

Advanced

Models

hw2

Part 2



a)

a. Consider the following plots which show the application of a Moving Average Filter (in blue) to the Texas car crashes data. Match the filters described by a_1 and a_2 to their corresponding plots. Explain why the two filtered time series differ in terms of their smoothness.

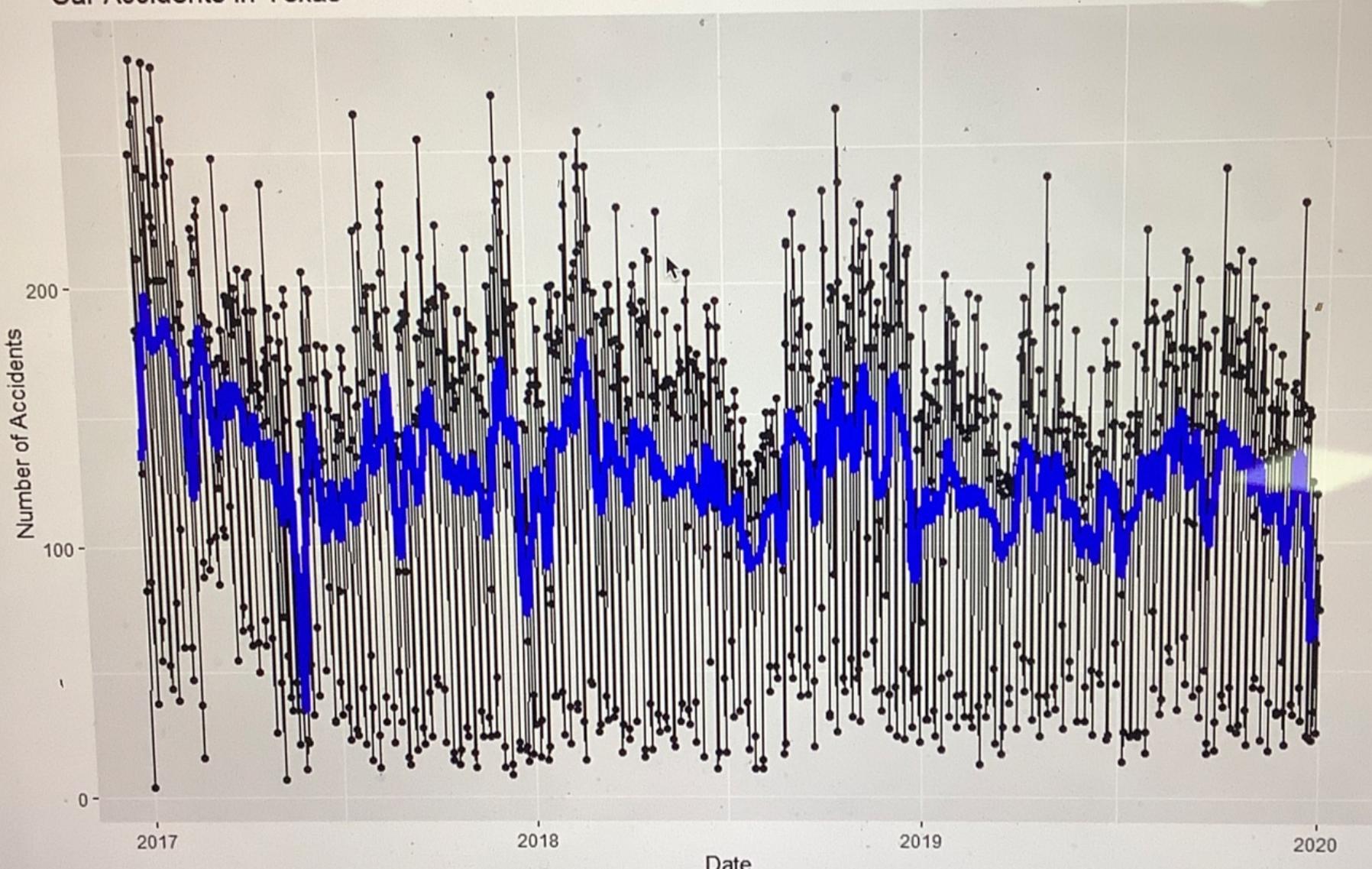
- $a_1 = (\frac{1}{14}, \frac{1}{7}, \frac{1}{7}, \frac{1}{7}, \frac{1}{7}, \frac{1}{7}, \frac{1}{7}, \frac{1}{14})$
- $a_2 = (\frac{1}{60}, \frac{1}{30}, \frac{1}{30}, \dots, \frac{1}{30}, \frac{1}{60})$, where a_2 is length 31

