

Analysis Note of the Experiment

Measurement of diffractive Central Exclusive Production of h^+h^- pairs ($h = \pi, K, p$) in proton-proton collisions at $\sqrt{s} = 200$ GeV with forward proton reconstruction in Roman Pot detectors

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Abstract

In this note we present analysis of diffractive Central Exclusive Production using 2015 data from proton-proton collisions at $\sqrt{s} = 200$ GeV. This dataset was collected with newly installed Roman Pot detectors in Phase II* configuration which ensured efficient triggering and measuring diffractively scattered protons. We describe intermediate stages of analysis involving choice of selection cuts, comparison of data with Monte Carlo models folded into detector acceptance, and study of systematic uncertainties specific to the analysis. Finally, we show the physics outcome of the analysis. Parts of the analysis which are of more technical nature (calculation of efficiencies, derivation of corrections to efficiencies, adjustment of the STAR simulation, systematic uncertainty of efficiencies) are described in a supplementary analysis note [1].

ver. 2.0

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List of contributions¹

Leszek Adamczyk	Analysis coordination/supervision, production of picoDST, production of embedded MC samples
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Change log

21 Nov 2019	ver. 1.0	Initial revision
3 Feb 2020	ver. 2.0	Modifications and corrections at the GPC level: - corrected detector resolutions (Sec. 6.5), - introduced RP total efficiency correlation (Sec. 6.2.3 and Appendix E), - extended the closure tests (Sec. 6.6.2), - added luminosity uncertainty systematics (Sec. 7.1), - added systematic uncertainty related to TPC track quality cuts (Sec. 7.3), - corrected MC predictions drawn on Figs. 5.11 and 5.12

¹See also list of contributions in Ref. [1], since presented document utilizes all fruits of work described in referenced note. Reference [1] should be treated as a note supplementary to the current document.

1. Introduction

1.1 Central Exclusive Production

The Central Exclusive Production (CEP) takes place when interacting particles form in the mid-rapidity region a state X (“central production”) and no other particles are produced in possible additional interactions between initial state particles (“exclusive”). The initial state particles can either dissociate, excite or stay intact. The latter case of CEP in proton-proton collisions can be written as

$$p + p \rightarrow p + X + p \quad (1.1)$$

and depicted as in Fig. 1.2. Mass and rapidity of state X is related to forward protons kinematics by

$$M_X = \sqrt{s} \left(\xi_1 \xi_2 \sin^2(\alpha/2) - (1 - \xi_1 - \xi_2) \cos^2(\alpha/2) \right) \stackrel{\alpha=\pi}{=} \sqrt{s \xi_1 \xi_2}, \quad (1.2) \quad y_X = \frac{1}{2} \ln \frac{\xi_1}{\xi_2}, \quad (1.3)$$

where α is angle between scattered protons and $\xi = (|\vec{p}_0| - |\vec{p}|)/|\vec{p}_0|$ is the fractional momentum loss of proton.

1.2 Double IPomeron Exchange

Reaction from Eq. (1.1) can exhibit purely electromagnetic ($\gamma\gamma$ interaction), mixed ($\gamma\mathcal{O}$ interaction) or purely strong nature ($\mathcal{O}\mathcal{O}$ interaction). The last type is dominant at RHIC energies. In this energy regime it is typically characterized by the lack of hard scale, therefore perturbative QCD cannot be applied and Regge theory [2] is used instead. An object \mathcal{O} does not have unequivocal QCD representation - in Regge formalism it is the so-called “trajectory” (IReggeon, IR). IReggeon with quantum numbers of vacuum is called ”IPomeron“ (IP) and IP-IP reaction (Fig. 1.1) is called ”Double IPomeron Exchange“.

Processes involving IPomeron exchange are referred as diffraction due to cross-section in scattering angle resembling similar shape to intensity pattern of diffracted light. For low values of Mandelstam t (small scattering angles) cross-section takes exponential form

$$\frac{d\sigma}{dt} \propto e^{-B|t|}, \quad (1.4)$$

where the slope parameter B reflects the transverse size of the interaction region.

