

**ARLAB**

ME/CprE/ComS 557

# **Computer Graphics and Geometric Modeling**

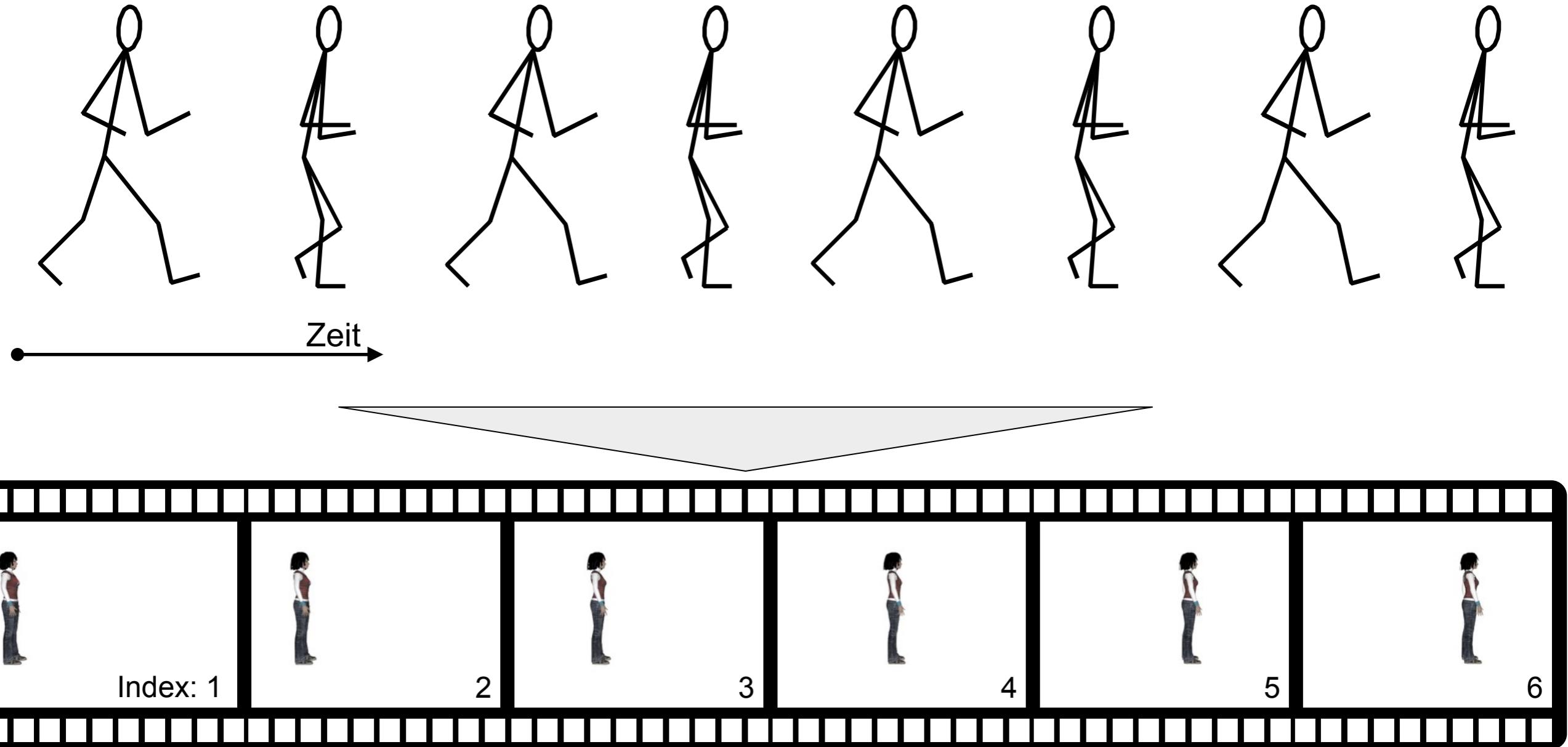
## **Hierarchical Scenes**

November 19th, 2015

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**IOWA STATE UNIVERSITY**  
OF SCIENCE AND TECHNOLOGY

# Animations

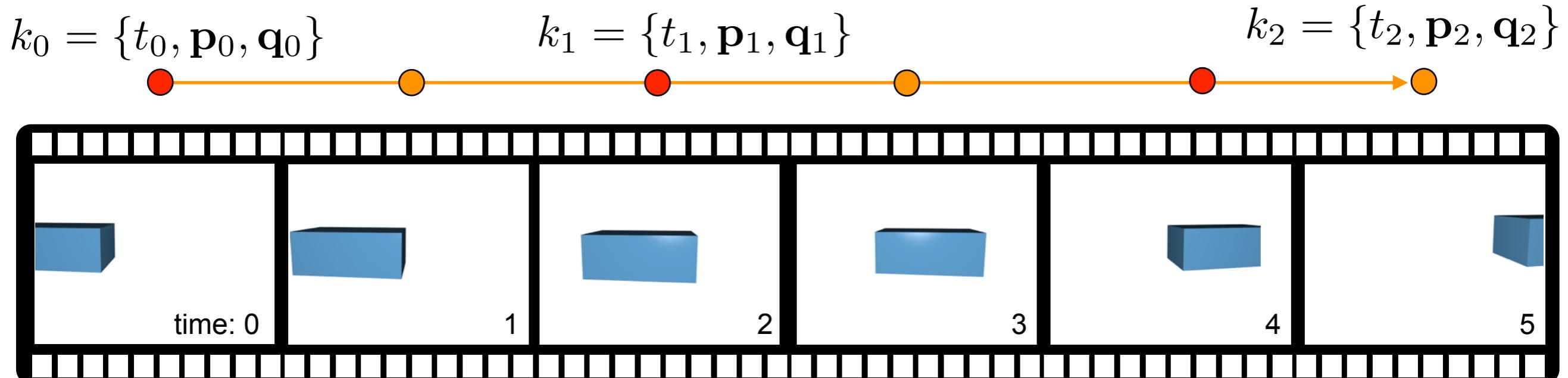


Animation is the process to generate moving objects on screen. The computer graphics rendering pipeline only generates static scenes. Animation techniques alter this scene from frame to frame. Thus, objects appear as moving objects.

# Representing the keyframes

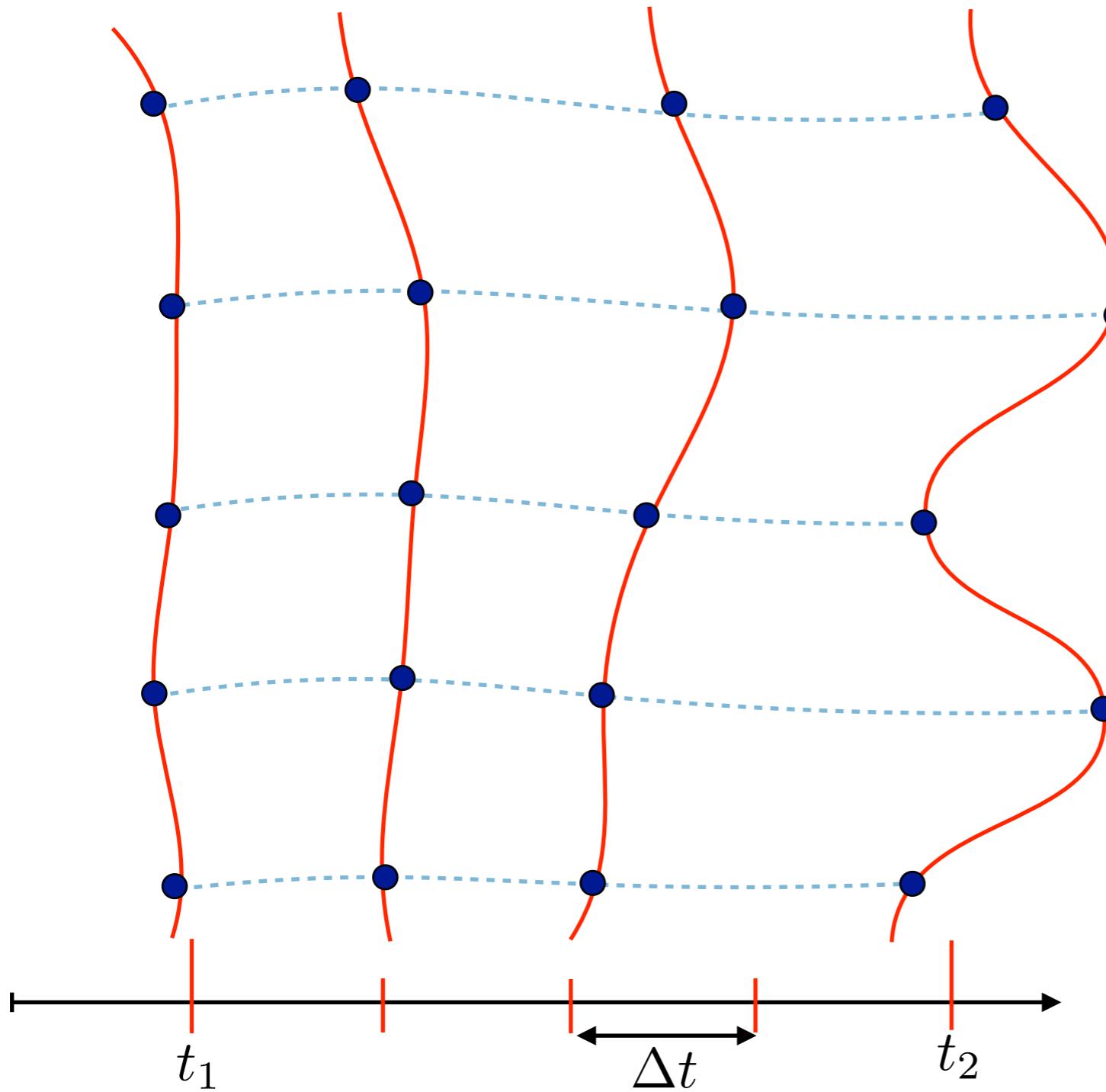
For every keyframe  $k_i$  ● we store  
the time fraction in an interval between 0 and 1  
the position as vector with {x, y, z} coordinates  
the orientation of the object as quaternion  $q = \{x, y, z, w\}$

$$k_i = \{t_i, \mathbf{p}_i, \mathbf{q}_i\}$$



# Constant Motion

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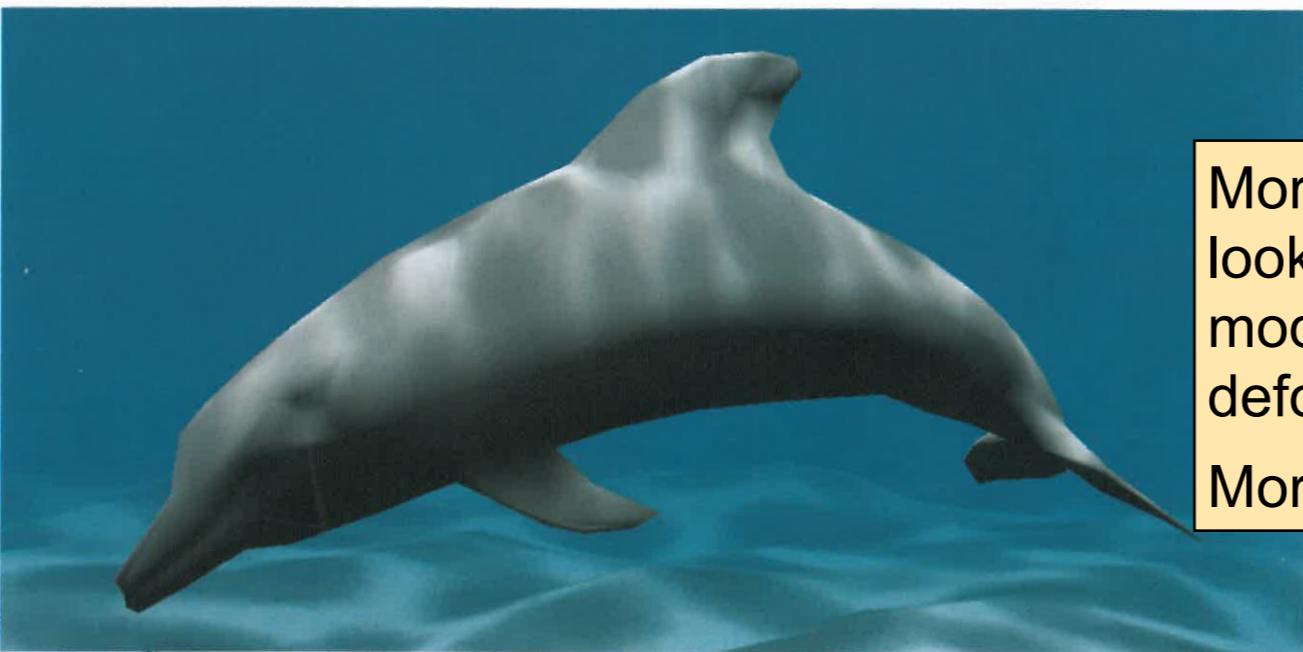


For constant motion, divide the time interval between the keyframes in  $n+1$  subintervals

$$\Delta t = \frac{t_2 - t_1}{n + 1}$$

The time for the  $j$ th frame is:

$$t = t_1 + j \Delta t$$



Morphing

Morphing is a technique that facilitates natural looking motion. It deforms the mesh of a 3D model during runtime using one or multiple deformation models.

Morphing is a shorten term of metamorphosing

# Content

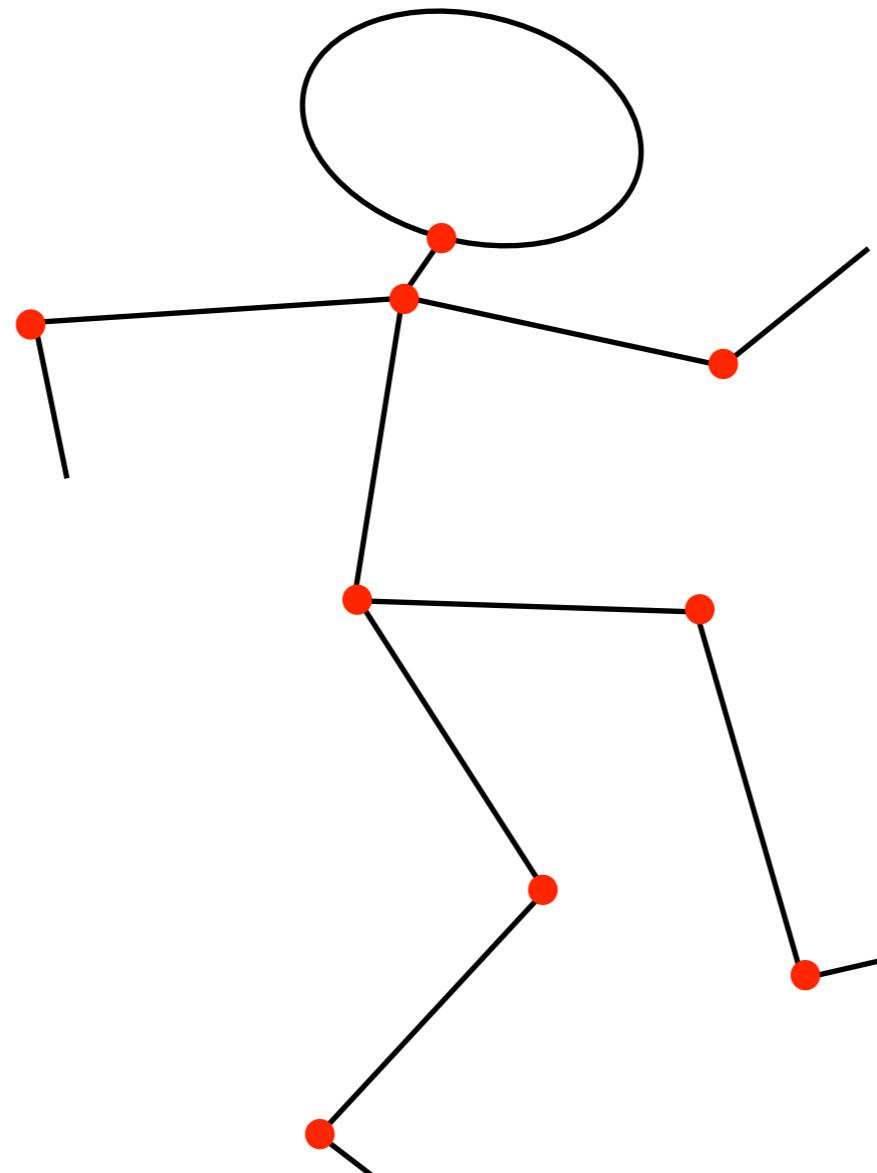
- Hierarchical Modeling
- Graph data structures
- Scenegraphs and Scenegraph APIs

# Video



# Articulated Figure Animation

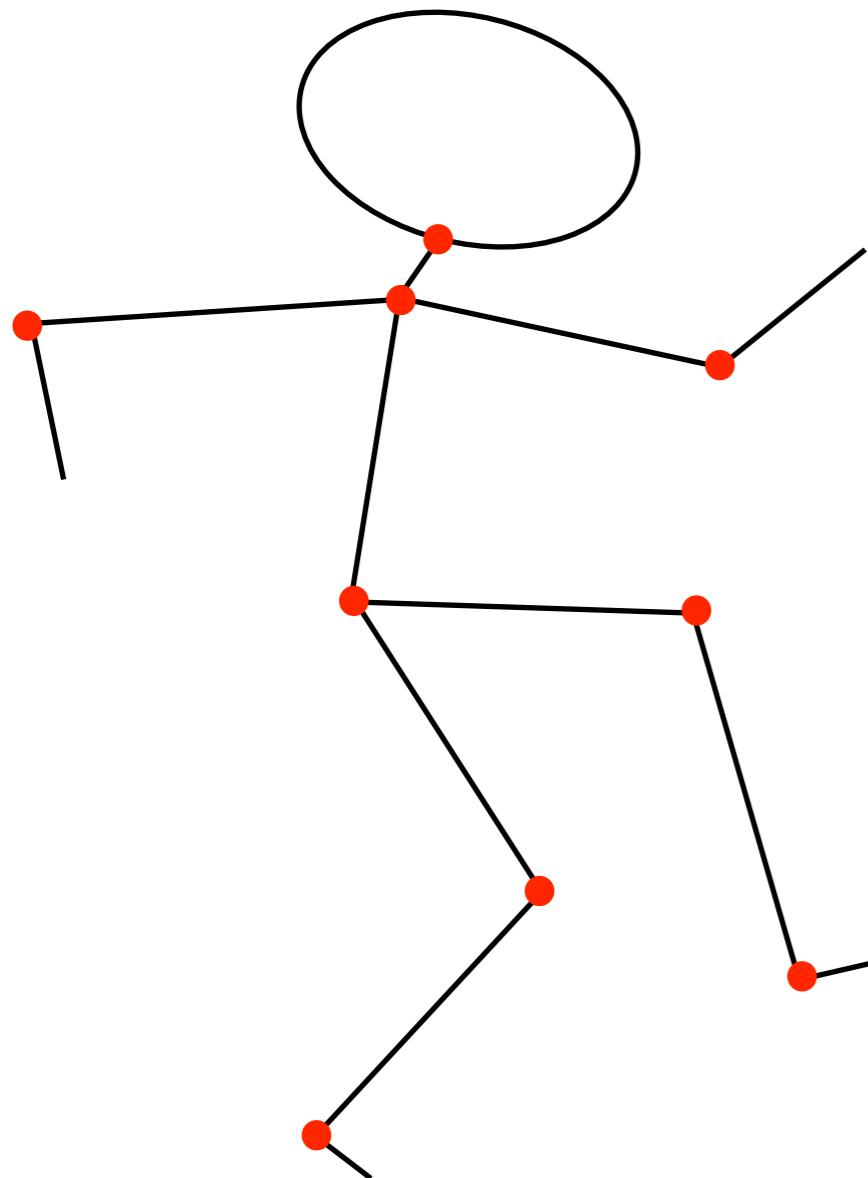
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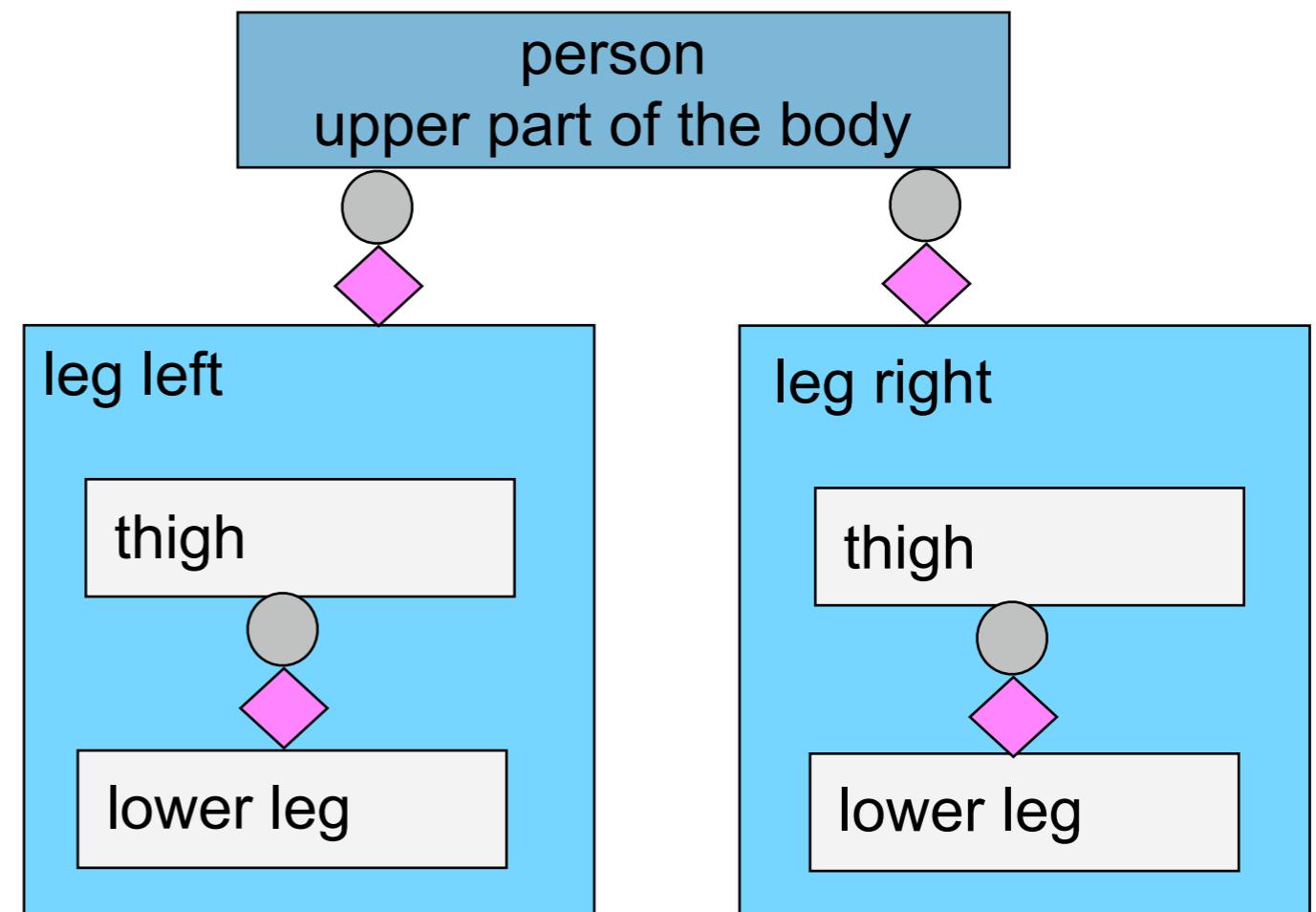
The basic technique for animating people, insects, vehicles, etc. are **articulated figures**, which are a hierarchical structure of single objects connected by joints.

We formally create a stick figure also called a **skeleton** which we wrap into a skin.

# Hierarchical Modeling



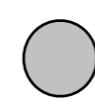
We design a complex model by modularizing the specification of the geometry into subcomponents. One way is the **top-down design**



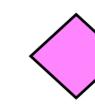
Whenever it is possible, construct your models hierarchically.



