

**ARLAB**

ME/CprE/ComS 557

# **Computer Graphics and Geometric Modeling**

## **Rendering**

October 1st, 2015

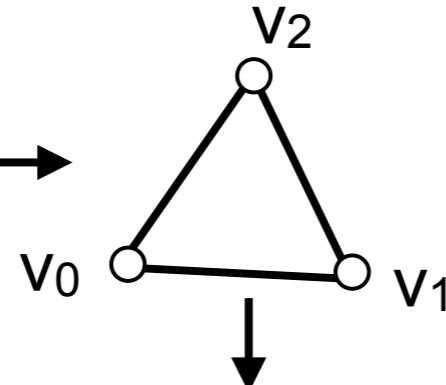
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**IOWA STATE UNIVERSITY**  
OF SCIENCE AND TECHNOLOGY

# Content

- Rendering algorithm and rasterization
- Shading / Fragment Shader
- Depth Test

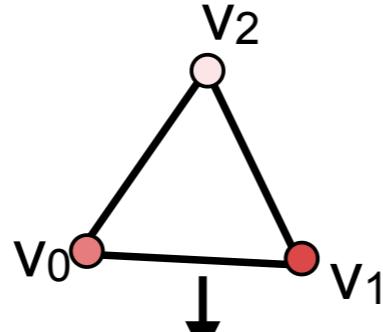
# Rendering: from model to pixel



*Display List of a  
3D model*

Vertex Operation

- Calculate vertex colors
- Primitive Assembly



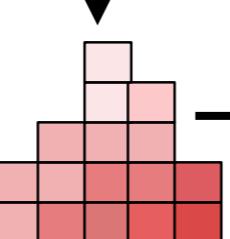
Rasterization

- Shading: fills the primitive (e.g., polygon, quad, etc.) with color

Fragment Operation

Depth Buffer Test

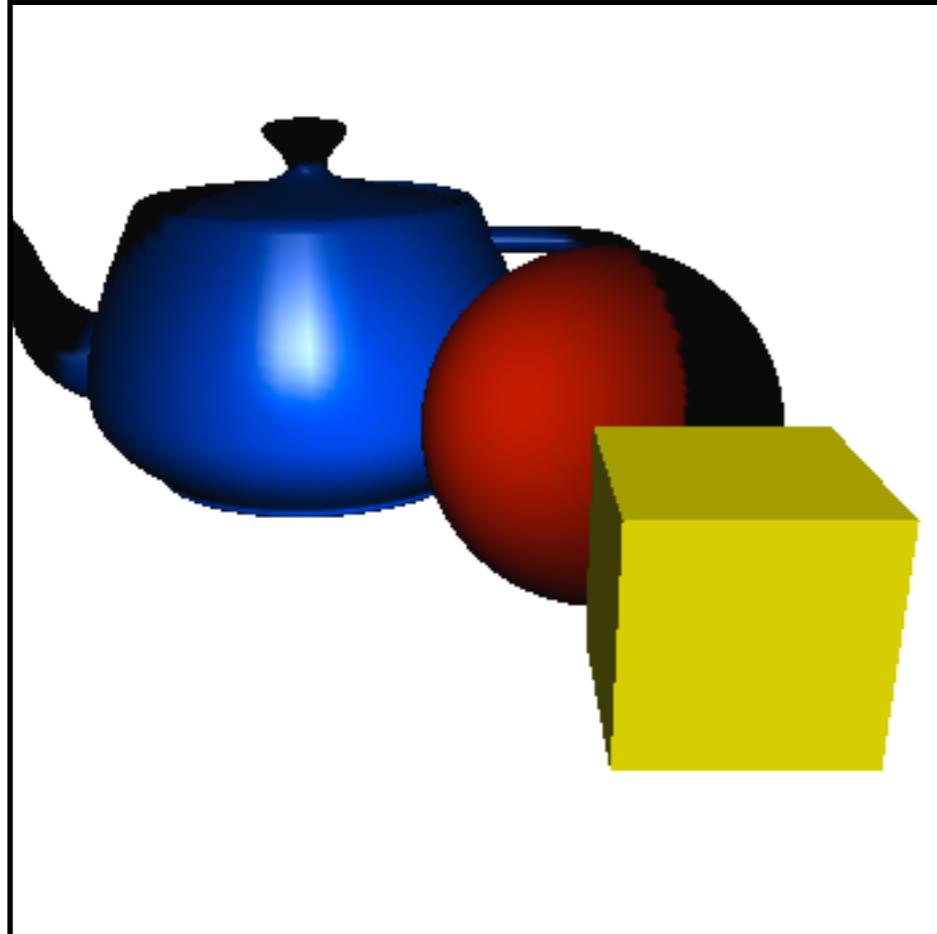
*Image data in  
Frame Buffer*





# Rendering Algorithm / Rasterization

# Sequence of Drawing (1/2)



*Output on display*

## Code snippet of the display function:

(Every function encases all function calls that are necessary to draw the objects)

```
void draw_scene(void)
{
    // draw solid cube
    draw_solid_cube();

    // draw a solid sphere
    draw_solid_sphere();

    // draw a teapot
    draw_solid_teapot();
}
```

What is the sequence of drawing?

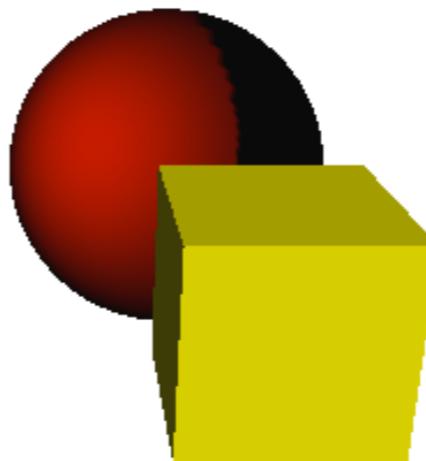
# Sequence of Drawing (2/2)



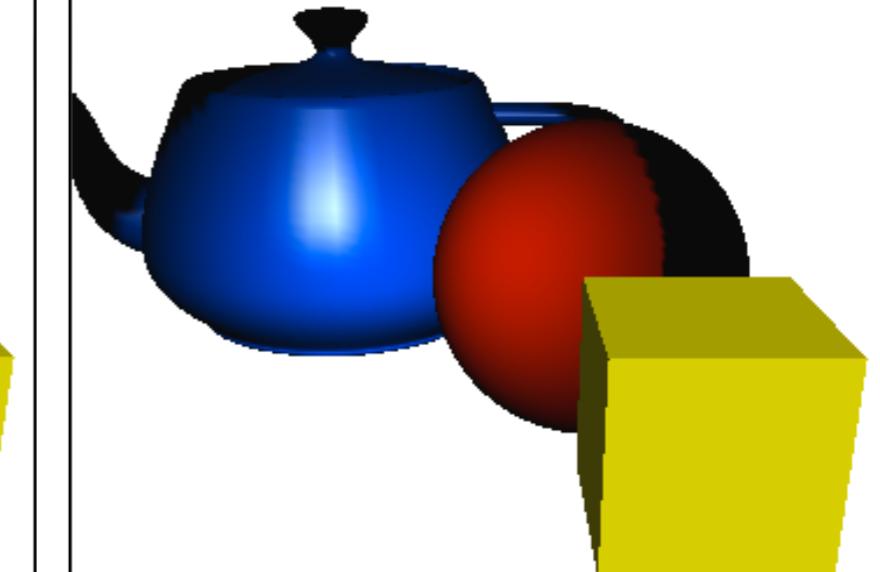
Step 1



Step 2



Step 3



Why do we only see the last image on screen?

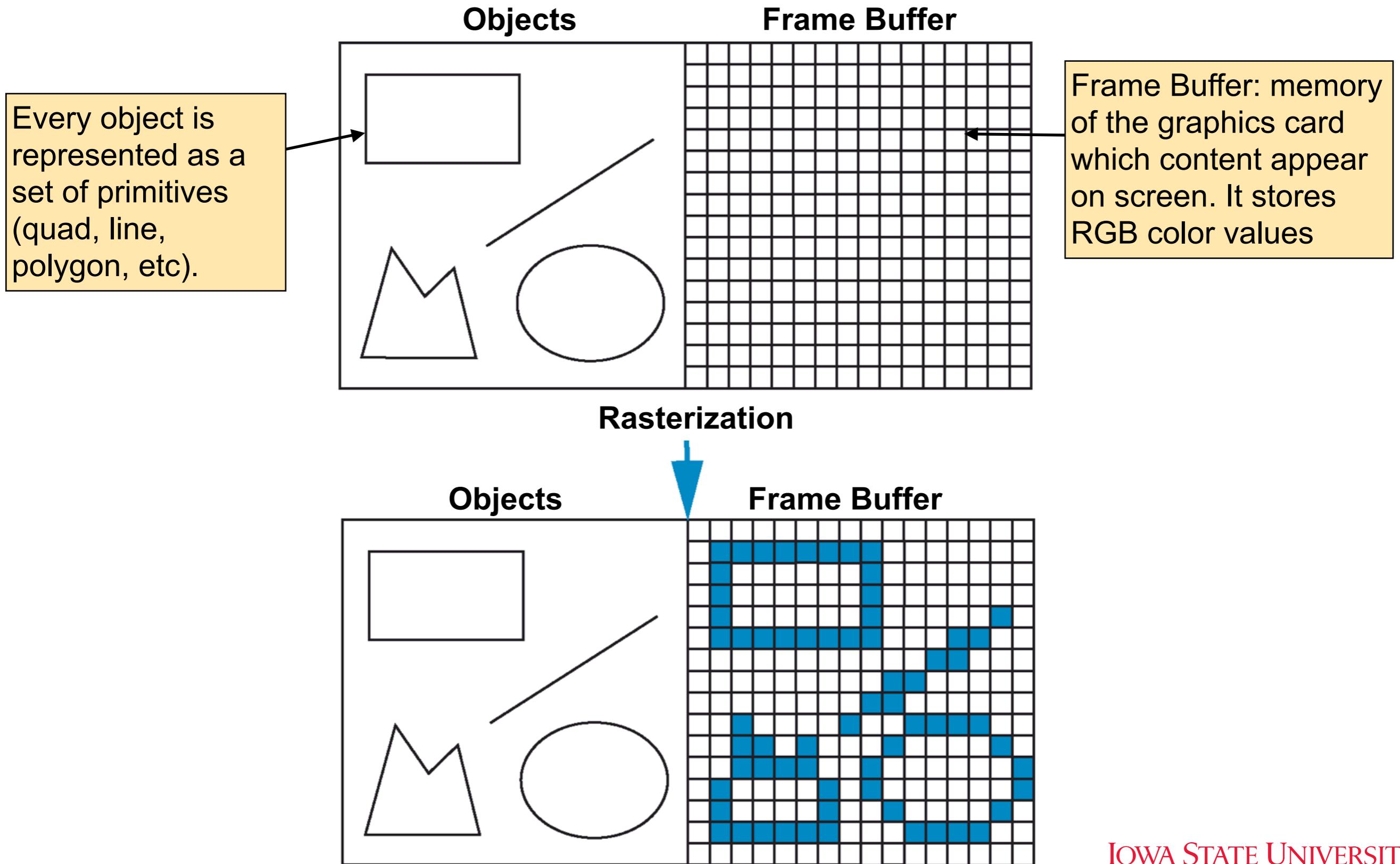
*Output on display*

Sequence  
of execution

```
// draw solid cube  
draw_solid_cube();  
  
// draw a solid sphere  
draw_solid_sphere();  
  
// draw a teapot  
draw_solid_teapot();
```