Diffractive events have specific property of the ”rapidity gap“ which is an angular region free of hadrons. In DIPPE two such gaps are present, marked in Fig. 1.2 as $\Delta\eta_1$ and $\Delta\eta_2$. Figure 1.3 shows the topology of the DIPPE event on top of the STAR detector, with centrally produced particles marked with green arrows and two forward protons escaping the interaction point inside the beampipe drawn with red arrows.

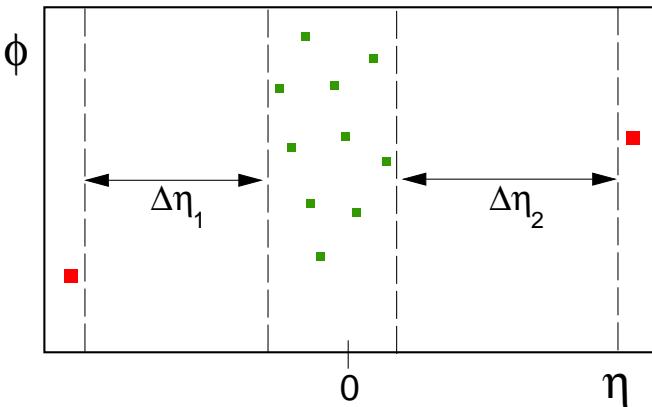


Figure 1.2: CEP represented in $\eta\phi$ space.

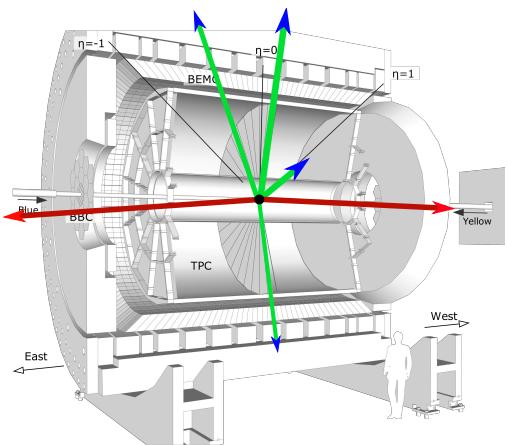


Figure 1.3: Central Production event at STAR.

DIPE is a spin-parity filter - the fact that scattered particles have all quantum numbers unchanged after the interaction, only production of central states satisfying Eq. (1.5) is allowed

$$I^G J^{PC} = 0^+ \text{even}^{++}. \quad (1.5)$$

The lowest order QCD picture of the IPomeron is a pair of oppositely colored gluons (colour singlet). This fact makes the DIPE recognized as the gluon-rich environment process in which bound states of gluons ("glueballs") or hybrid mesons could be produced.

For detailed introduction to the topic of diffraction see Refs. [3, 4].

1.3 Physics motivation for the measurement

STAR collected in 2015 large dataset dedicated for measurement of the Central Diffraction (DIPE in particular). Since that year the experiment was enriched with Roman Pot Phase II* subsystem and thus gained possibility of detection of forward scattered protons. It enabled studies of properties of the central state with respect to observables related to exchanged IPomerons. No such measurement was performed before at that high c.m.s. energy ($\sqrt{s} = 200$ GeV) characterized by small contamination from subleading Reggeon exchanges, which makes it particularly attractive. A brief list of physics issues that can be covered with the study described in this note is briefly introduced below.

1.3.1 DIPE differential cross-sections, mass spectrum

As stated in Sec. 1.2 DIPE is dominantly a soft process whose theoretical description is done mainly using phenomenological tools, thus measurement of differential cross-sections may help to verify various production models.

The main focus is put on the simplest state (and most numerously) produced in DIPE, namely a pair of oppositely charged pions, $\pi^+\pi^-$. It can be formed either in a non-resonant or resonant mechanism. In the first case the $\pi^+\pi^-$ continuum can be modelled by the exchange of the off-shell pion between IPomerons. Currently there are two models of this reaction on the market [5, 6], [7]. In the second case the IPomerons directly couple into resonance (e.g. $f_2(1270)$), which then decays to $\pi^+\pi^-$. Attempts to calculate cross-section for this production mechanism are presented in Ref. [6] and [8].

