

## Commutative, Associative, and Distributive Laws

### Commutative Laws

$$a + b = b + a \quad \text{ex: } 3 + 4 = 4 + 3$$

$$a \times b = b \times a \quad \text{ex: } 2 \times 5 = 5 \times 2$$

Does not work for subtraction or division

### Associative Laws

$$(a + b) + c = a + (b + c) \quad \text{ex: } (2 + 3) + 5 = 2 + (3 + 5)$$

$$(a \times b) \times c = a \times (b \times c) \quad \text{ex: } (1 \times 2) \times 4 = 1 \times (2 \times 4)$$

Does not work for subtraction or division

Sometimes easier to add or multiply in different order

$$19 + 36 + 4 = 19 + (36 + 4) = 19 + 40 = 59$$

$$2 \times 16 \times 5 = (2 \times 5) \times 16 = 10 \times 16 = 160$$

### Distributive Laws

$$a \times (b + c) = a \times b + a \times c$$

$$\text{ex: } 3 \times (2 + 4) = 3 \times 6 = 18$$

$$(3 \times 6) + (3 \times 4) = 6 + 12 = 18$$

Does not work for division

Sometimes easier to break up difficult multiplication

$$6 \times 24 = 6 \times (20 + 4) = (6 \times 20) + (6 \times 4) = 120 + 24 = 144$$

Or to combine

$$16 \times 6 + 16 \times 4 = 16 \times (6 + 4) = 16 \times 10 = 160$$

Can use for subtraction

$$26 \times 3 - 24 \times 3 = (26 - 24) \times 3 = 2 \times 3 = 6$$

Can use in long additions

$$6 \times 7 + 2 \times 7 + 3 \times 7 + 5 \times 7 + 4 \times 7 = (6 + 2 + 3 + 5 + 4) \times 7 = 20 \times 7 = 140$$