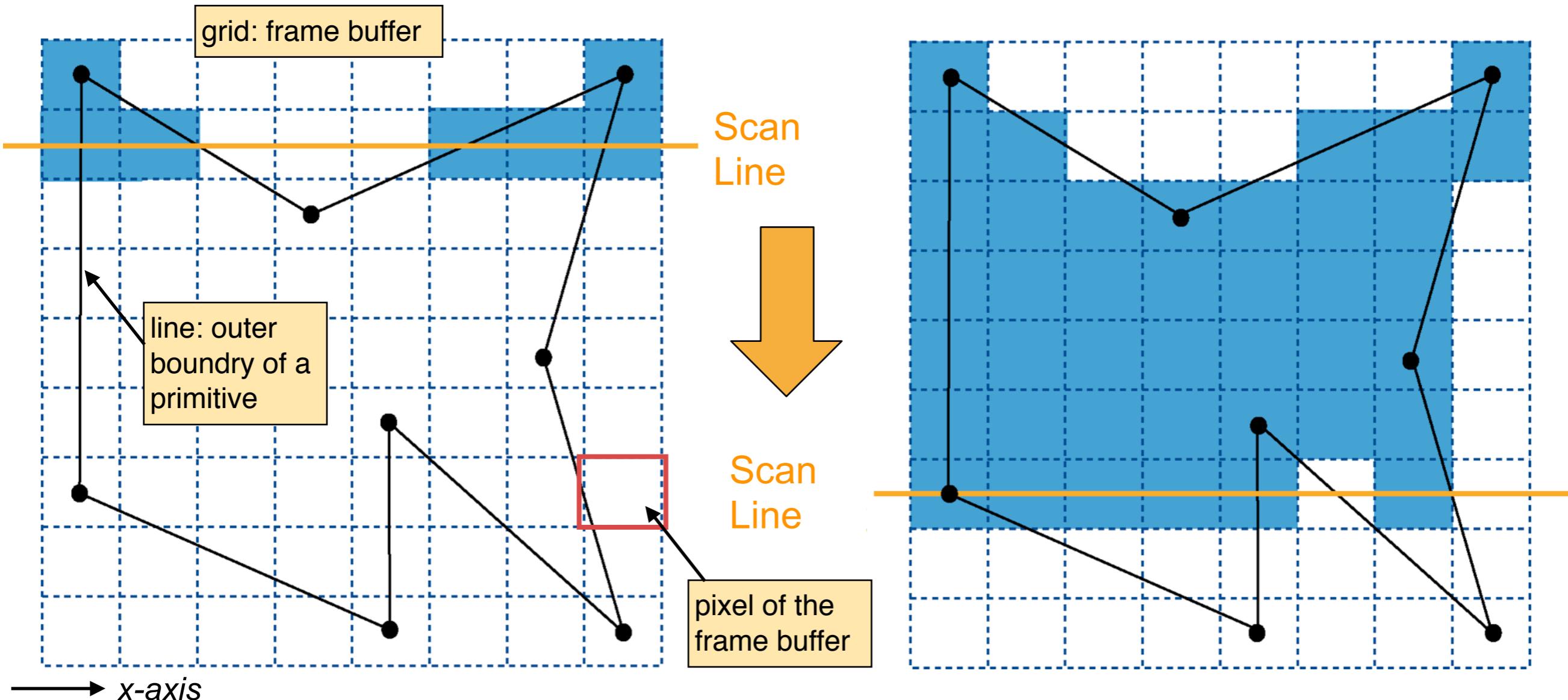
Code is executed from the top to the bottom of the file. The rendering algorithm draws the object in the sequence on screen in which the objects appear in the code.

# Rasterization



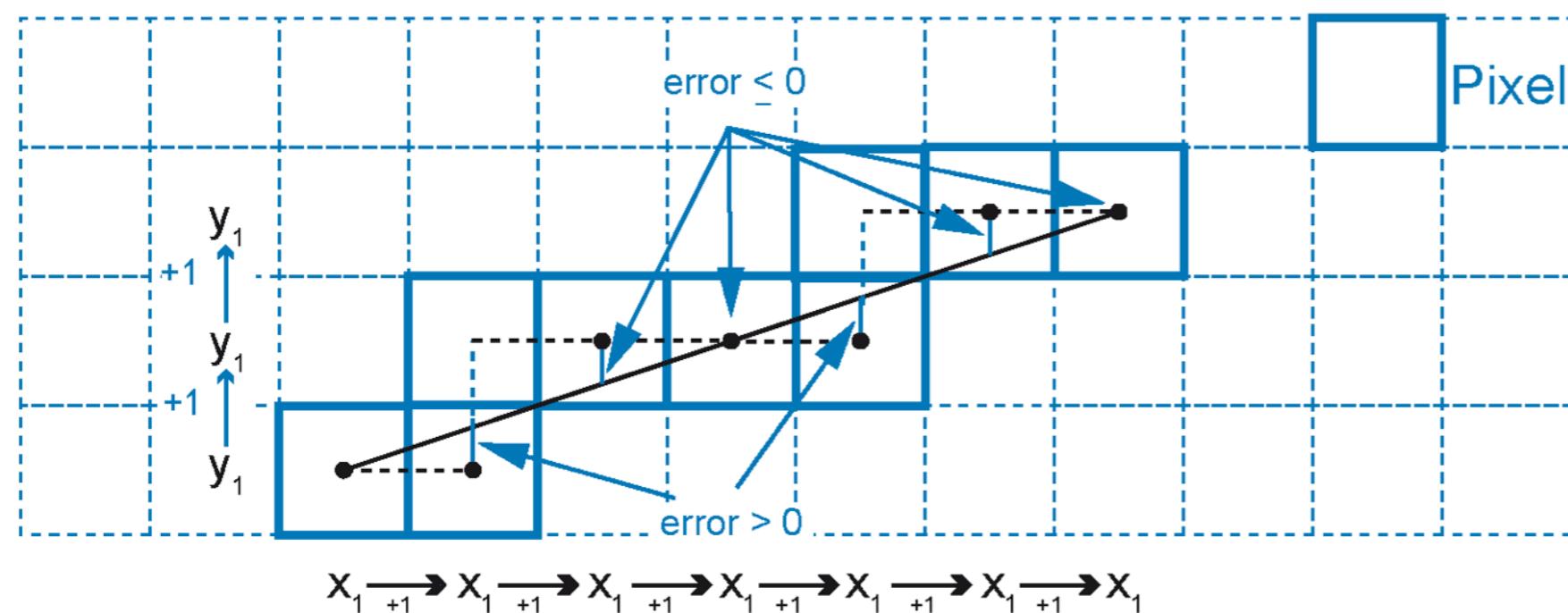
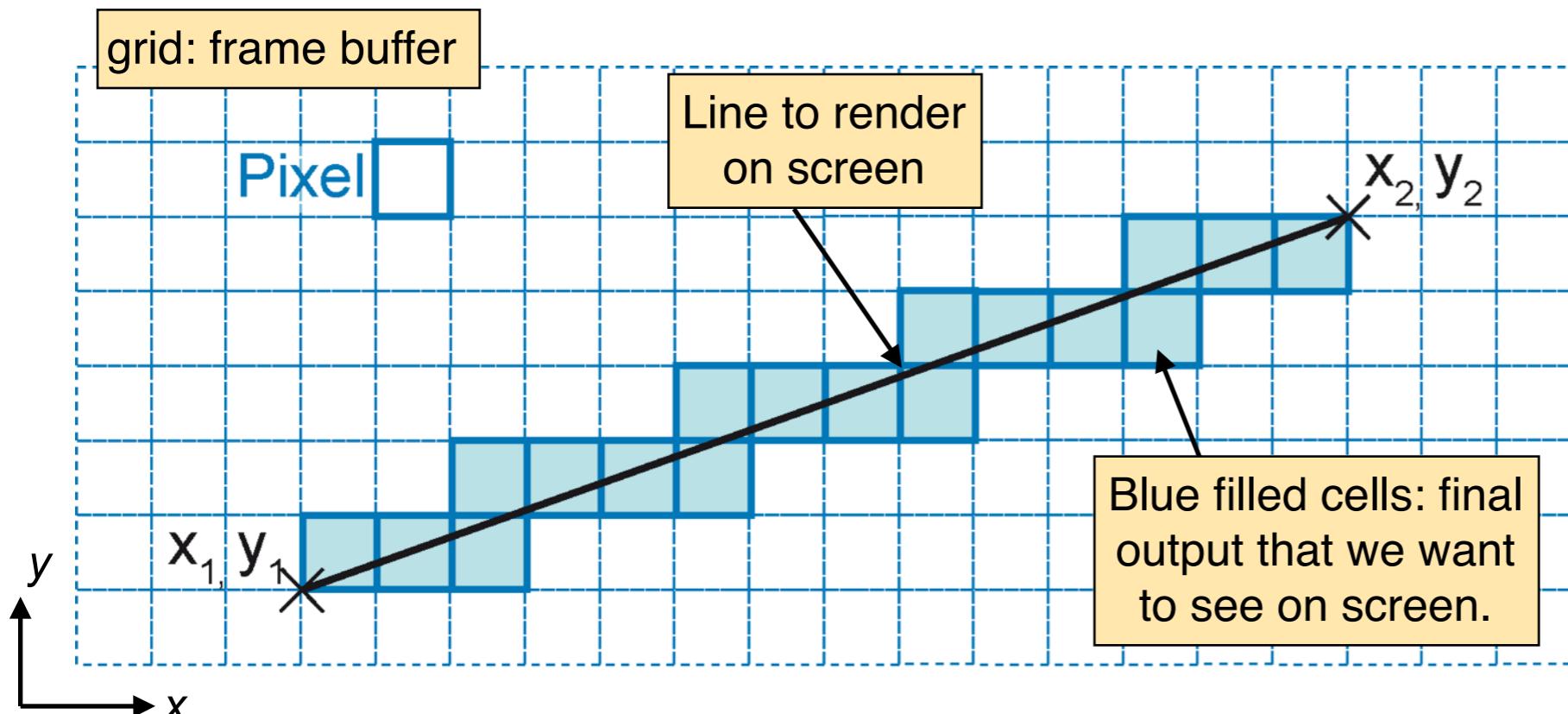
# Filling of Surfaces - Scan-Line-Algorithm

The Scan-Line-Algorithm is a method to fill surfaces of OpenGL primitives



The **Scan-Line-Algorithm** fills a primitive by pushing a scan line in parallel to the x-axis from the top of the screen to the very bottom. The intersection of the scan line with the outer boundary are calculated and all pixels within the primitive are filled (switched on; at this time, no color has been calculated). The algorithm only works with closed primitives.

# Rasterization of Lines - Bresenham-Algorithm



The goal of the rasterization of a line is to select a set of pixels that are close to the line which shall be rendered on screen.