Understanding of the mass spectrum in $\pi^+\pi^-$ channel is important to learn about relative contribution from continuum and resonant production, as well as relative production of resonances. Recognition of resonant states may indicate candidates for low-mass glueballs of $J^{PC} = 0^{++}$, however presence of underlaying scalar $q\bar{q}$ states makes this task challenging.

Other channels, like K^+K^- , are also of great interest. Comparison of the cross-sections for production of $\pi^+\pi^-$ and K^+K^- gives information about strength of the IPomeron coupling to different quark flavors. Also, structures in $d\sigma/dm$ can be easier attributed to resonances by measuring more than one channel and known branching ratios thereof.

Detection of intact protons scattered at very small angle with respect to the beamline enables determination of the reaction plane which makes the Partial Wave Analysis (PWA) more precise and differential in few more variables. It also allows to look at the the cross-sections more differentially, especially with respect to properties of exchanged IPomerons, like carried squared four-momentum t , azimuthal separation of IPomerons in the transverse plane $\Delta\varphi$ or relative momentum of IPomerons Δp_T . The last quantity was proposed to suppress pure $q\bar{q}$ states with respect to these with gluonic content [9].

1.3.2 Absorption and rescattering effects

One can imagine in diagram in Fig. 1.1 additional soft lines e.g. between protons in the initial state, or protons or central state particles in the final state. These so-called rescattering effects (or absorption effects) lead to production of hadrons other than these belonging to central state X hence the diffractive signature of an event in form of rapidity gap is no longer present. Additionally, rescattering may not lead to production of additional hadrons but to redistribution of exclusive cross section over different regions in phase space. Measurement of the probability that the state X will remain exclusive and forward protons will remain intact, in other words the rapidity gap survival probability S^2 , would be valuable ingredient for development of absorption models.

1.3.3 Size of interaction region

From the measurement of protons in Roman Pots one is able to reconstruct squared four-momenta transferred in proton-IPomeron vertices and determine the differential cross-section $d\sigma/d|t|$. Fit of exponent allows to extract the slope parameter B . Knowledge on the slope parameter gives insight to the transverse size of the interaction region.

2. Data set

2.1 Trigger

Presented analysis made use of data taken in 2015 during $p + p$ collisions at $\sqrt{s} = 200$ GeV. The main trigger designed for studies of Central Diffraction in run 15 was RP_CPT2. It was formed of the following conditions combined by logical AND ($\&\&$):

1. **(ET $\&\&$!IT) || (!ET $\&\&$ IT)** = signal in at least one RP on each side of the STAR central detector - to ensure presence of two forward-scattered protons; a veto was imposed on simultaneous signal in RPs above and below the beamline, which might have originated either from proton dissociation, or pile-up event,
2. **!BBC-E $\&\&$!BBCW $\&\&$!ZDCE $\&\&$!ZDCW** = veto on any signal in small BBC tiles or ZDCs on any side of STAR central detector - such requirement is in accordance with the double-gap topology of CEP events, it mostly filtered out CEP events with proton(s) dissociation or parallel pile-up event(s),
3. **TOF ≥ 2** = at least 2 hits in TOF - aim of this condition was to ensure activity in the mid-rapidity; since the lowest multiplicity allowed in CEP is 2, that was the lower threshold of L0 TOF multiplicity.

This trigger was running with an average prescale of 5 and average DAQ rate of 250 Hz, which allowed to collect in total about 560 M events corresponding to 16.5 pb^{-1} of integrated luminosity. More information about number of events per run, rates etc. can be found under link provided in Ref. [10], which contains selected data from STAR run log [11]. Luminosity data used in this analysis comes from Ref. [12].

All RP triggers which were intended for usage in diffractive physics analyses or efficiency studies are listed in Tab. 2.1. Components used in definitions of these triggers are outlined in Fig. 2.1. Detailed explanation of all trigger bits can be found in Refs. [13, 14]. Explanation of naming convention in Roman Pot system can be found in Ref. [15].

