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Linear Regression and Regularization

The loss function that includes the La penalty is given by

$$\vec{L} = \sum_{i} (\vec{w} \vec{x}_{i} - \vec{y}_{i})^{2} + \lambda |\vec{w}|_{i}^{2}$$

In terms of X (the matrix whose rows are {x.3) and if:

Minimizing I:

$$\frac{\partial I}{\partial \vec{w}} = 2X^T X \vec{w} - 2X^T \vec{y} + 2\lambda \vec{w} = 0$$

$$(X^TX+\lambda^{1})\vec{w} = Y^T\vec{y}$$

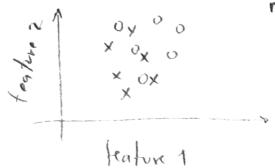
$$\vec{w} = (x^T x + \lambda 1)^T x^T \vec{y}$$

Solution with no regularization: $\vec{w} = (\vec{x} \cdot \vec{x})^T \vec{x}^T \vec{y}$

The solution is changed by the term $\lambda 11$. This penalty prevents the values of \vec{w} from being too high. Higher values of \vec{w} are usually due to overfitting. The penalty then prevents overfitting.

Density Estimation

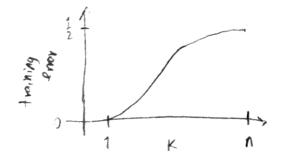
n = number of data points



KNN with K=n: A point has \(\frac{n}{2}\) neighbors from each class. Then the training error is \(\frac{1}{2}\).

KNN with k=1: A point from the training set will be its own neighbor. Then the training error is 0.

The training error would look like



The monotonic behaviour is not gravanteed.

Feature Selection and Prepioussing

There are two main things that could be improved:

- 1) They are selecting the features set F by minimizing the training error using all of the data D. They should use a train-test split and cross-validation to minimize the validation error and safeguard against random chance.
- 2) The validation providere is done on a subset D'CD. The set F was selected by using all of D. There is a train-test contamination. The feature set F will perform good on D' because it was selected based on DCD'. They sould perform this validation on new data.