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```
CONTEXT TrafficLightColors

EXTENDS

SETS

Light

CONSTANTS

red

green

AXIOMS

axm1: false\langle \text{theorem} \rangle Light = \{red, green\}

axm2: false\langle \text{theorem} \rangle red \neq green

END
```

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# CONTEXT PersonIO

Description of the person if physically in or out of the room Description of the person if physically in or out of the room

## **EXTENDS**

#### **SETS**

 ${\bf Person IOS tate}$ 

## **CONSTANTS**

in

out

## **AXIOMS**

```
\begin{minipage}{0.9\textwidth} $\tt axm1: false $\langle theorem \rangle$ $PersonIOS tate = \{out, in\} $\\ \tt axm2: false $\langle theorem \rangle$ $out \neq in $\\ \end{minipage}
```

**END** 

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# **CONTEXT** SensorIO

Context describing the sensor states Context describing the sensor states

## **EXTENDS**

#### **SETS**

SensorState Set of sensor statesSet of sensor states

## **CONSTANTS**

on Sensor signal onSensor signal on off Sensor signal offSensor signal off

## **AXIOMS**

```
axm1: false
\langle theorem \rangle SensorState = \{off, on\} axm2: false
\langle theorem \rangle off \neq on
```

**END** 

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```
CONTEXT Room
Context describing the room states
Context describing the room states

EXTENDS

SETS
RoomState

CONSTANTS
empty
full

AXIOMS
axm1: false⟨theorem⟩ RoomState = {empty, full}
axm2: false⟨theorem⟩ empty ≠ full

END
```

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Room

#### MACHINE m0

First implementation of the model. The entry and exit of a person is considered without any external restriction to the room capacity.

First implementation of the model. The entry and exit of a person is considered without any external restriction to the room capacity.

```
restriction to the room capacity.
REFINES
SEES Room
VARIABLES
       room
INVARIANTS
       inv1: false\langle \text{theorem} \rangle \ room \in RoomState
EVENTS
Initialisation true(extended)
      falsethenbegin
            act1: trueroom := emptyroom := empty
Event Person_Go_In \( \text{ordinary} \) \( \hat{\text{=}} \)
falseextendsrefines
      falsewherewhen
            grd1: false(theorem) trueroom = emptyroom = empty
      truethenbegin
```

falseextendsrefines

end

falsewherewhen

**Event** Person\_Go\_Out ⟨ordinary⟩  $\hat{=}$ 

 $grd1: false \langle theorem \rangle true room = full room = full true then begin act1: true room := emptyroom := empty$ 

act1: trueroom := fullroom := full

**END** 

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#### MACHINE m1

Second implementation of the model. The entry and exit of a person is restringed by a traffic light that denote if the room is empty or full.

Second implementation of the model. The entry and exit of a person is restringed by a traffic light that denote if the room is empty or full. m0

**REFINES** m0

Room, Traffic Light Colors

**SEES** Room, TrafficLightColors

#### **VARIABLES**

room

tfl Traffic Light VariableTraffic Light Variable

#### **INVARIANTS**

```
inv1: false(theorem) tfl \in Light
```

#### **EVENTS**

Initialisation true(extended)

## falsethenbegin

```
\begin{tabular}{ll} {\tt act1: false} & {\tt false} & {\tt room} := empty \\ & {\tt act2: true} & {\tt fl} := red \\ & {\tt end} \\ \end \\ \e
```

**Event** Person\_Go\_In  $\langle \text{ordinary} \rangle =$ 

Person\_Go\_In

#### trueextendsrefines Person\_Go\_In

## falsewherewhen

```
 \begin{array}{ll} & \texttt{grd1: false} \langle \texttt{theorem} \rangle \ \texttt{false} room = emptyroom = empty \\ & \texttt{grd2: false} \langle \texttt{theorem} \rangle \ \texttt{true} tfl = greentfl = green \\ & \texttt{truethenbegin} \\ & \texttt{act1: false} room := fullroom := full \\ & \texttt{act2: true} tfl := redtfl := red \\ & \texttt{end} \end{array}
```

**Event** Person\_Go\_Out  $\langle \text{ordinary} \rangle =$ 

Person\_Go\_Out

# trueextendsrefines Person\_Go\_Out

## falsewherewhen

```
\label{eq:grd1:false} \begin{array}{l} \operatorname{grd1:\ false}\langle \operatorname{theorem}\rangle \ \operatorname{false}room = fullroom = full} \\ \operatorname{truethenbegin} \\ \operatorname{act1:\ false}room := emptyroom := empty \\ \operatorname{end} \end{array}
```

**Event** Traffic\_Switch\_Green ⟨ordinary⟩  $\hat{=}$ 

This is for the signal to know the state of the environment (due to the absence of the output sensor).)

This is for the signal to know the state of the environment (due to the absence of the output sensor).)