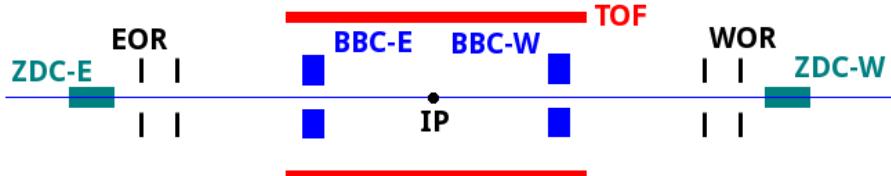


Figure 2.1: Sketch of the trigger components used in definitions of diffractive triggers in run 15.

Trigger name	Definition	Events [M]	Comment
RP_CPT	EOR $\&\&$ WOR	73.3	Loose trigger (mostly elastic events) designed for monitoring/trigger efficiency study
RP_CPT	EOR $\&\&$ WOR $\&\&$!BBC-E $\&\&$!BBCW $\&\&$!ZDCE $\&\&$!ZDCW $\&\&$ TOF ≥ 1	38.9	Intended to be main CEP trigger (later switched to RP_CPT2 due to large prescale avoided in RP_CPT2 by larger suppression of backgrounds)
RP_CPT2	(ET $\&\&$!IT) (!ET $\&\&$ IT) $\&\&$!BBC-E $\&\&$!BBCW $\&\&$!ZDCE $\&\&$!ZDCW $\&\&$ TOF ≥ 2	556.5	Main CEP trigger Note: On Apr 14 added upper TOF limit (10)
RP_CPX	IT $\&\&$!BBC-E $\&\&$!BBCW $\&\&$!ZDCE $\&\&$!ZDCW $\&\&$ TOF ≥ 2	40.1	The same as RP_CPT2 but only IT configuration
RP_CPEI	ET $\&\&$ IT $\&\&$!BBC-E $\&\&$!BBCW $\&\&$!ZDCE $\&\&$!ZDCW $\&\&$ TOF ≥ 2	15.6	Control trigger for CPT2 to estimate effect of !(ET $\&\&$ IT) veto

Table 2.1: Central Diffraction physics triggers and control triggers involving Roman Pot detectors in run 15.

2.2 Reconstruction software

Raw data was processed with STAR libraries in versions SL17f. All four trigger datasets were processed: production_pp200trans_2015, production_pp200long2_2015, production_pp200long3_2015 and production_pp200long_2015 (see [16]).

The following BFC options were used in the reconstruction:

```
DbV20160418,pp2015c,btof,mtd,mtdCalib,pp2pp,-beamline,beamline3D,useBTOFmatchOnly,VFStoreX,  
fmsDat,fmsPoint,fpsDat,BEmcChkStat,-evout,CorrX,OSpaceZ2,OGridLeak3D,-hitfilt
```

Main attention should be put on option **useBTOFmatchOnly** which forced vertexing algorithm to form vertices only from the global TPC tracks which are matched with hits in the TOF system. This solution was found to yield significantly larger signal reconstruction efficiency (vertexing efficiency) and better resolutions. The study which lead to above conclusions, presented in Ref. [17], was performed on the same dataset processed with older libraries SL15k (without useBTOFmatchOnly option).

2.3 Data format

The analyzed data was stored in ROOT files in the picoDST format which was in large part a skimmed MuDST (standard STAR format). The picoDST format was introduced in Ref. [18]. PicoDST description files (C++ headers etc.) can be found in the analysis code repository [19].

3. Monte Carlo simulations

This chapter contains description of MC generators and MC samples used for determination of signal event reconstruction and selection efficiency (Sec. 3.1), modelling of background contribution (Sec. 3.2), and comparison of hadron level cross sections with model predictions (Sec. 3.3). Apart from described samples also single particles (π , K , p) embedded into zero-bias data were used for the purpose of the TPC and TOF reconstruction efficiency calculations, but their description is omitted here as related calculations were presented in Ref. [1].

