

## Lista #4

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This question will ask you to solve numerically a heterogeneous-agent economy. Suppose there is a continuum of individuals that are subject to endowment shocks. A person's endowment is  $e^z$ , where  $z$  follows the following stochastic process:

$$z' = \rho z + \varepsilon$$

where  $\varepsilon \sim N(0, \sigma^2)$ . The individual's instantaneous utility function is given by

$$u(c) = \frac{c^{1-\gamma} - 1}{1-\gamma}$$

and they discount the future with the factor  $\beta \in (0, 1)$ . Each person has access to a bond that pays interest rate  $r$ . Their budget constraint can then be written as:

$$c + a' = e^z + (1+r)a$$

Let  $\beta = 0.96$  and  $\gamma = 1.0001$  for now.

The interest rate  $r$  is determined to clear the bond market. The bond is available in zero net supply.

## Exercícios

1. Let  $\rho = 0.9$  and  $\sigma = 0.01$ . Use the Tauchen method to discretize the stochastic process in a Markov chain with 9 states. (Use 3 standard deviations for each side.)
2. Discretize the asset space using a grid and solve the individual's problem for each state variable.
3. Find the stationary distribution  $\pi(z, a)$  and use it to compute the aggregate savings in the economy. Find the equilibrium interest rate.
4. Suppose  $\rho = .97$ . Redo the analysis. How does the interest rate compare now? Explain.
5. Suppose  $\gamma = 5$ . Redo the analysis. How does the interest rate compare now? Explain.
6. Suppose  $\sigma = .05$ . Redo the analysis. How does the interest rate compare now? Explain.
7. Relate your results with Table 2 in Aiyagari (1994).