

Hennessey Milner Logic (HML)

- Specification by means of properties to be satisfied

Imple \models Property

- Modal (local : either immediate or consecutive properties)

$\langle a \rangle F$: possible a and then F

$[a] F$: whenever we execute a later F

- Global temporal properties still missing
- Semantics capture the intended meaning :

$$\langle a \rangle F \quad \exists p \xrightarrow{a} p' \quad p' \models F$$

$$[a] F \quad \forall p \xrightarrow{a} p' \quad p' \models F$$

Key fact : $p \xrightarrow{a} \Leftrightarrow p \models [a] \text{ff}$

- Negation can be represented by duality

$$p \not\models F \Leftrightarrow p \models F^c \quad (\text{therefore } F^c \sim \neg F)$$

Immediate consequence : formulas have no moral

We can specify impossible requirements : $F \wedge F^c$.

- Semantics of CCS by means of formulas :

Just playing with $p \models F$ the other way around

$$p \sim q \Leftrightarrow (\forall F (p \models F \Leftrightarrow q \models F))$$

Technical requirement : only works for image-finite procs.

- An apparent contradiction : finite formulas fully characterize the behaviour of arbitrary processes

Because an infinite set of finite formulas "perfectly approximate any "infinite property"

- Next we will add recursive formulas that will capture those "infinite properties" in a finite way.