### falseextendsrefines

**END** 

# falsewherewhen

```
\begin{array}{c} {\tt grd1: \ false \langle theorem \rangle \ true} room = emptyroom = empty} \\ {\tt grd2: \ false \langle theorem \rangle \ true} tfl = redtfl = red \\ {\tt true} then begin \\ {\tt act1: \ true} tfl := greentfl := green \\ {\tt end} \end{array}
```

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```
MACHINE m2
                                                                                                             m1
REFINES m1
                                                                Room, Traffic Light Colors, Sensor IO, Person IO\\
SEES Room, TrafficLightColors, SensorIO, PersonIO
VARIABLES
       room
       tfl Traffic Light variableTraffic Light variable
       ss Sensor variableSensor variable
       wio Wire from sensor to controllerWire from sensor to controller
       p Person In/Out variablePerson In/Out variable
INVARIANTS
       inv_room1: false(theorem) room = full \Rightarrow tfl = red
       inv_room2: false\langle \text{theorem} \rangle \ room = full \Rightarrow p = in
       inv_ss1: false\langle \text{theorem} \rangle ss \in SensorState
       inv_ss2: false(theorem) ss = on \Rightarrow wio = 0
       inv_ss3: false(theorem) ss = off \land wio = 0 \Rightarrow tfl = red
       inv_wio1: false(theorem) wio \in \{0, 1\}
       inv_wio2: false(theorem) wio = 1 \Rightarrow tfl = green
       inv_wio3: false(theorem) wio = 0 \Leftrightarrow (p = in \land room = full) \lor (p = out \land room = empty)
       inv_wio4: false(theorem) wio = 1 \Rightarrow p = in \land room = empty
       inv_p1: false(theorem) p \in PersonIOState
       inv_p2: false(theorem) p = out \Rightarrow room = empty
EVENTS
Initialisation true(extended)
      falsethenbegin
             act1: falseroom := emptyroom := empty
            act2: falsetfl := redtfl := red
            act4: truewio := 0wio := 0
            act3: truess := offss := off
             act5: truep := outp := out
      end
Event Person_Go_In \( \text{ordinary} \) \( \hat{\text{e}} \)
      Event where the controller knows the signal from the cable (which assumes a person has entered)
      and then changes the state.
      Event where the controller knows the signal from the cable (which assumes a person has entered) and then
                                                                                                 Person_Go_In
      changes the state.
falseextendsrefines Person_Go_In
      falsewherewhen
             grd1: false(theorem) trueroom = emptyroom = empty
             grd2: false(theorem) truewio = 1wio = 1
      truethenbegin
            act1: trueroom := fullroom := full
            act2: truewio := 0wio := 0
             act3: truet fl := redt fl := red
      end
Event Person_Go_Out ⟨ordinary⟩ ≘
      Exit event. As there is no exit sensor, we can assume that both states (To be inside and room is
      full) change simultaneously.
      Exit event. As there is no exit sensor, we can assume that both states (To be inside and room is full)
                                                                                               Person_Go_Out
      change simultaneously.
trueextendsrefines Person_Go_Out
      falsewherewhen
             grd1: false(theorem) falseroom = fullroom = full
             grd2: false(theorem) truep = inp = in
      truethenbegin
             act1: falseroom := emptyroom := empty
```

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```
act2: truep := outp := out
      end
Event Traffic_Switch_Green (ordinary) \hat{=}
      Event where sensor is on and it is satisfied that entry can be allowed.
      Event where sensor is on and it is satisfied that entry can be allowed.
                                                                                      Traffic_Switch_Green
trueextendsrefines Traffic_Switch_Green
      falsewherewhen
            grd1: false\langle \text{theorem} \rangle falseroom = emptyroom = empty
            grd2: false(theorem) falsetfl = redtfl = red
            grd3: false(theorem) truess = onss = on
      truethenbegin
            act1: falsetfl := greentfl := green
      end
Event Sensor_Turn_On (ordinary) \hat{=}
      Event where sensor is on with no one is staging
      Event where sensor is on with no one is staging
falseextendsrefines
      falsewherewhen
            grd1: false(theorem) truess = offss = off
            grd2: false(theorem) truewio = 0wio = 0
      truethenbegin
            act1: truess := onss := on
      end
Event Person_Go_Out_Sensor (ordinary) \hat{=}
      Event where situation satisfied that person who is waiting, can go inside.
      Event where situation satisfied that person who is waiting, can go inside.
falseextendsrefines
      falsewherewhen
            grd1: false(theorem) truetfl = greentfl = green
            grd2: false(theorem) truess = onss = on
      truethenbegin
            act1: truep := inp := in
               Person physically go inside
               Person physically go inside
            act2: truess := offss := off
               sensor is turned off
               sensor is turned off
            act3: truewio := 1wio := 1
      end
END
```

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