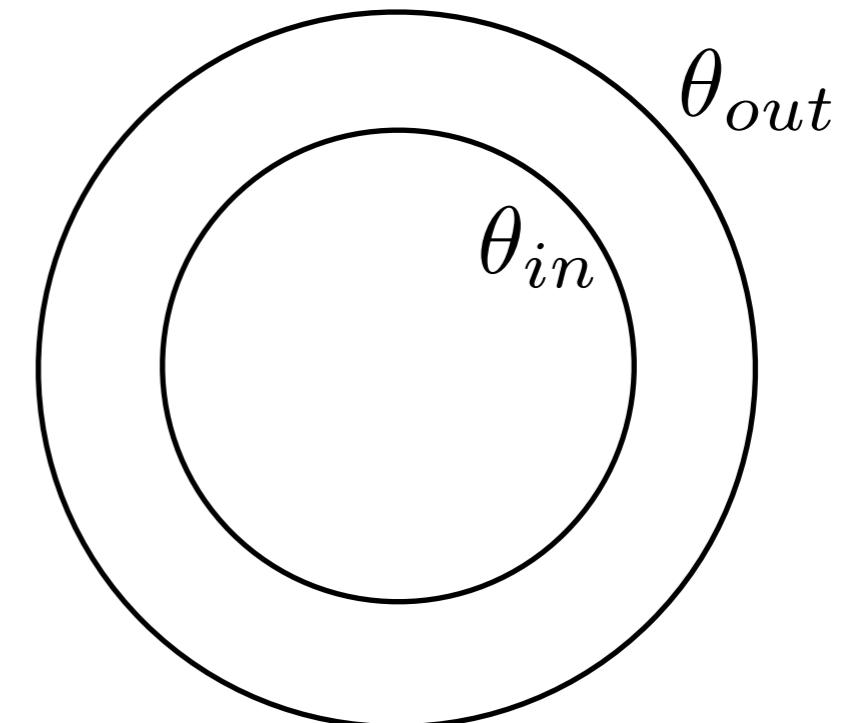
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We interpolate between inner and outer circle using a Hermine interpolation

$$\text{smoothstep}(x) = 3x^2 - 2x^3$$

$$x = \theta_{out} - \theta_{in}$$



GLSL Function - smoothstep



Perform Hermite interpolation between two values

```
genType smoothstep( genType edge0, genType edge1, genType x);
```

Parameters:

- edge0 - Specifies the value of the lower edge of the Hermite function.
- edge1 - Specifies the value of the upper edge of the Hermite function.
- x - Specifies the source value for interpolation.

Code:

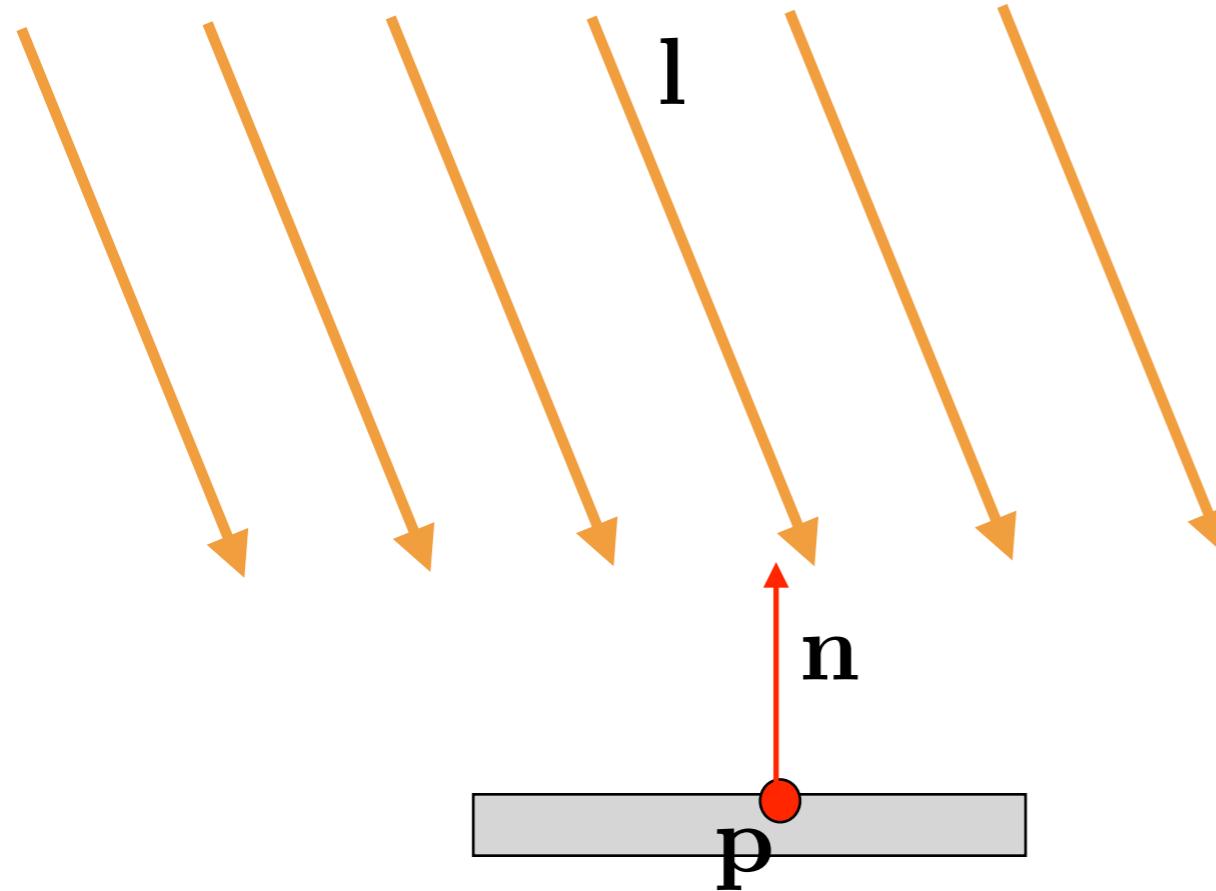
```
float smoothstep(float edge0, float edge1, float x)
{
    // Scale, bias and saturate x to 0..1 range
    x = clamp((x - edge0)/(edge1 - edge0), 0.0, 1.0);
    // Evaluate polynomial
    return x*x*(3 - 2*x);
}
```