Primitive node



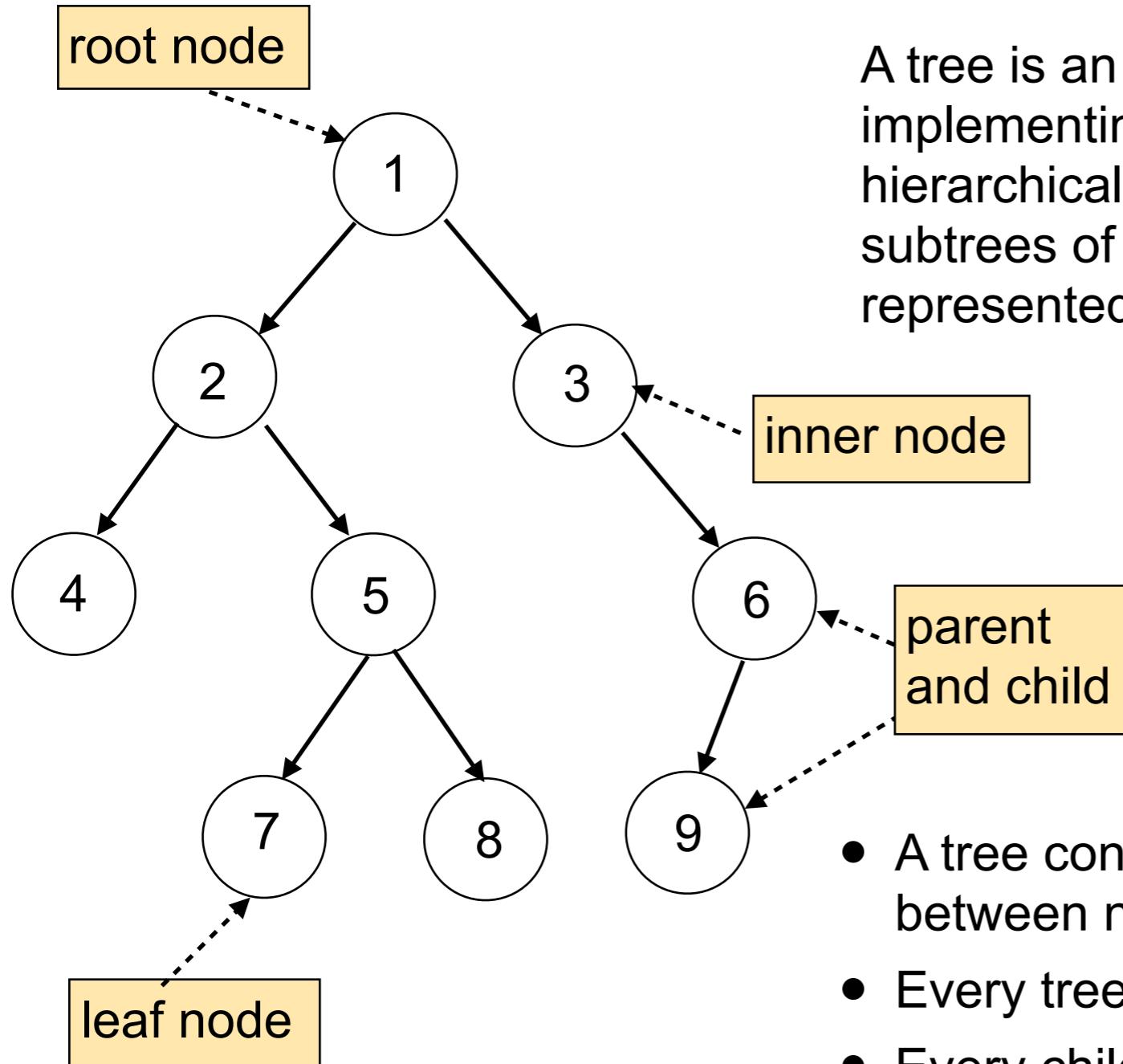
Instance node



Transformation node

# Tree Data Structure Notation

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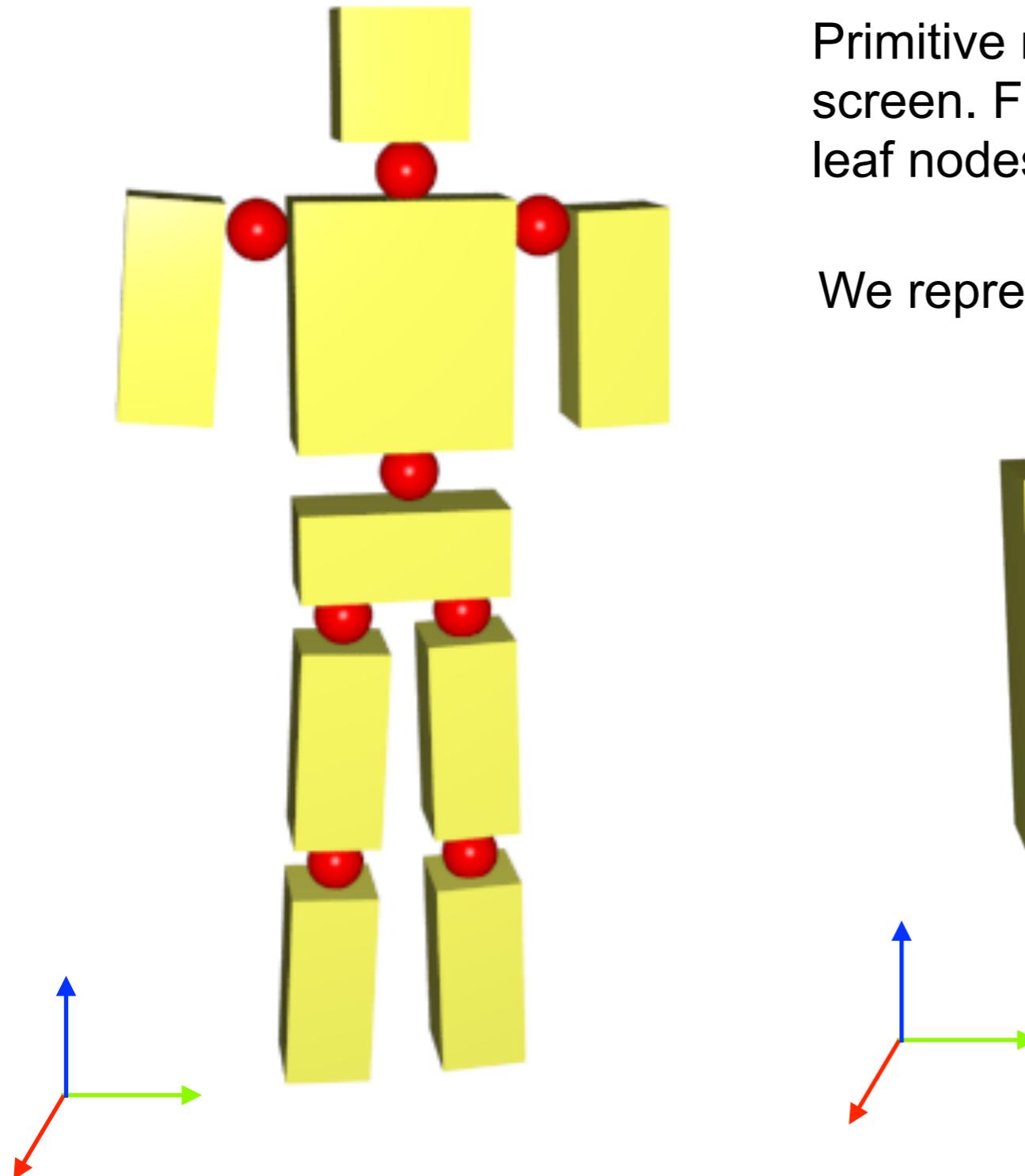


A tree is an abstract data type or data structure implementing this tree that simulates a hierarchical tree structure, with a root value and subtrees of children with a parent node, represented as a set of linked nodes.

- A tree consists of nodes and association between nodes
- Every tree has ONE root node
- Every child has only one parent
- Parent can have multiple children

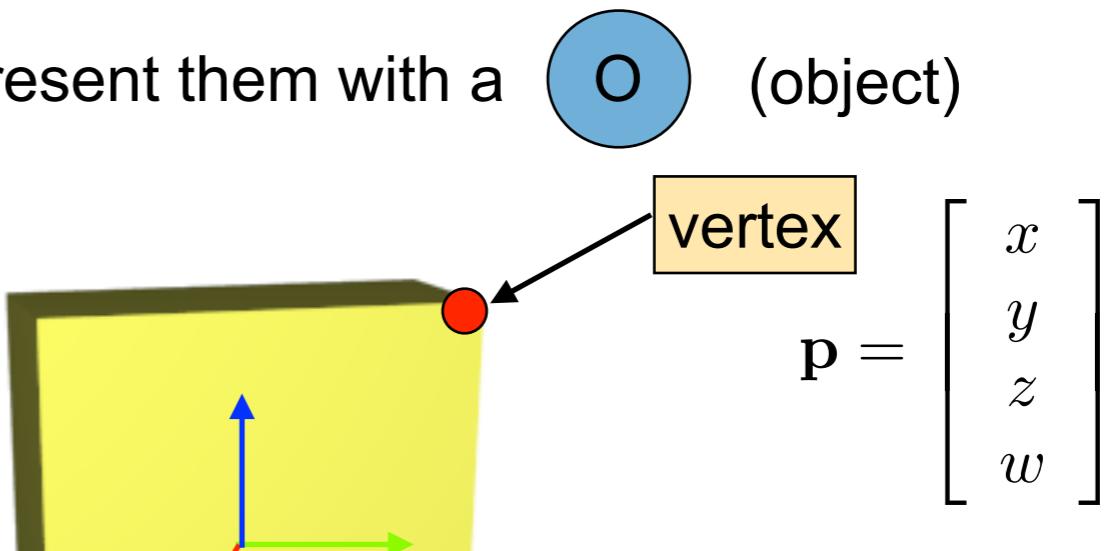
# Primitive Nodes

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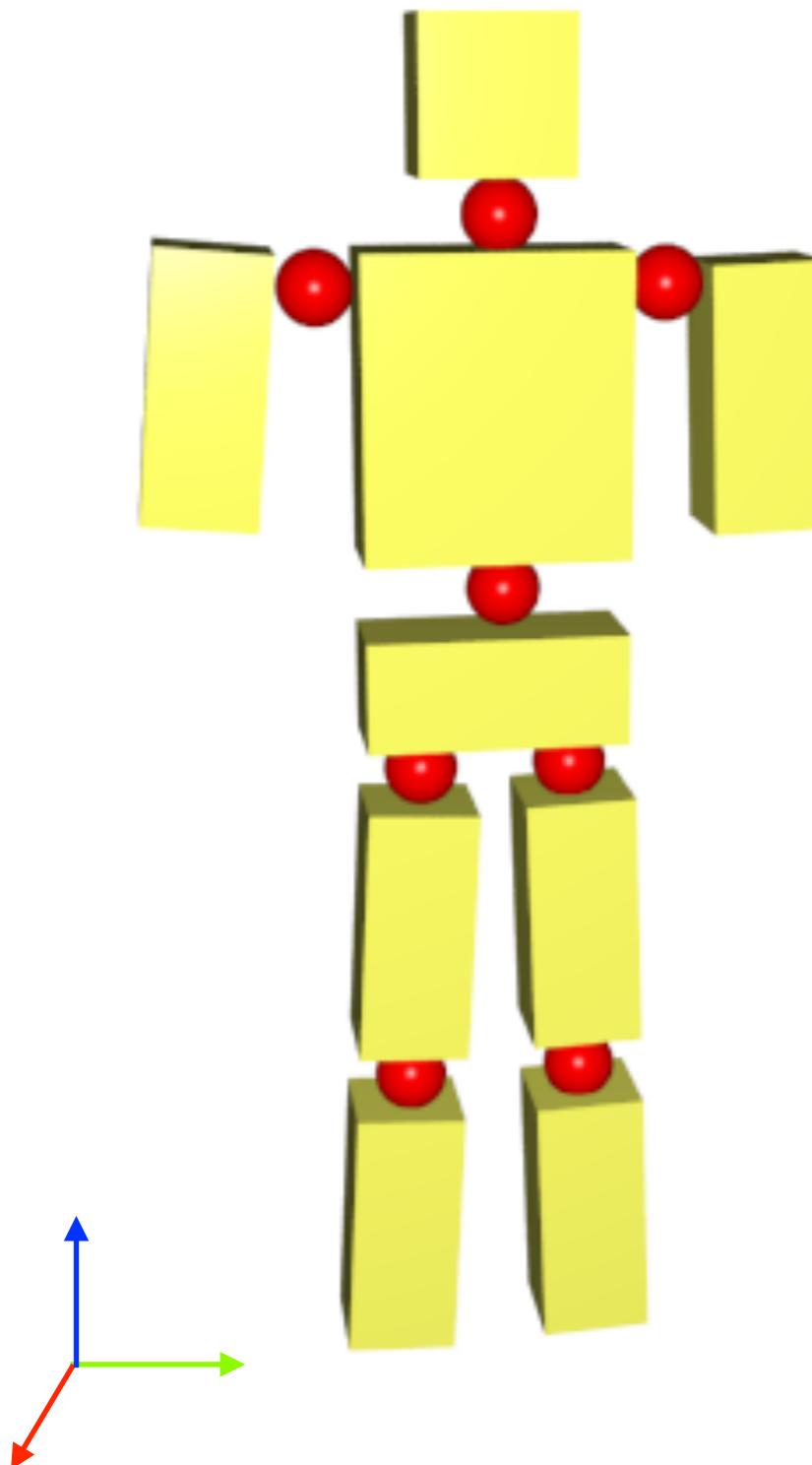
Primitive nodes are instances that render objects on screen. From a graph point of view, those nodes are leaf nodes, which have no further children.

We represent them with a



# Instance Transformation

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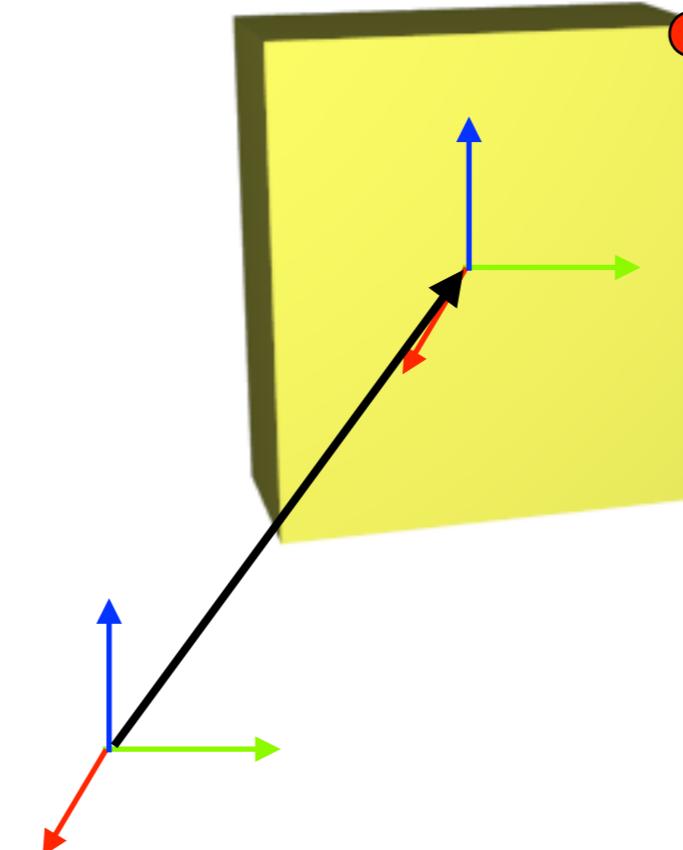
Primitive nodes are instances that render objects on screen. From a graph point of view, those nodes are leaf nodes, which have no further children.

We represent them with a

$T$  (object)

vertex

$$\mathbf{p} = \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

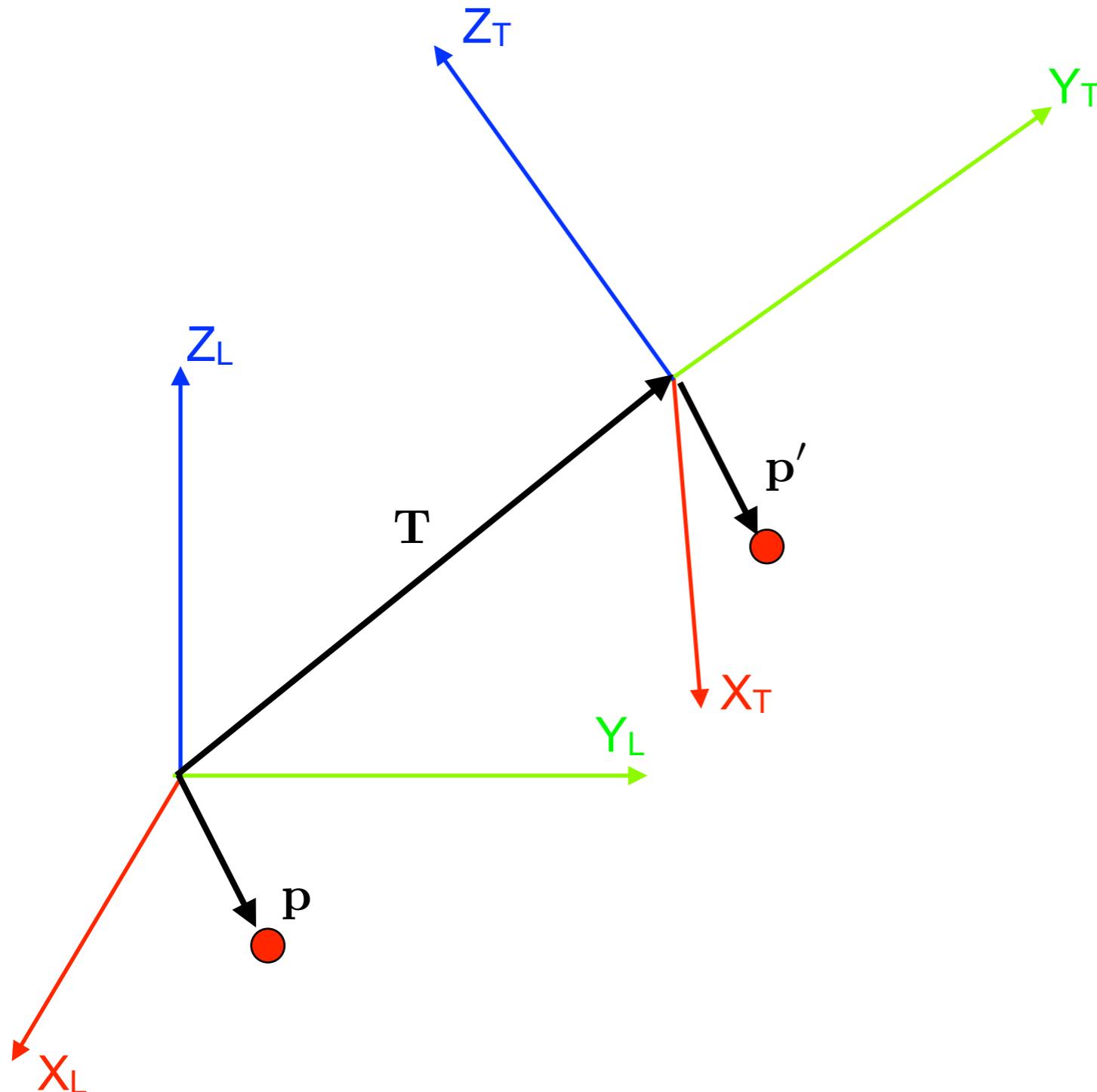


$$\mathbf{T} = \begin{bmatrix} r_{00} & r_{01} & r_{02} & x \\ r_{10} & r_{11} & r_{12} & y \\ r_{20} & r_{21} & r_{22} & z \\ 0 & 0 & 0 & w \end{bmatrix}$$

$$\mathbf{p}' = \mathbf{T} \mathbf{p}$$

# Transformation Reminder

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Every transformation can be considered as a coordinate system transformation: the matrix represents a new coordinate system. Multiplying a point with a matrix moves this point into a new coordinate system T.

$$T = \begin{bmatrix} r_{00} & r_{01} & r_{02} & x \\ r_{10} & r_{11} & r_{12} & y \\ r_{20} & r_{21} & r_{22} & z \\ 0 & 0 & 0 & w \end{bmatrix}$$

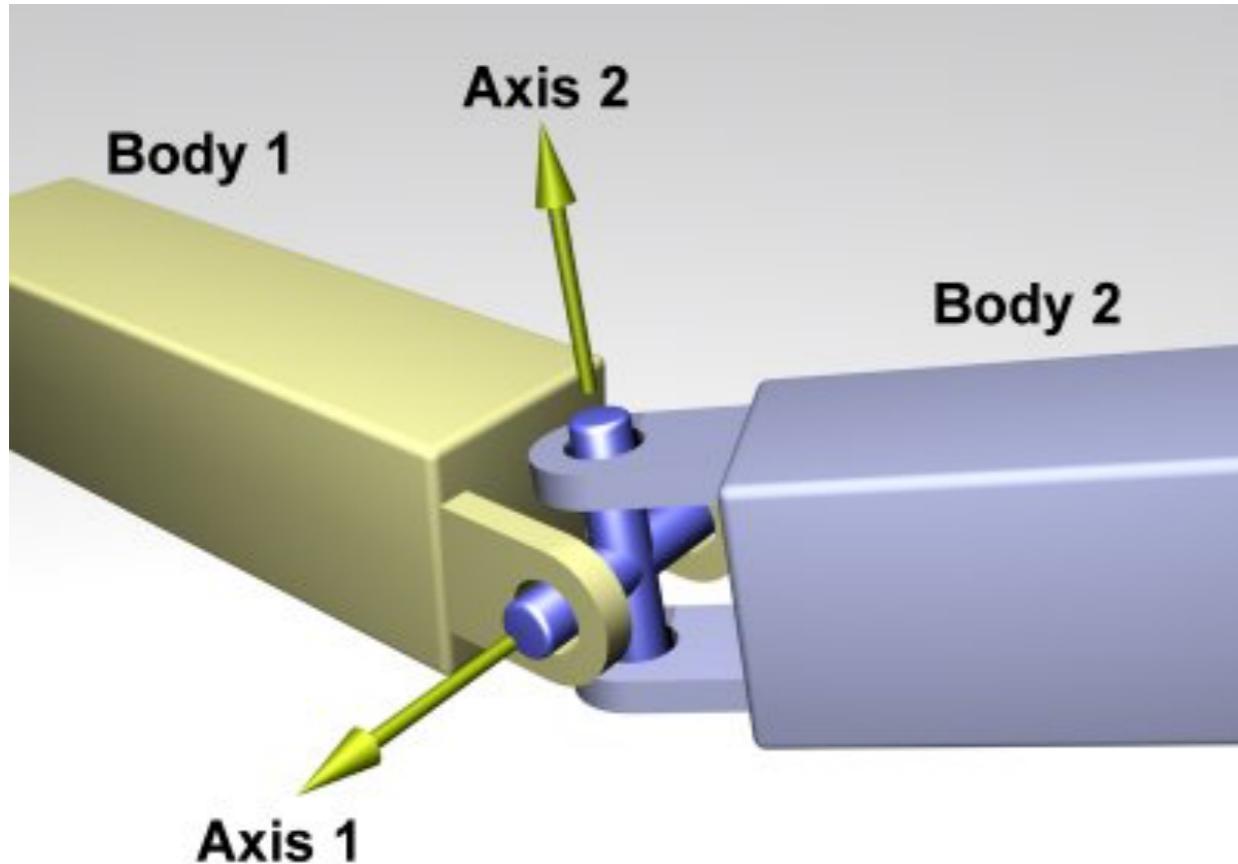
$$p' = T p$$

All further transformation are with respect to this coordinate system.

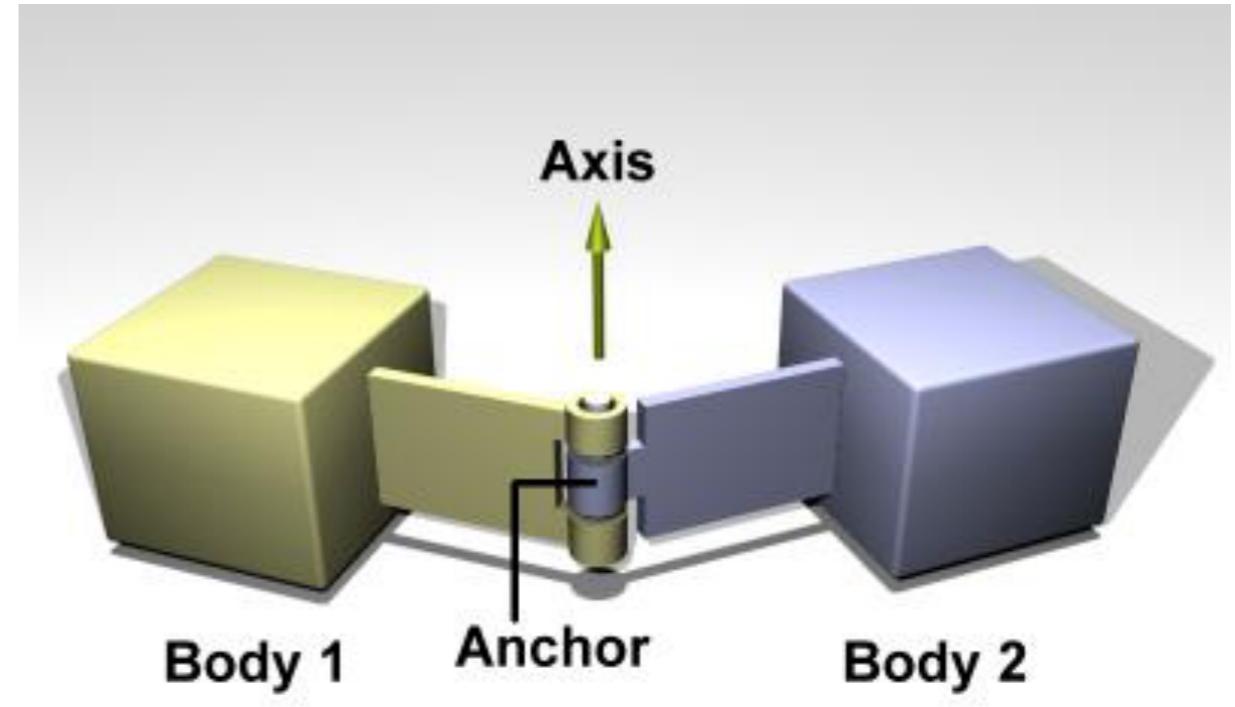
# Joint Transformation

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Joint transformations are used to simulate movement at a joint.