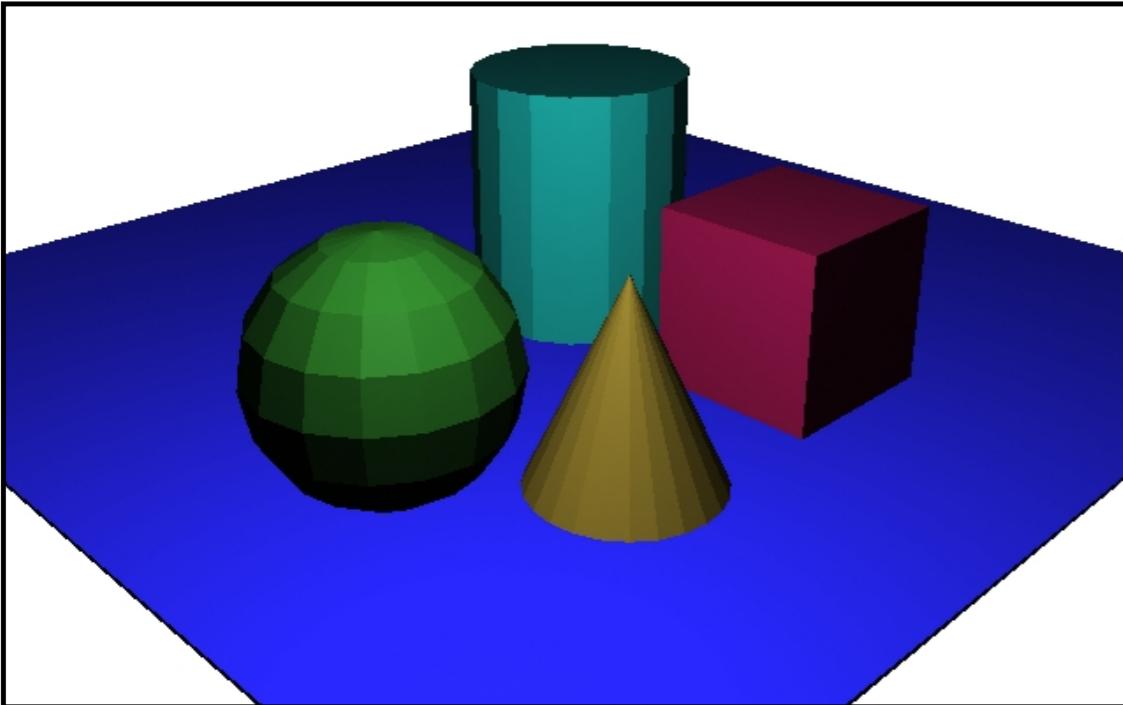
The Bresenham-Algorithm (1965) is an efficient way to render lines. It allows to raster a line by using only additions and subtraction operations.

- Start point for the algorithm is the start of a line / line loop. The start pixel is drawn on screen.
- Every step, the x-value is increased by one.
- The error on y between the ideal line and the center of the pixel is calculated.
- y is increased by one if the error rate exceeds a threshold.

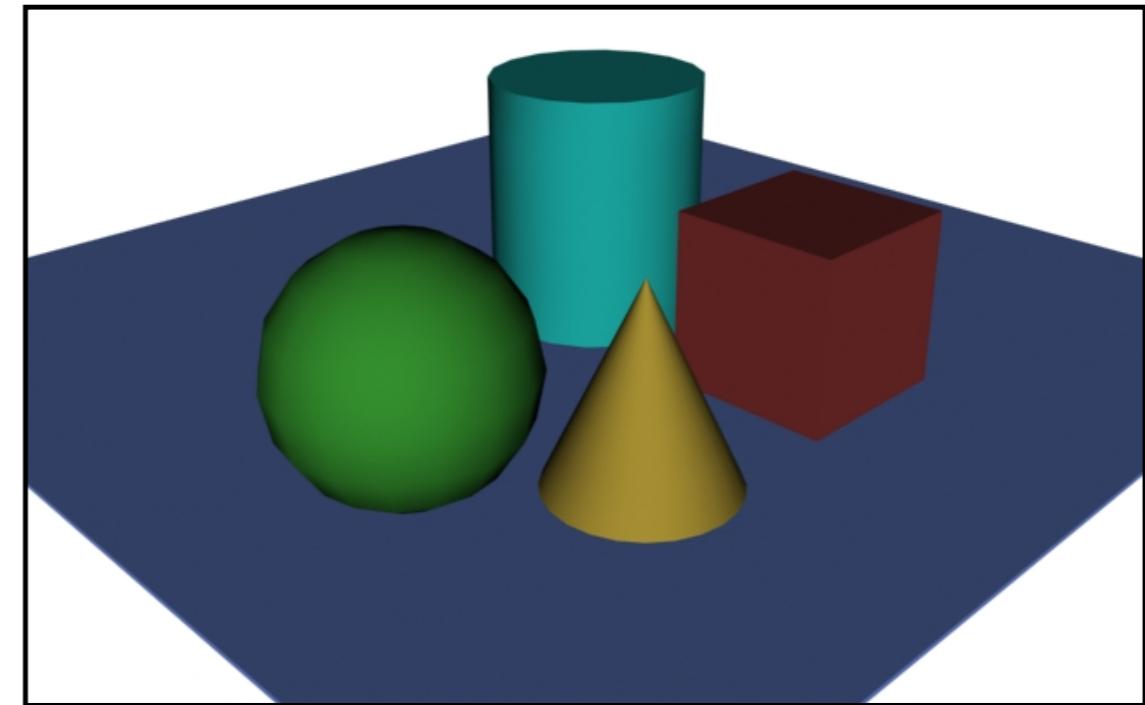


# Shading / Fragment Shader

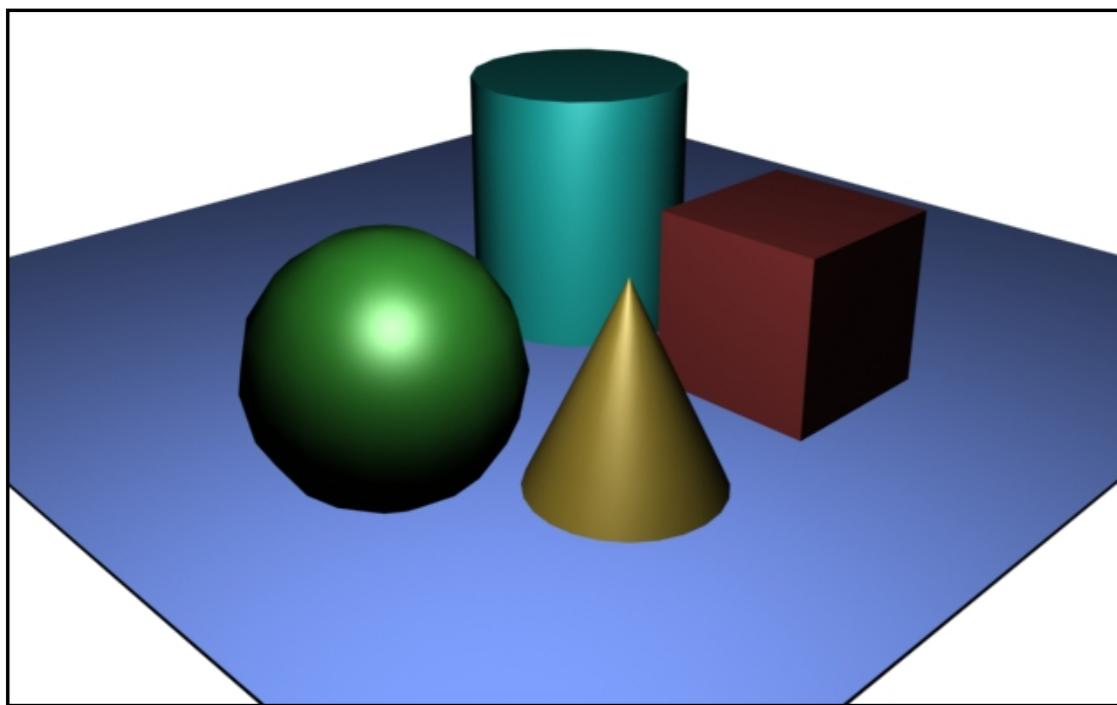
# Shading



*Flat Shading*



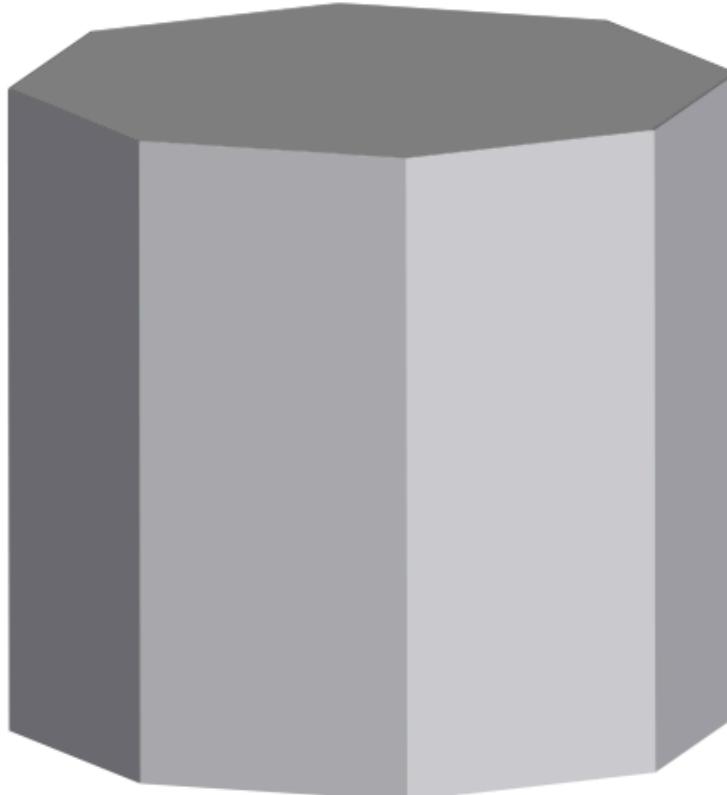
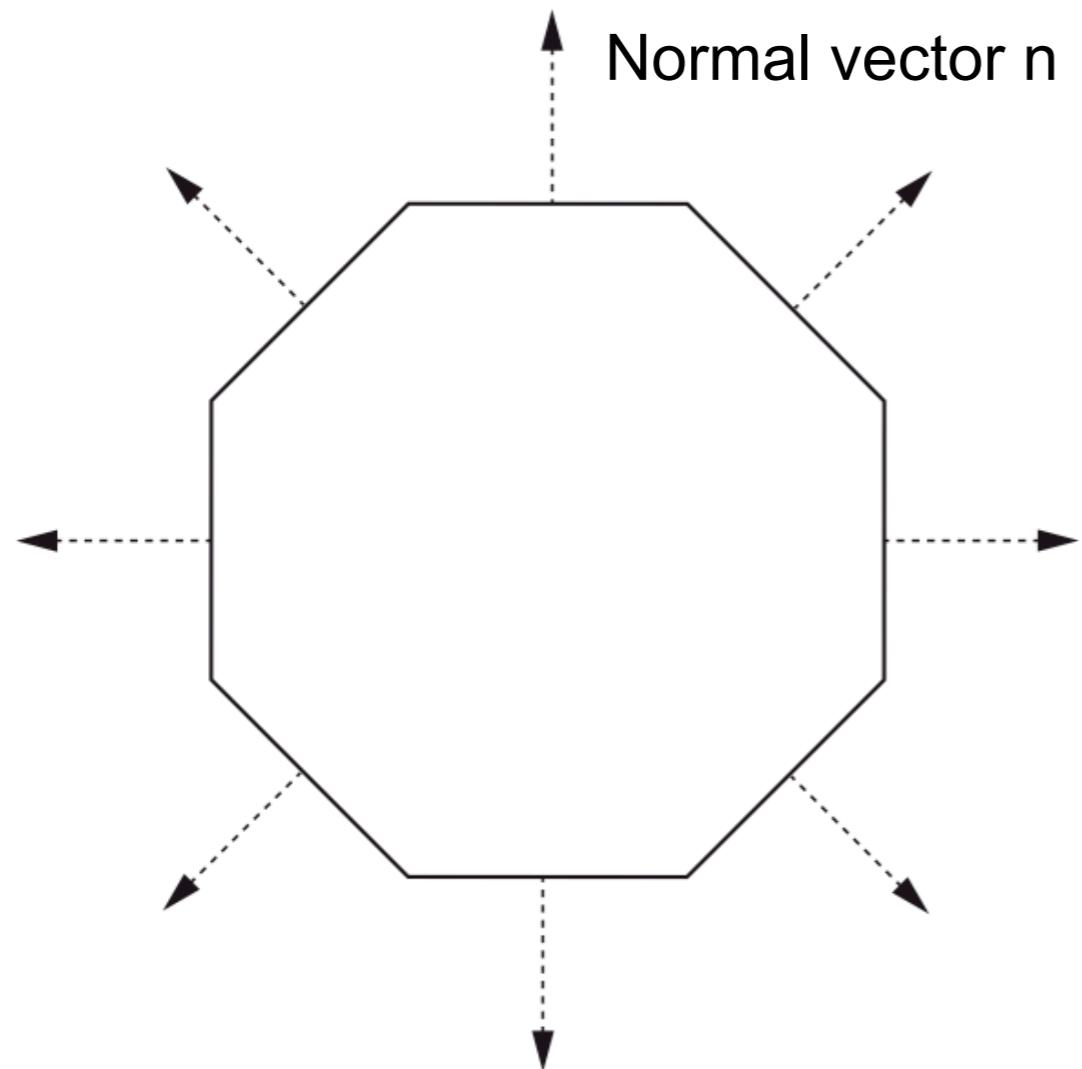
*Gouraud Shading*