Directional Light

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Directional Light



1. Calculate the angle between light and surface normal n .

$$\alpha = \mathbf{l} \cdot \mathbf{n}$$

2. Check whether the surface is directed towards the light.

if($\alpha < 0.0$)draw

Described by:

- light direction
- intensity
- color

Code Example

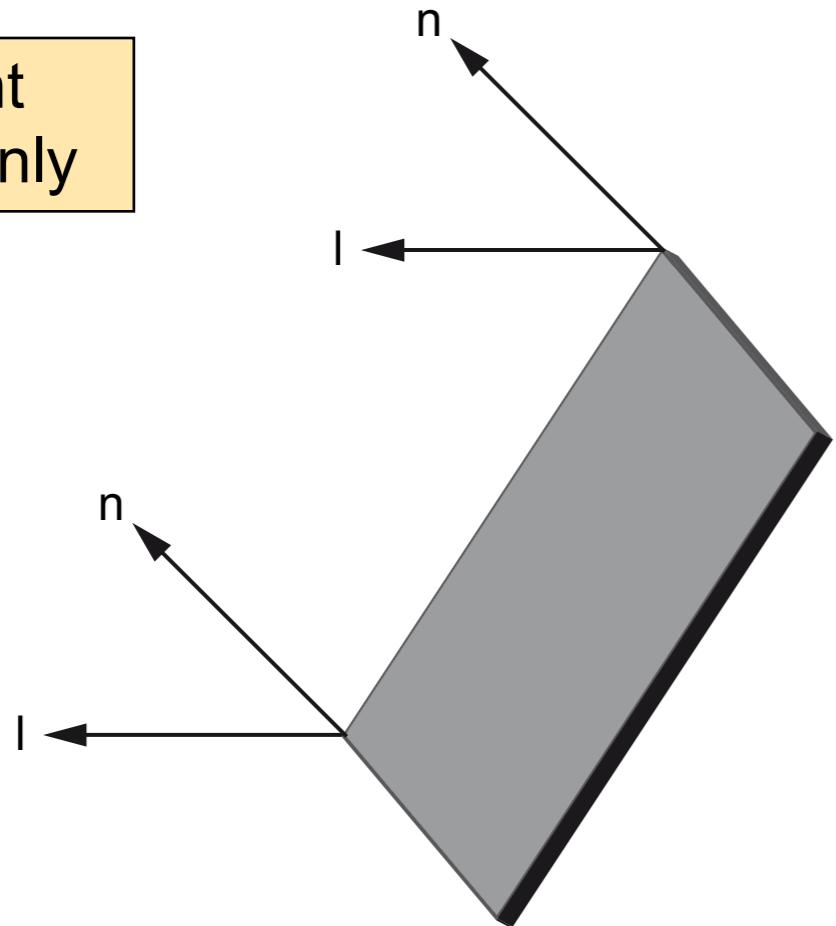


```
//////////////////////////////  
// Directional light  
//  
if(light_position.w == 0.0) {  
    // this is a directional light.  
  
    // 1. the values that we store as light position is our light direction.  
    vec3 light_direction = normalize(light_position.xyz);  
  
    // 2. We check the angle of our light  
    float light_to_surface_angle = dot(light_direction, transformedNormal.xyz);  
  
    // 3. Check the angle, if the angle is smaller than 0.0,  
    if(light_to_surface_angle > 0.0)attenuation = 1.0;  
    else attenuation = 0.0;  
}
```

Point / Spot Light vs. Directional Light

One light
vector only

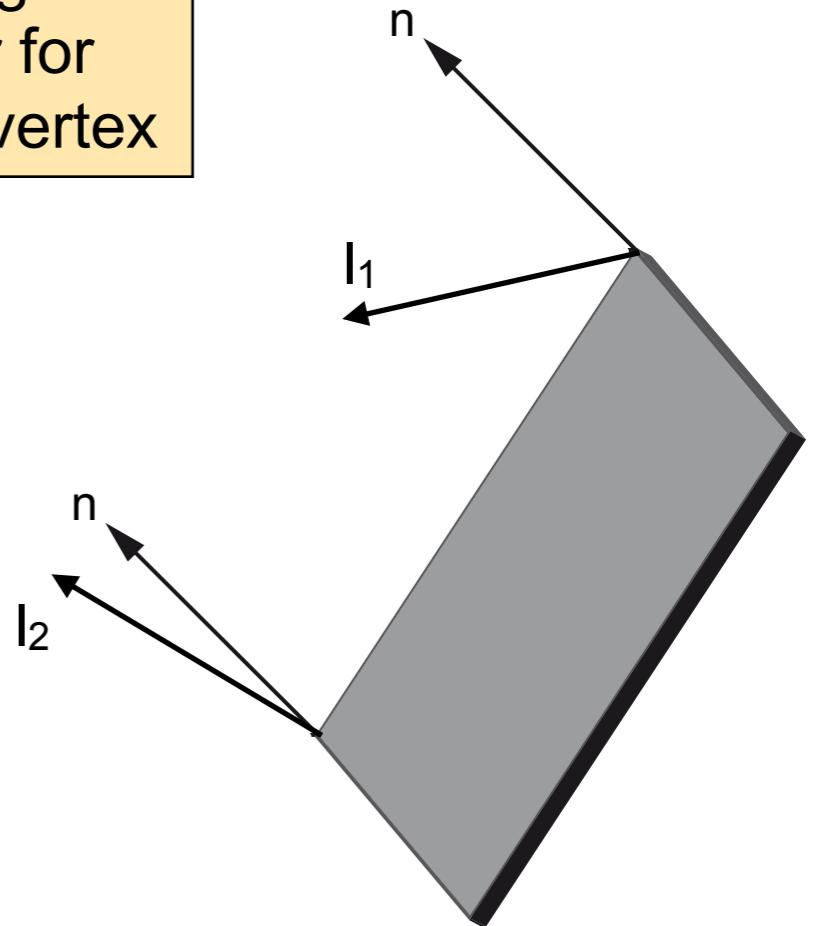
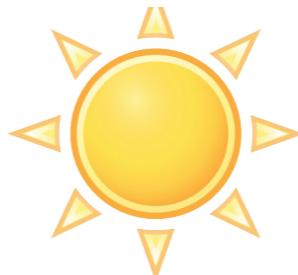
directional
light