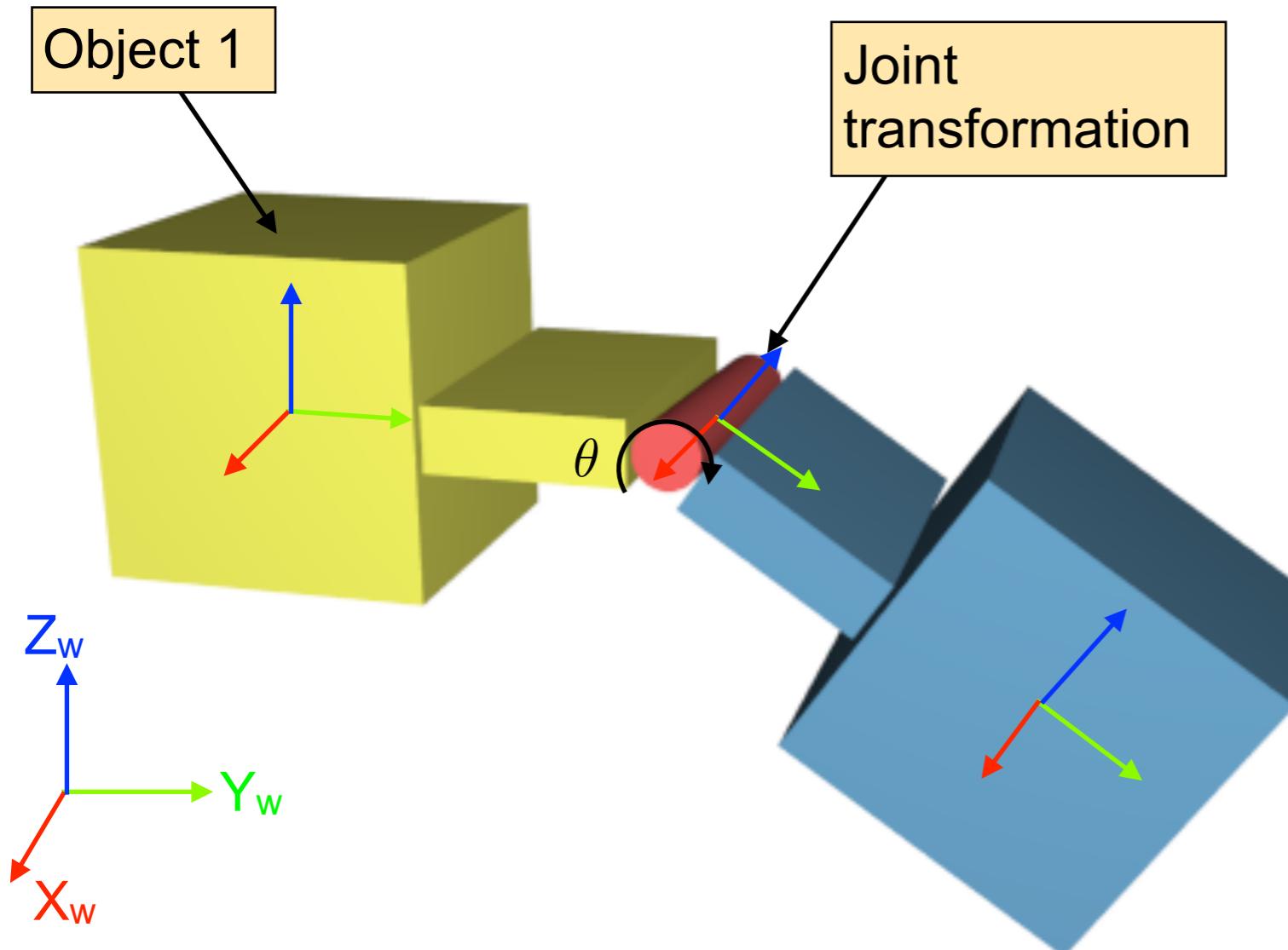
*Universal joint (source: odm)*



*Hinge joint (source: odm)*

- Different degrees of freedom (rotational and/or linear)
- Simulate the kinematics of an object
- Can be constraint

# Joint Transformation

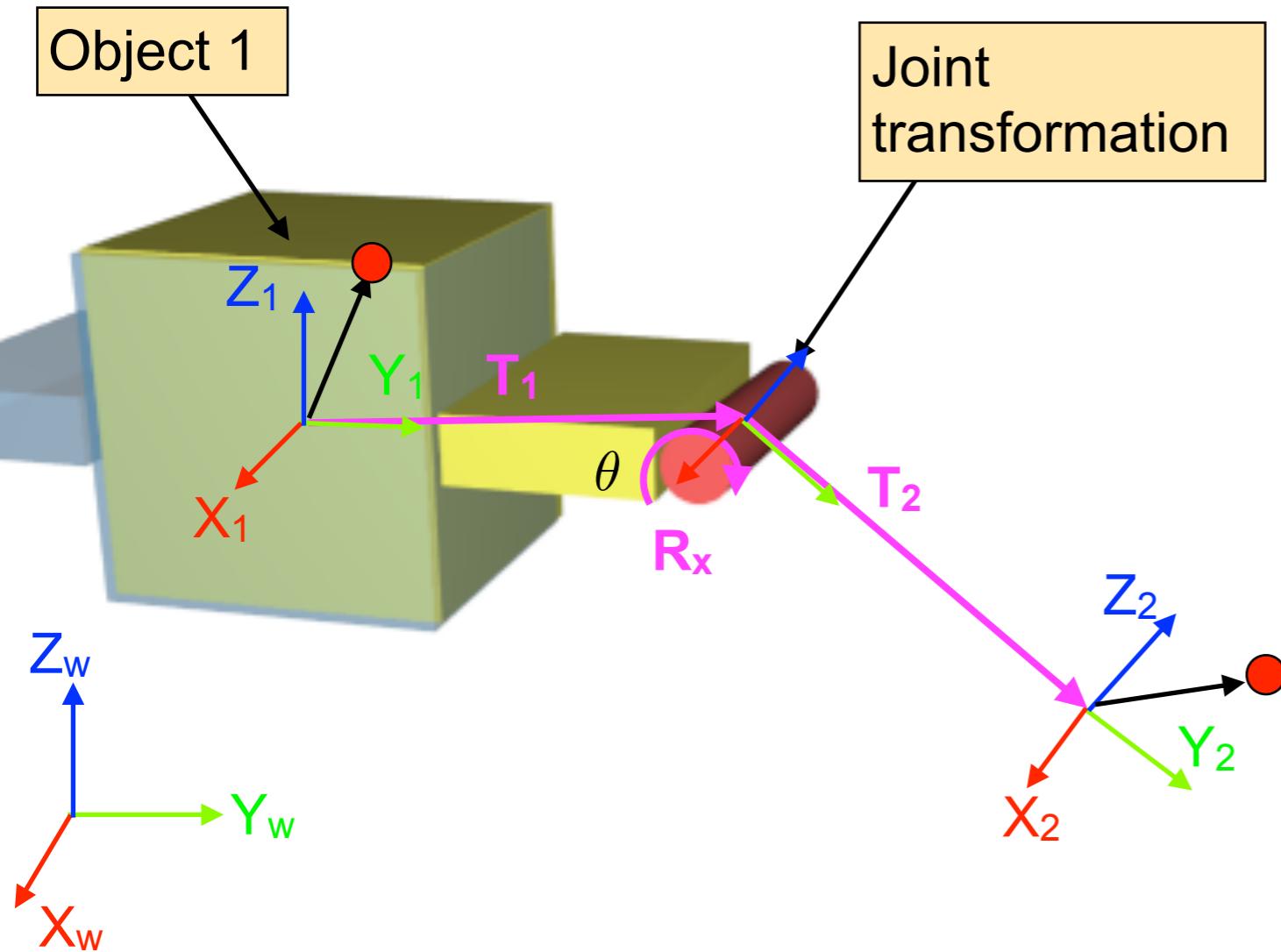


A joint transformation is a rotational and or linear transformation matrix along with a motion restriction, if required.

$$\mathbf{R}_x = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos(\theta) & -\sin \theta & 0 \\ 0 & \sin(\theta) & \cos(\theta) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\theta = \{\theta_{min}, \theta_{max}\}$$

# Joint Transformation



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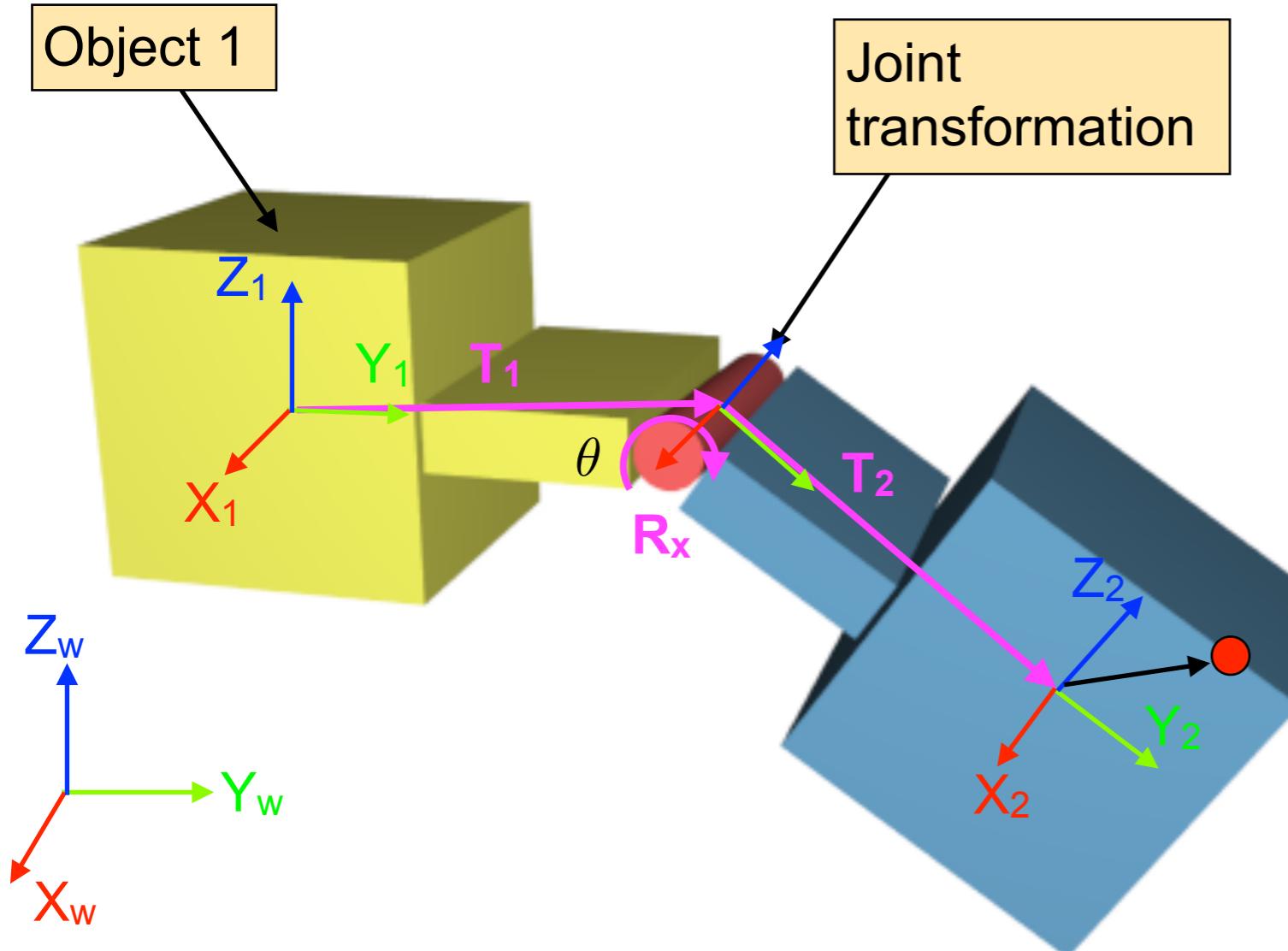
$$\theta = \{\theta_{min}, \theta_{max}\}$$

- Consider, the blue box is described in the first local coordinate system.
- We like to move it into the second one using a joint constraint, with

$$\mathbf{p}' = T_2 R_x T_1 \mathbf{p}$$

# Joint Transformation

ARLAB



A joint transformation is a rotational and or linear transformation matrix along with a motion restriction, if required.

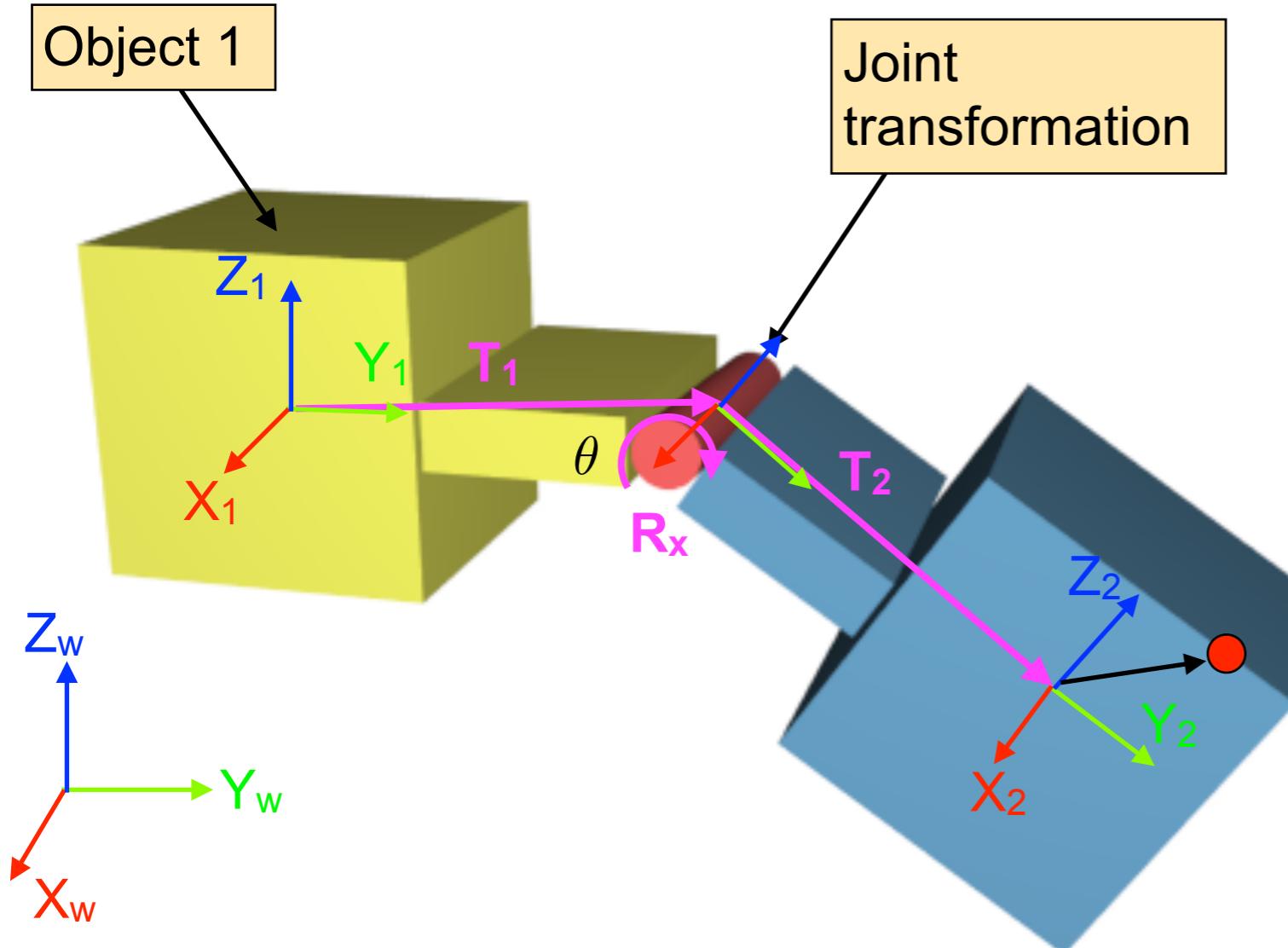
$$R_x = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos(\theta) & -\sin(\theta) & 0 \\ 0 & \sin(\theta) & \cos(\theta) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\theta = \{\theta_{min}, \theta_{max}\}$$

- Consider, the blue box is described in the first local coordinate system.
- We like to move it into the second one using a joint constraint, with

$$\mathbf{p}' = T_2 R_x T_1 \mathbf{p}$$

# Joint Transformation



We represent them with a

J

(joint)

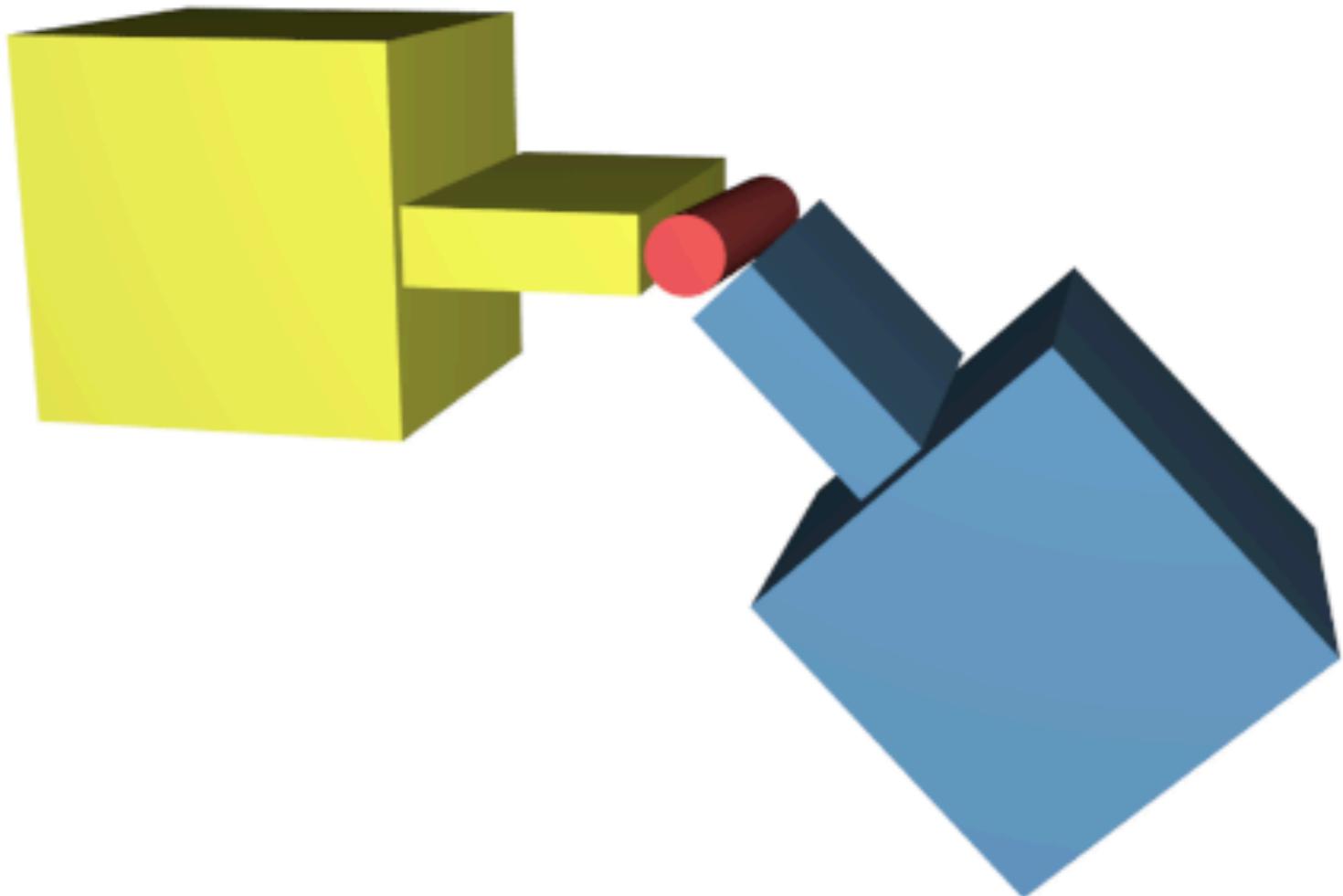
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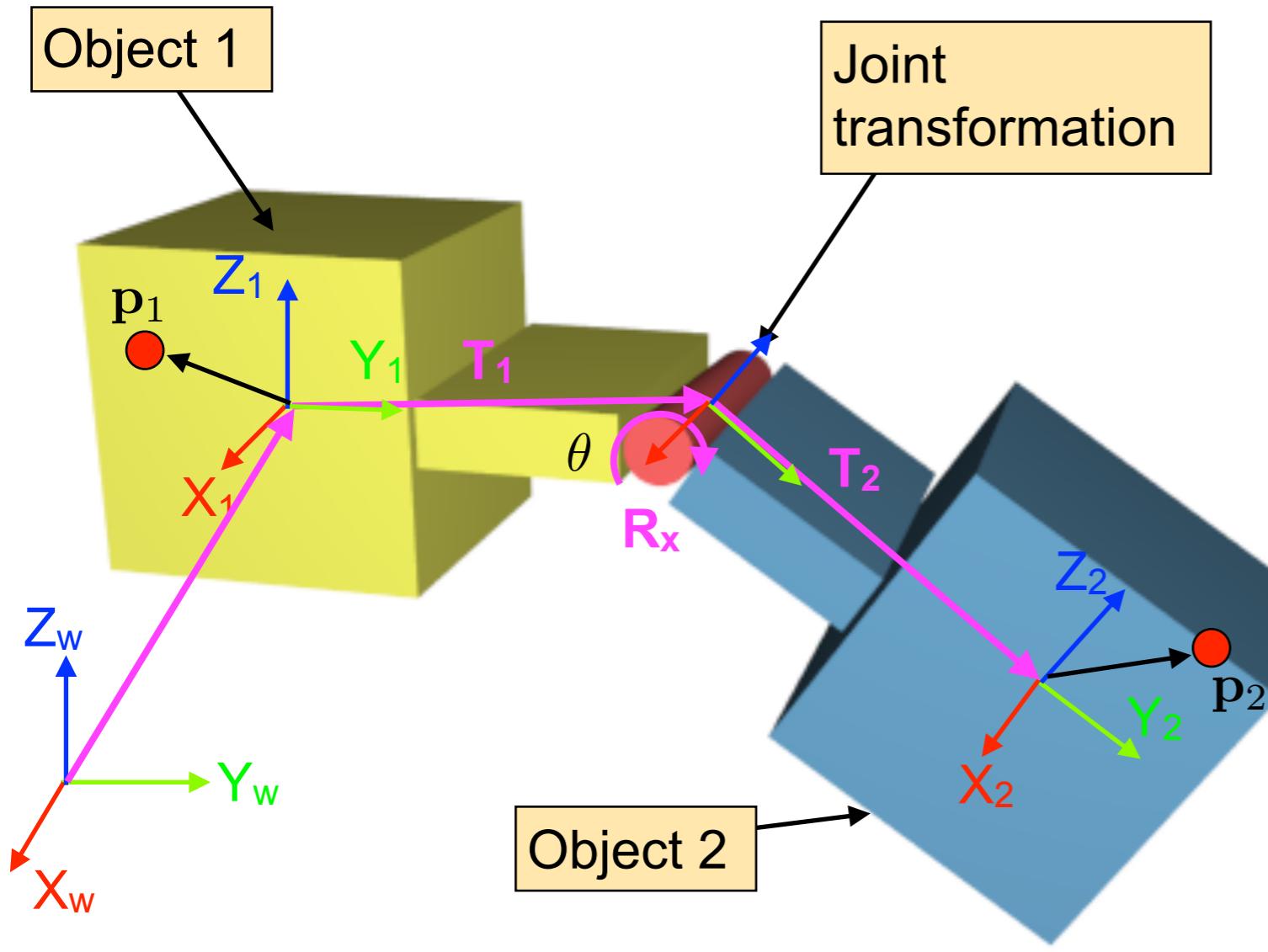
$$\theta = \{\theta_{min}, \theta_{max}\}$$

# Video

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# Moving Object 1



Consider, we use a transformation matrix  $T_{w1}$  to move the first object around. All points of object 1 are transformed with

$$\mathbf{p}'_1 = \mathbf{T}_{w1} \mathbf{p}_1$$

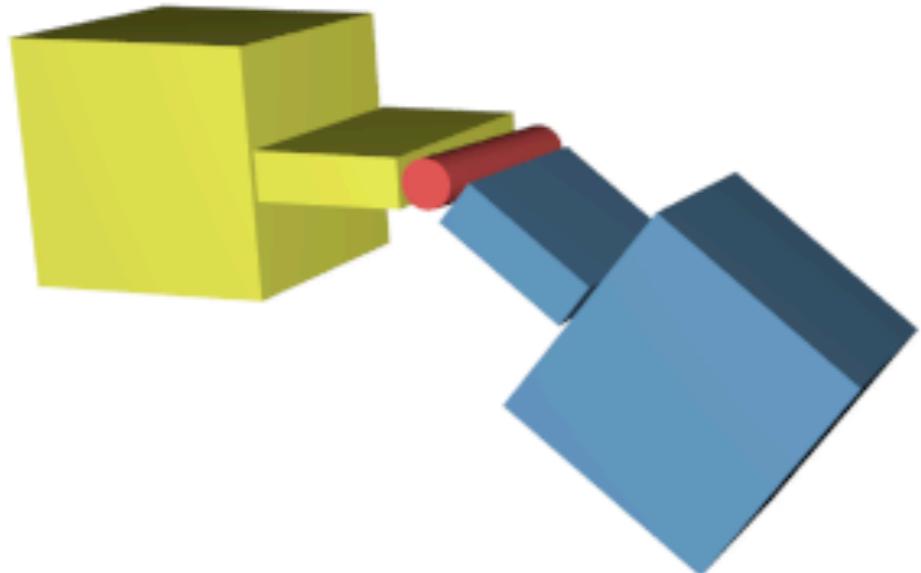
Since object 2, respectively all points of object two also depend on  $T_{w1}$ , all points follow the same transformation.

$$\mathbf{p}'_2 = \mathbf{T}_2 \mathbf{R}_x \mathbf{T}_1 \mathbf{T}_{w1} \mathbf{p}_2$$

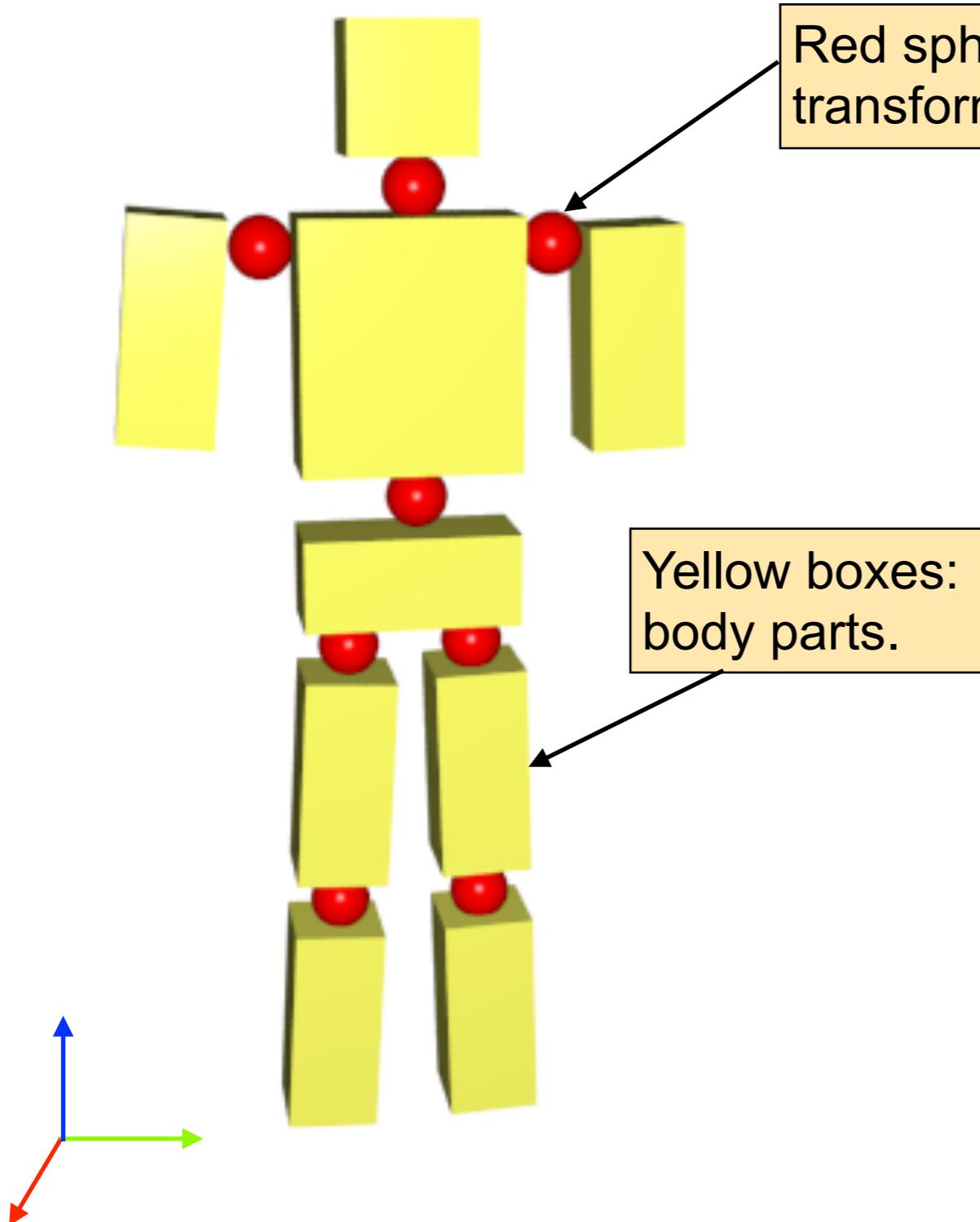
This allows us to build a hierarchical representation of transformed objects.