*Phong Shading (not implemented in OpenGL)*

Shading is the process that fills the primitives (e.g., polygons, triangles, quads etc.) with color. The task is to determine a color value for each pixel on screen.

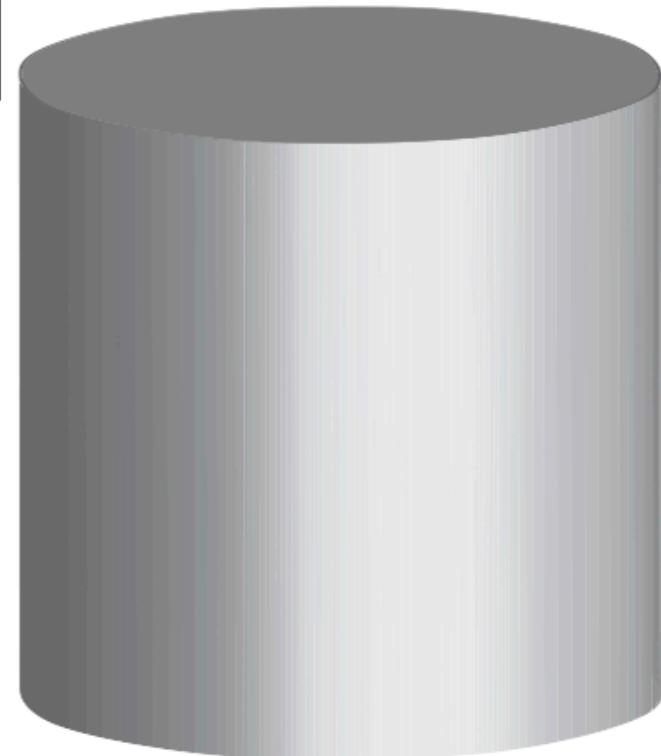
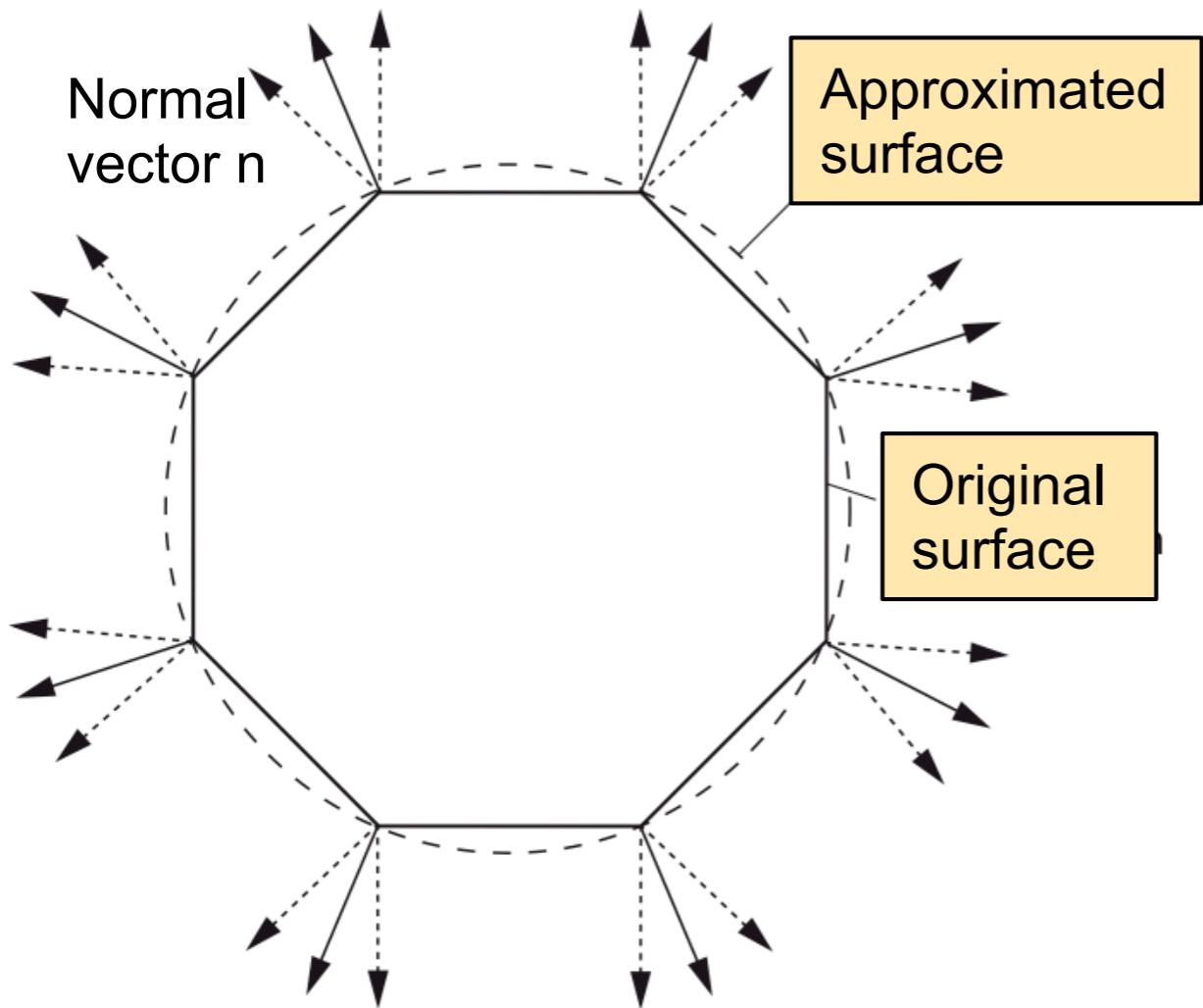
# Flat Shading



*The Flat Shading method calculates one color for each surface with respect to the surface normal.*

- Accentuates the individual polygons
- One color is assigned to each polygon
- Very fast
- Color is computed for one vertex and assigned to entire polygon
- Specular highlights are rendered poorly