Directional Light; $w = 0.0$

One light
vector for
each vertex

point light



Point Light; $w = 1.0$

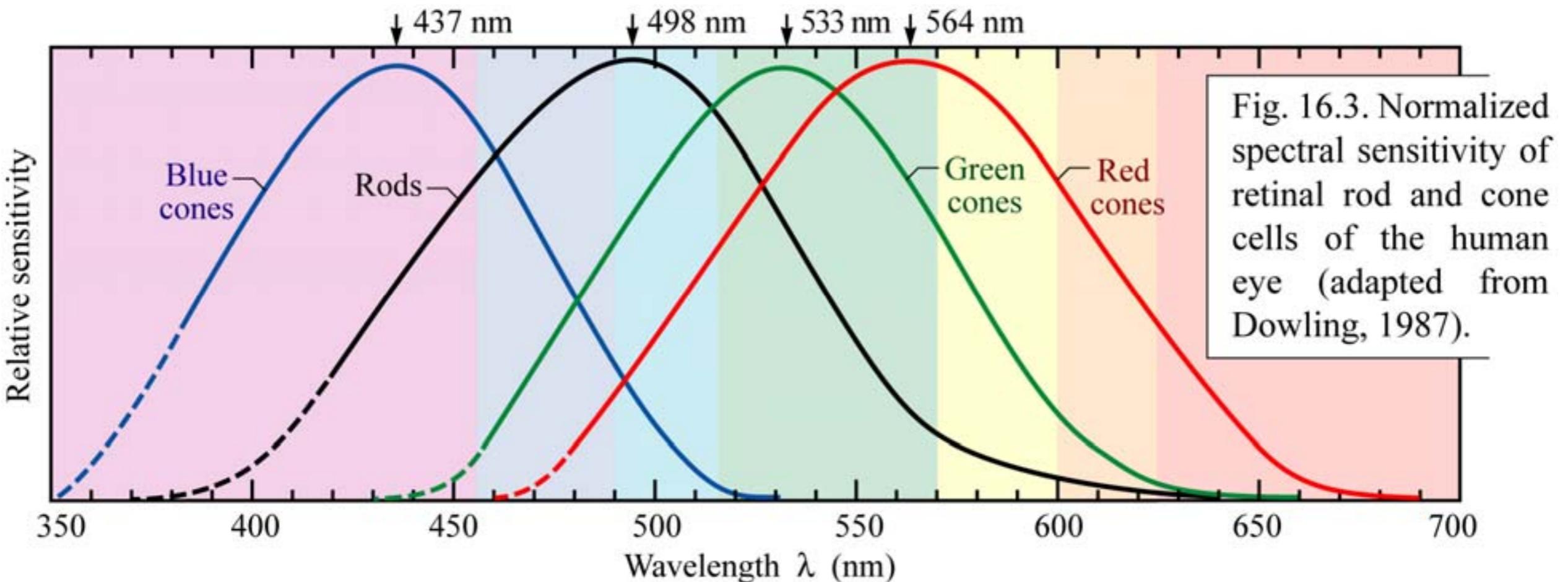
```
GLfloat lightPos0[] = {4.0f, 0.0f, 8.0f, 1.0f};
```

```
GLfloat lightPos1[] = {-1.0f, 0.5f, 0.5f, 0.0f};
```

Directional light is faster to calculate because the graphics card can pre-calculate the light vector once for all vertices.

Light and Color Perception

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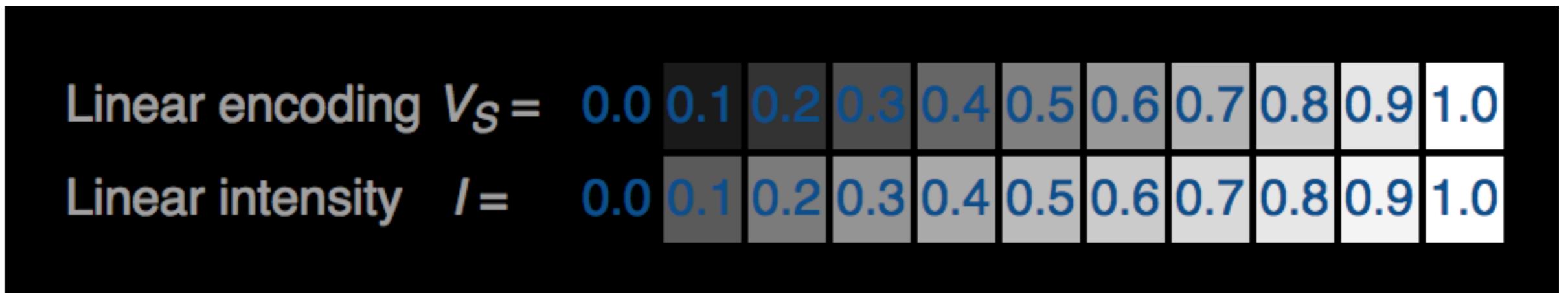


The human eye perceives light / color in a non-linear way.