3.1 Exclusive signal

3.1.1 GenEx $\pi^+\pi^-$ embedded into zero-bias data

Signal sample with exclusive $\pi^+\pi^-$ was prepared with GenEx [20] event generator. Each event has been passed independently through Geant3 simulation of the STAR detector (STARsim) and Geant4 simulation of the RP Phase II* detectors, merged at the end and fully embedded into the same zero-bias data event. Before passing through the STAR detector model, events were filtered in order to gain production efficiency. At the particle level pions were required to have $p_T > 0.15$ GeV and $|\eta| < 1$, while forward scattered protons (after added beam divergence) were required to fit within fiducial region envelope (Eq. (4.4)) extended by 3 standard deviations of the angular beam divergence.

3.1.2 Forward scattered protons embedded into zero-bias data

Independent embedded MC sample was prepared especially for determination of the RP track reconstruction and selection efficiency. Large sample of forward scattered protons from GenEx was simulated in Geant4 and embedded into zero-bias data. The same runs were simulated from which data were used in the physics analysis. Independent forward proton MC embedded into zero-bias data had advantage in possibility of using entire sample of zero-bias triggers - it is different in case of TPC signal embedding, when only small fraction of data (“adc files”) carries enough information for MC and data overlay.

3.1.3 Fast MC generator for particle identification studies

Corrections reflecting identification efficiency and misidentification probability requires good modeling of detector response in terms of dE/dx and TOF time ($\rightarrow m_{\text{TOF}}^2$) measurement, which were used for this purpose as described in Sec. 4.2.7. In addition to this, significant number of simulated events is needed to reduce statistical uncertainties of efficiency. The former was provided by adjusting dE/dx spectra from embedded MC to match the data, as elaborated in Chap. 7 of Ref. [1]. The latter, however, was not easy to achieve for exclusive K^+K^- and $p\bar{p}$ whose identification is most challenging and information about identification efficiency is the most needed among studied species. Specially for study of particle (exclusive pair) identification a dedicated MC simulation was prepared.

This dedicated MC simulation was designed to work as follows (simulation of single CEP event of predefined pair ID is described):

1. The position of z_{vtx} was drawn from predefined distribution.
2. Kinematics of central state particles was set: momentum (magnitude) p , pseudorapidity η and azimuthal angle ϕ of positive and negative charge particles were drawn from predefined distributions.
3. Both particles were tested if doubled radius of curvature $2R$ of associated track in the magnetic field of the TPC ($B = 0.5$ T, $R \propto p_T/B$) is smaller than the radius of TOF detector barrel (assumed 212 cm). If not then event was skipped and procedure was restarted (back to 1.).
4. The particles were propagated from the vertex at $(0, 0, z_{\text{vtx}})$ through the magnetic field of TPC using Newton’s method with the time step (in the laboratory) equal 100 ps, corresponding to space step < 3 cm.
5. After step 4. the position of the TOF cell was known allowing to calculate the TOF path length L between the vertex and position of the TOF hit. Also the TOF hit time t was then known, further smeared by adding random number from normal distribution with mean at 0 and standard deviation $\sigma_{\text{TOF}} = 60$ ps to account for the finite TOF time measurement resolution. In addition to this, reconstructed tracks’ (transverse) momenta were defined as the true momenta smeared by 6 MeV if $p_T < 0.3$ GeV or by $2.4 \text{ MeV} + 1.2\% \times p_T$ if $p_T > 0.3$ GeV, to account for finite TPC momentum resolution. At this stage it was possible to calculate m_{TOF}^2 using Eq. (C.8).