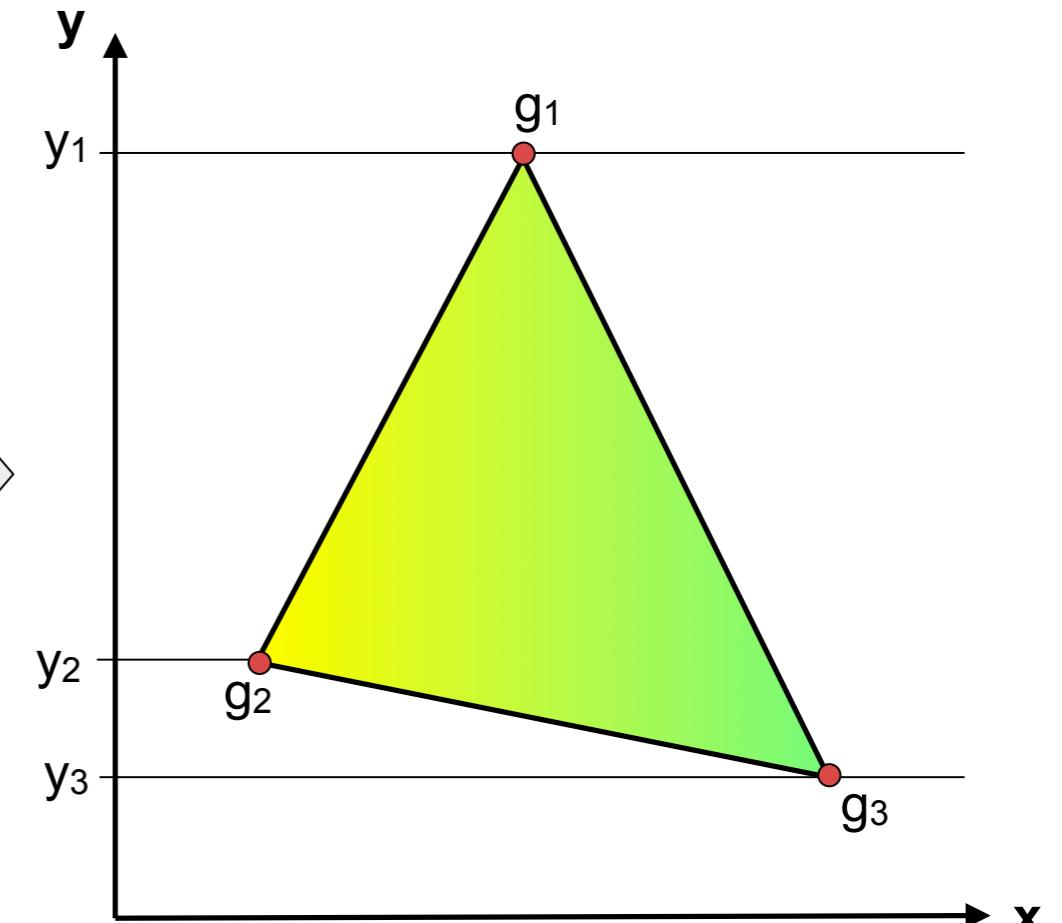
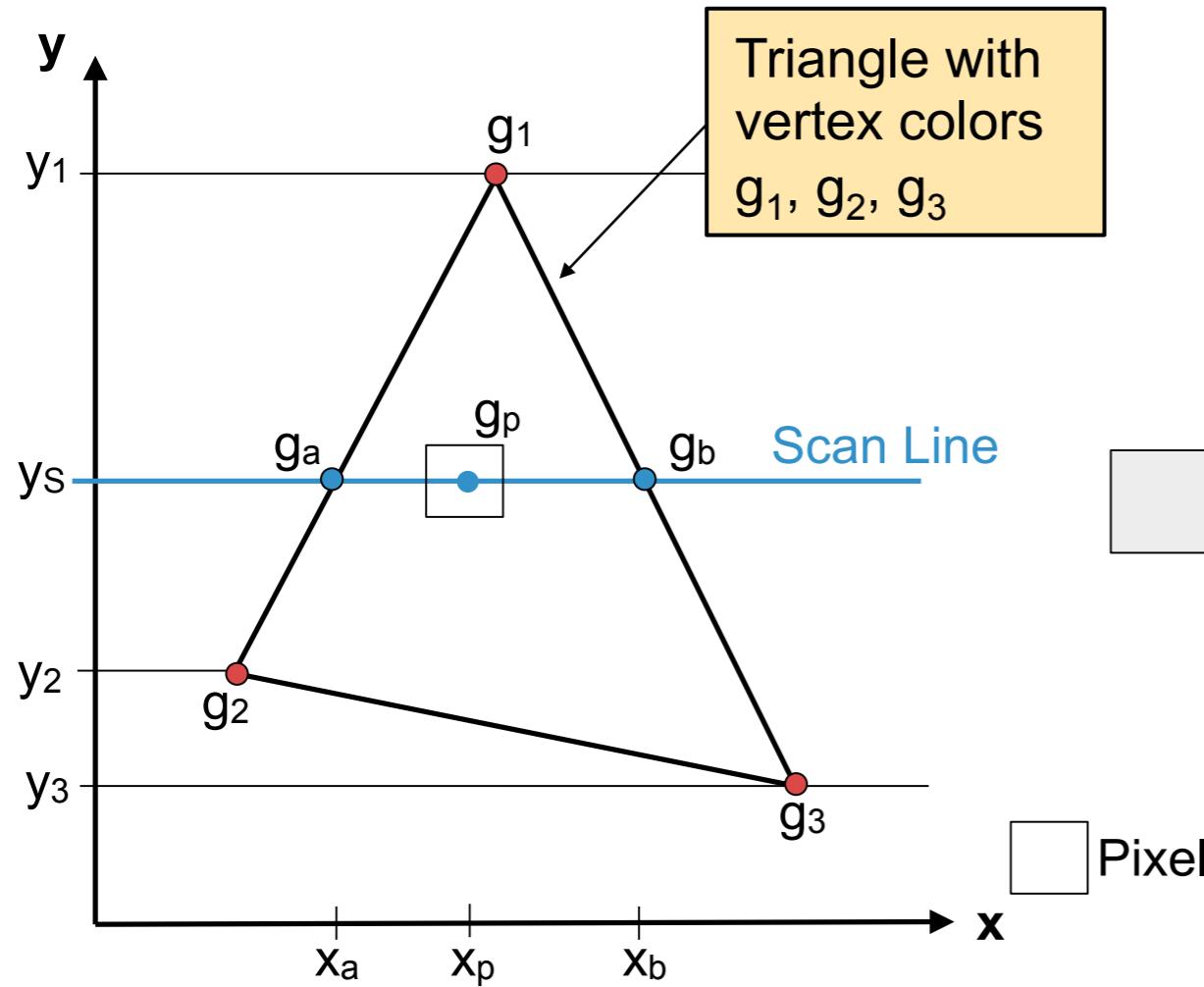
# Gouraud Shading (1/2)



*Calculate the normal vectors at each contact vertex between two surfaces in order to approximate a smooth surface.*

- Smooths the edges between polygons
- Color is linearly interpolated from vertex points
- Specular highlights appear interpolated

# Gouraud Shading (2/2)



The interpolation of a pixel color takes two steps: first, the color at the triangle edges are calculated. Secondly, the pixel color is calculated.

$$g_a = g_1 - (g_1 - g_2) \cdot \frac{y_1 - y_s}{y_1 - y_2}$$

$$g_b = g_1 - (g_1 - g_3) \cdot \frac{y_1 - y_s}{y_1 - y_3}$$

$$g_p = g_b - (g_b - g_a) \cdot \frac{x_b - x_p}{x_b - x_a}$$

$g_a, b$ : Color at the polygon edge

$g_p$ : Color of the pixel

# Comparison



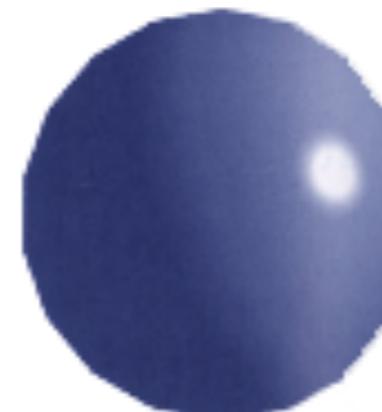
**Flat Shading**



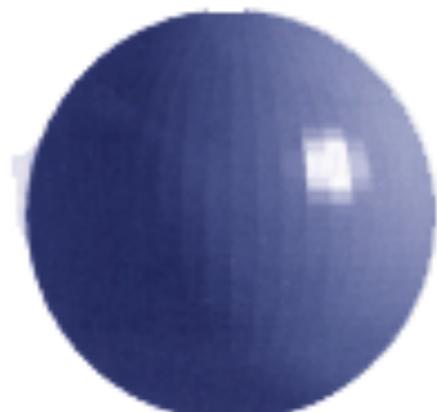
**Gouraud Shading**



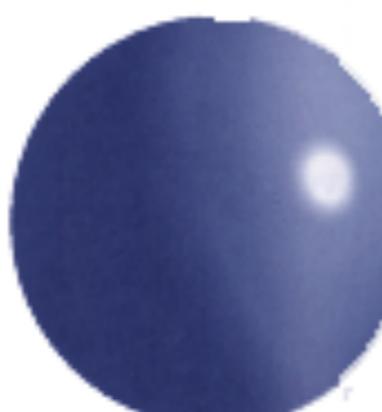
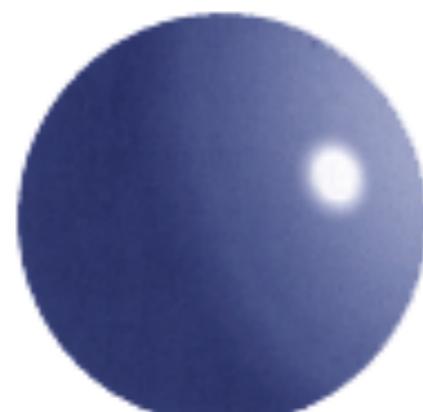
**Phong Shading**