Color Models

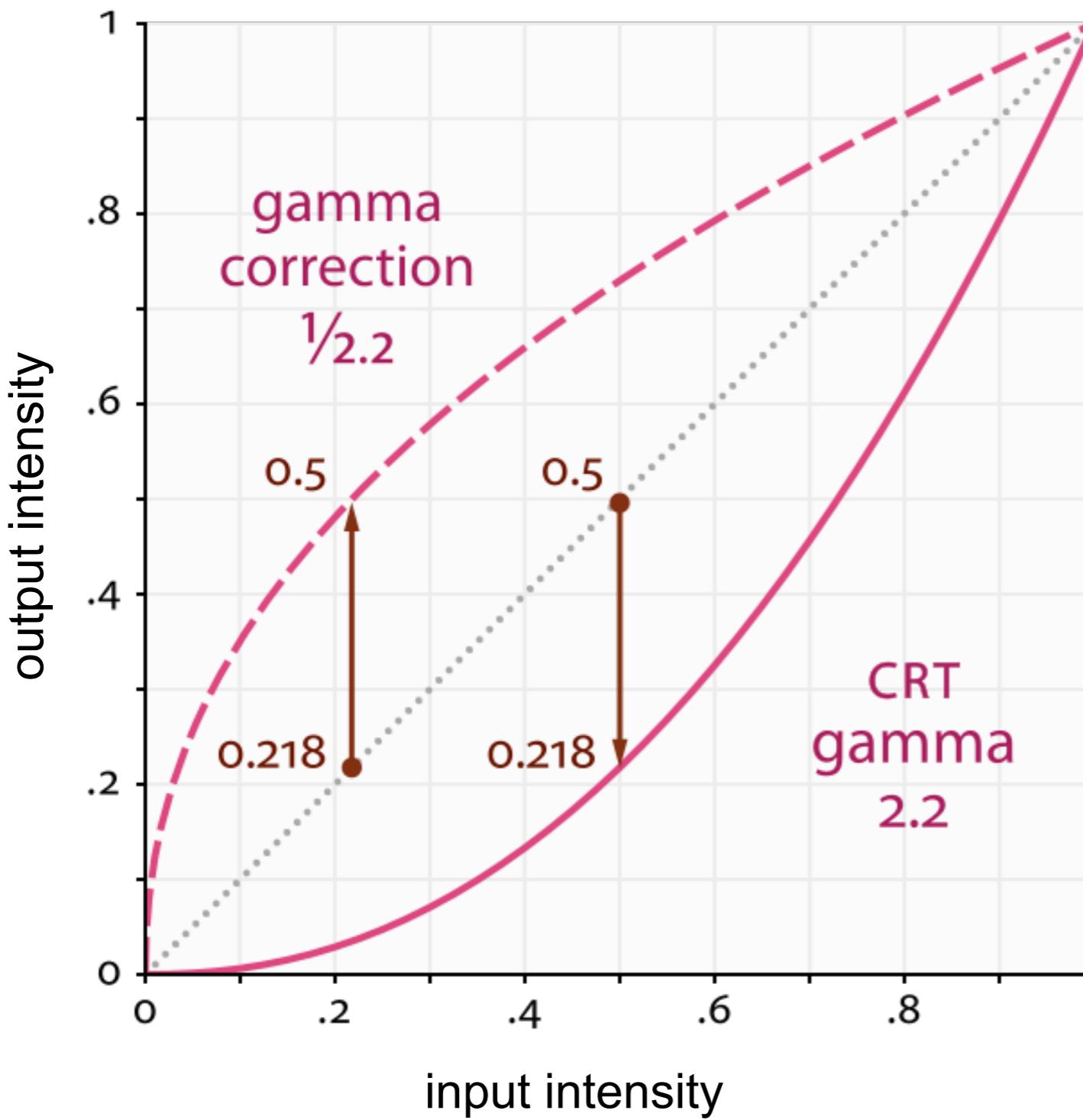
Color models scale linear, we expect to see twice the intensity of a color when we double the value.

This is a generic example that mimics the effect (since the display uses gamma correction, it is difficult to demonstrate this effect.)



Colors look natural with
gamma correction than
without.

Gamma Correction



Gamma correction of images adapts the image color to the non-linear manner in which humans perceive light and color.

It was originally invented to take advantages of the bandwidth necessary to transport a signal to the display.

$$I_{out} = A \cdot I_{in}^{\gamma}$$

- A is a constant, which is $A = 1$, in a common case. But it can range between 0-1. It is used to boost the intensity.
- γ is the correction coefficient. which depends on the display. A gamma value for a CRT monitor is $1/2.2$

Code Example

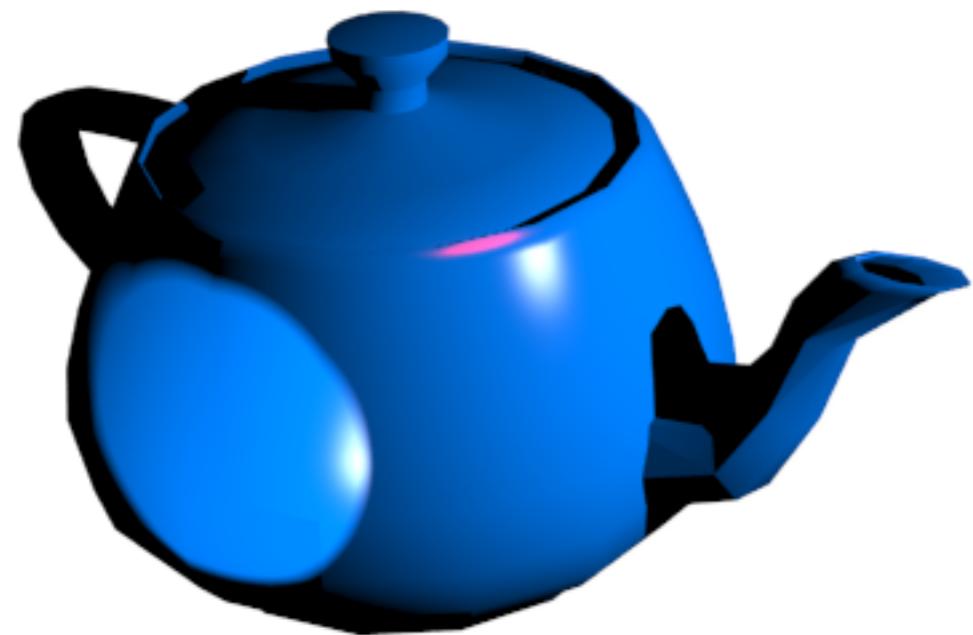
```
// Calculate the linear color  
vec3 linearColor = out_ambient_color + attenuation *  
(out_diffuse_color + out_specular_color);
```

```
// Gamma correction  
vec3 gamma = vec3(1.0/2.2);  
vec3 finalColor = pow(linearColor, gamma);
```