# Video

**ARLAB**



# Tree of objects

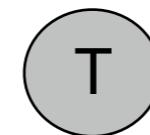
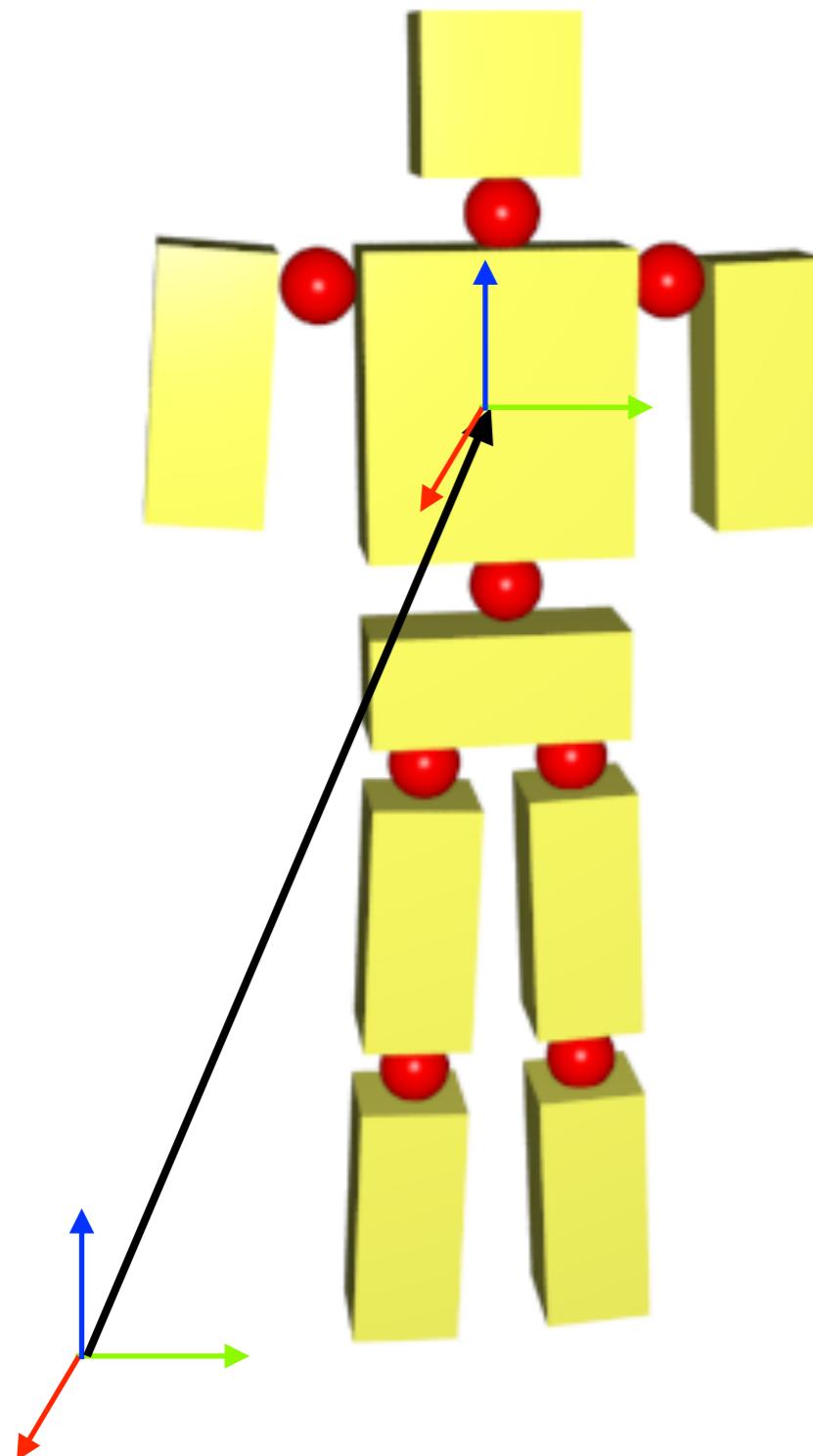


- J joint
- T transformation
- O object

- Object nodes are leaf nodes! They do not take any additional children.
- Joint and transformation nodes are inner nodes.

# Tree of objects

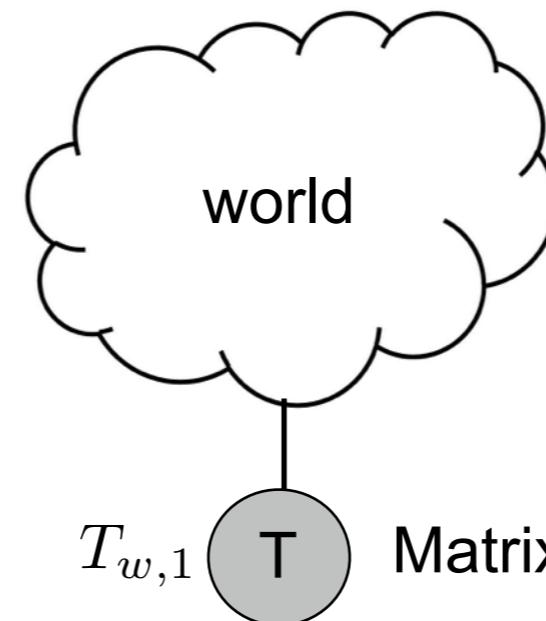
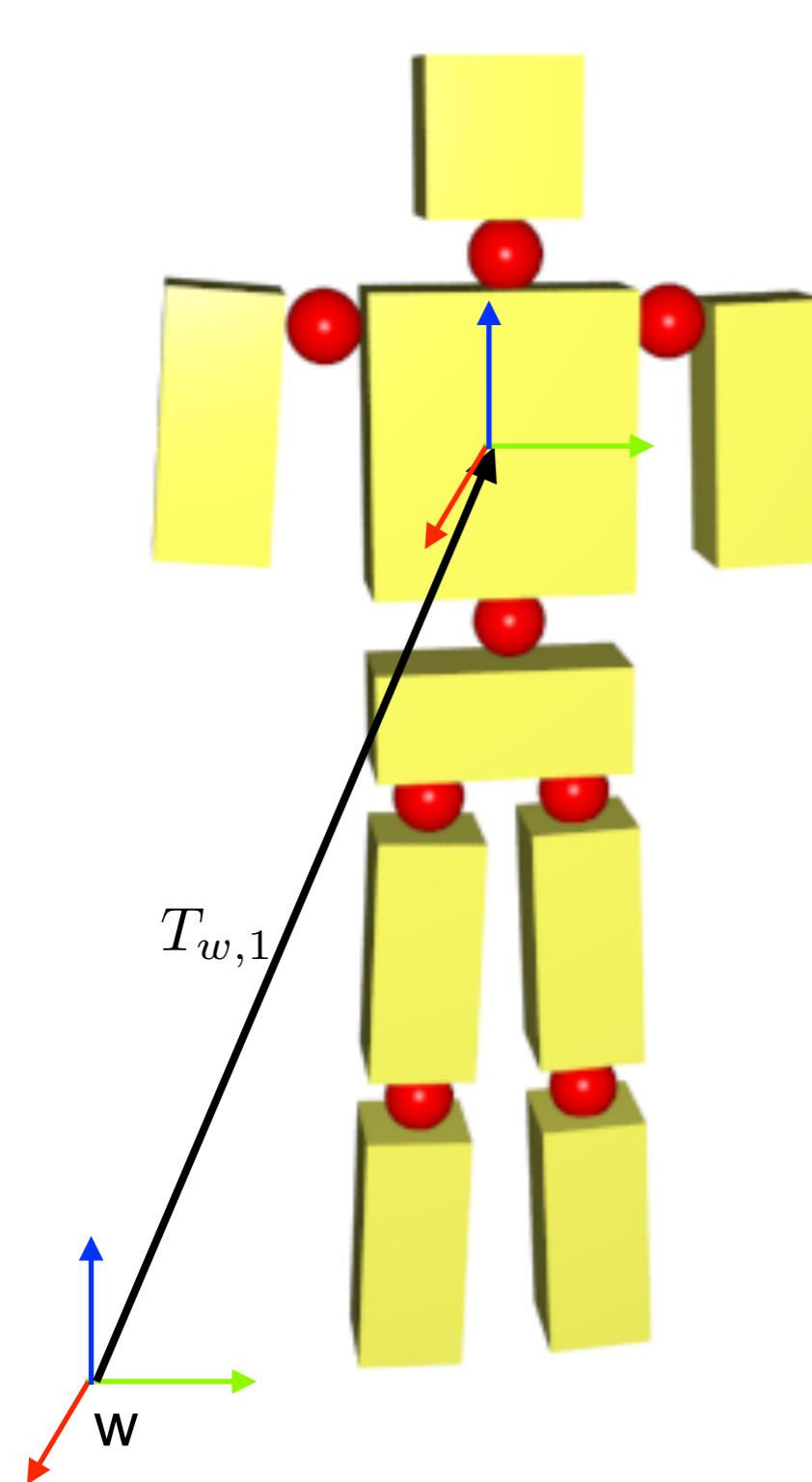
ARLAB



transformation for the world  
(identity matrix)

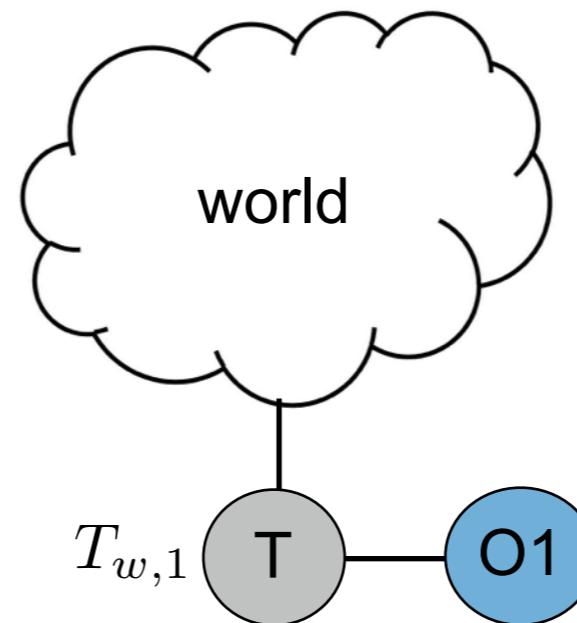
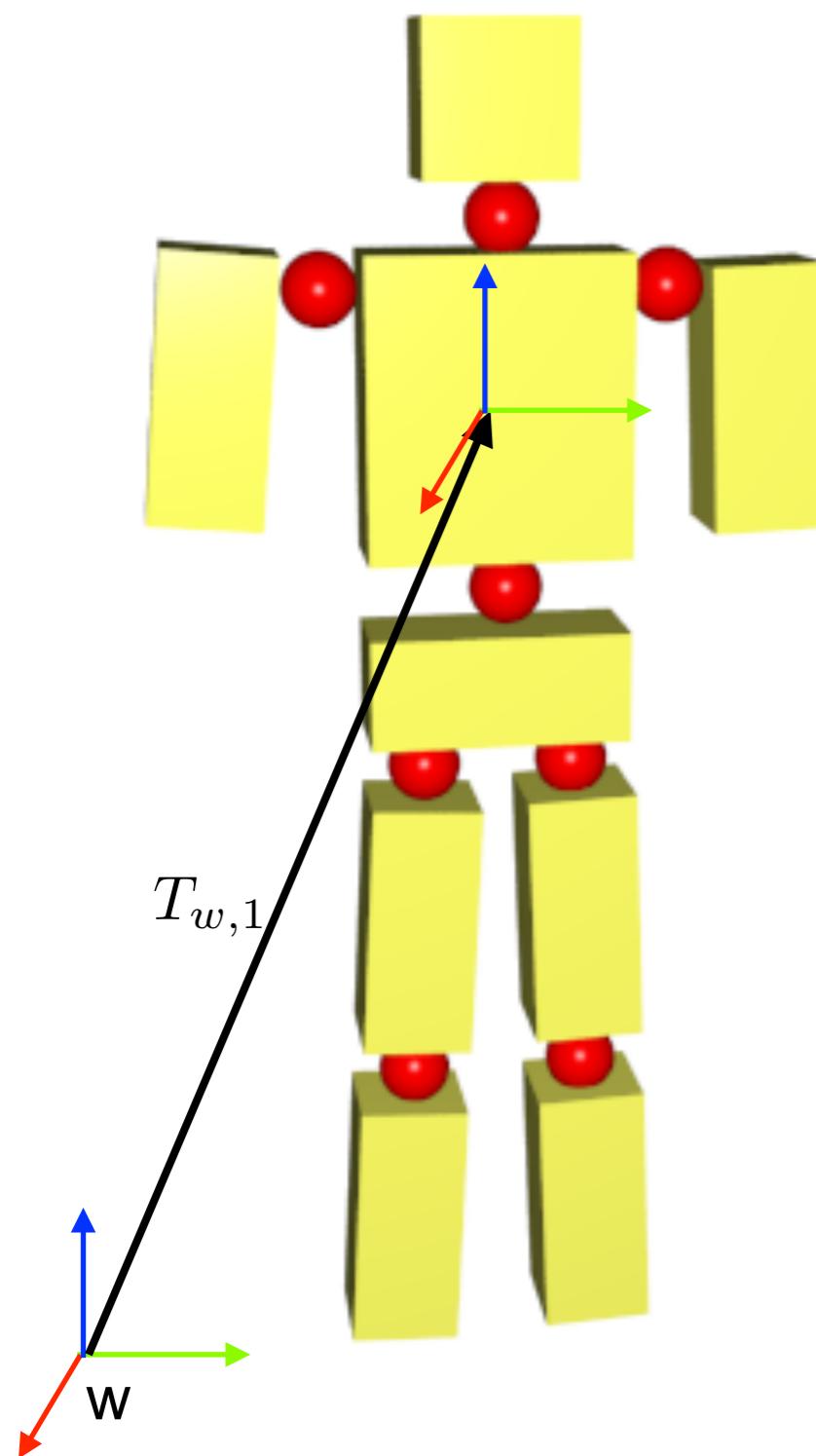
# Tree of objects

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# Tree of objects

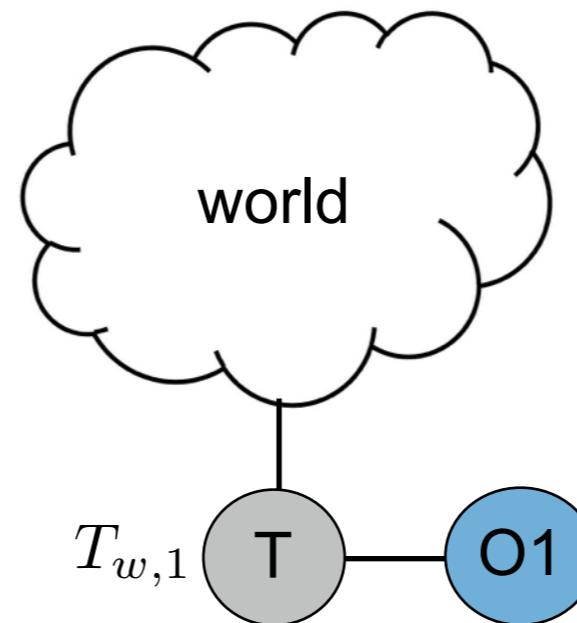
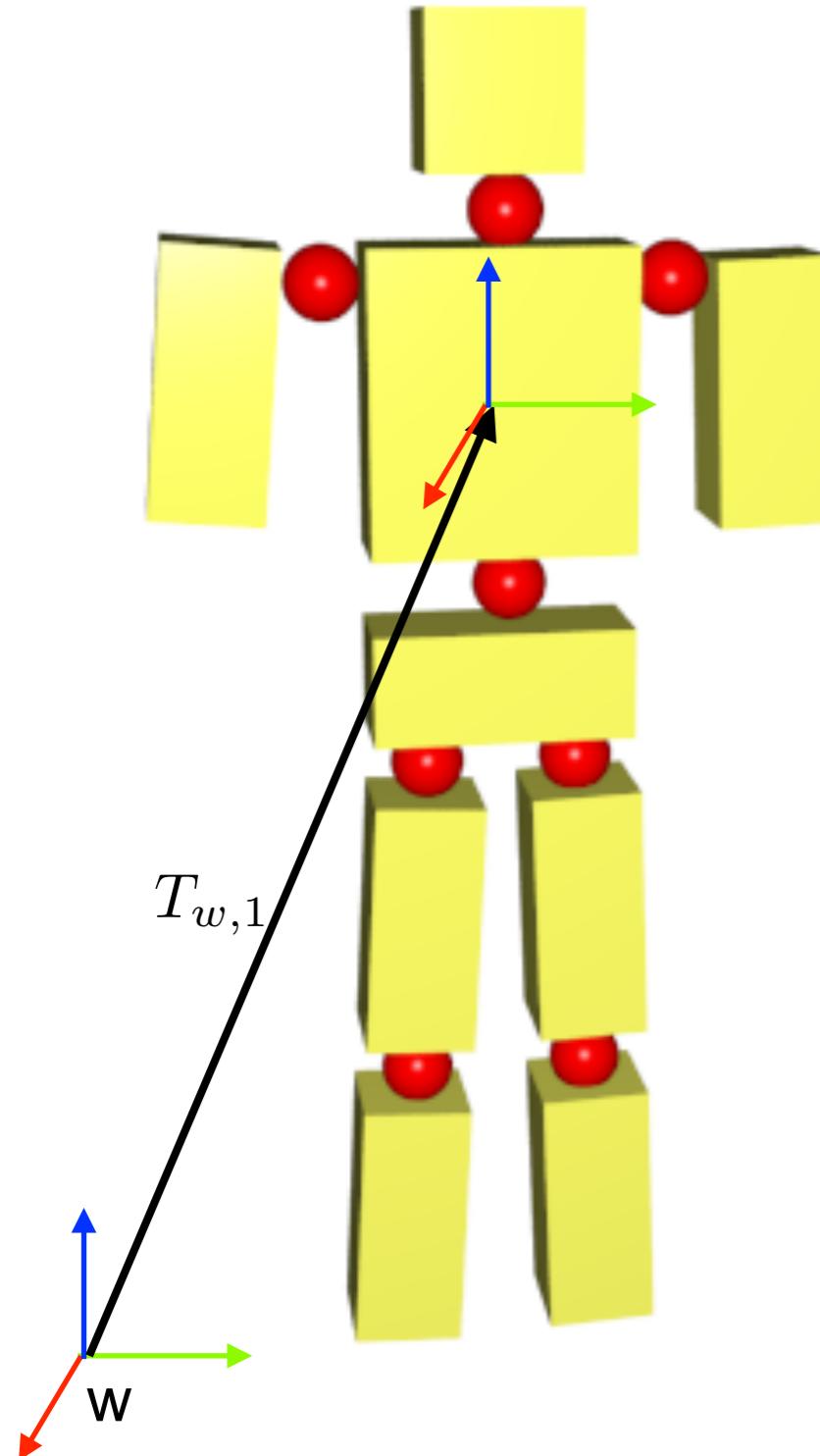
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$$\mathbf{p}'_1 = T_{w,1} \mathbf{p}_1$$