**81 Polygons**



**2500 Polygons**

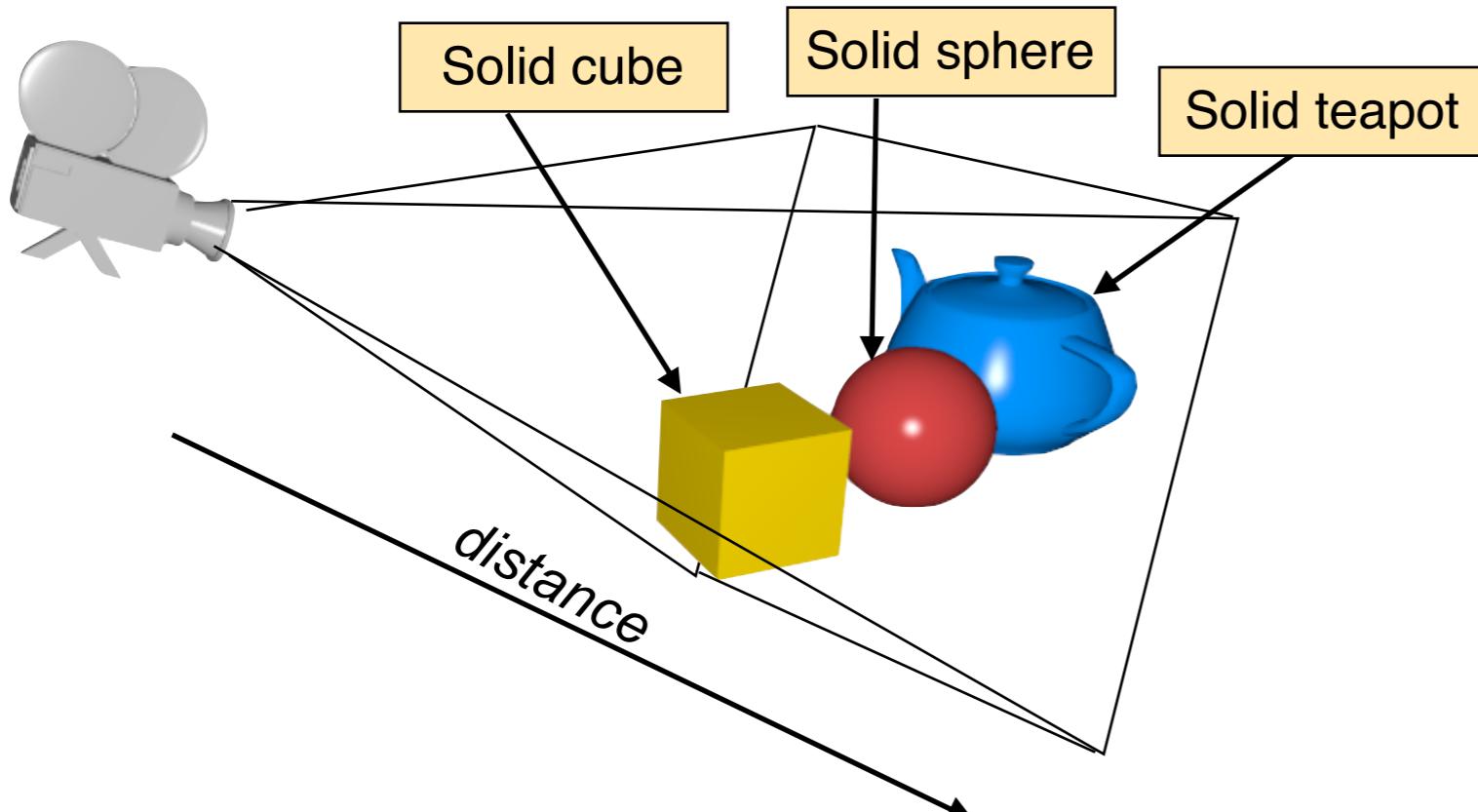


**25000 Polygons**



# Depth Test

# Considering the Render Sequence

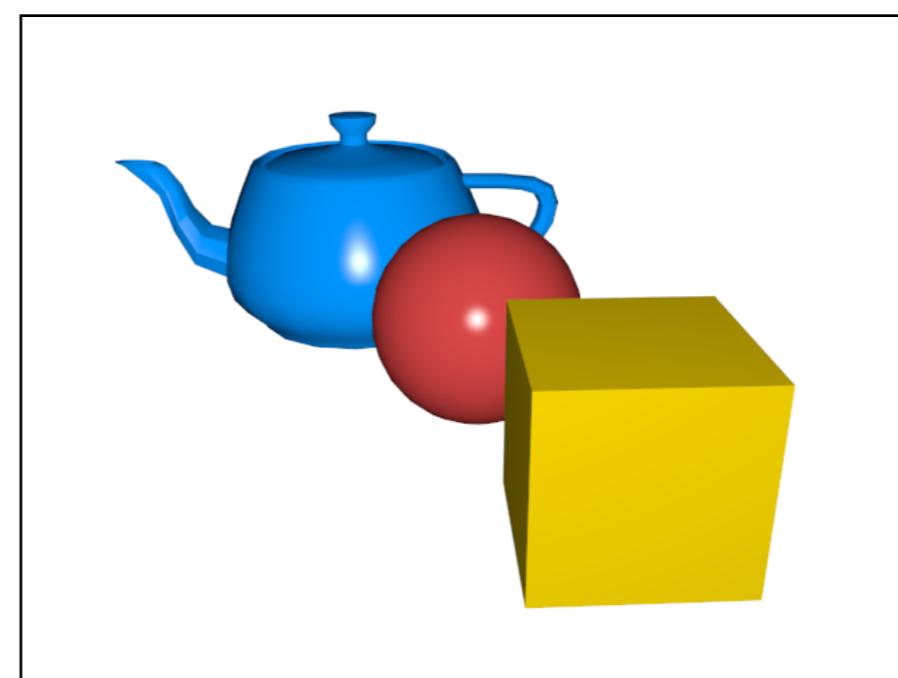


```
void draw_scene(void)
{
    // draw solid cube
    draw_solid_cube();

    // draw a solid sphere
    draw_solid_sphere();

    // draw a teapot
    draw_solid_teapot();
}
```

The rendering sequence of all objects depends on their location in the code. The object that primitives are rendered first are also written into the frame buffer in the very first place.



*Output on display*

# Considering the Render Sequence

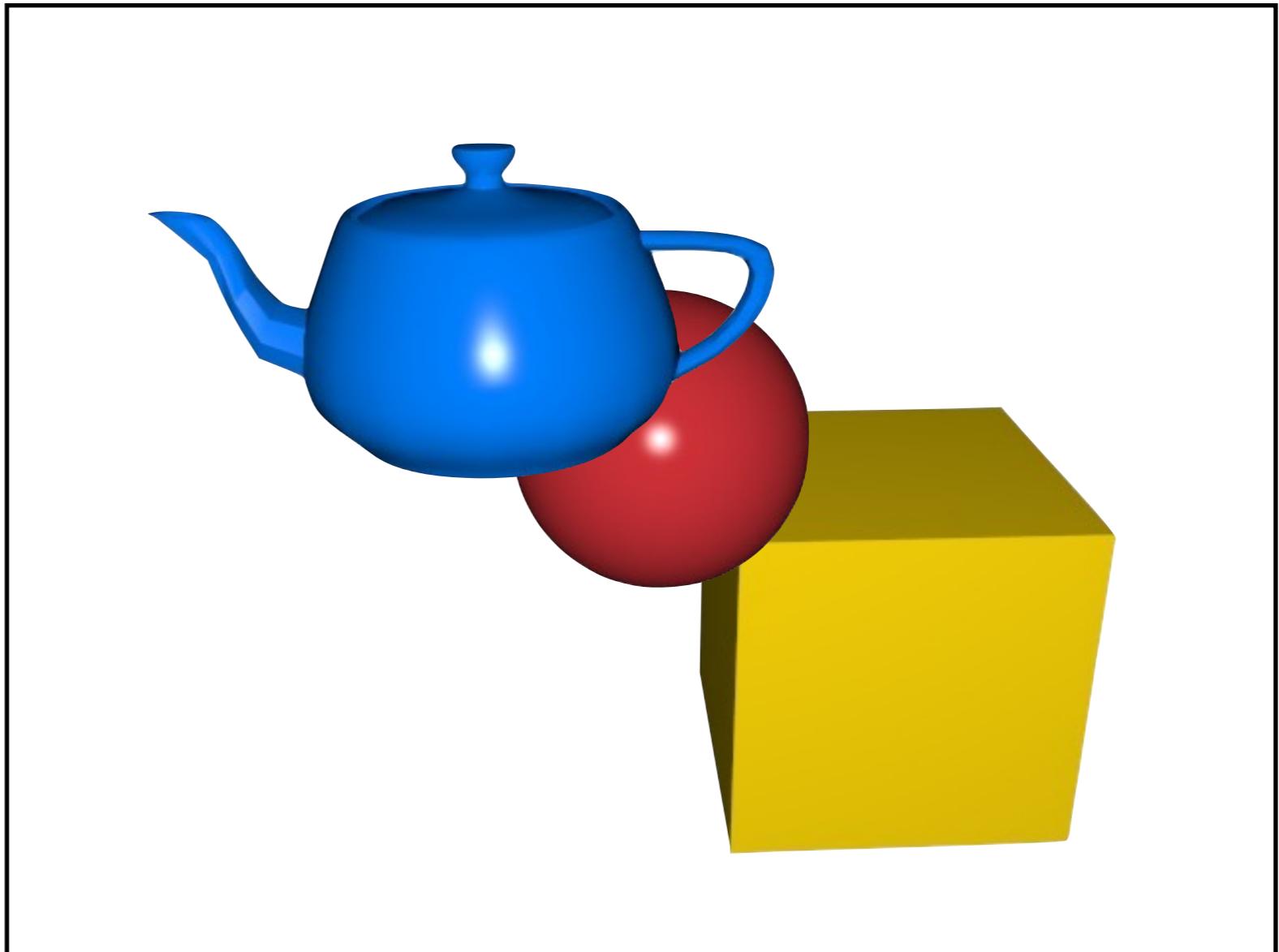


**Code snippet of the  
display function:**

```
void draw_scene(void)
{
    // draw solid cube
    draw_solid_cube();

    // draw a solid sphere
    draw_solid_sphere();

    // draw a teapot
    draw_solid_teapot();
}
```



*Output on display*

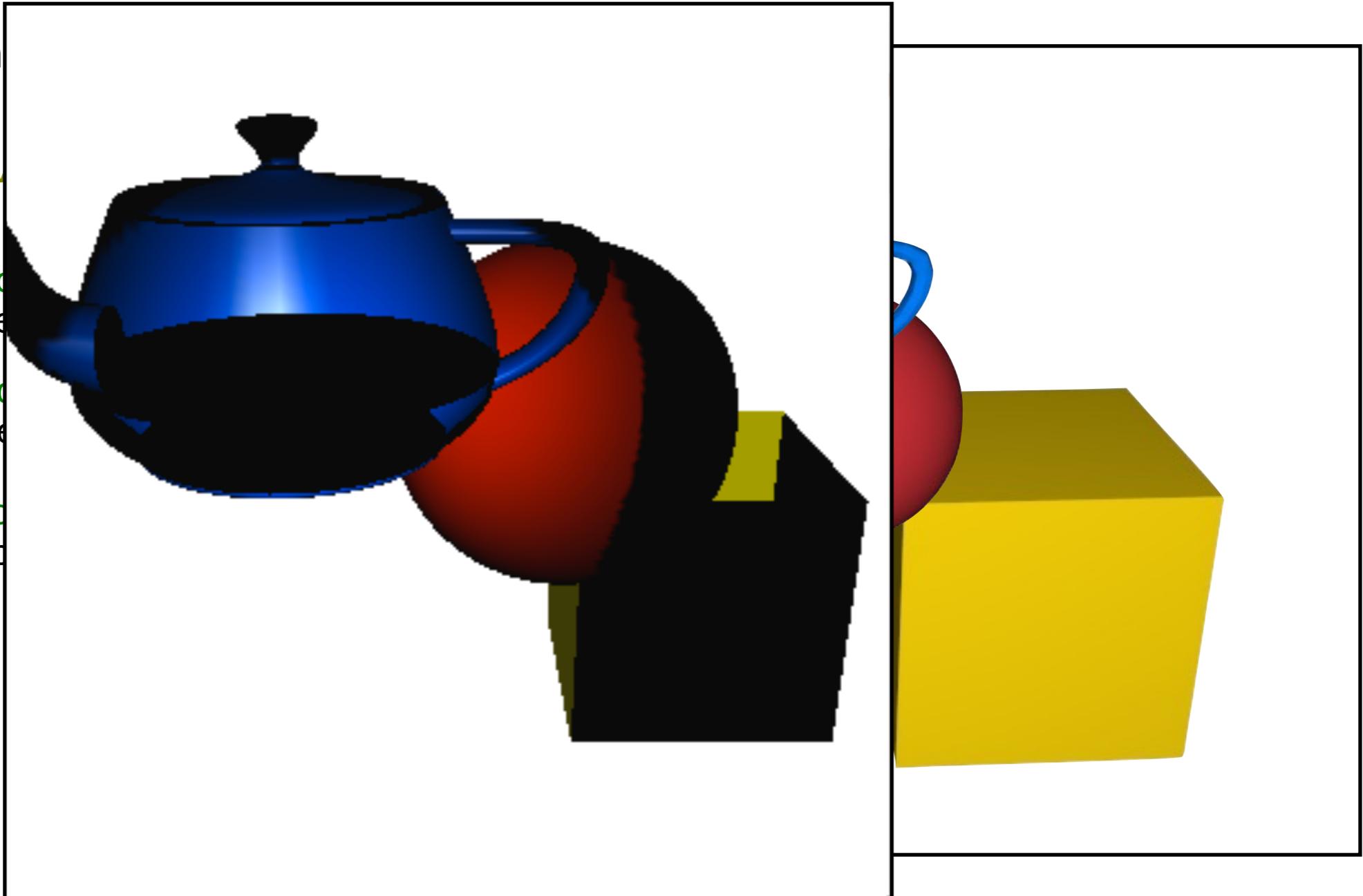
Why do we not see something like this?