Answer:

$$a_1 = \left(\frac{1}{14}, \frac{1}{7}, \frac{1}{7}, \frac{1}{7}, \frac{1}{7}, \frac{1}{7}, \frac{1}{7}, \frac{1}{14} \right)$$

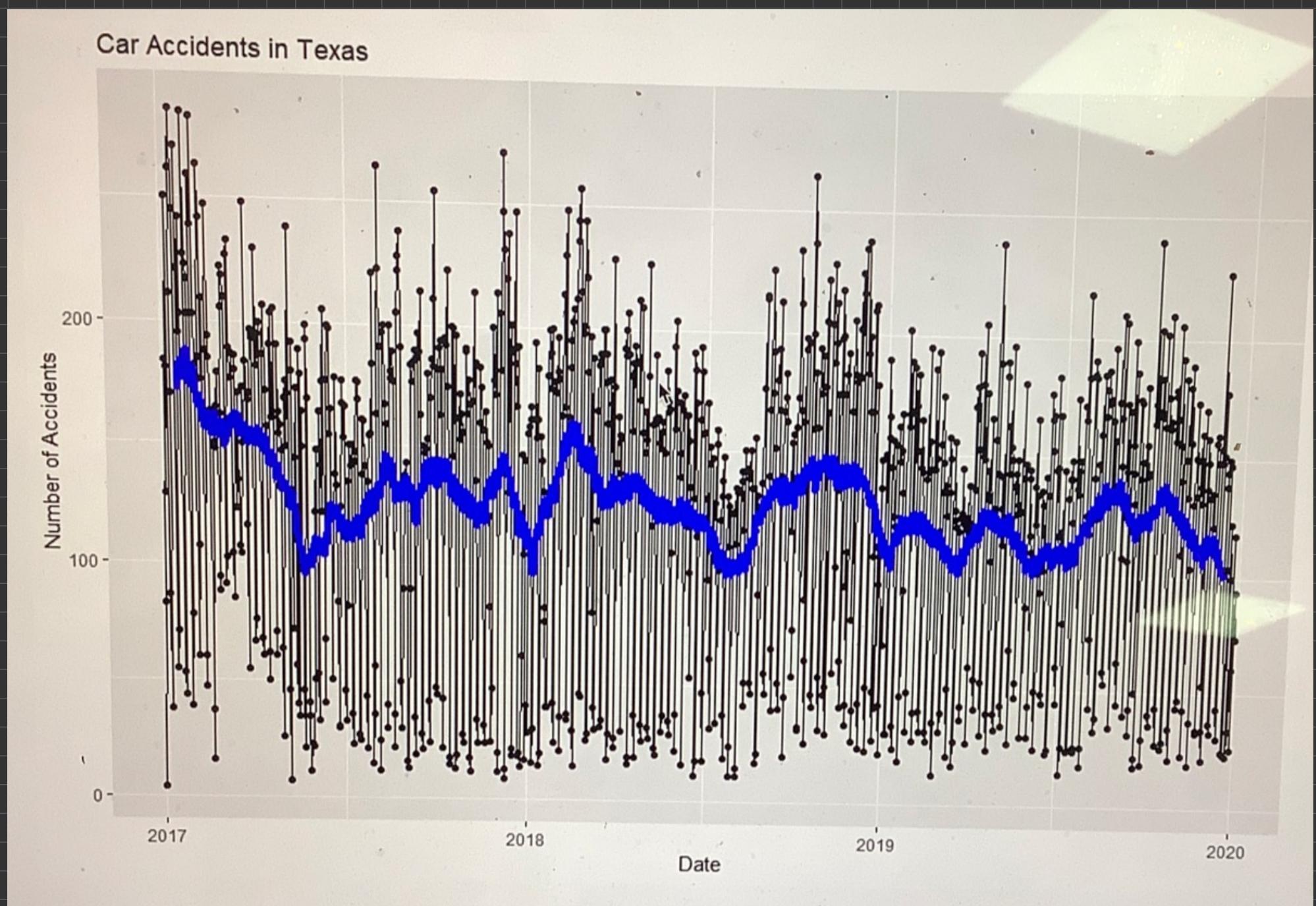
Corresponds to the first plot (this plot)?