# Tree of objects

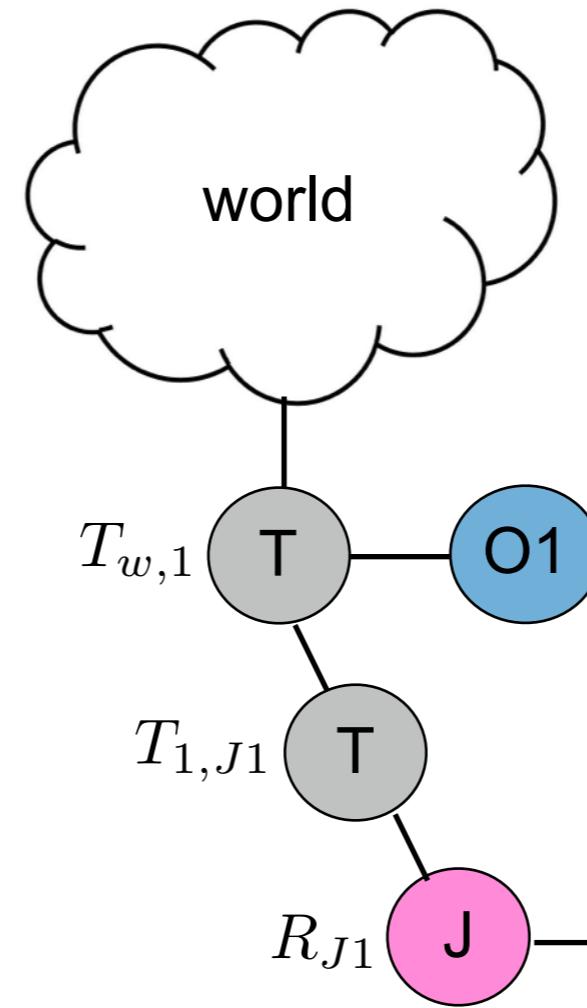
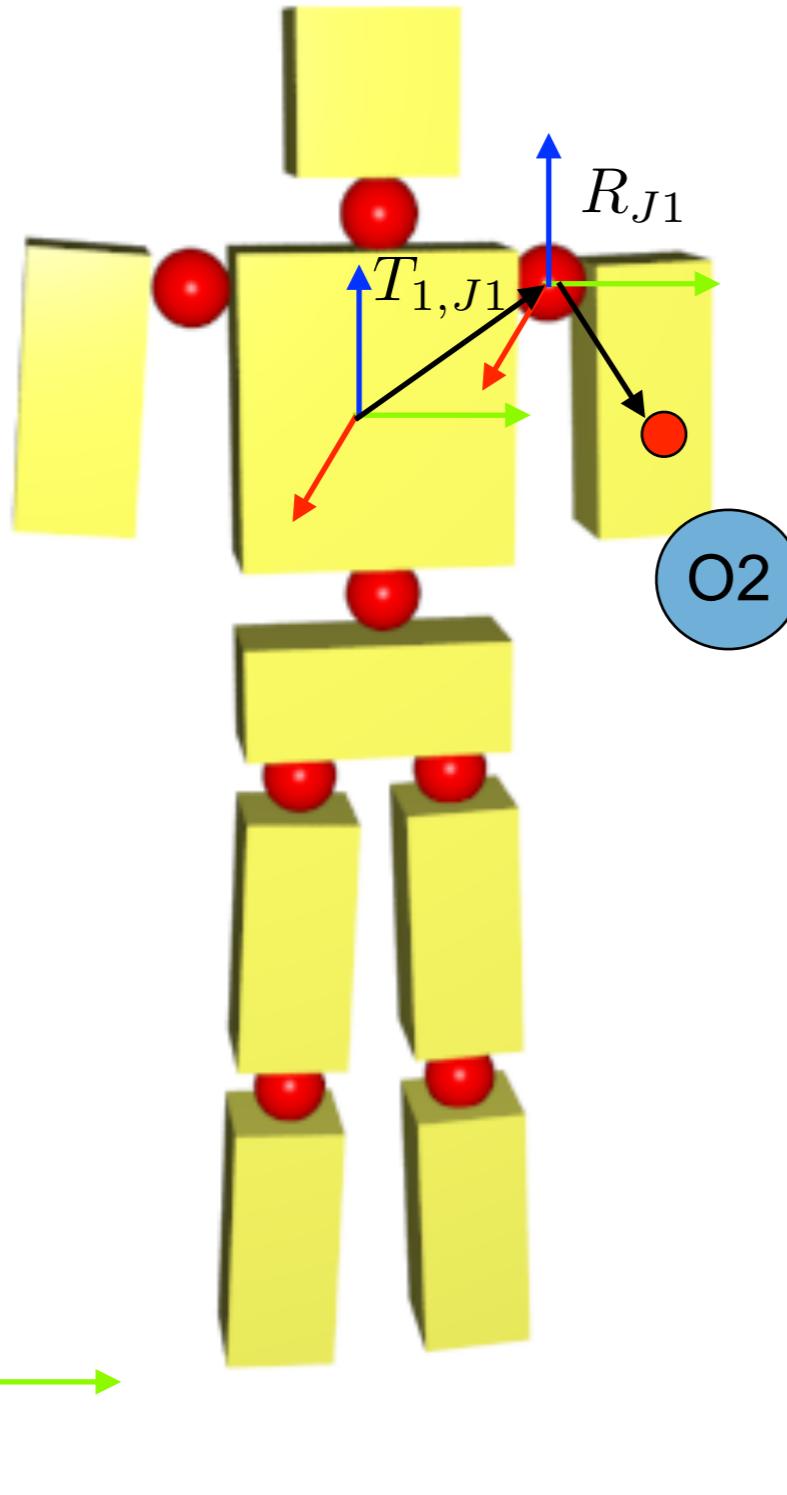
ARLAB



$$\mathbf{p}'_1 = T_{w,1} \mathbf{p}_1$$

# Tree of objects

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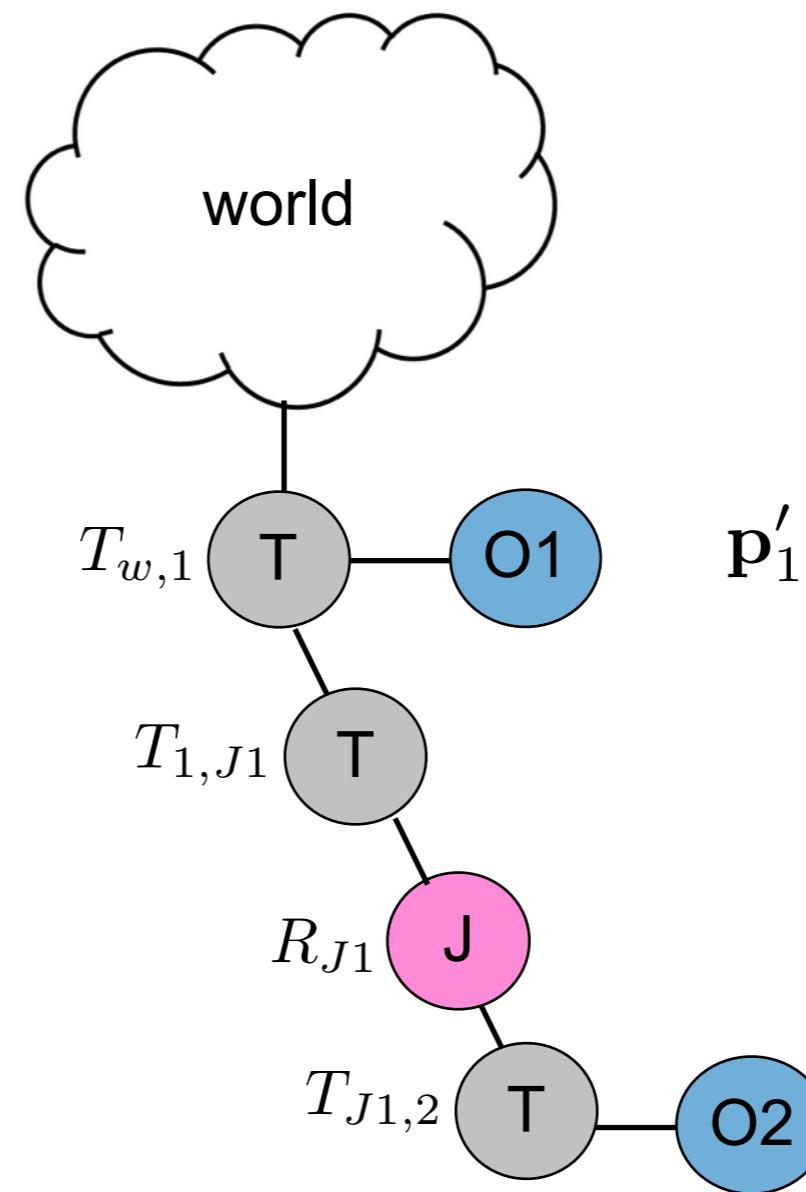
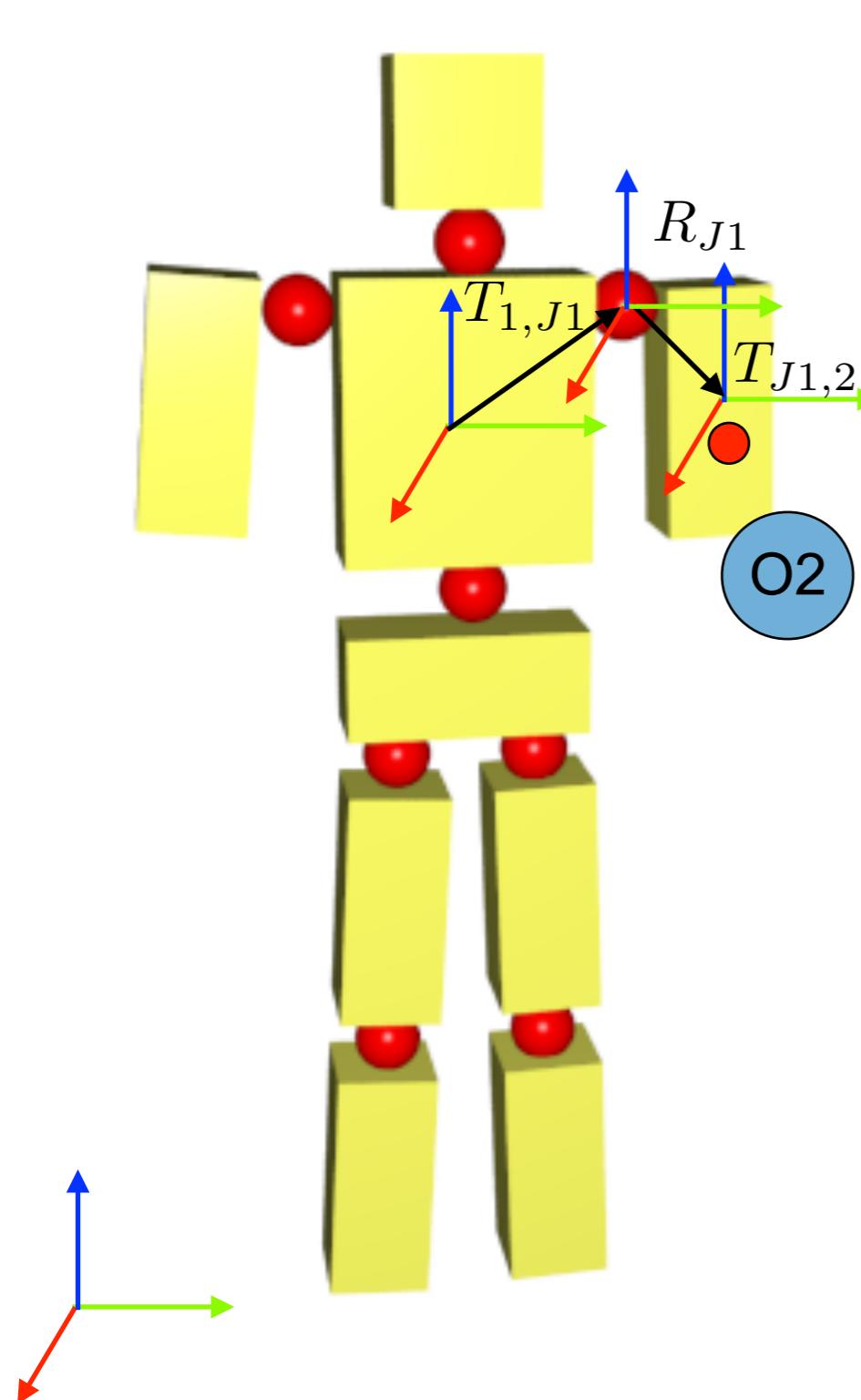
$$\mathbf{p}'_1 = T_{w,1} \mathbf{p}_1$$

$$\mathbf{p}'_2 = R_{J1} T_{1,J1} T_{w,1} \mathbf{p}_2$$

**Version 1: represent all point with respect to  $R_{J1}$**

# Tree of objects

ARLAB



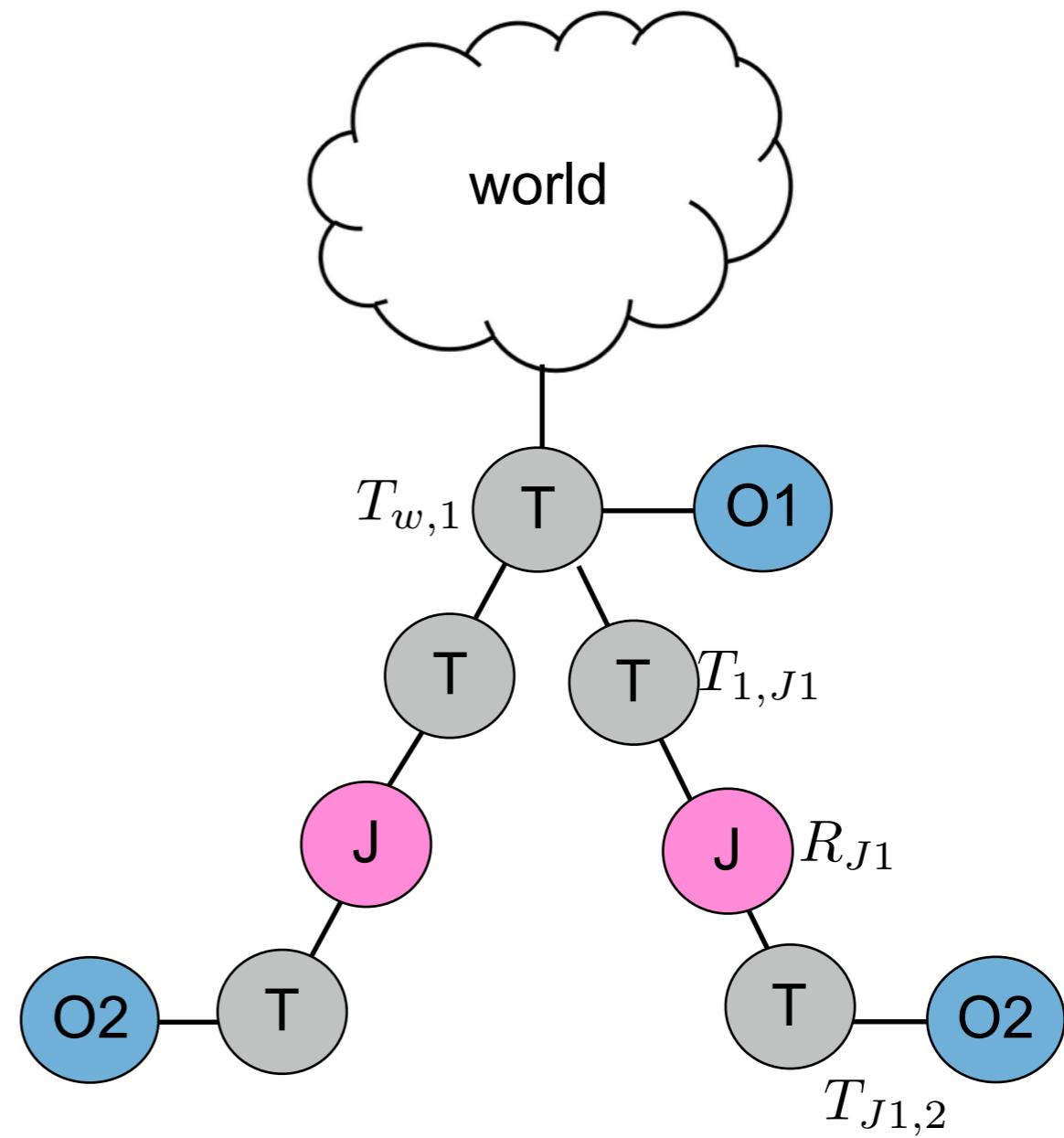
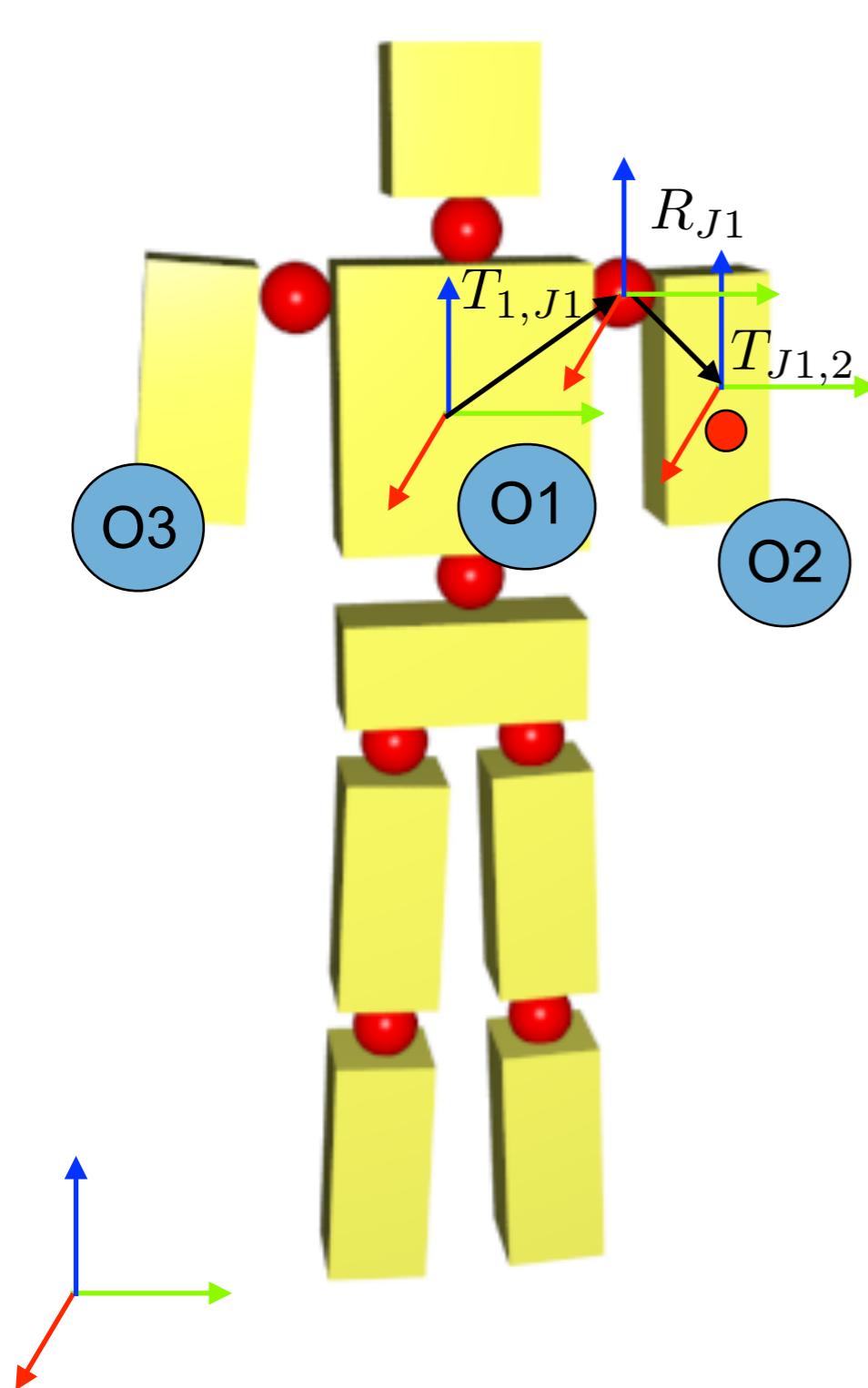
$$\mathbf{p}'_1 = T_{w,1} \mathbf{p}_1$$

$$\mathbf{p}'_2 = R_{J1} R_{1,J1} R_{w,1} T_{J1,2} \mathbf{p}_2$$

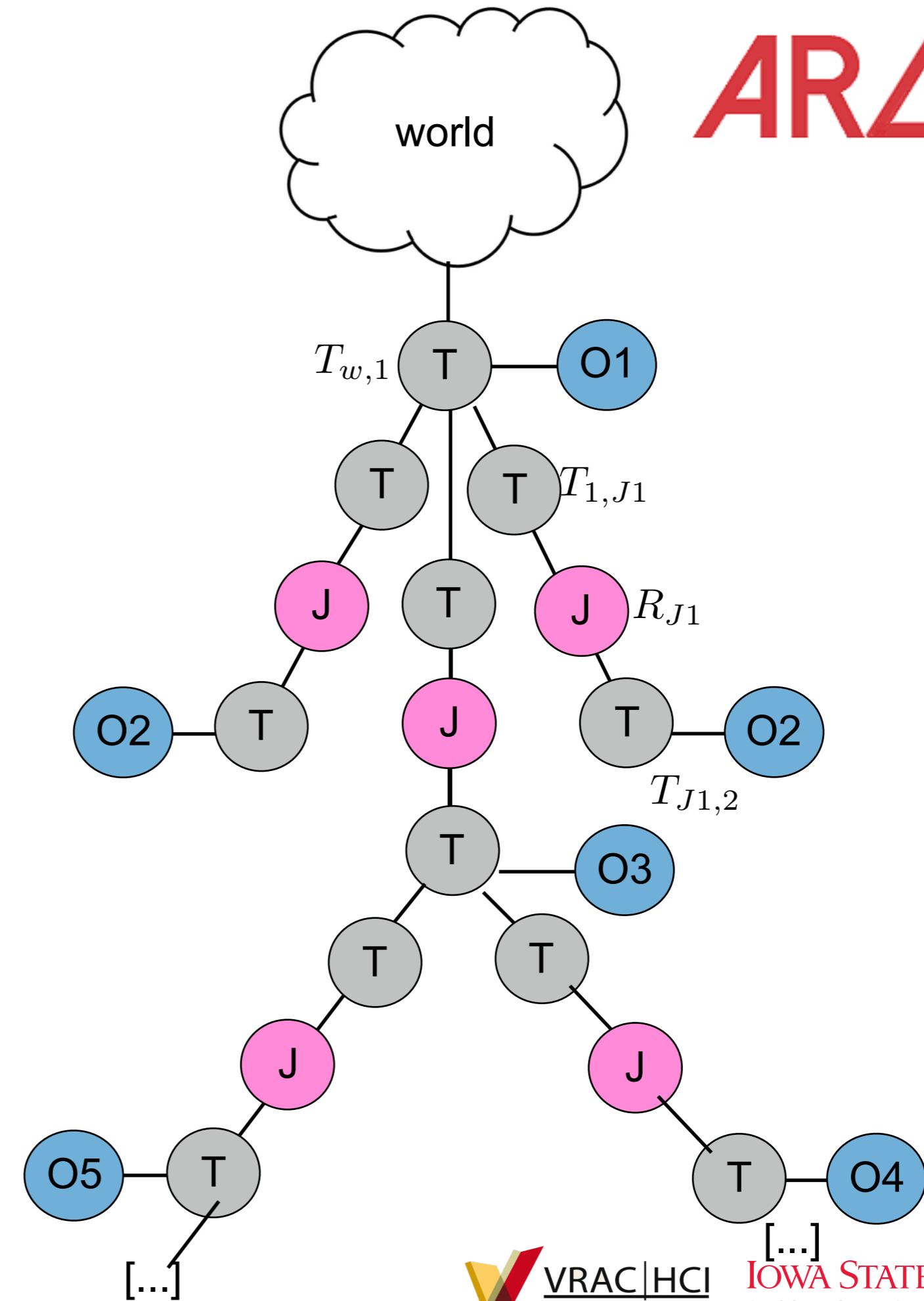
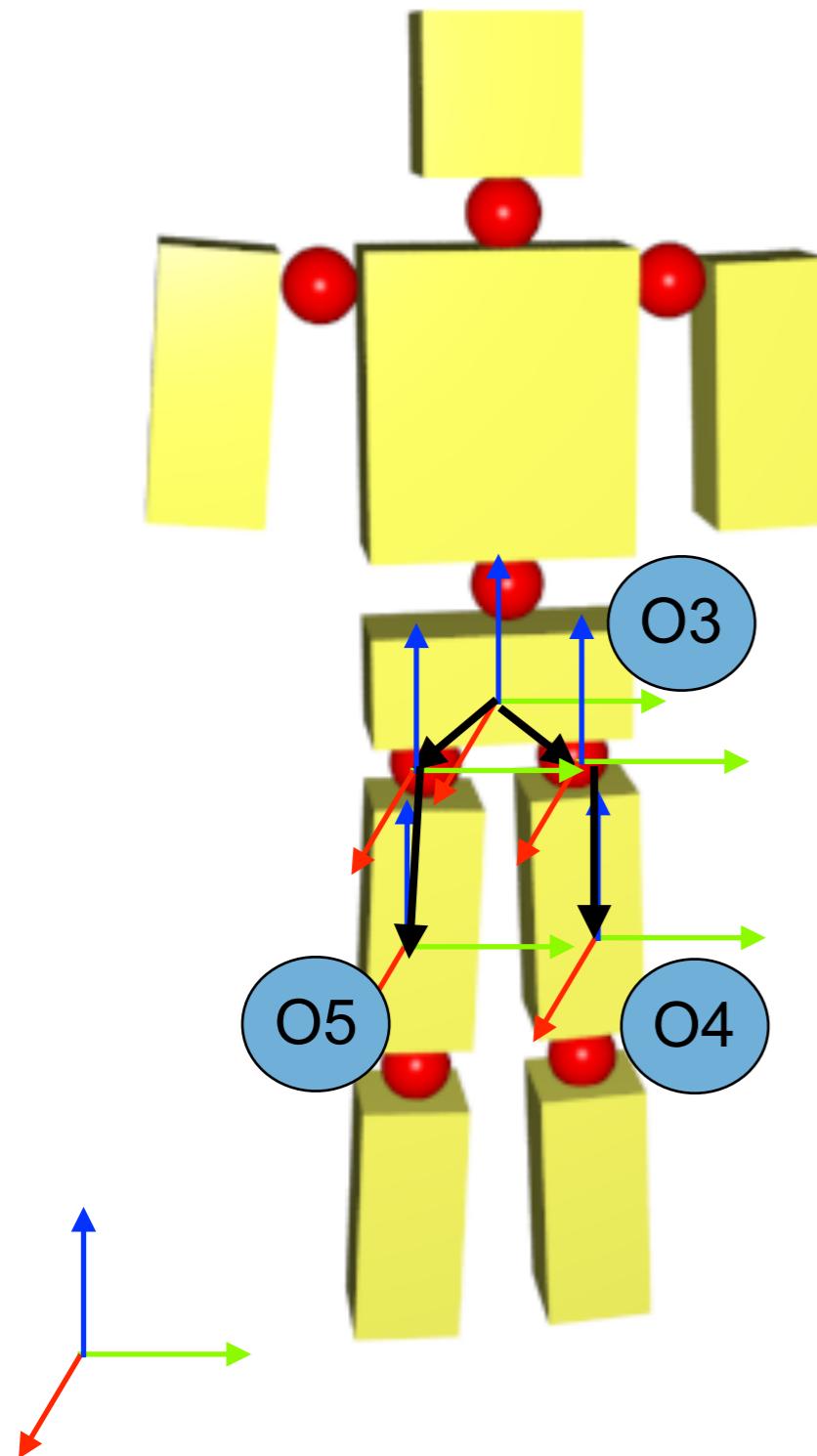
**Version 2: add an additional transformation and represent all point with respect to  $T_{J1,2}$**