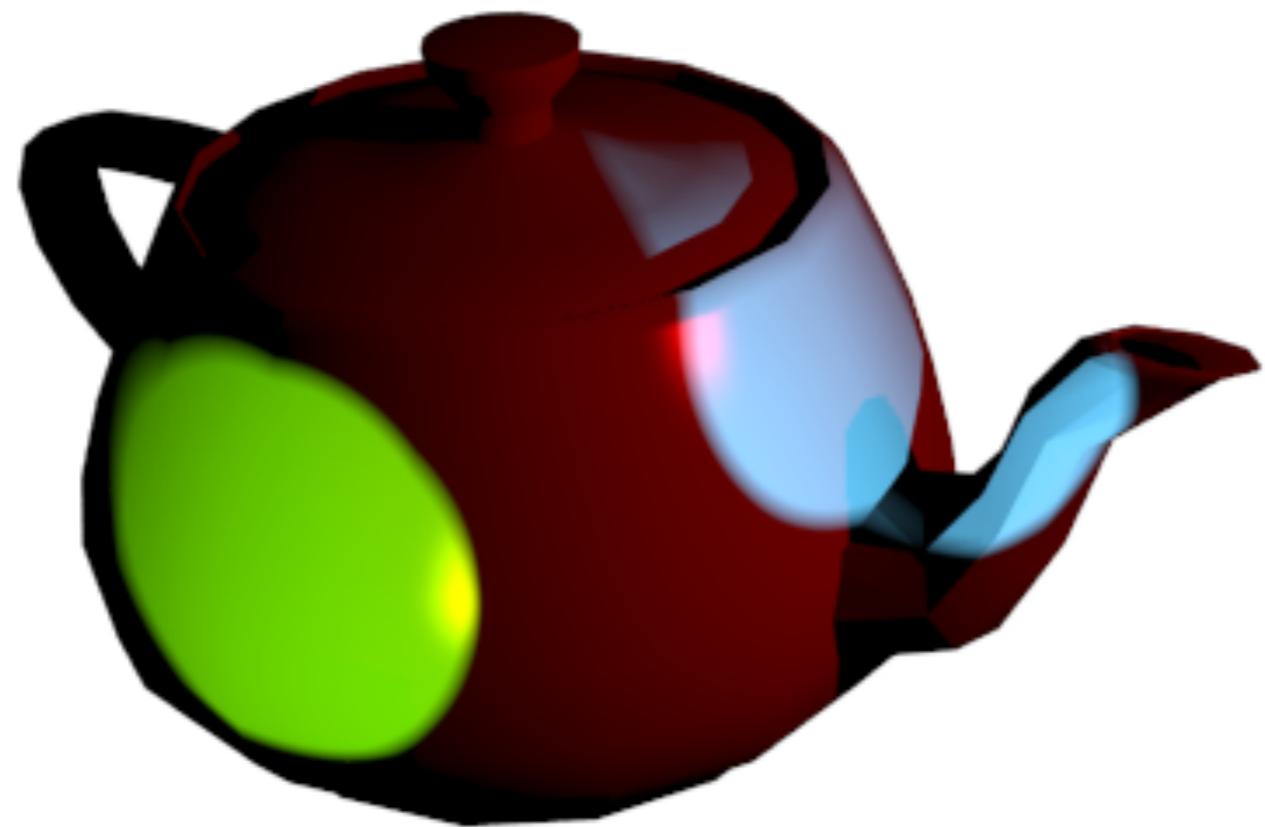
```
// Pass the color  
pass_color = finalColor;
```

How do we transform a light source?

What can we do to maintain multiple different light sources at the same time?



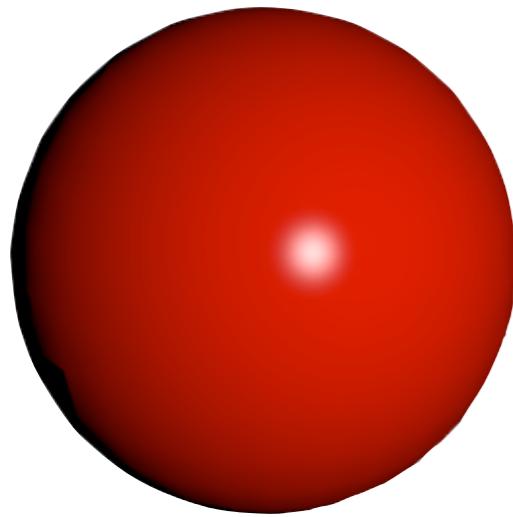
How can we add color to light?



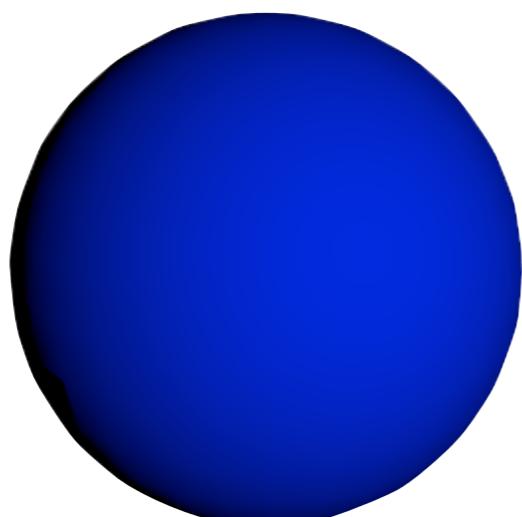
How can we improve the visual quality of the scene - or - what parameters are responsible for the visual quality?