# Considering the Render Sequence



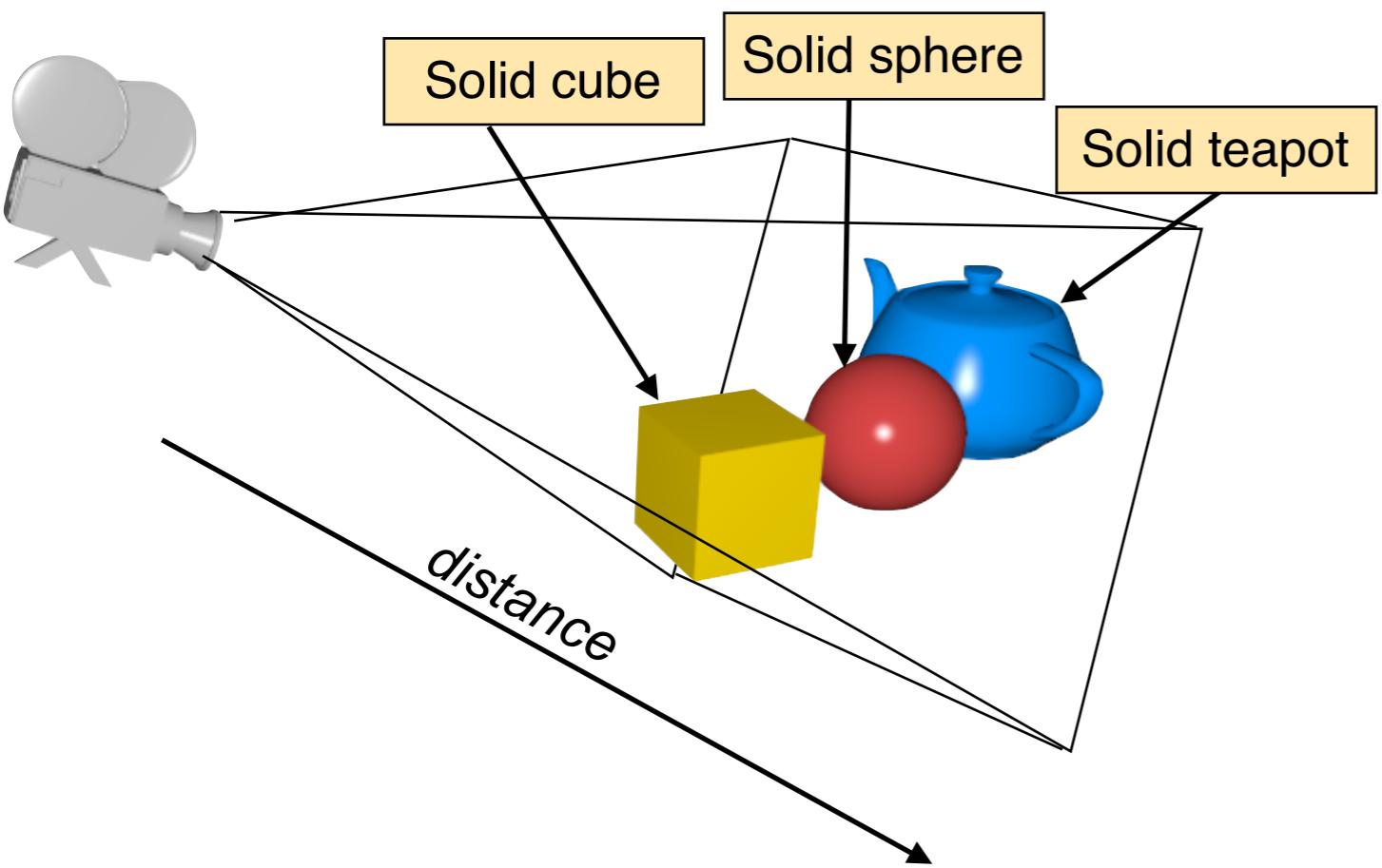
**Code snippet of the  
display function:**

```
void draw_scene()  
{  
    // draw solid cube  
    draw_solid_cube();  
  
    // draw a solid sphere  
    draw_solid_sphere();  
  
    // draw a teapot  
    draw_solid_teapot();  
}
```

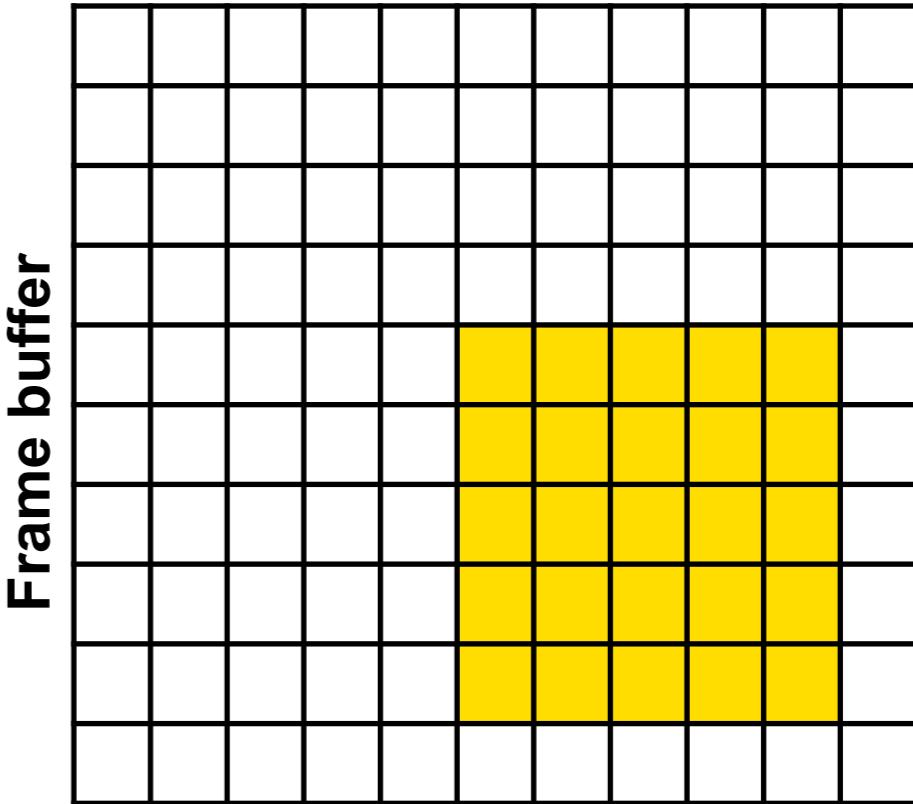


Why do we not see something like this?

# Depth Buffer



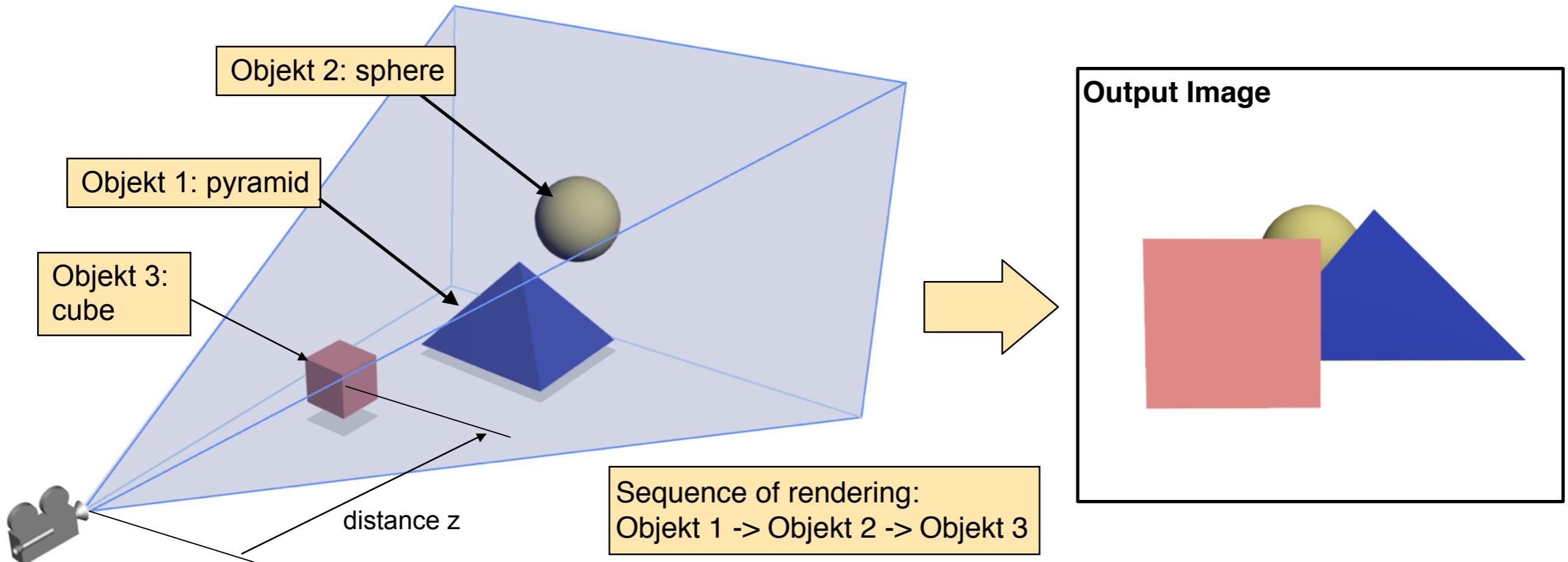
- Memory of the graphics hardware that keeps the distances values between objects (per pixel) on screen and the virtual camera.
- Same size in pixel than the frame buffer.
- Can only keep one value, usually you keep the distance to the closest object.
- Depth values are stored in a range between 0 (close) and 1 (far clipping plane)




Depth buffer

0.5 0.504 0.5 0.5 0.5  
0.5 0.5 0.5 0.5 0.5  
0.5 0.5 0.5 0.5 0.5  
0.5 0.5 0.5 0.5 0.5  
0.5 0.5 0.5 0.5 0.5

# Depth Buffer Test



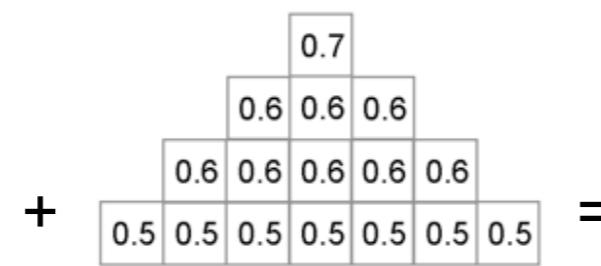
- The Depth Buffer Test (of z-buffer test; developed by Cutmull) is used to test whether an object that should be rendered on screen is closer to the virtual camera than an object which has already been rendered into the frame buffer.
- Consider, the depth buffer keeps the depth information per pixel of the closest object to the virtual camera.
- A new object is only rendered into the frame buffer, if its pixel values are closer to the camera than the object which has already been rendered.