Car Accidents in Texas



$$a_2 = \left(\frac{1}{60}, \frac{1}{30}, \frac{1}{30}, \dots, \frac{1}{30}, \frac{1}{60} \right)$$

Corresponds to the second plot (this plot) 2

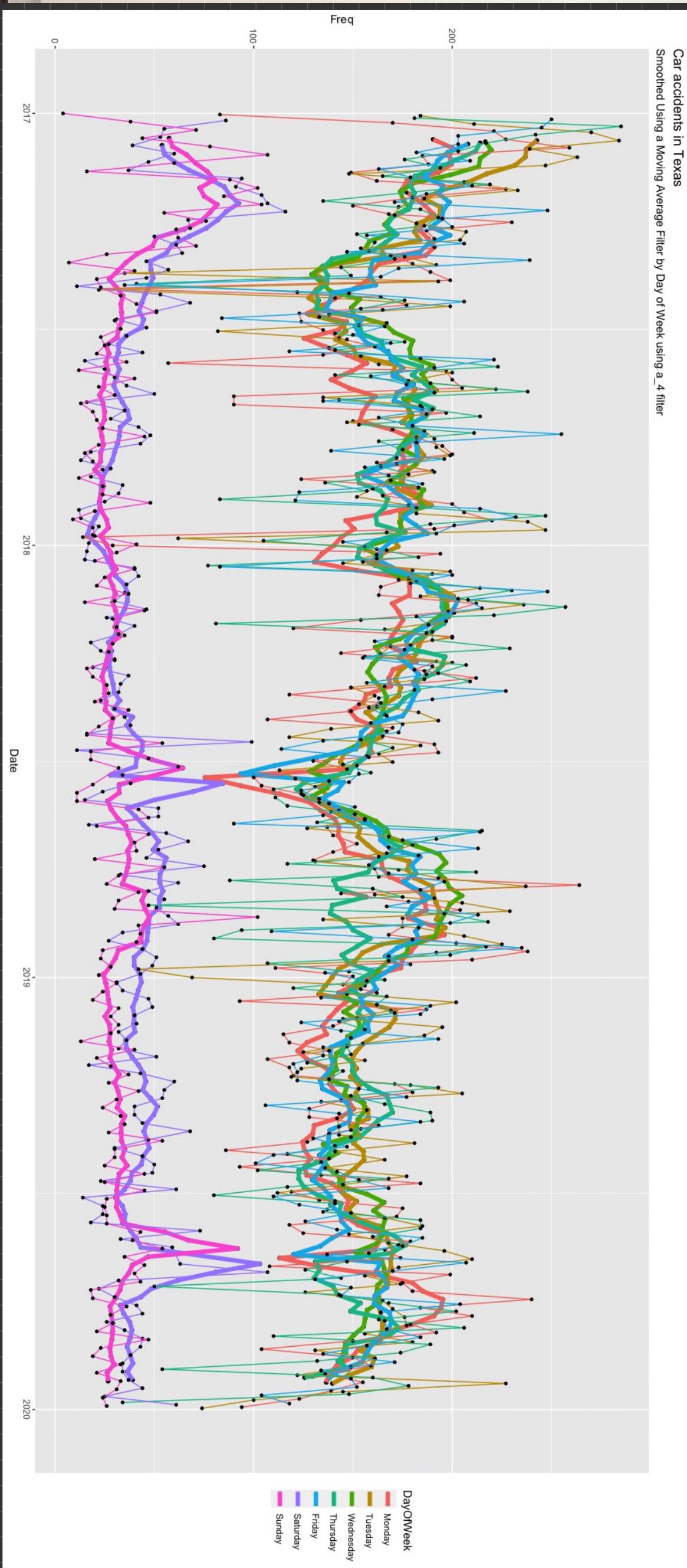


a_2 filter will have a smoother effect than a_1 because each neighbor weight of a_2 is smaller than any of the a_1 filter neighbors weights. If a neighbor value x' differs a lot to the current value x_t at time t or any of the other neighbors considered in the filter window in the original time series; that x' value will be normalized by $\frac{1}{30}$ or $\frac{1}{60}$ in the a_2 filter; making that this does not affect abruptly the trend of the filtered time series.