Light and Material

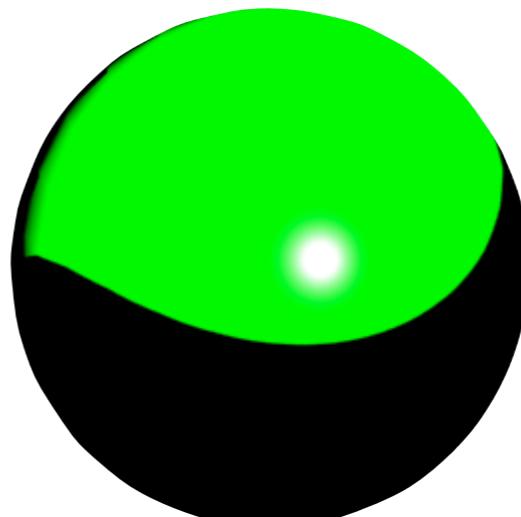
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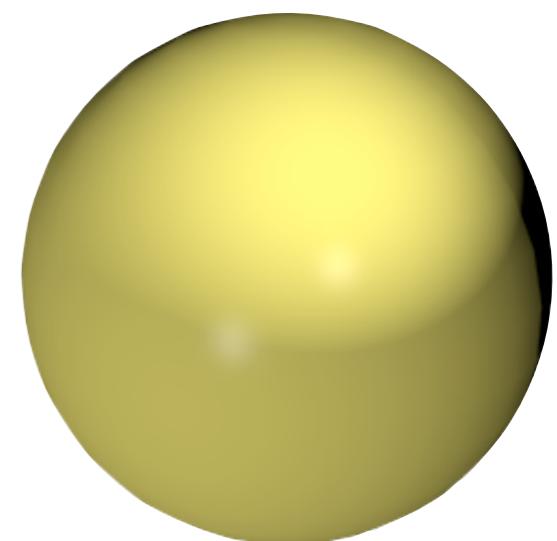
Highlight on
the surface of
a diffuse object



Diffuse surface,
no highlights are
visible



Spotlight with
small highlight and
sharp cutoff angle



Little highlight and
smooth cutoff angle

***How do we realize transparency?**

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Code Example

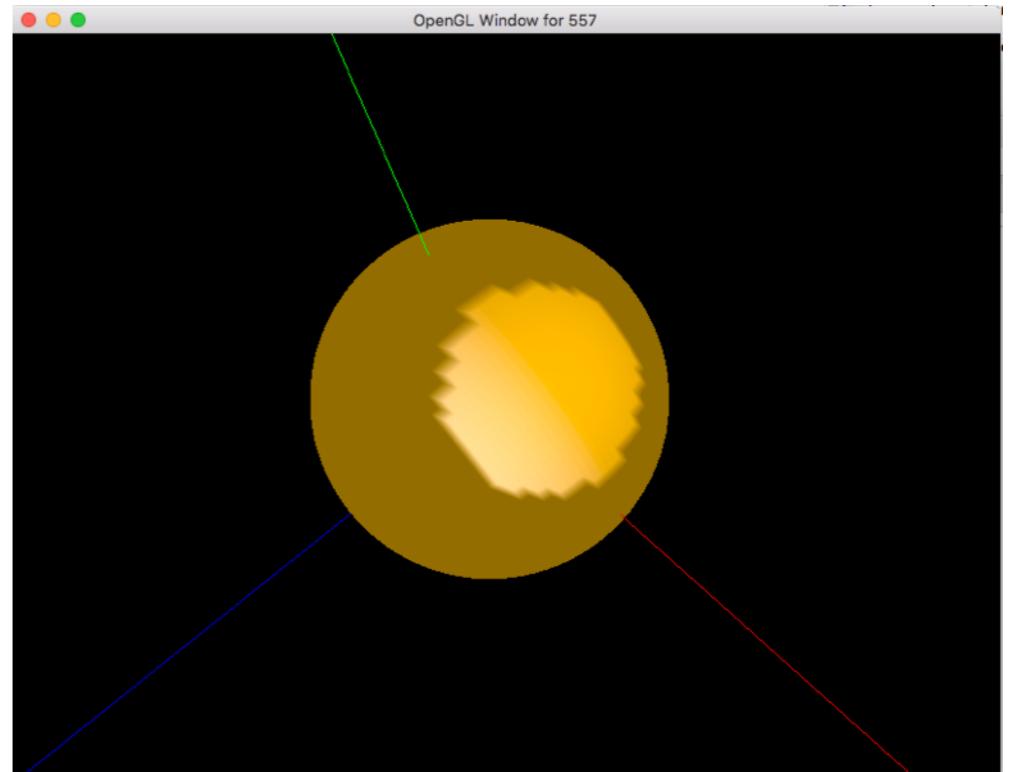
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Two New Examples