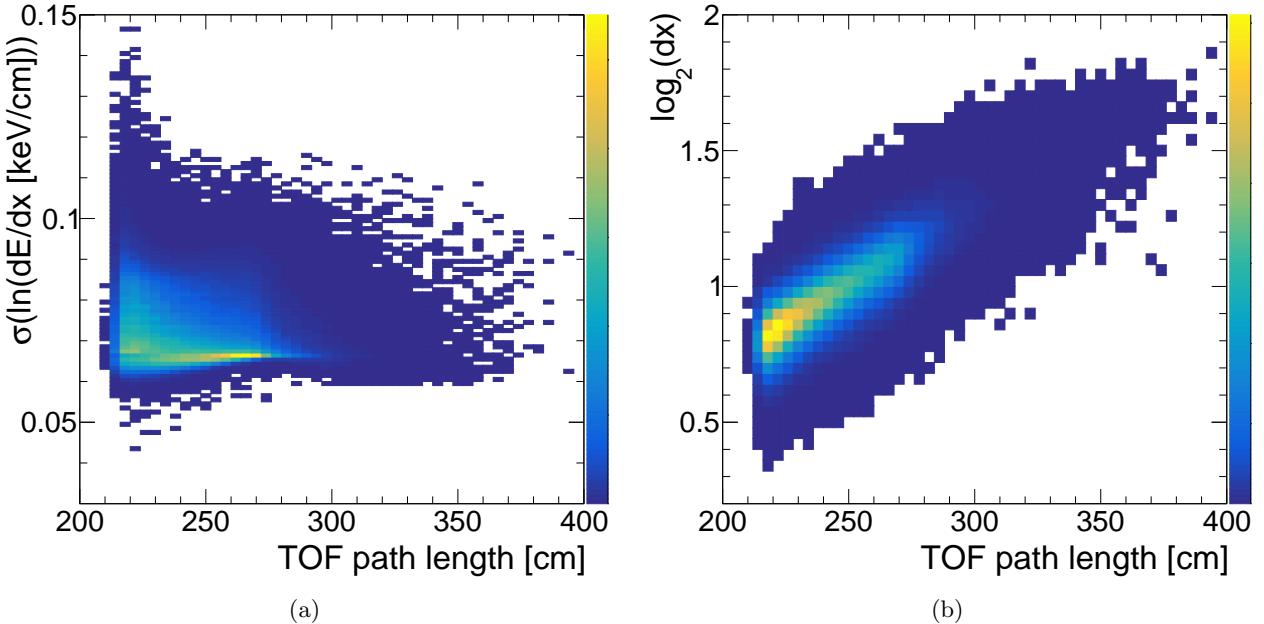


Figure 3.1: Correlation between uncertainty of the natural logarithm of $dE/dx/(1 \text{ keV}/\text{cm})$ and track TOF path length (3.1a) and correlation between base 2 logarithm of dx and track TOF path length (3.1b). The distributions were obtained for the exclusive event candidates after full selection, with all three types of particle pairs combined.

6. The dE/dx measurement was simulated. For each particle a dE/dx was drawn from the distribution of the form given by Eq. (7.6) and of parameters (for given particle ID and momentum) which were extracted from the data and tabulated in Tab. 7.1, all contained in Chap. 7 of Ref. [1]. This assured that the simulated dE/dx exactly matched the data. Once dE/dx for both particles (tracks) was obtained, value of the dE/dx error (more strictly: uncertainty of $\ln(dE/dx [\text{keV}/\text{cm}])$) and value of $\log_2(dx)$ was also set up. These quantities depend on the number of TPC hit points used in the reconstruction of dE/dx (the more hits in tracks, the better resolution of dE/dx and higher dx), which obviously is not accessible without full STAR simulation in Geant. This problem was solved by extracting dependence of $\sigma(\ln(dE/dx))$ and $\log_2(dx)$ on the TOF path length from the data (from CEP events, Fig. 3.1). Since the length of the TOF path is very strongly correlated with the number of hits forming the track and thus number of hits used to reconstruct dE/dx , one is allowed to draw $\sigma(\ln(dE/dx))$ and $\log_2(dx)$ from their distributions for particular TOF path lengths calculated in 5. and use as measured ones. In this way the simulation preserves relevant connections between dE/dx -related quantities. After these steps are taken the $n\sigma_X$ ($X = \pi, K, p$) variables are calculated for each track using the definition (Eq. (4.9)), in exactly the same way as it is done during standard data reconstruction.
7. Event information needed to study pair identification was stored in the ROOT tree: ID of particles forming a pair, their three-momenta, m_{TOF}^2 , $n\sigma_\pi$, $n\sigma_K$ and $n\sigma_p$.