On the other hand the a_1 weights for any neighbor are either $\frac{1}{7}$ or $\frac{1}{4}$; so if a value abruptly grows or decreases, it will be multiplied by a number greater than any of a_2 weights, hence making that the trend of the filtered time series a_1 be affected more drastically by abrupt changes in neighbor values.

b)

- b. Consider the plot shown in Figure 3 which shows the Moving Average Filter specified by $a_3 = (\frac{1}{3}, 0, 0, 0, 0, 0, 0, \frac{1}{3}, 0, 0, 0, 0, 0, 0, \frac{1}{3})$. Create an analogous plot for the filter $a_4 = (\frac{1}{7}, 0, 0, 0, 0, 0, 0, \frac{1}{7}, 0, 0, \dots, 0, \frac{1}{7})$ where a_4 is of length 43. Explain why the two filtered time series (applying filters a_3 and a_4) differ in terms of their smoothness.



Result:

a_4 filter will have a smoother effect than a_3 . There are many more "0" value weights for neighbors in a_4 than a_3 . Hence, many more neighbors that could abruptly change their value, they are not considered for the filtered a_4 times series trend. Also, any considered neighbor for the a_4 filter will be multiplied by a smaller value than any considered neighbor for the a_3 filter. So, a_4 filter normalizes more any noise with abrupt behaviour, making the general trend to be smoother.

C)

- c. Suppose a legislator wants to know about the effectiveness of a traffic law that went into effect in Texas in September of 2017 that prohibited texting while driving. The legislator appreciates that the daily data on car crashes will be noisy and is willing to consider easy-to-understand summaries of the trend in the series, but is not interested in a fancy statistical analysis using causal inference methods. Provide a reason why assessing the impact of the law on traffic crashes by visual inspection of the filtered time series may not be a good idea.

With the plots obtained with the filters, the legislator could find visually certain trend in the filtered time series after September in 2017. This trend could lead to the conclusion that there is certain correlation in the data after September 2017 when the traffic law went into effect. So, the legislator could be concluding that the law had effect. However, correlation does not imply causation. The fact that there could be certain correlation between the data after September 2017, does not imply that it was due to the traffic law that went into effect. There are many variables that could have NOT been taken into account. For example, it could have been the case that oil price increased after September 2017. Hence, many people in Texas decided to NOT use their cars, affecting the number of crashes.

APPENDIX (CODE)



CODE PART A

```
1 #####  
2 #Importing the libraries to be used  
3 library(ggplot2)  
4 library(gridExtra)  
5 library(tidyverse)  
6 library(astsa)  
7 library(xts)  
8 library(lubridate)  
9  
10 #Importing the data from the csv file  
11 data1 <- read.csv("/Users/rafa/Documents/Master Austin/MAESTRÍA_AUSTIN/Advanced Predictive Models/HW2/file2.xls", header=TRUE, stringsAsFactors=FALSE)  
12 data1_2 <- data.frame(Freq = data1$Freq, Date = as.Date(data1$date))  
13  
14 # Apply kernel smoothing to the imported data  
15 a <- c(1/14, rep(1/7, 6), 1/14)  
16 |  
17 ma_smoothed_data <- data.frame(  
18   Freq = stats::filter(data1$Freq,  
19     sides = 2,  
20     filter = a), Date = as.Date(data1$date))  
21 #Plotting the data and the smoothed time series  
22 gg_data <- ggplot(ma_smoothed_data, aes(x = Date, y = Freq, group=1))+  
23   geom_line(size = 3.5, color = "blue") +  
24   geom_point(shape = 21, size = 1, fill = "white", color = "black") +geom_line(data=data1_2,size=0.5,color="black")  
25  
26 gg_data  
27  
28  
29
```

