



UNIVERSIDADE DO MINHO

Arquitetura e Cálculo

Exercícios Timed-Automata

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Capítulo 1

Resolução dos Exercícios

1.1 Exercício 1

```
R:<L,L0,Act,C,TR,inv>
L=off,low,bright
L0=off
Act = {press}
C   = {y}
Tr  = {t1,t2,t3,t4}
      t1=(off,true,press,{y},low)
      t2=(low,y>=5, press,{},off)
      t3=(low,y<5,  press,{},bright)
      t4=(bright,true, press,{},off)
inv = {x->>true | x in L}
```

Figura 1.1: Resolução

1.2 Exercício 2

```
R : Lamp || User = {L1 >< L2 , L0,1 >< L0,2,Act||h ,C1 U C2 ,Tr||h,Inv||h }
L1 >< L2 = {(off,idle) ,(low,idle) ,(bright,idle)}
L0,1 >< L0,2 = (off,idle)
Act||h= {tau_press}
C1 U C2 ={y}
Tr||h={t1,t2,t3,t4}
      t1=((off,idle)    --- ((true,true)), Tau_press,{y}) ---> (low,idle))
      t2=((low,idle)   --- ( (y>=5,true), Tau_press, {}) ---> (off,idle))
      t3=((low,idle)   --- ( (y<5, true), Tau_press, {}) ---> (bright,idle))
      t4=((bright,idle) --- ( (true,true), Tau_press, {}) ---> (off,idle))

Inv||h= {x->>true | x in L1 >< L2}
```

Figura 1.2: Resolução

1.3 Exercício 3

Auxiliar:

(Worker || Hammer) = {L1 >< L2 , L0,1 >< L0,2, Act||h , C1 U C2 , Tr||h, Inv||h }

L1 >< L2 = {(rest, free) , (work, busy)}

L0,1 >< L0,2 = (rest, free)

Act||h={Tau_go, Tau_done, hit}

C1 U C2={x, y, z}

Tr||h = {t1, t2, t3}

t1=((rest, free)--- (true, Tau_go, {x, y, z}) ----> (work, busy))

t2=((work, busy)--- (x>=1, hit, {x}) ----> (work, busy))

t3=((work, busy)--- ((z>=10, y>=5), done, {}) ----> (rest, free))

((work, busy)--- ((y>=5, z>=10), (done!, done?), {y, z}) ----> (rest, free))

((work, busy)--- (x>=1, hit, {x}) ----> (Work, busy))

Inv||h =

A cor de rosa são os invariante.

R: (Worker || Hammer || Nail) = {L1 >< L2 >< L3 , L0,1 >< L0,2 >< L0,3 , Act||h||n , C1 U C2 U C3 , Tr||h||n , Inv||h||n }

L1 >< L2 >< L3 = {(rest, free, up) , (work, busy, half), (work, busy, done)}

L0,1 >< L0,2 >< L0,3 = (rest, free, up)

Act||h||n = {Tau_go, Tau_done, Tau_hit}

C1 U C2 U C3 = {x, y, z}

Tr||h||n = {t1, t2, t3, t4, t5, t6, t7, t8, t9, t10, t11, t12}

t1=((rest, free, up) --- (true, Tau_go, {x, y, z}) ----> (work, busy, up))

t2=((work, busy, up) --- (x>=1, Tau_hit, {x}) ----> (work, busy, half))

t3=((work, busy, half) --- (x>=1, Tau_hit, {x}) ----> (work, busy, done))

t4=((work, busy, done) --- ((z>=10, y>=5, true), Tau_done, {}) ----> (rest, free, up))

t5=((work, busy, done) --- (true, null, {}) ----> (rest, free, up))

t6=((work, busy, half) --- ((z>=10, y>=5, true), Tau_done, {}) ----> (rest, free, half))

t7=((rest, free, half) --- (true, Tau_go, {x, y, z}) ----> (work, busy, half))

t8=((work, busy, up) --- ((z>=10, y>=5, true), Tau_done, {}) ----> (rest, free, up))

t9=((work, busy, done) --- ((z>=10, y>=5, true), Tau_done, {}) ----> (rest, free, done))

t10=((work, busy, done) --- (true, null, {}) ----> (work, busy, up))

t11=((rest, free, done) --- (true, null, {}) ----> (rest, free, up))

t12=((rest, free, done) --- (true, Tau_go, {x, y, z}) ----> (work, busy, done))