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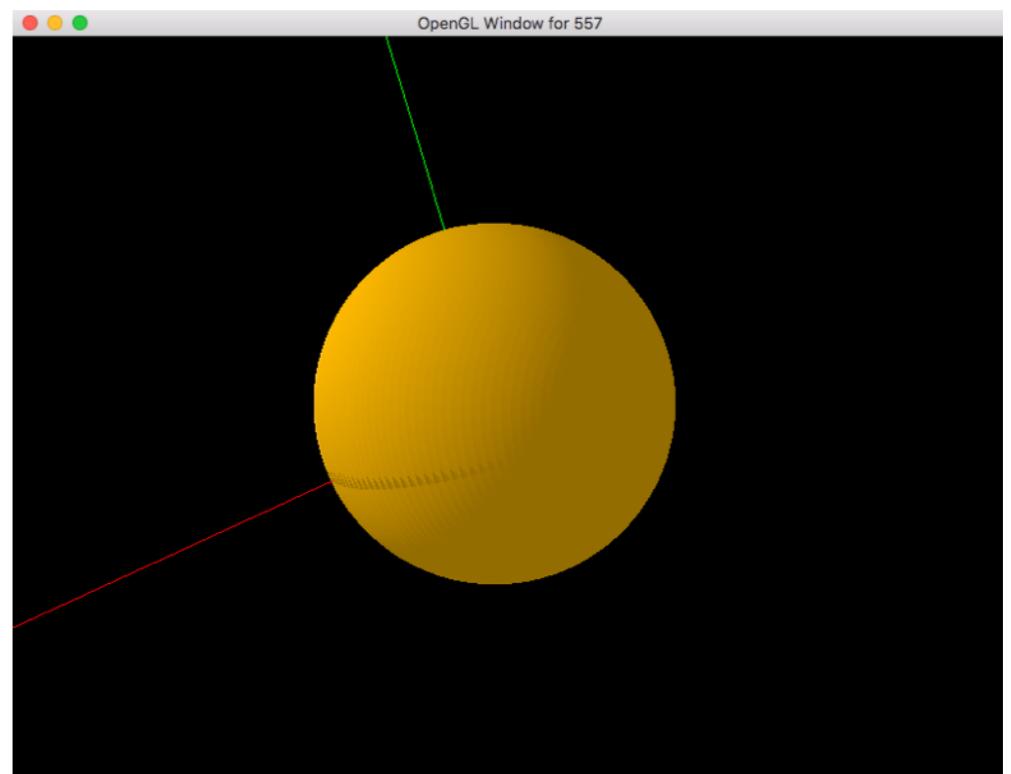
07_SpotLight

Shows how to realize a spot light.



08_DirectLight

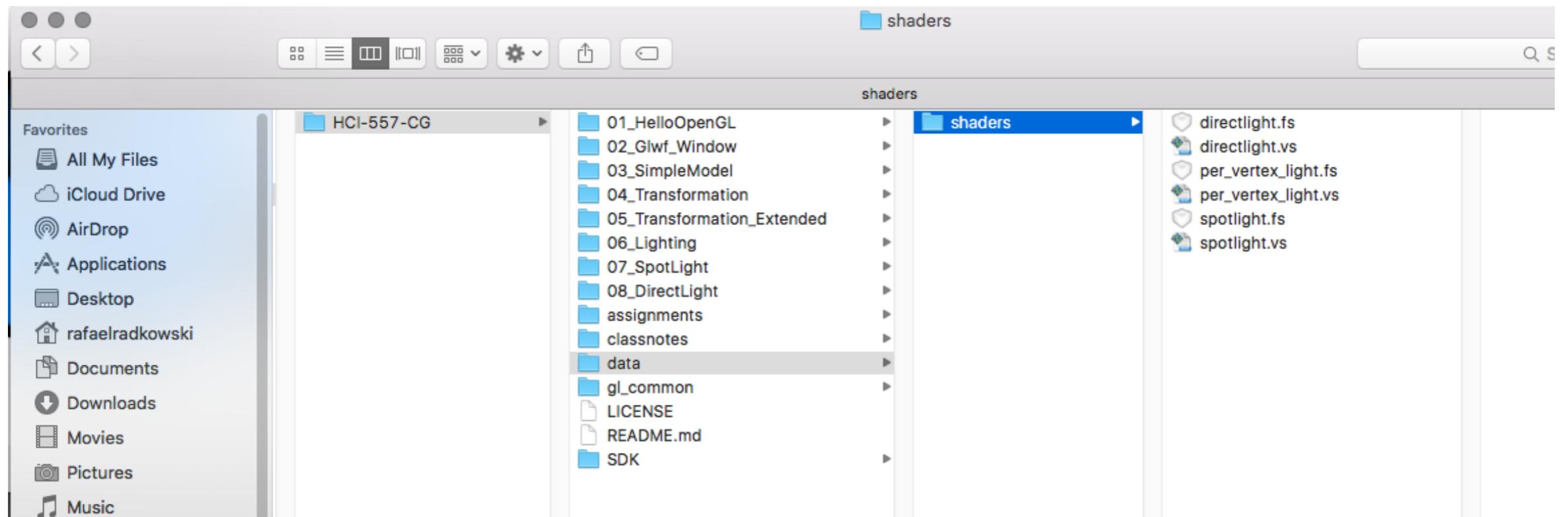
Shows how to realize a direct light.



GLSL Shader Code Location



Shader code is not saved in files in **data/shaders**



.vs - vertex shader code

.fs - fragment shader code

Advantage: no need to compile the C++ application when you make changes

Disadvantage: an additional file to handle and to load.

Code Example

```
38 void main(void)
39 {
40     vec3 normal = normalize(in_Normal);
41     vec4 transformedNormal = normalize(transpose(inverse(modelMatrixBox)) * vec4( normal, 1.0 ));
42     vec4 surfacePostion = modelMatrixBox * vec4(in_Position, 1.0);
43
44     vec4 surface_to_light = normalize( light_position - surfacePostion );
45
46     // Diffuse color
47     float diffuse_coefficient = max( dot(transformedNormal, surface_to_light), 0.0);
48     vec3 out_diffuse_color = diffuse_color * diffuse_coefficient * diffuse_intensity;
49
50     // Ambient color
51     vec3 out_ambient_color = vec3(ambient_color) * ambient_intensity;
52
53     // Specular color
54     vec3 incidenceVector = -surface_to_light.xyz;
55     vec3 reflectionVector = reflect(incidenceVector, transformedNormal.xyz);
56     vec3 cameraPosition = vec3( -viewMatrixBox[3][0], -viewMatrixBox[3][1], -viewMatrixBox[3][2]);
57     vec3 surfaceToCamera = normalize(cameraPosition - surfacePostion.xyz);
58     float cosAngle = max( dot(surfaceToCamera, reflectionVector), 0.0);
59     float specular_coefficient = pow(cosAngle, shininess);
60     vec3 out_specular_color = specular_color * specular_coefficient * specular_intensity;
61
62
63     //attenuation
64     float distanceToLight = length(light_position.xyz - surfacePostion.xyz);
65     float attenuation = 1.0 / (1.0 + attenuationCoefficient * pow(distanceToLight, 2));
66
67     /////////////////////////////////
68     // Spotlight
69     // 1. Normalize the cone direction
70     vec3 cone_direction_norm = normalize(cone_direction);
71
72     // 2. Calculate the ray direction. We already calculated the surface to light direction.
73     // All what we need to do is to inverse this value
74     vec3 ray_direction = -surface_to_light.xyz;
75
76     // 3. Calculate the angle between light and surface using the dot product again.
77     // To simplify our understanding, we use the degrees
78     float light_to_surface_angle = degreesacos(dot(ray direction, cone direction norm));
```

Shaders.h/.cpp

Shaders.h/.cpp is a file with function to support shader code loading, program set up, and error handling.