# Depth Buffer Example (1/3)



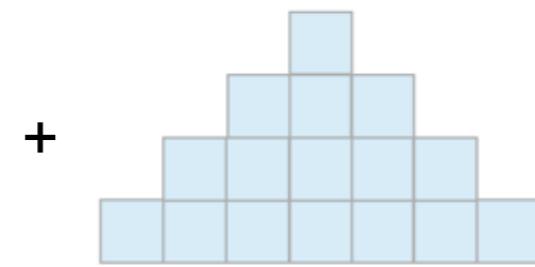
**VRAC | HCI**

## Depth Buffer



8 bit memory in depth buffer

## Frame Buffer



3 x 8 bit memory  
for RGB values

## *Initialization*

## *First object to draw*

## *After Rendering*



z = 0.6

# Depth Buffer Example (2/3)



**Depth Buffer**

1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0	1.0	1.0	0.7	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0	1.0	0.6	0.6	0.6	1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0	0.6	0.6	0.6	0.6	1.0	1.0	1.0	1.0
1.0	1.0	1.0	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	1.0
1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0

$$\begin{array}{c}
 + \\
 \begin{matrix} & & & * \\ & 0.9 & & \\ 0.9 & 0.9 & 0.9 & \\ & 0.9 & 0.8 & 0.9 & 0.9 \\ & 0.9 & 0.9 & 0.9 & \\ & & 0.9 & & \end{matrix} \\
 = 
 \end{array}$$

1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0	1.0	0.9	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	0.9	0.9	0.9	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	0.9	0.9	0.8	0.8	0.7	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	0.9	0.9	0.6	0.6	0.6	1.0	1.0	1.0	1.0
1.0	1.0	1.0	0.6	0.6	0.6	0.6	0.6	1.0	1.0	1.0	1.0
1.0	1.0	1.0	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	1.0
1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0

Parts of the second object remain hidden

**Frame Buffer**

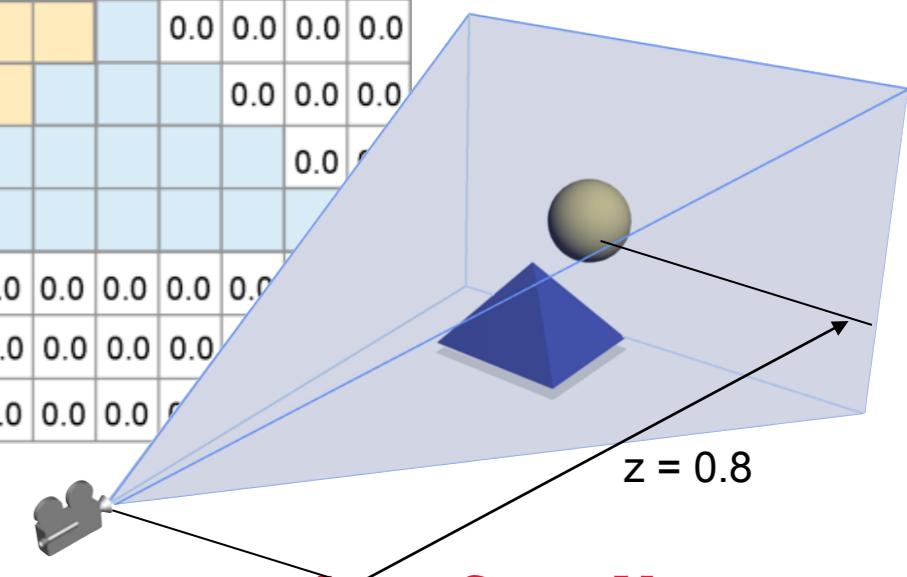
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0

$$\begin{array}{c}
 + \\
 \begin{matrix} & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \end{matrix} \\
 = 
 \end{array}$$

0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0

Second object

After Rendering



After rendering of the first object

\* Note, the depth buffer stores no color values. The colors on this slide should only help to understand this concept

# Depth Buffer Example (3/3)



**Depth Buffer**

1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0	0.9	1.0	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	0.9	0.9	0.9	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	0.9	0.9	0.8	0.9	0.7	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	0.9	0.9	0.9	0.6	0.6	0.6	1.0	1.0	1.0
1.0	1.0	1.0	1.0	0.6	0.6	0.6	0.6	0.6	1.0	1.0	1.0
1.0	1.0	1.0	0.5	0.5	0.5	0.5	0.5	0.5	0.5	1.0	
1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	
1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	
1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	

+

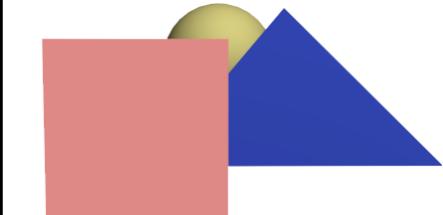
0.3	0.3	0.3	0.3	0.3	0.3
0.3	0.3	0.3	0.3	0.3	0.3
0.3	0.3	0.3	0.3	0.3	0.3
0.3	0.3	0.3	0.3	0.3	0.3
0.3	0.3	0.3	0.3	0.3	0.3

\*

1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	1.0	0.9	1.0	1.0	1.0	1.0	1.0	1.0
1.0	1.0	1.0	0.9	0.9	0.9	1.0	1.0	1.0	1.0	1.0
1.0	1.0	0.9	0.9	0.8	0.9	0.7	1.0	1.0	1.0	1.0
1.0	1.0	1.0	0.9	0.9	0.9	0.6	0.6	0.6	1.0	1.0
1.0	1.0	1.0	1.0	0.6	0.6	0.6	0.6	0.6	1.0	1.0
1.0	1.0	1.0	0.5	0.5	0.5	0.5	0.5	0.5	0.5	1.0
1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	
1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	

=

**Output Image**



**Frame Buffer**

0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0

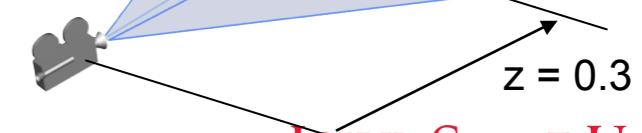
+


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0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0

*Third object*

*After  
Rendering*



*After rendering of the second object*

\* Note, the depth buffer stores no color values. The colors on this slide should only help to understand this concept

# Depth Buffer in OpenGL



Three things need to be done:

- 1. During initialization: init the depth buffer memory.**

The depth buffer is a memory. The program needs to know that it should use this memory.

- 2. Enable the capability.**

The depth buffer test is a capability of the fixed-function rendering pipeline. It must be enabled or disabled as required.

- 3. Clear the buffer before you draw a new frame.**

The buffer must be cleared before a new frame is rendered. Therefore, it has to be filled with the maximum value 1.0

# Code Example

Code from your main.cpp files

```
//// Main render loop

// Set up our green background color
static const GLfloat clear_color[] = { 0.6f, 0.7f, 1.0f, 1.0f };
static const GLfloat clear_depth[] = { 1.0f, 1.0f, 1.0f, 1.0f };

// This sets the camera to a new location
// the first parameter is the eye position, the second the center location, and the third the up vector.
SetViewAsLookAt(glm::vec3(1.0f, 1.0f, 2.5f), glm::vec3(1.0f, 0.0f, 0.0f), glm::vec3(0.0f, 1.0f, 0.0f));

// Enable depth test
// ignore this line, it allows us to keep the distance value after we project each object to a 2d canvas.
glEnable(GL_DEPTH_TEST);

// This is our render loop. As long as our window remains open (ESC is not pressed), we'll continue to render things.
while(!glfwWindowShouldClose(window))
{
    // Clear the entire buffer with our green color (sets the background to be green).
    glClearBufferfv(GL_COLOR , 0, clear_color);
    glClearBufferfv(GL_DEPTH , 0, clear_depth);
```

# Enable / Disable State Machine Functions



```
glEnable(GLenum cap);
```

```
glDisable(GLenum cap);
```

Enable or disable a capability of the graphics hardware.

## Parameter:

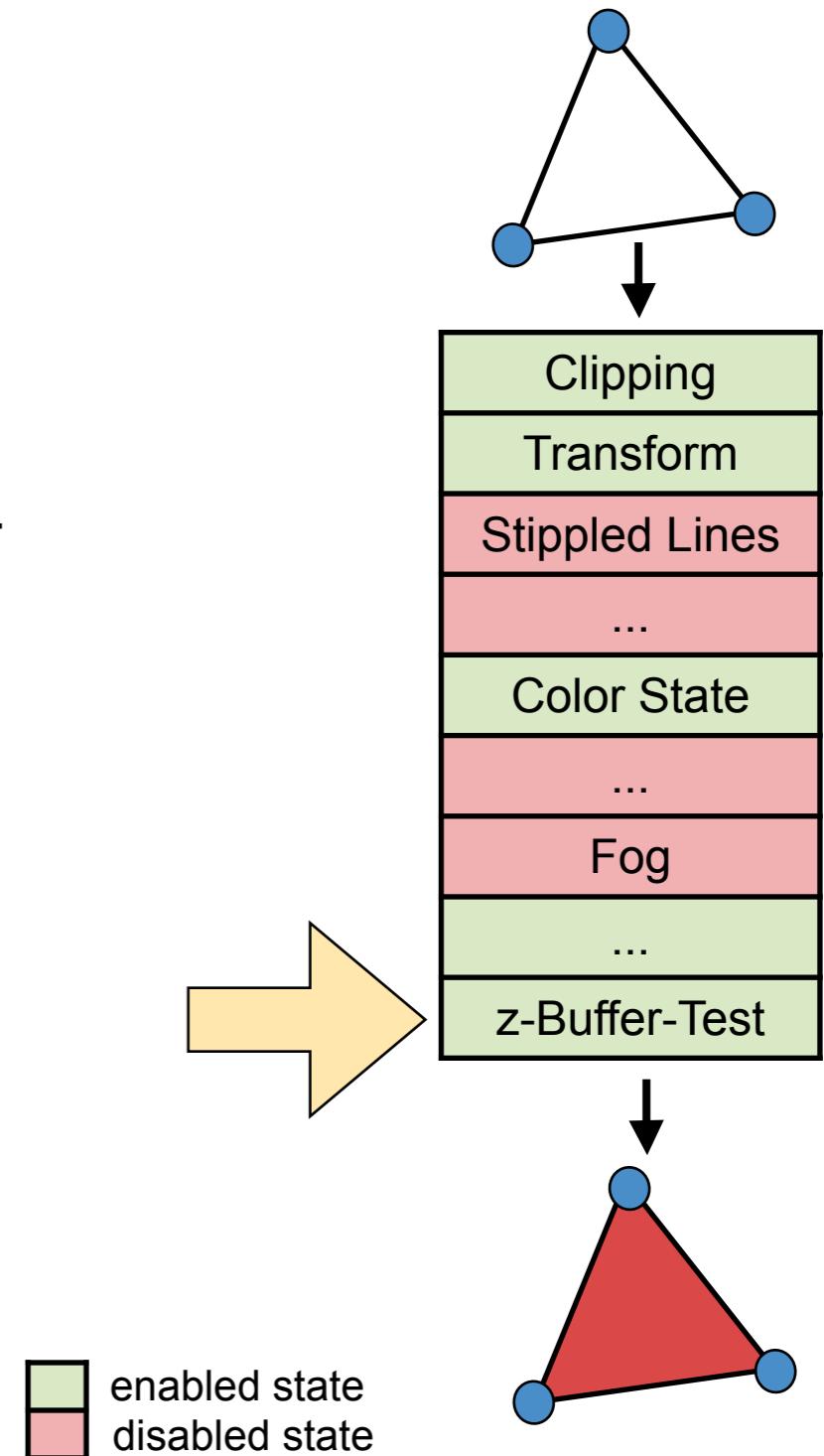
- cap: specifies a symbolic constant that indicates the GL capability

## Examples:

**GL\_BLEND**: If enabled, blend the computed fragment color values with the values in the color buffers.

**GL\_DEPTH\_TEST**: If enabled, do depth comparisons and update the depth buffer.

**GL\_STENCIL\_TEST**: If enabled, do stencil testing and update the stencil buffer.



# Thank you!

## Questions

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