# Tree of objects

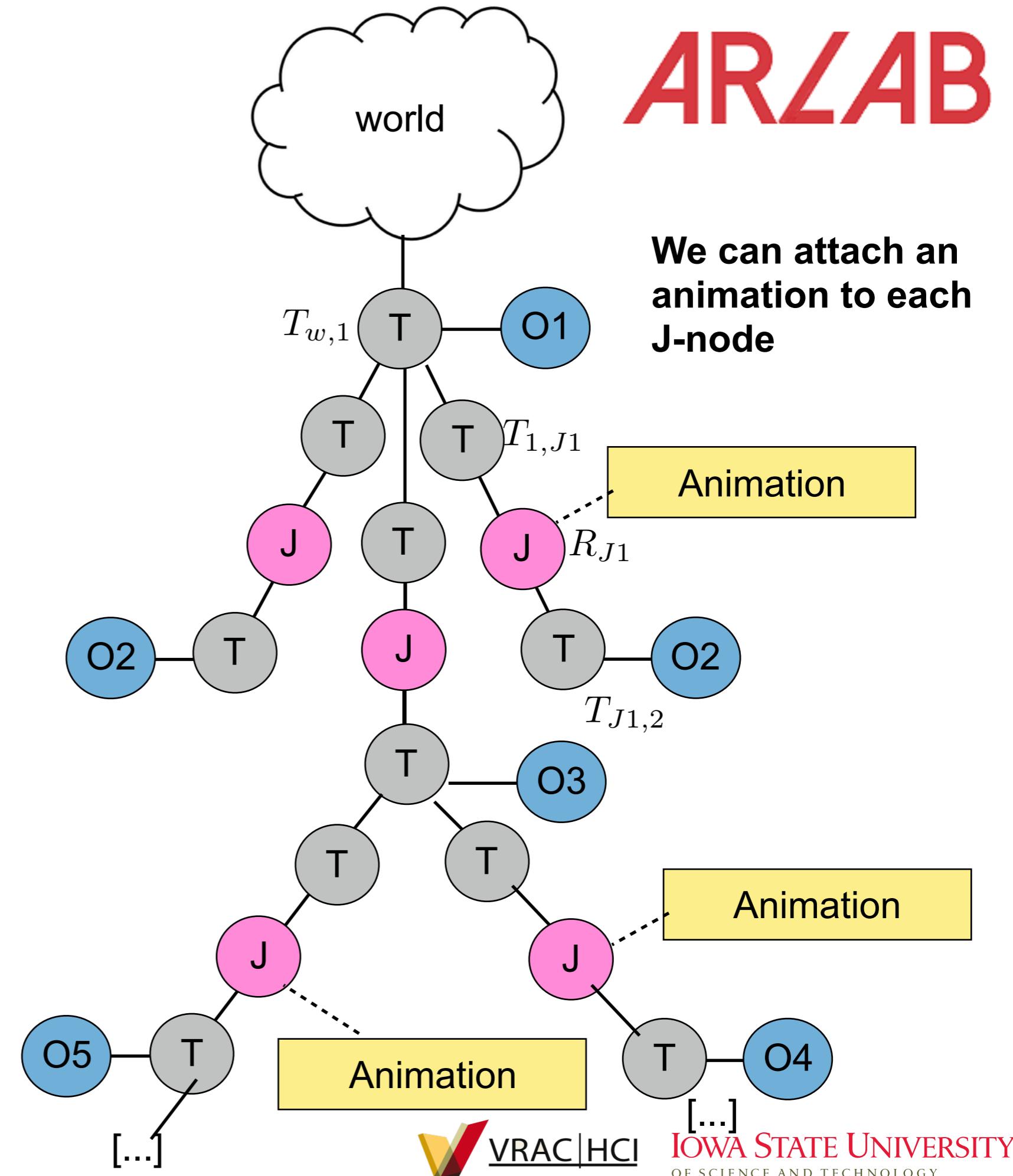
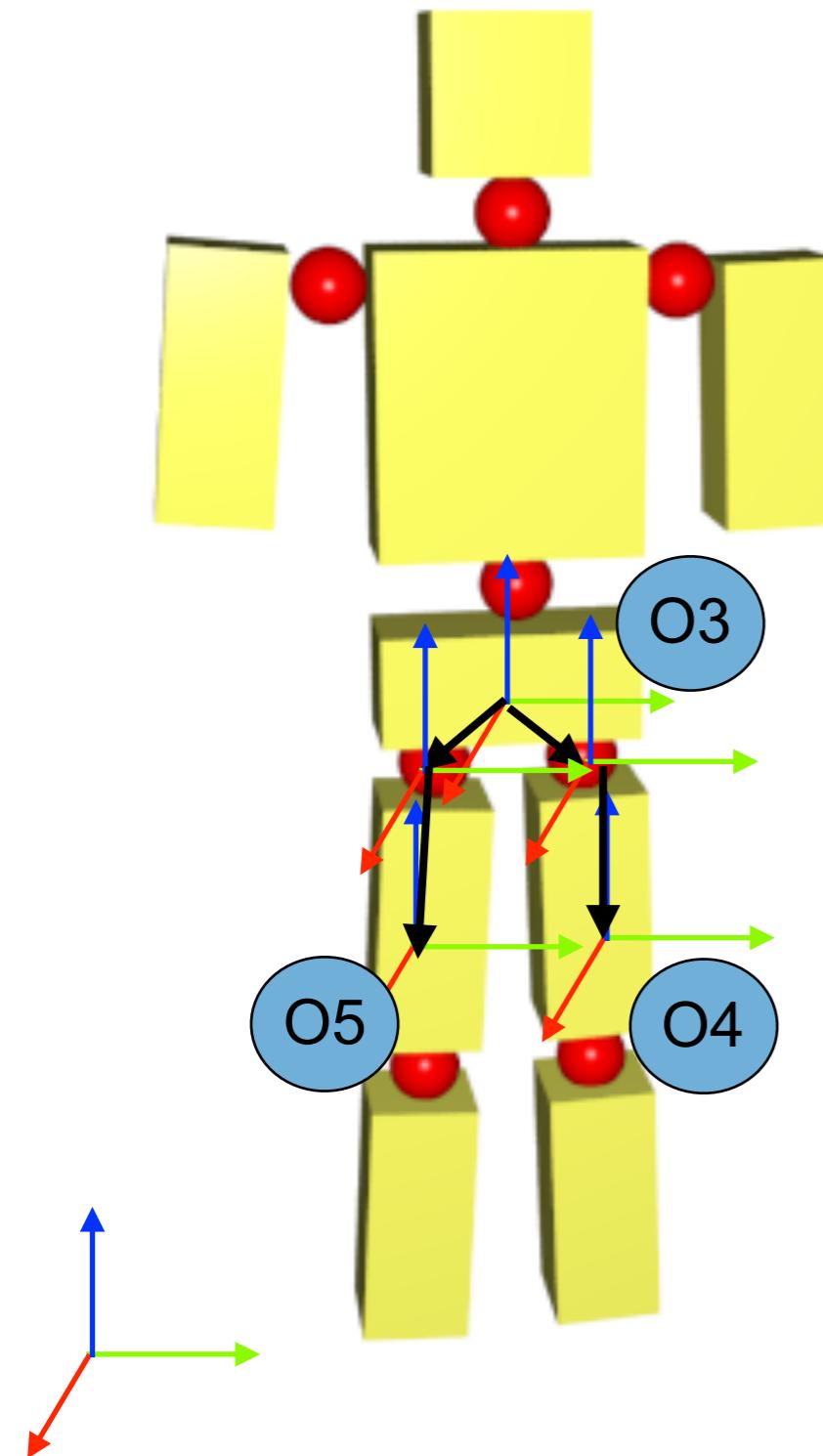
**ARLAB**



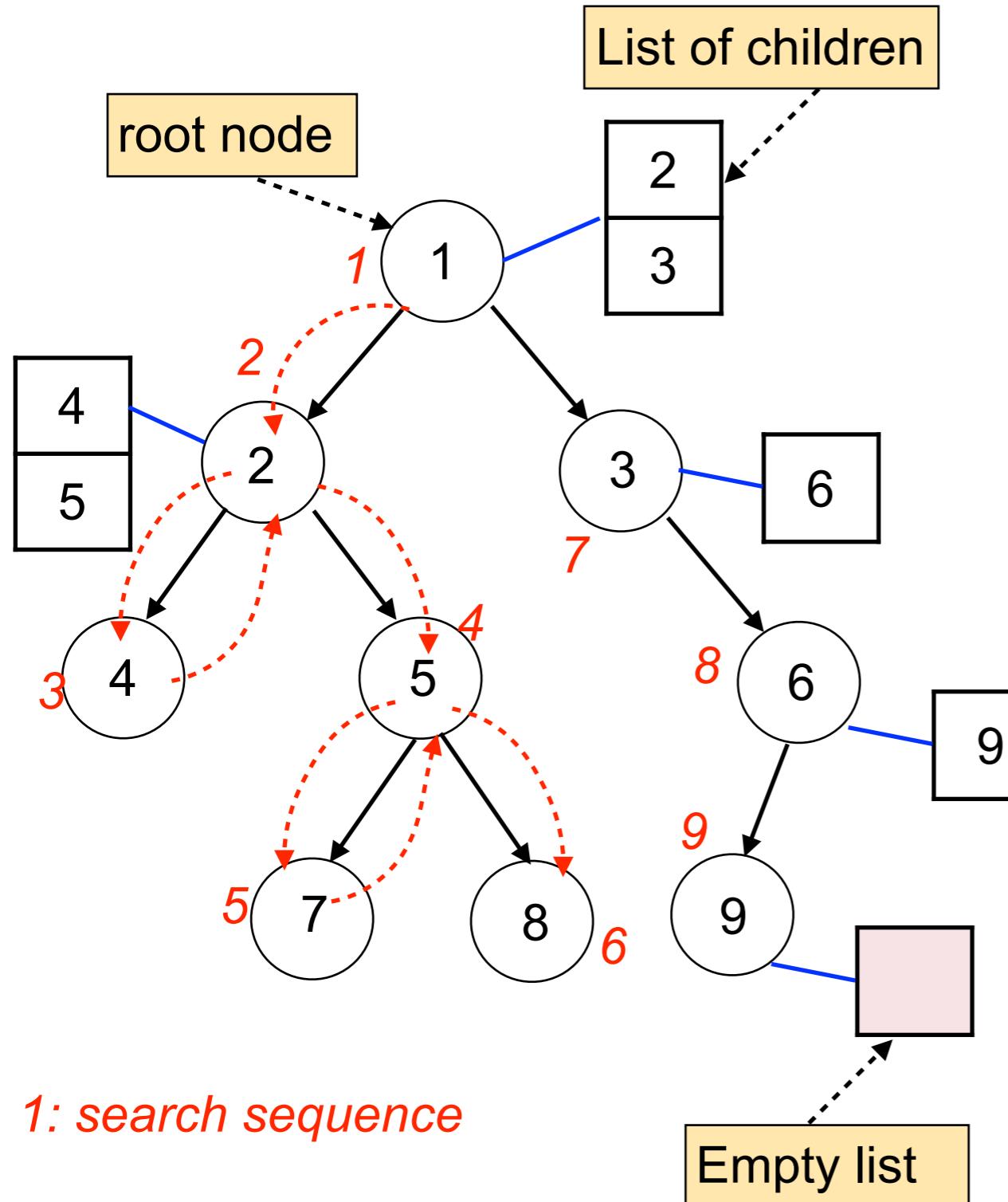
# Tree of objects



# Tree of objects



# Tree Traversal Operation



## Depth First Search

is an algorithm for traversing or searching tree data structures

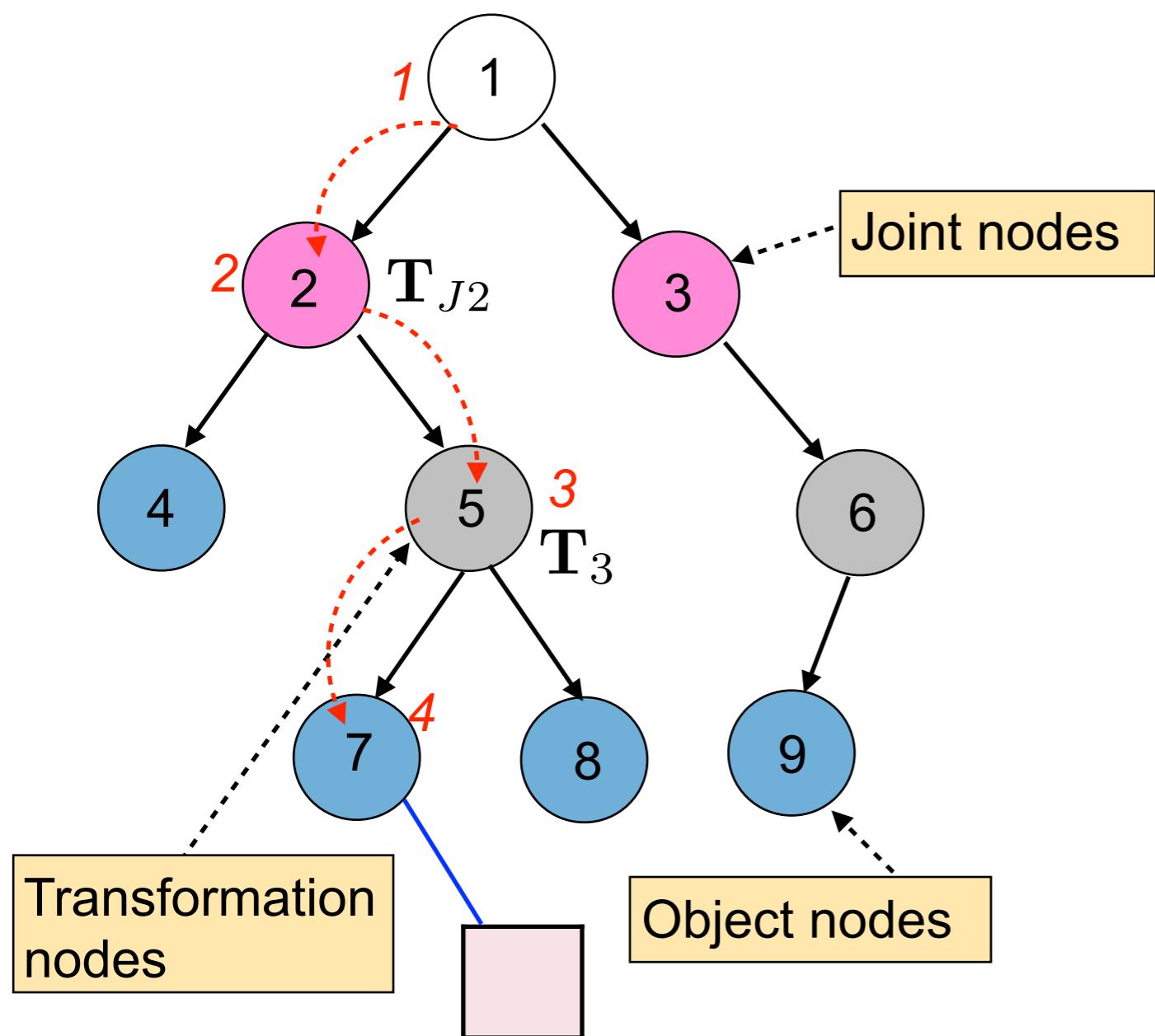
```
void traverse (Node& n)
{
    n-> do something

    int num_children = n.numChilds();

    for(int i=0; i< num_children; i++)
    {
        Node child = n->getChild(i);

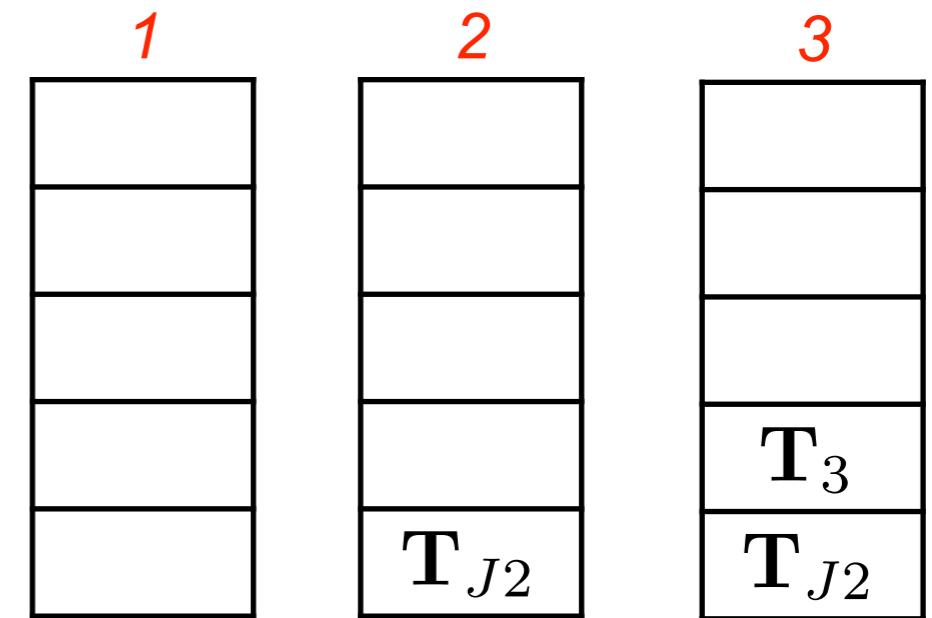
        traverse(child);
    }
}
```

# Tree Traversal Operation



Search for paths from root to empty child list

We can use a **stack** to remember the path.

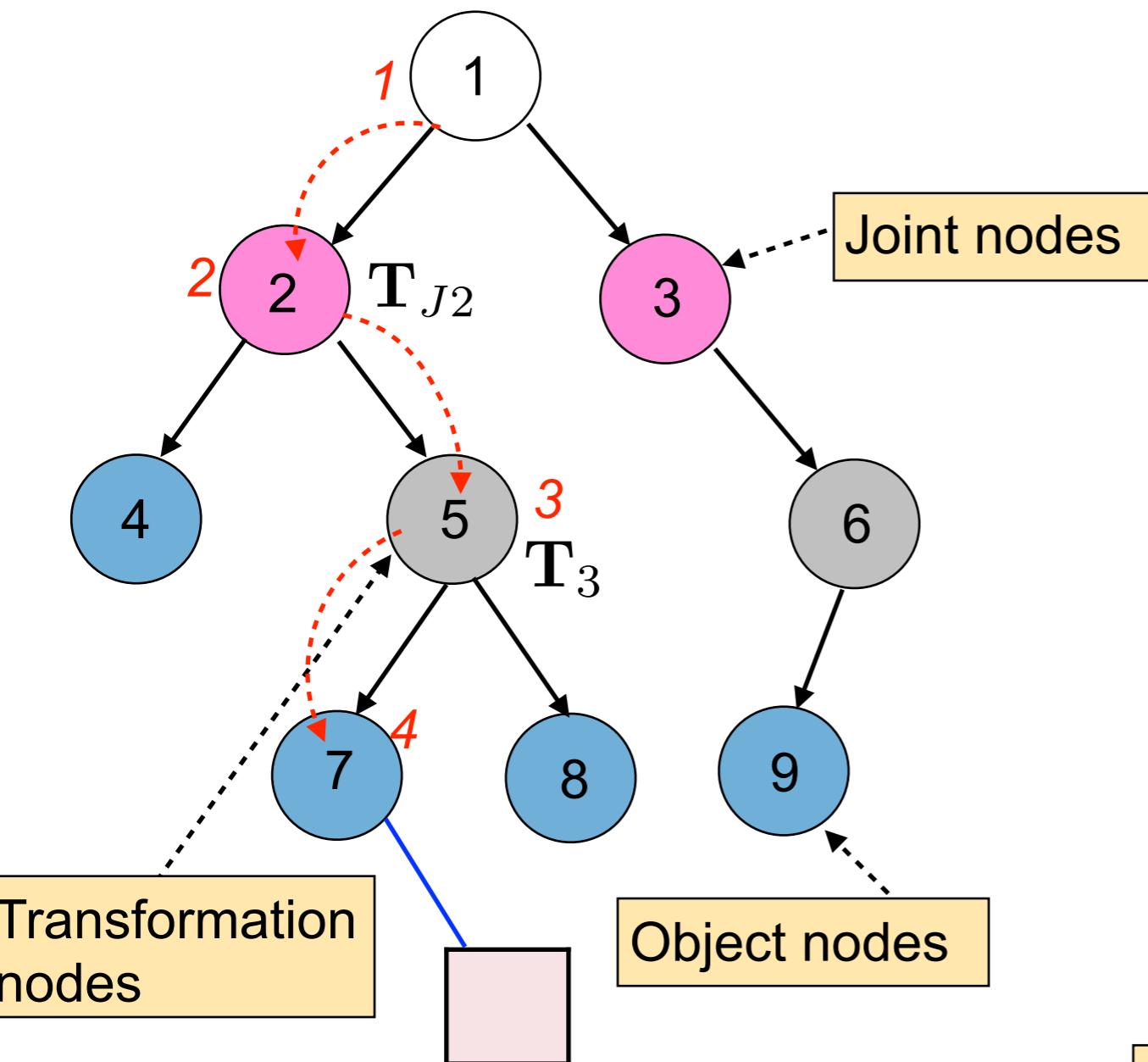


Every time, we reach an empty child list, we can accumulate the path.

$$p' = T_3 \ T_{J2} \ p$$

# Tree Traversal Operation

Search for paths from root to empty child list



```
void traverse (Node& n)
{
    //remember the path
    stack.add(transformation)

    int num_children = n.numChilds();
    for(int i=0; i< num_children; i++)
    {
        Node child = n->getChild(i);

        traverse(child);
    }

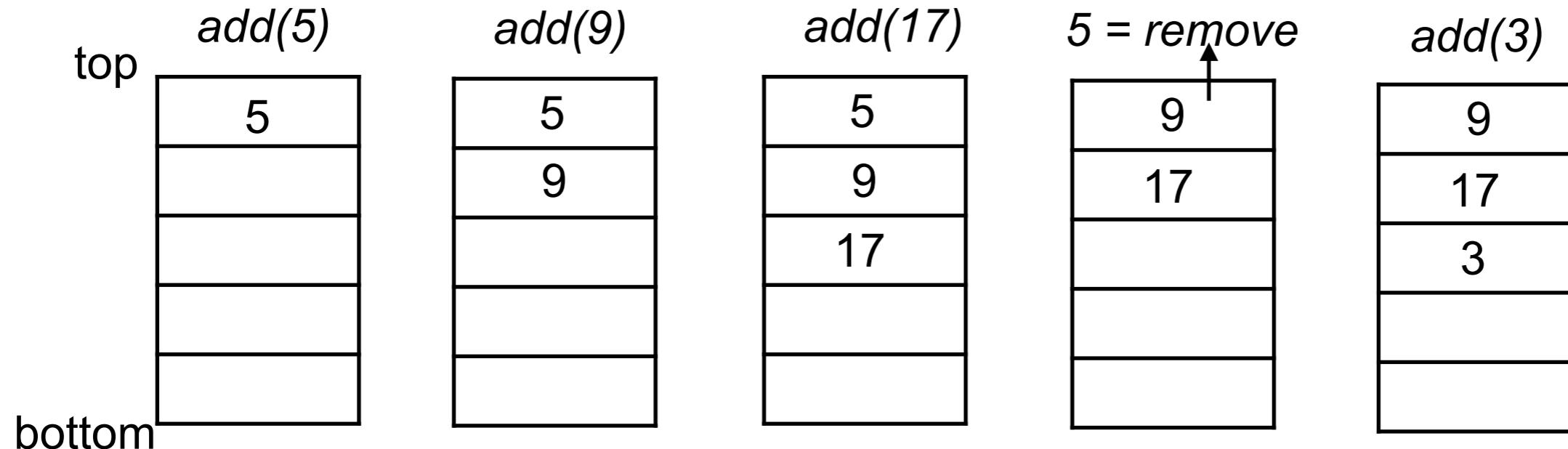
    stack.remove(transformation)
}
```