CODE PART B

```
30 #-----Part b-----  
31  
32 #importing the data from the csv file  
33 data1 <- read.csv("/Users/rafa/Documents/Master Austin/MAESTRÍA_AUSTIN/Advanced Predictive Models/HW2/file2.xls", header=TRUE, stringsAsFactors=FALSE)  
34 data1_2<-data.frame(Freq = data1$Freq, Time = data1>Date, DayOfWeek = data1$DayOfWeek)  
35 #the filtering weights  
36 a<-c(rep(c(1/7,0,0,0,0,0),6),1/7)  
37 #filtered data  
38 ma_smoothed_data <- data.frame(  
39   Freq = stats::filter(data1$Freq,  
40     sides = 2,  
41     filter = a), Time = data1>Date, DayOfWeek = data1$DayOfWeek)  
42 #Splitting the data by day  
43 monday<-data1_2[data1_2$DayOfWeek=="Monday",]  
44 tuesday<-data1_2[data1_2$DayOfWeek=="Tuesday",]  
45 wednsday<-data1_2[data1_2$DayOfWeek=="Wednesday",]  
46 thursday<-data1_2[data1_2$DayOfWeek=="Thursday",]  
47 friday<-data1_2[data1_2$DayOfWeek=="Friday",]  
48 saturday<-data1_2[data1_2$DayOfWeek=="Saturday",]  
49 sunday<-data1_2[data1_2$DayOfWeek=="Sunday",]  
50 # Splitting the smoothed data by day  
51 monday_s<-ma_smoothed_data[ma_smoothed_data$DayOfWeek=="Monday",]  
52 tuesday_s<-ma_smoothed_data[ma_smoothed_data$DayOfWeek=="Tuesday",]  
53 wednsday_s<-ma_smoothed_data[ma_smoothed_data$DayOfWeek=="Wednesday",]  
54 thursday_s<-ma_smoothed_data[ma_smoothed_data$DayOfWeek=="Thursday",]  
55 friday_s<-ma_smoothed_data[ma_smoothed_data$DayOfWeek=="Friday",]  
56 saturday_s<-ma_smoothed_data[ma_smoothed_data$DayOfWeek=="Saturday",]  
57 sunday_s<-ma_smoothed_data[ma_smoothed_data$DayOfWeek=="Sunday",]  
58  
59 # Making that the levels appear in the ggplot in descendin order as Monday, Tuesday, Wednesday, Thursday , Friday, Saturday, Sunday  
60 #instead of having alphabetical order  
61 ma_smoothed_data$DayOfWeek <- factor(ma_smoothed_data$DayOfWeek,  
62                                         levels=c("Monday", "Tuesday", "Wednesday", "Thursday", "Friday", "Saturday", "Sunday"),  
63                                         labels=c("Monday", "Tuesday", "Wednesday", "Thursday", "Friday", "Saturday", "Sunday"))  
64 #Making the plot  
65 gg_all <- ggplot(ma_smoothed_data, aes(x = Time, y = Freq, group=DayOfWeek), colour=DayOfWeek)+geom_point() +geom_line(lwd=2,aes(color=DayOfWeek)) +  
66   geom_line(data=monday, size=0.5, aes(color=DayOfWeek))+geom_point(data=monday, aes(x=Time,y=Freq), shape = 21, size = 1, fill = "black", color = "black") +  
67   geom_line(data=tuesday, size=0.5, aes(color=DayOfWeek))+geom_point(data=tuesday, aes(x=Time,y=Freq), shape = 21, size = 1, fill = "black", color = "black") +  
68   geom_line(data=wednsday, size=0.5, aes(color=DayOfWeek))+geom_point(data=wednsday, aes(x=Time,y=Freq), shape = 21, size = 1, fill = "black", color = "black") +  
69   geom_line(data=thursday, size=0.5, aes(color=DayOfWeek))+geom_point(data=thursday, aes(x=Time,y=Freq), shape = 21, size = 1, fill = "black", color = "black") +  
70   geom_line(data=friday, size=0.5, aes(color=DayOfWeek))+geom_point(data=friday, aes(x=Time,y=Freq), shape = 21, size = 1, fill = "black", color = "black") +  
71   geom_line(data=saturday, size=0.5, aes(color=DayOfWeek))+geom_point(data=saturday, aes(x=Time,y=Freq), shape = 21, size = 1, fill = "black", color = "black") +  
72   geom_line(data=sunday, size=0.5, aes(color=DayOfWeek))+geom_point(data=sunday, aes(x=Time,y=Freq), shape = 21, size = 1, fill = "black", color = "black") +  
73   scale_x_date() +  
74   labs(title = "Car accidents in Texas", subtitle = "Smoothed Using a Moving Average Filter by Day of Week using a_4 filter")  
75 gg_all
```