For the purpose of determination of pair identification efficiency in CEP analysis described in this note, parameters of vertex distribution were set to match the data: $\langle z_{\text{vtx}} \rangle = 0$ and $\sigma(z_{\text{vtx}}) = 50 \text{ cm}$, as well as z_{vtx} was required to lie within the analysis limits (cut C2). Distribution of particle η was set to flat and limited to analyzed range $|\eta| < 0.7$, while particle ϕ was defined as uniformly distributed in full azimuth ($2\pi \text{ rad}$), both fairly agreeing with expectations from physics models and observations in data.

3.2 Background modelling

The following MC samples were used to study non-exclusive backgrounds:

- Central Diffraction (CD) events from Pythia 8.1 generator with MBR model of IPomeron flux, filtered at generation to ensure lack of signal in BBC-large, passed through Geant3 simulation of the STAR detector (STARsim) and Geant4 simulation of the RP Phase II* detectors, partially embedded into zero-bias data (only the simulated RP response embedded),

- Minimum Bias events from Pythia 8.1 generator with MBR model of IPomeron flux, filtered at generation to ensure lack of signal in BBC-large, passed through Geant3 simulation of the STAR detector (STARsim) and Geant4 simulation of the RP Phase II* detectors, partially embedded into elastic trigger (RP_ET) data (only the simulated RP response embedded).

Listed background samples were not fully embedded since large amount of CPU time would be required to obtain satisfactory statistics, while they were expected to only provide qualitative description of the backgrounds. It was also found unnecessary to embed TPC tracks into zero-bias data to obtain reliable agreement between distributions of desired quantities presented below.

MC samples from Pythia generator were additionally filtered before passing through Geant to increase generation efficiency, as well as overcome difficulty arising from missing simulation of the BBC-large in STARsim. For each event, all charged particles were analytically propagated through the magnetic field of TPC with the helical paths resulting from their hadron-level momenta. If any of these particles crossed the volume of BBC-large detector, event was dropped from generation.

3.3 Model predictions

The following MC samples were produced for comparisons of the measured cross section with model predictions. The list contains all models which are currently available.

3.3.1 GenEx

The GenEx [20] event generator is based on a simple phenomenological models [5, 21] of continuum production mechanism of $\pi^+\pi^-$ or K^+K^- pairs. In the implemented model absorption corrections are not taken into account explicitly. A damping factor was estimated to be of the order of 2-5 ($\pi^+\pi^-$) and 2 (K^+K^-) [22]. To account for absorption the cross sections obtained from GenEx are scaled by 0.25 and 0.4 for $\pi^+\pi^-$ and K^+K^- , respectively, to fit DiMe predictions which include absorption effects (see below). Predictions are also sensitive to the choice of meson form factor. GenEx predictions are shown using exponential form factor with $\Lambda_{off}^2 = 1.0 \text{ GeV}^2$. Changes of Λ_{off}^2 by 50% lead to cross section changes up to a factor of 2.

3.3.2 DiMe

The DiMe [7] event generator is also based on a simple phenomenological model [23] of continuum production mechanism of $\pi^+\pi^-$ or K^+K^- pairs. However, DiMe in contrary to GenEx models absorption effects with four different models for absorption available. The prediction from "model 1" giving the best consistency with data is used in the comparisons. DiMe predictions are also sensitive to the choice of meson form factor. Three different parameterizations of meson form factor are implemented. We chose exponential form with the same slope as used for GenEx predictions. Therefore the differences between GenEx and DiMe are almost entirely due to the absorption.

3.3.3 Pythia8 MBR

The MBR model [24] implemented in PYTHIA8 [25] was founded to describe inclusive central diffraction (CD, $p + p \rightarrow p + X + p$) cross section at CDF while exclusive h^+h^- state occurs from fragmentation and hadronization of the central state based on the Lund string model. MBR model implemented in PYTHIA8.165 allows generation of the central state starting from the mass threshold of $2m_h$. In later versions region below 1 GeV mass was excluded. Therefore PYTHIA8 expectations for very low masses are in question but are shown for completeness.