Creates a shader program

```
GLuint CreateShaderProgram(string vertex_source, string fragment_source);
```

- vertex source - the vertex shader source code
- fragment_source - the fragment shader source code
- return - GLuint of the shader program

Loads a shader program from a file and creates the related program

```
GLuint LoadAndCreateShaderProgram(string vertex_file, string fragment_file);
```

- vertex_file - the file which stores the vertex shader code
- fragment_file - the file which stores the fragment shader code
- return - GLuint of the shader program

GLSL Reference page

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The OpenGL Shading Language reference pages have been merged with the OpenGL API reference pages.

<https://www.opengl.org/sdk/docs/man4/>

OpenGL Software Development Kit
DOCUMENTATION, SAMPLE CODE, LIBRARIES, AND TOOLS
FOR CREATING OPENGL-BASED APPLICATIONS

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Name
acos — return the arccosine of the parameter

Declaration

```
genType acos( genType x );
```

Parameters

x
Specify the value whose arccosine to return.

Description
atan returns the angle whose trigonometric cosine is x. The range of values returned by atan is [-pi, pi]. The result is undefined if |x| > 1.

Version Support

Function Name	OpenGL Shading Language Version											
	1.10	1.20	1.30	1.40	1.50	3.30	4.00	4.10	4.20	4.30	4.40	4.50
acos	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓

See Also
[sin](#), [cos](#), [asin](#), [tan](#)

GLSL only

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barrier
[glBeginConditionalRender](#)
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Once created, a named texture may be re-bound to its same original target as often as needed. It is usually much faster to use **glBindTexture** to bind an existing named texture to one of the texture targets than it is to reload the texture image using [glTexImage1D](#), [glTexImage2D](#), [glTexImage3D](#) or another similar function.

Notes

The `GL_TEXTURE_2D_MULTISAMPLE` and `GL_TEXTURE_2D_MULTISAMPLE_ARRAY` targets are available only if the GL version is 3.2 or higher.

Errors

`GL_INVALID_ENUM` is generated if `target` is not one of the allowable values.

`GL_INVALID_VALUE` is generated if `target` is not a name returned from a previous call to [glGenTextures](#).

`GL_INVALID_OPERATION` is generated if `texture` was previously created with a target that doesn't match that of `target`.

Associated Gets

`glGet` with argument `GL_TEXTURE_BINDING_1D`, `GL_TEXTURE_BINDING_2D`, `GL_TEXTURE_BINDING_3D`, `GL_TEXTURE_BINDING_1D_ARRAY`, `GL_TEXTURE_BINDING_2D_ARRAY`, `GL_TEXTURE_BINDING_RECTANGLE`, `GL_TEXTURE_BINDING_BUFFER`, `GL_TEXTURE_BINDING_CUBE_MAP`, `GL_TEXTURE_BINDING_CUBE_MAP`, `GL_TEXTURE_BINDING_CUBE_MAP_ARRAY`, `GL_TEXTURE_BINDING_2D_MULTISAMPLE`, or `GL_TEXTURE_BINDING_2D_MULTISAMPLE_ARRAY`.

OpenGL only

Version Support

Function / Feature Name	OpenGL Version											
	2.0	2.1	3.0	3.1	3.2	3.3	4.0	4.1	4.2	4.3	4.4	4.5
<code>glBindTexture</code>	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓

See Also

[glDeleteTextures](#), [glGenTextures](#), [glGet](#), [glGetTexParameter](#), [glIsTexture](#), [glTexImage1D](#), [glTexImage2D](#), [glTexImage2DMultisample](#), [glTexImage3D](#), [glTexImage3DMultisample](#), [glTexBuffer](#), [glTexParameter](#)

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sqrt — return the square root of the parameter

```
genType sqrt( genType x );  
  
genDType sqrt( genDType x );
```

genType : a generic datatype which is most of the time **float**, **vec2**, **vec3**, **vec4**

genDType : a generic datatype which is most of the time **double**, **vec2**, **vec3**, **vec4**

- Input datatype does not need to be the same as the output datatype, so you must know what the function does for you.
- BUT: if the input is a float datatype, the output is also a float datatype; same for double

GLSL Shader Functions



length — calculate the length of a vector

```
float length( genType x );
```

Parameters:

x - Specifies a vector of which to calculate the length.

pow — return the value of the first parameter raised to the power of the second

```
genType pow( genType x, genType y );
```

Parameters:

x - Specify the value to raise to the power y.

y - Specify the power to which to raise x.

GLSL Shader Functions



normalize — calculate the normalize product of two vectors

```
genType normalize(genType v);
```

Parameters:

v - Specifies the vector to normalize.

degrees — convert a quantity in radians to degrees

```
genType degrees(genType radians);
```

Parameters:

- radians - Specify the quantity, in radians, to be converted to degrees.

GLSL Shader Functions



acos — return the arccosine of the parameter

```
genType acos( genType x );
```

Parameters:

x - Specify the value whose arccosine to return.

dot — calculate the dot product of two vectors

```
float dot( genType x, genType y );
```

Parameters:

- x - Specifies the first of two vectors
- y - Specifies the second of two vectors

Thank you!

Questions

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