Inv||h||n

Inv(rest, free, up)=true

Inv(work, busy, half)= z<=60

Inv(work, busy, done)= z<=60

Inv(work, busy, up)=z<=60

Inv(rest, free, half)=true

Inv(rest, free, done)=true

1.4 Exercício 4

$N = \{\text{in}, \text{out}, d\} \mid d \in \mathbb{R}^+$

$R:T = \{t_1, t_2, t_3, t_4\}$

$t_1 = \{(\text{off}, t) \rightarrow d \rightarrow (\text{off}, t+d)\} \mid t, d \geq 0$
 $t_2 = \{(\text{on}, t) \rightarrow d \rightarrow (\text{on}, t+d)\} \mid t, d \geq 0 \text{ and } t+d \leq 2$
 $t_3 = \{(\text{off}, t) \rightarrow \text{in} \rightarrow (\text{on}, 0)\} \mid t \geq 0$
 $t_4 = \{(\text{on}, t) \rightarrow \text{out} \rightarrow (\text{off}, t)\} \mid 1 \leq t \leq 2$

Figura 1.3: Resolução

1.5 Exercício 5

$R: \{ \langle 0, \text{press} \rangle, \langle 3, \text{press} \rangle, \langle 4, \text{press} \rangle, \langle 0, \text{press} \rangle, \langle 5, \text{press} \rangle \}$

Figura 1.4: Resolução

1.6 Exercício 6

Não, pq existem vários traços que num sistema podem ser executados e no outro não.

Por exemplo:

$\langle 1, t \rangle, \langle x, t \rangle \mid 1 \leq x \leq 2$ não pode ser executado no segundo sistema.

No entanto, no segundo sistema também é possível acontecer o mesmo.

$\langle 1, t \rangle, \langle x, t \rangle \mid 0 \leq x < 1$

Figura 1.5: Resolução

1.7 Exercício 7

$R = \{ (s, \{x \rightarrow d\}), (v, \{x \rightarrow d\}) \mid d \in [0, 10] \} \cup$
 $\{ (t, \{x \rightarrow d\}), (v, \{x \rightarrow d\}) \mid d \in [0, 10] \}$

Sendo a_1 uma ação e d um delay:

$s \xrightarrow{a_1} t \Rightarrow v \xrightarrow{a_1} v \quad \text{AND} \quad t R v$

$s \xrightarrow{d} t \Rightarrow v \xrightarrow{d} v \quad \mid d \in [2, 10] \text{ AND } t R v$

Converso:

$v \xrightarrow{a_1} v \Rightarrow s \xrightarrow{a_1} t \quad \text{AND} \quad v R t$

$v \xrightarrow{d} v \Rightarrow s \xrightarrow{d} t \quad \mid d \in [2, 10] \text{ AND } v R t$

---- Para a outra possível ação:

$t \xrightarrow{a_1} t \Rightarrow v \xrightarrow{a_1} v \quad \text{AND} \quad t R v$

$t \xrightarrow{d} t \Rightarrow v \xrightarrow{d} v \quad \mid d \in [2, 10] \text{ AND } t R v$

Converso:

É exatamente igual ao de cima.

Logo são timed-Bisimulation

Por exemplo :

$s \xrightarrow{a_1} t \Rightarrow v \xrightarrow{a_1} v \quad \text{AND} \quad t R v = \text{True}$

$s \xrightarrow{d=3} t \Rightarrow v \xrightarrow{d=3} v \quad \text{AND} \quad t R v = \text{True}$

porque $\{ (t, \{x \rightarrow 3\}), (v, \{x \rightarrow 3\}) \} \in R$

Figura 1.6: Resolução