Pseudo code, the syntax does not work

# Stack and Queue

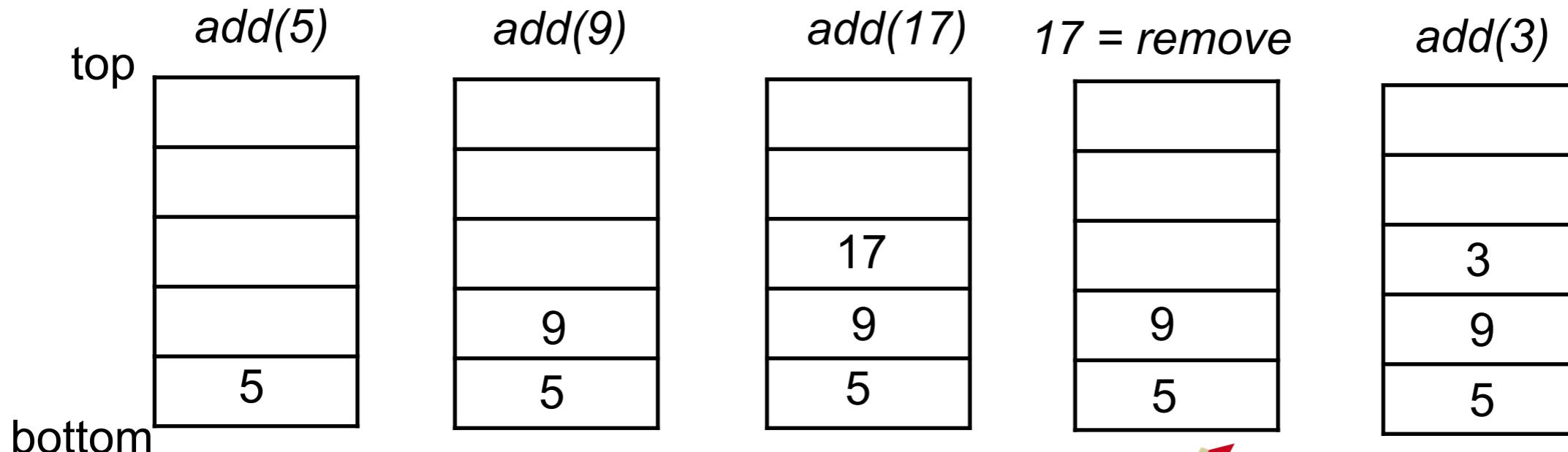
**Queues:** First-in-first-out

Elements are inserted at the bottom, but can only be removed from the top



**Stack:** Last-in-first-out

Elements are inserted at the top and can only be removed from the top



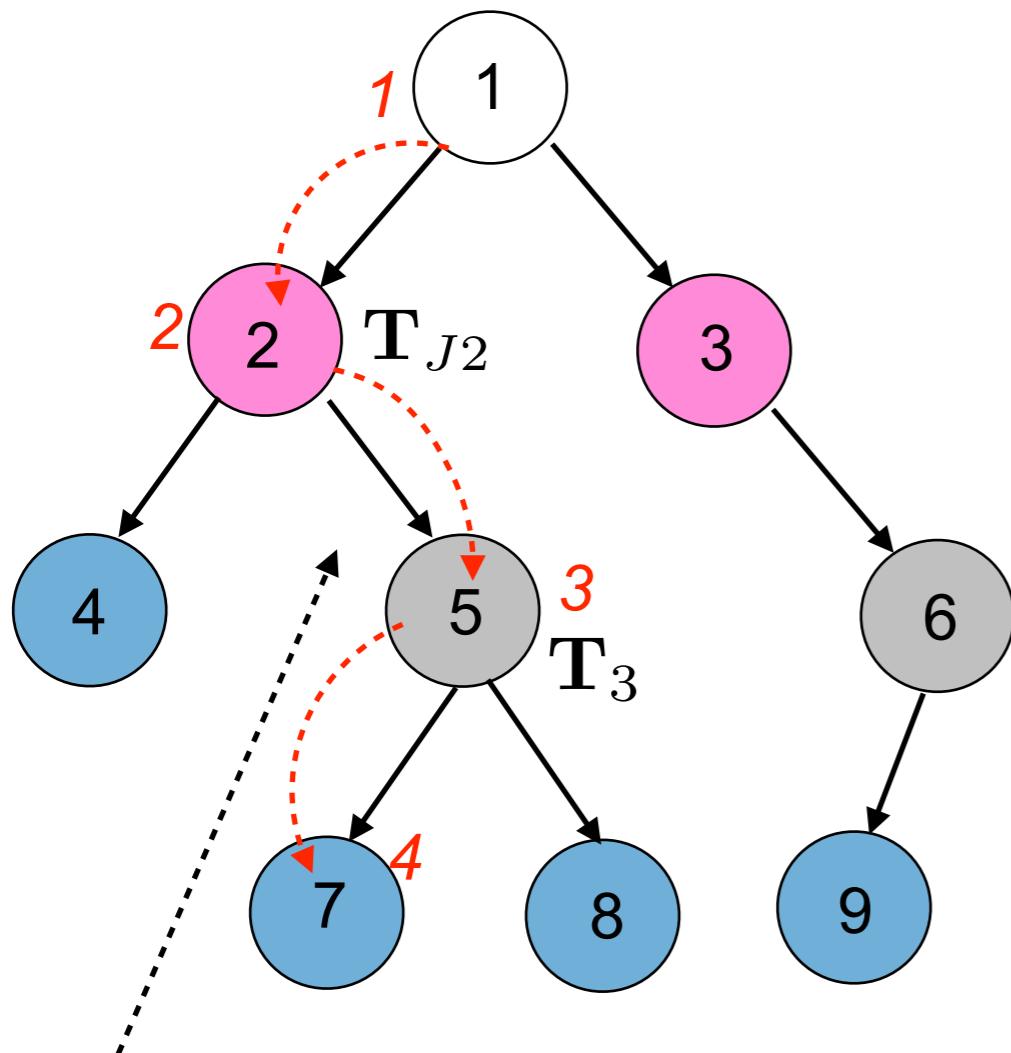
## Disadvantages:

- Requires a lot of programming and understanding of abstract data structures, recursion, search algorithms, etc. Be encouraged, if you like to do this (I bet, you all are) !!!

## Advantages:

- The new layer of abstractions (nodes and the tree structure) helps you to keep track of your objects in the scene, transformation, animations, etc.
- Almost all professional packages and open source graphics packages implement a hierarchical tree structure; so it is worth to understand how it works.
- We can extend this principle (node inheritance) to other graphics features such as light, material, transparency,

# Node Inheritance



Transformation is passed from parents to child nodes

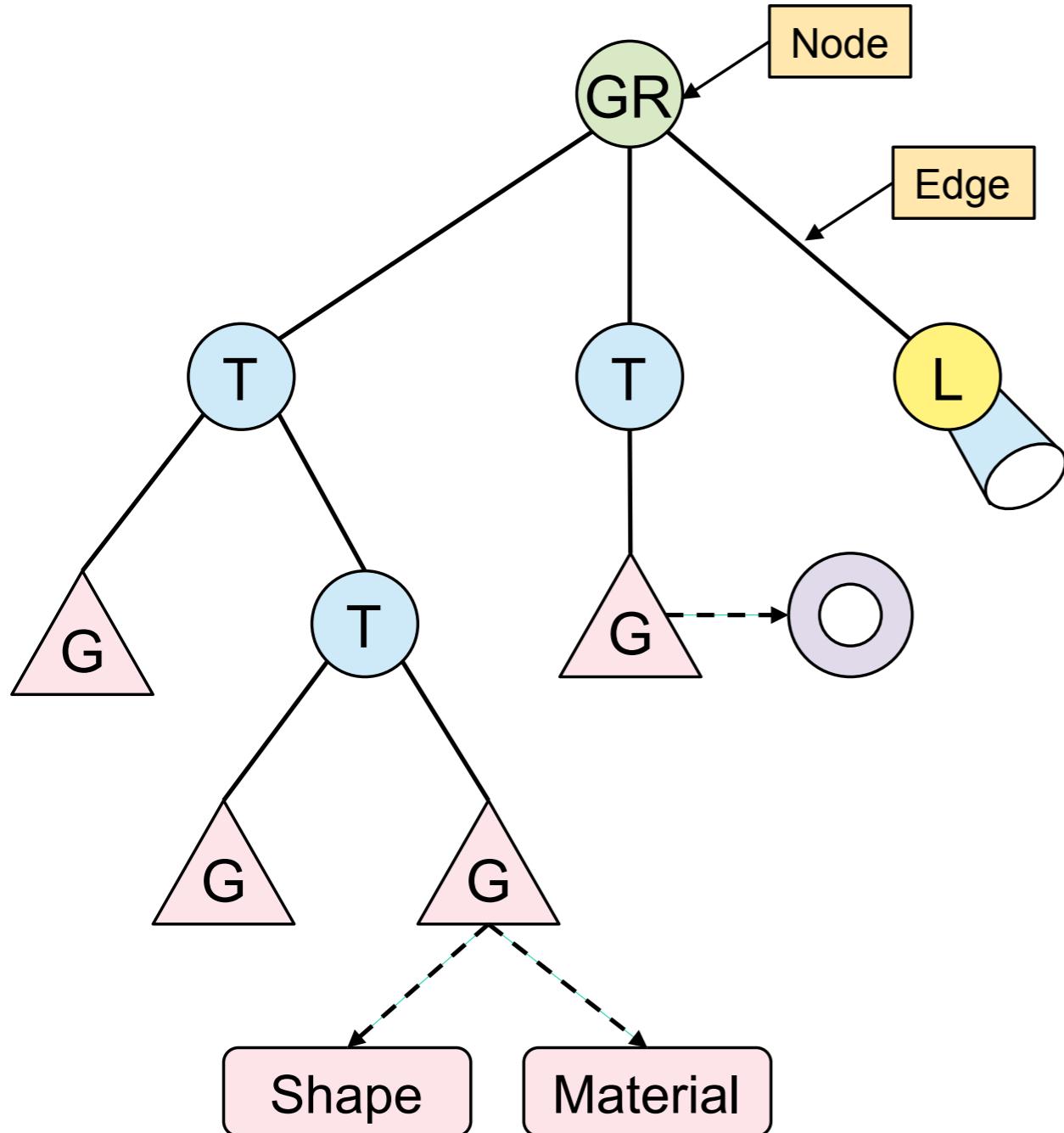
A node represents a graphics application property, i.e. transformation, light, etc.

The graph structure implements inheritance: **a parent passes its properties to its children.**



# Scenegraphs and Scenegraph APIs

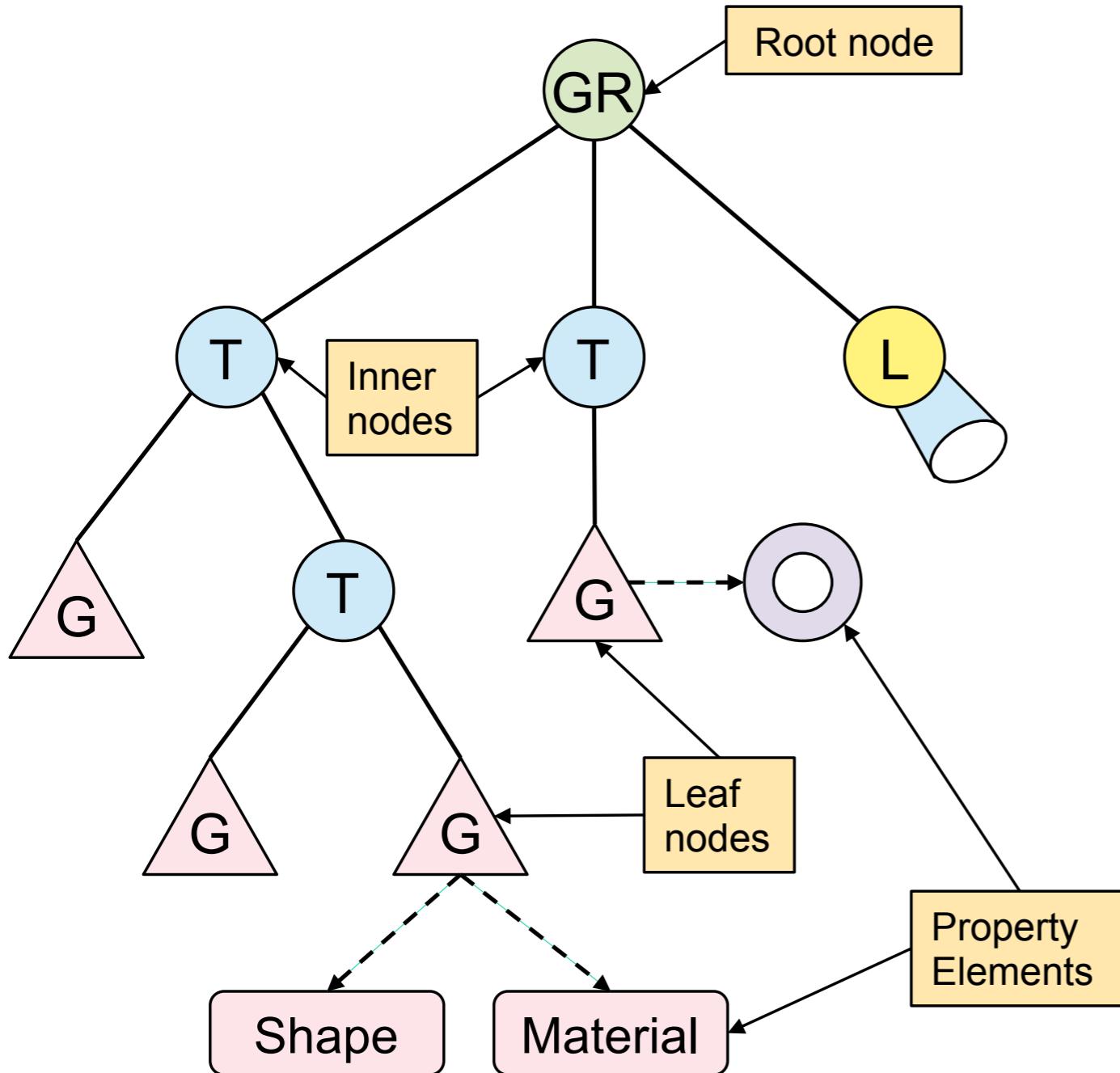
# What is a scenegraph?



A scene graph is a hierarchical data structure that facilitates the organization and the optimization of a 3D scene. It is represented by a tree structure (Direct Acyclic Graph). Its nodes represent scene elements, the edges between the nodes represent associations between the nodes that help to structure the scene.

*Schematic representation of a scene graph*

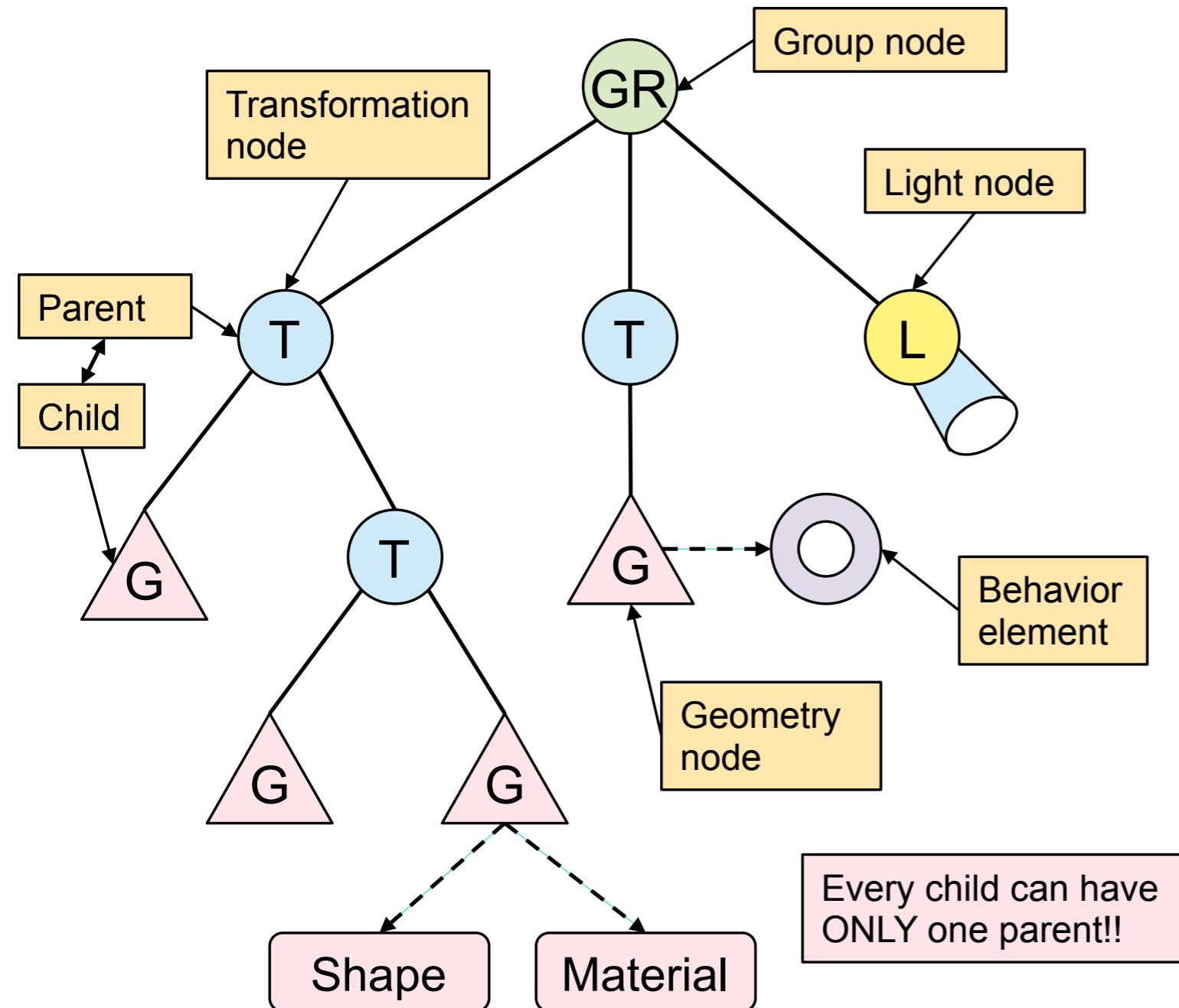
# Scenegraph Node Types



*Schematic representation of a scene graph*

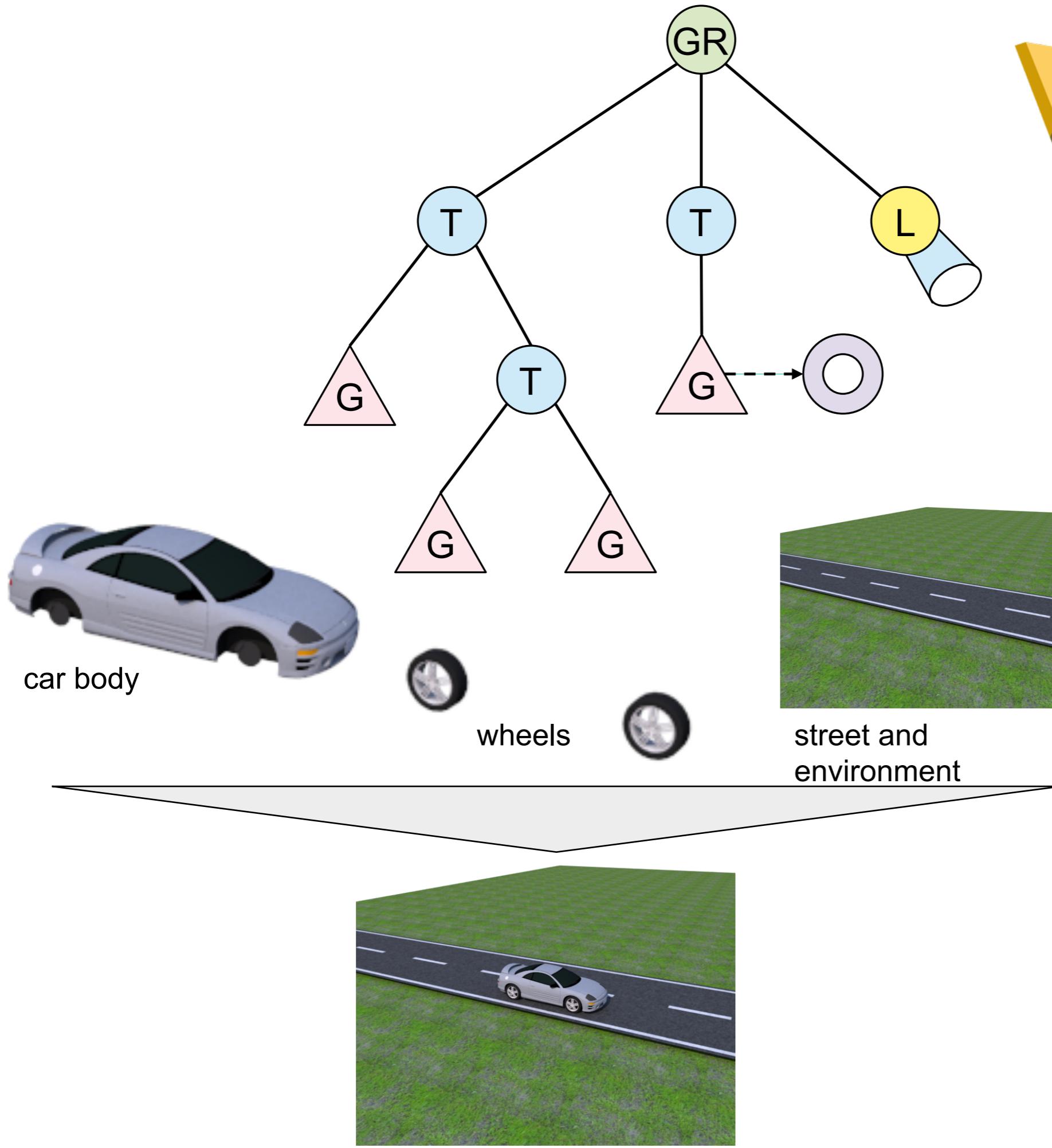
- Root node: this is the start node of every scene graph. It keeps "the entire scene."
- Leaf nodes represent geometry to render (e.g., 3D models). They do not accept further child nodes.
- Inner nodes represent relations between nodes, which are mainly used to structure the scene, e.g., transformations.
- Property elements describe the appearance and the behavior. They are not scene graph nodes.

# Scenegraph Nodes



- **GR** A Group node is used to structure the scene and to join multiple nodes to one logical unit.
- **T** A Transformation nodes represents a transformation matrix.
- **G** A Geometry node keeps OpenGL primitive information, thus, it can be used to represent 3D or 2D models.
- **L** A light node represents the OpenGL light sources.

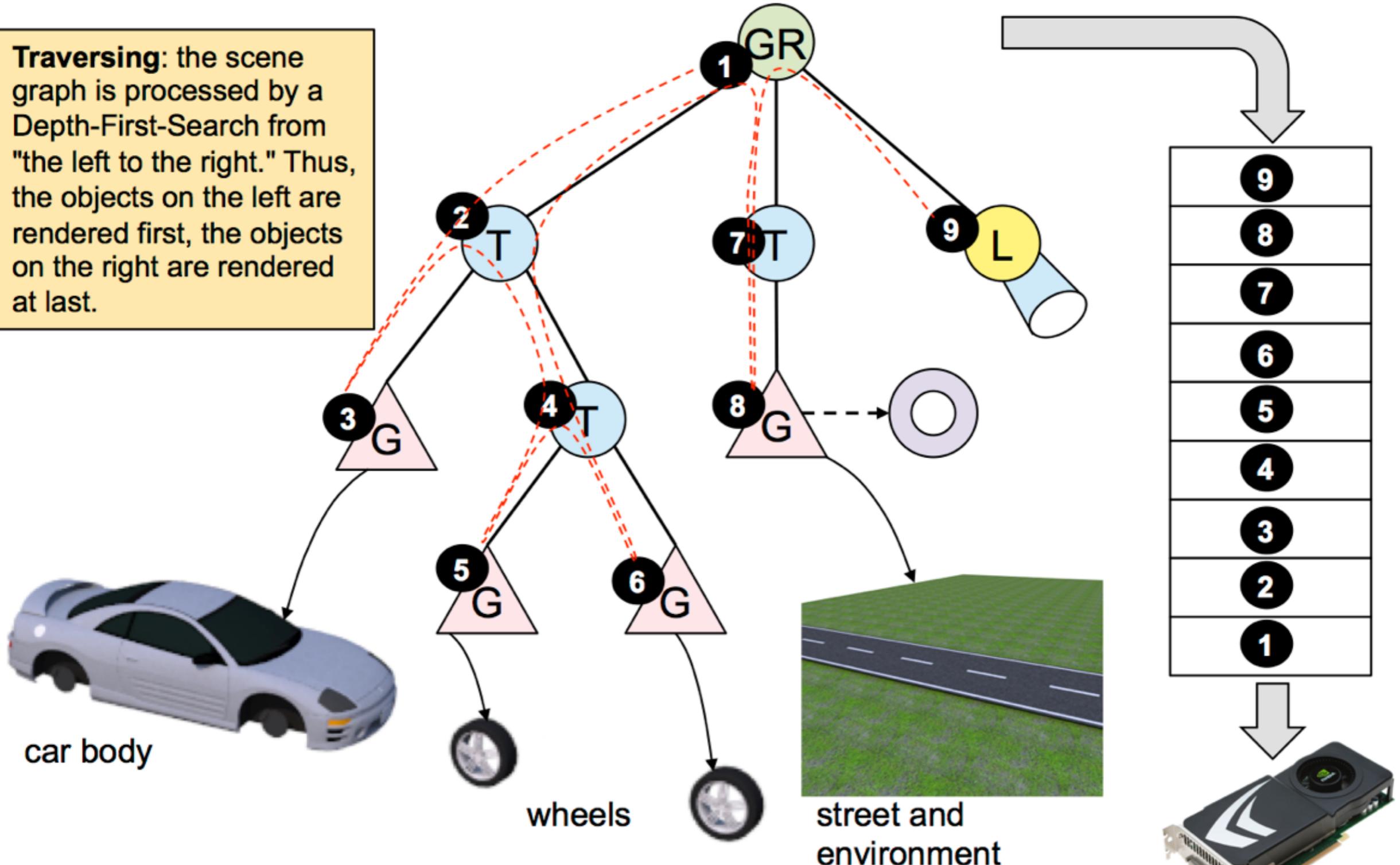
*Schematic representation of a scene graph*



# Traversing a Scenegraph



**Traversing:** the scene graph is processed by a Depth-First-Search from "the left to the right." Thus, the objects on the left are rendered first, the objects on the right are rendered at last.



# OpenSceneGraph



OpenSceneGraph is an open source 3D graphics programming toolkit that can be used for a vast amount of 3D applications.

It provides functions to

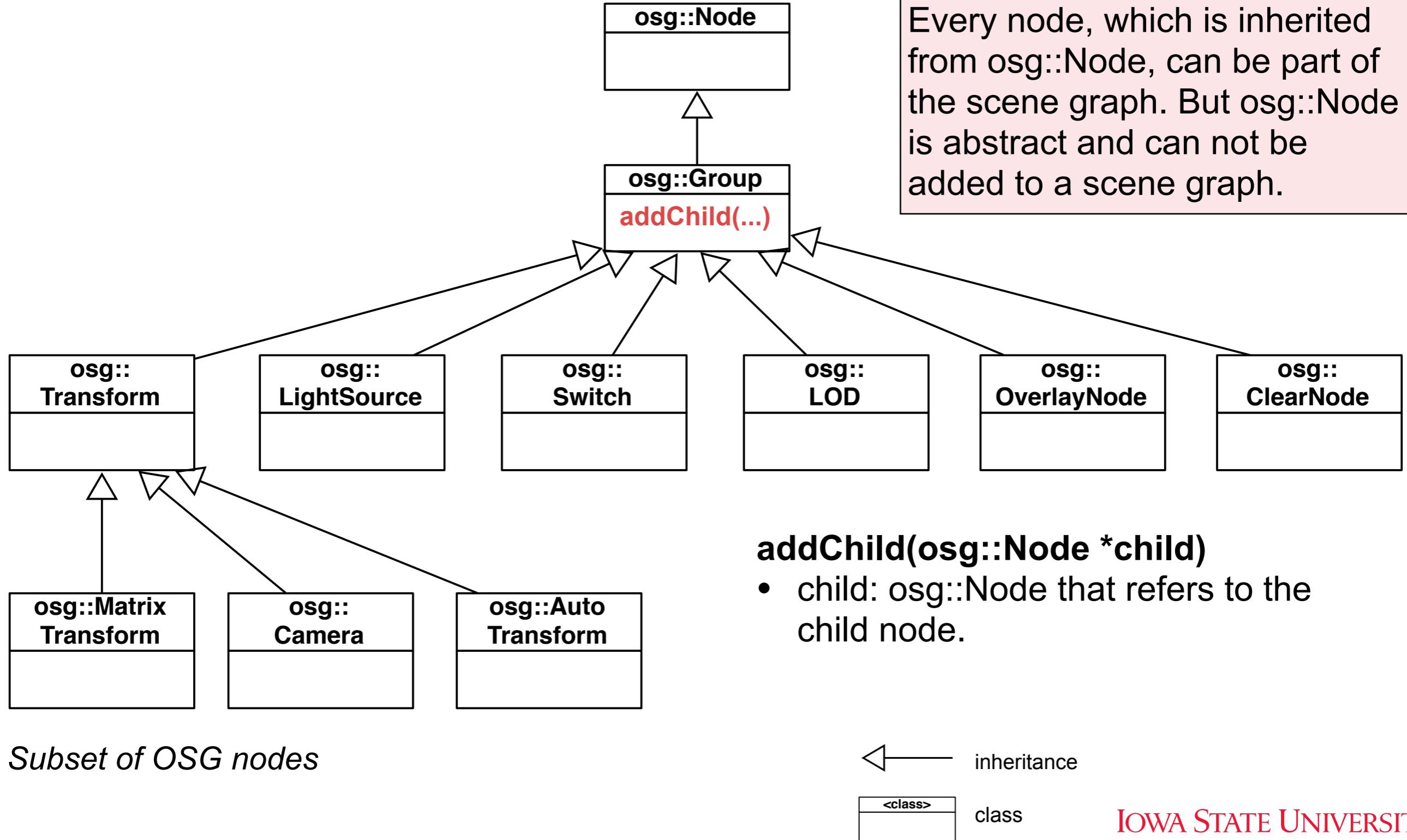
- build a scene graph
- loading and writing 3D models / images
- animation framework
- effects like environment mapping, shadows, particles.
- scene graph optimization
- interaction functions (e.g., Ray Intersection Test)
- basic collision detection.
- C++, Object Oriented Programming

<http://www.openscenegraph.com>

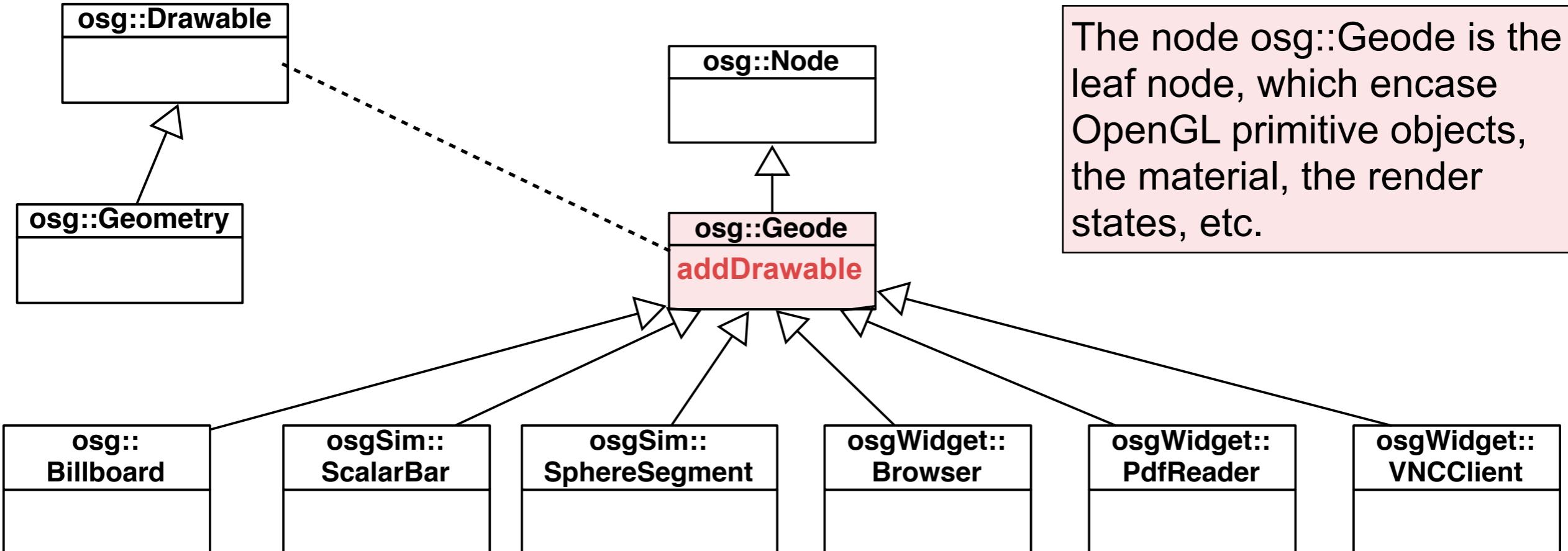


SITY

# Node Hierarchy



# Geometry Nodes



Add a Drawable to the Geode.

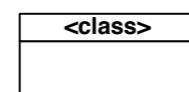
**bool addDrawable (Drawable \*drawable)**

- `drawable`: a geometry object of type `osg::Drawable`

The node `osg::Geode` is the leaf node, which encase OpenGL primitive objects, the material, the render states, etc.

The class `osg::Drawable` stores OpenGL primitives. It cannot be part of the scene graph and need to be associated with an `osg::Geode` object.

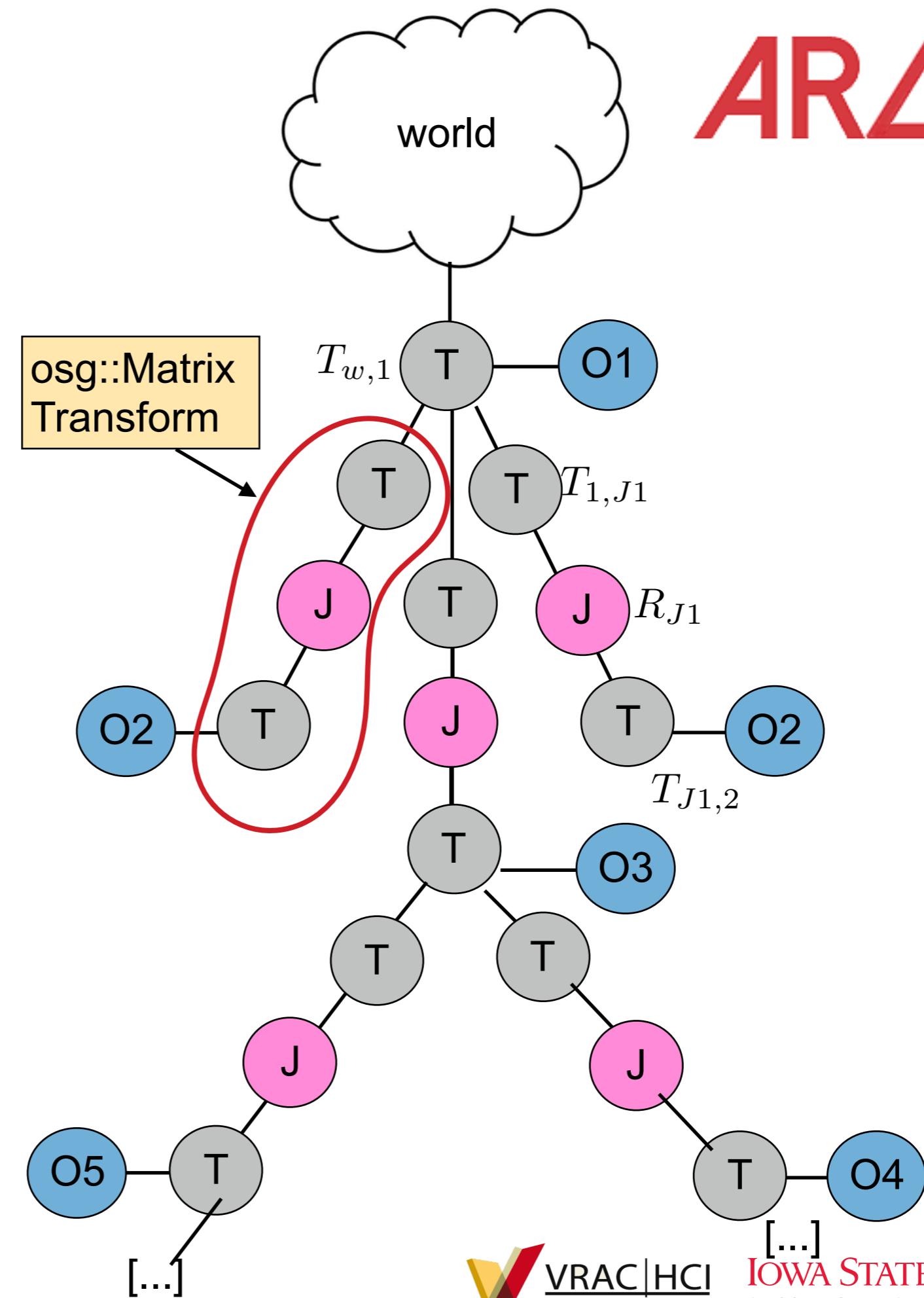
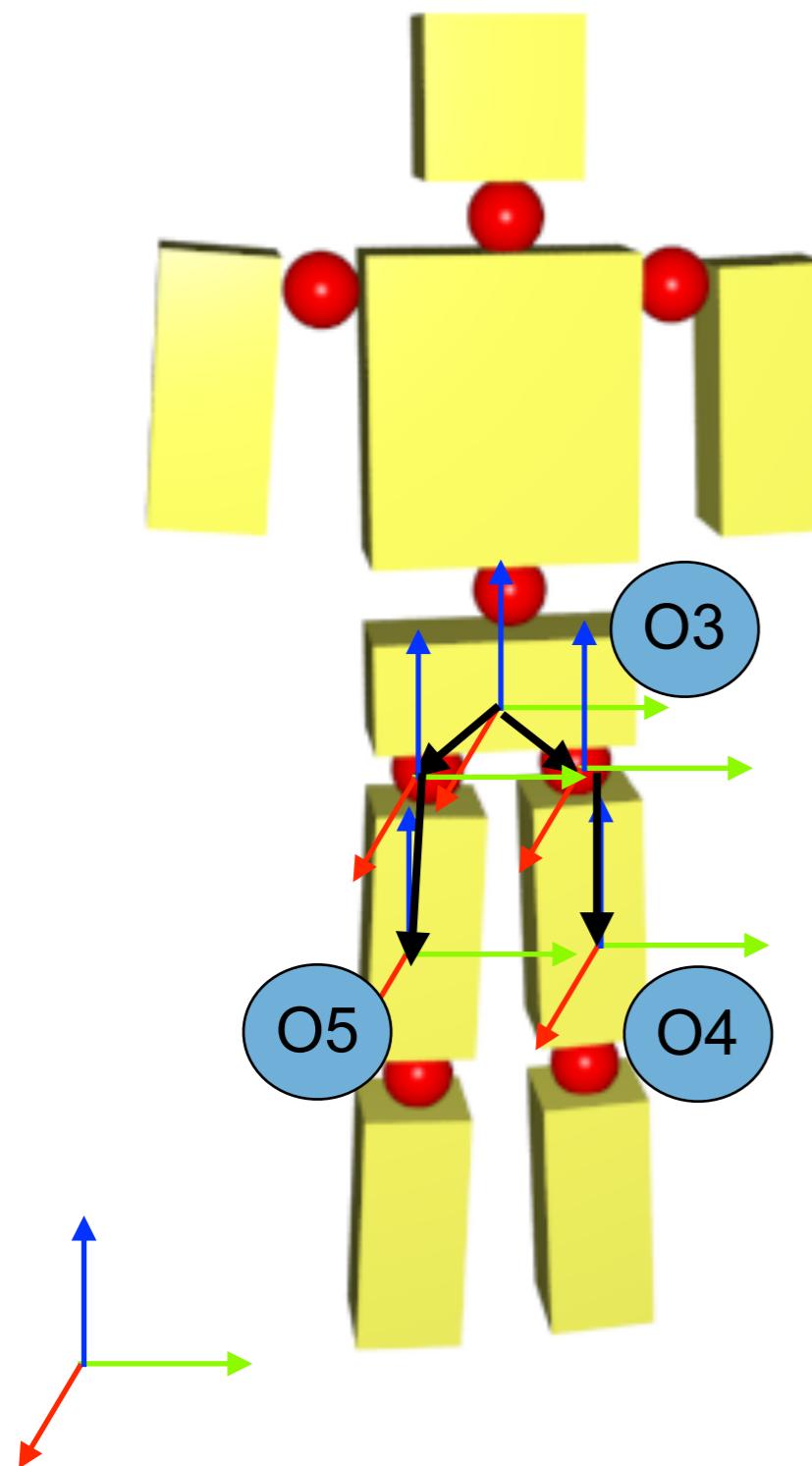
← inheritance



class

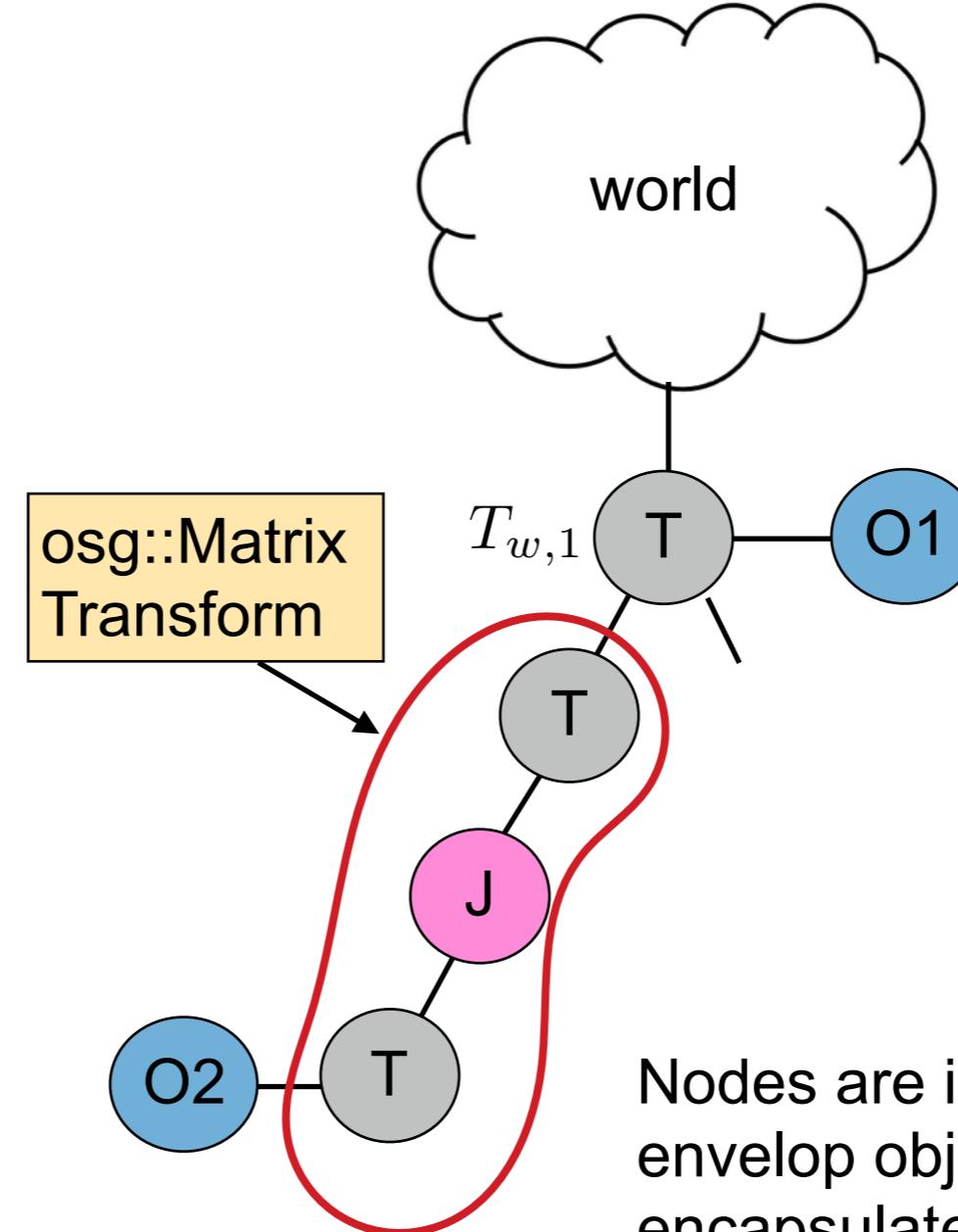
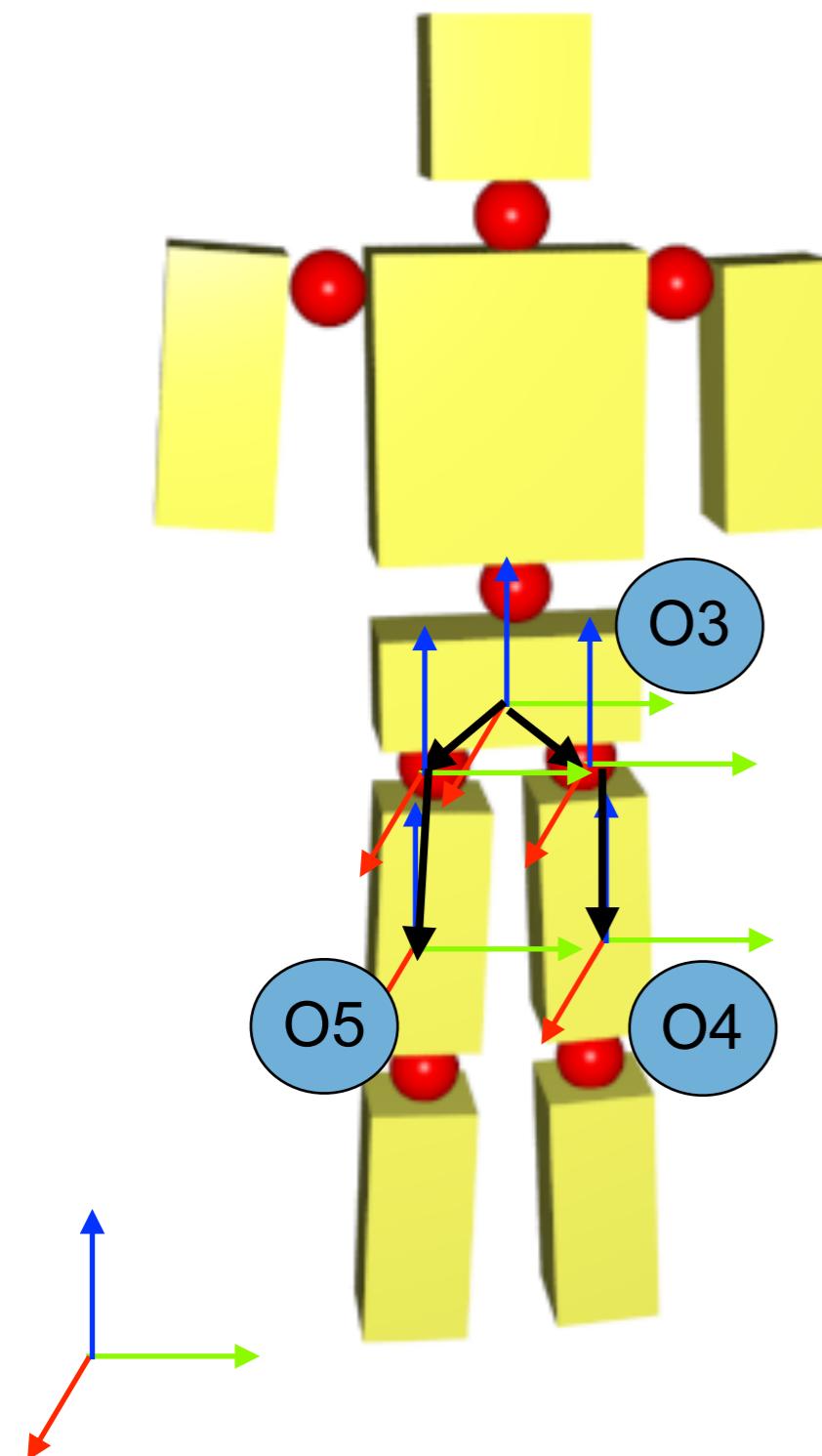
# Tree of objects

ARLAB



# Tree of objects

ARLAB



Nodes are implemented as envelop objects which encapsulate the graphics objects along with all graphics properties. The nodes do not implement the graphics properties!

Distinguish between objects that do graphic and objects that implement the scene graph.

# Scenegraph Optimization

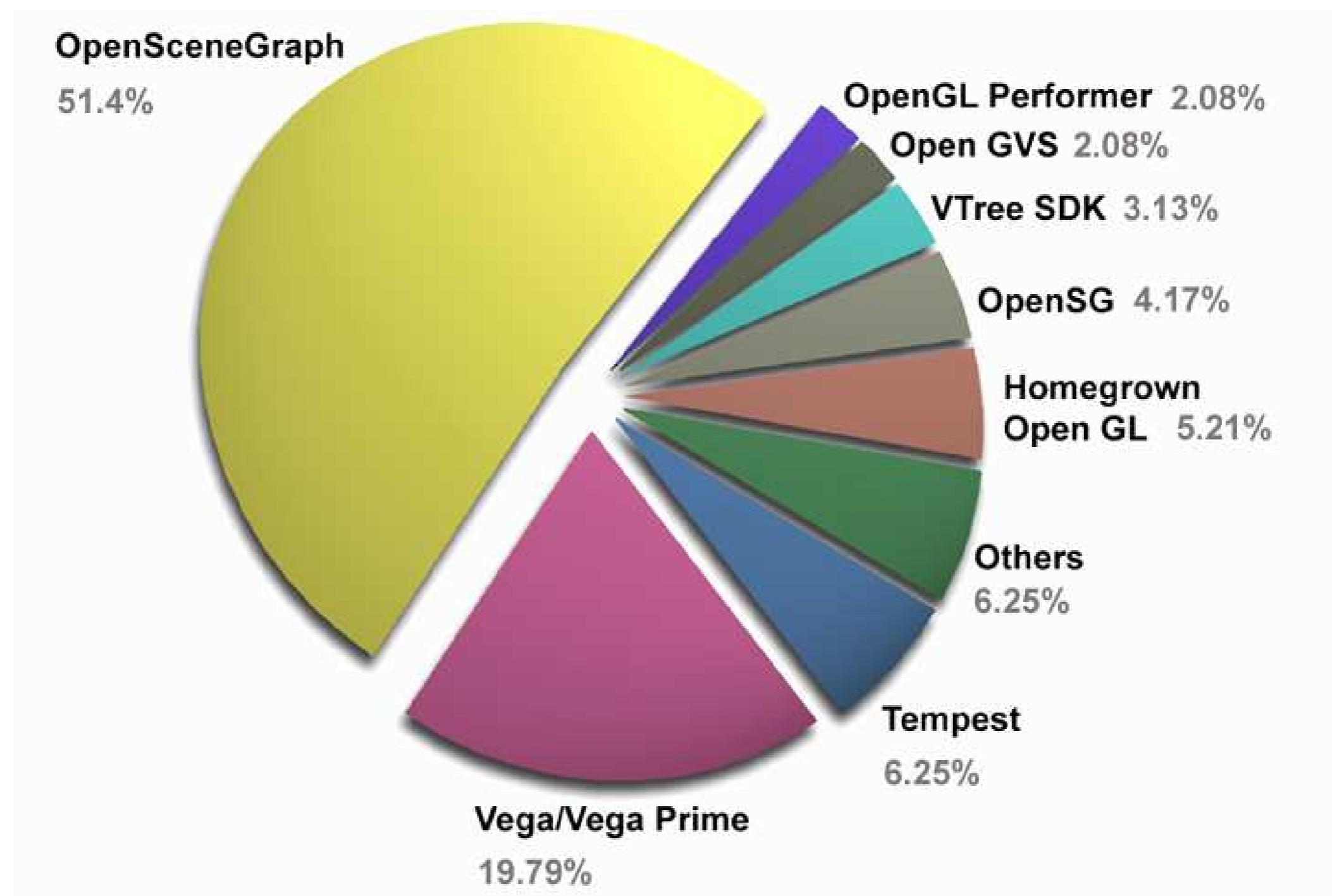


## Why we should use a scene graph?

Scene Graphs are used to optimize the processing of primitives.

- The policy is: as less primitives are passed to the graphics card as better it is.
- Typical optimization processes are
- Culling Operations  
(View Frustum Culling, Occlusion Culling)
- Level-of-Detail
- State sorting
- Helps you to keep track of your objects and scene elements

# Scenegraph poll



*MODSIM Poll on Preferred IG System (MODSIM.org, 2005)*

# Thank you!

## Questions

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