4. Event selection

Complete list of analysis cuts used for signal extraction is presented in Sec. 4.1. Detailed description of each cut can be found in Sec. 4.2. [For PDF readers: you can directly move to description of given cut by clicking on corresponding bold cut number **CX** at the start of line in the list of cuts.]

4.1 List of cuts¹

C1. Exactly 1 primary vertex with TPC track(s) matched with hits in TOF.

C2. TPC vertex from C1 is placed within $|z_{\text{vtx}}| < 80$ cm.

C3. Exactly 2 opposite-sign primary TPC tracks (C3.2) of good quality (C3.4) matched with hits in TOF (C3.1) and reconstructed within kinematic region of high TPC acceptance (C3.3), with associated global tracks characterized by small distance of closest approach (DCA) to the primary vertex (C3.5) and high proximity to each other at the beamline (C3.6).

C3.1. Exactly 2 TOF-matched (match flag > 0) primary tracks and no additional primary tracks matched with BEMC clusters,

C3.2. Tracks are of opposite signs,

C3.3. Both tracks are contained within the kinematic range: $|\eta| < 0.7$, $p_T > 0.2$ GeV,

C3.4. Associated global tracks satisfy quality criteria: $N_{\text{hits}}^{\text{fit}} \geq 25$, $N_{\text{hits}}^{\text{dE/dx}} \geq 15$, $|d_0| < 1.5$ cm,

C3.5. Associated global tracks match well to the prim. vertex: $\text{DCA}(R) < 1.5$ cm, $|\text{DCA}(z)| < 1$ cm,

C3.6. Associated global tracks are close at the beamline: $|\Delta z_0| < 2$ cm.

C4. Exactly 1 RP track on each side of STAR central detector (C4.3) of good quality (C4.1), with local angles consistent with the IP being the track origin (C4.2), lying within fiducial region of high geometrical acceptance (C4.4).

C4.1. RP tracks contain only track-points with at least 3 (out of 4) planes used in reconstruction,

C4.2. Local angles (θ_x^{RP} , θ_y^{RP}) consistent with expectation for protons originating from the IP

$$-2 \text{ mrad} < \theta_x^{\text{RP}} - x^{\text{RP}}/|z^{\text{RP}}| < 4 \text{ mrad}, \quad -2 \text{ mrad} < \theta_y^{\text{RP}} - y^{\text{RP}}/|z^{\text{RP}}| < 2 \text{ mrad},$$

C4.3. Exactly 1 track passing cuts C4.1-C4.2 per side,

C4.4. Tracks passing cut C4.3 lie within the fiducial (p_x, p_y) region defined as:

$$0.2 < |p_y| < 0.4, \quad -0.2 < p_x, \quad (p_x + 0.3)^2 + p_y^2 < 0.5^2 \quad (\text{all in GeV}).$$

C5. Vertex z -positions measured in TPC and reconstructed from the difference of proton detection time in west and east RPs are consistent with each other within the resolution (at $3.5\sigma_{\Delta z_{\text{vtx}}}$ level):

$$|\Delta z_{\text{vtx}}| = |z_{\text{vtx}}^{\text{TPC}} - z_{\text{vtx}}^{\text{RP}}| < 36 \text{ cm}.$$

C6. No signal in any tile of BBC-large (east or west) with $\text{ADC} > \text{ADC}_{\text{thr}}$ and $100 < \text{TDC} < 2400$, where ADC_{thr} is specific for each channel (see Tab. 4.1).

C7. Maximally 3 reconstructed TOF clusters $N_{\text{cltrs}}^{\text{TOF}} \leq 3$.

C8. Particle/pair identification (PID):

C8.1. Identification of particle pairs based on dE/dx (χ^2) and m_{TOF}^2 (def. in Sec. 4.2.7 and App. C):

```
if  $\chi^2(\pi\pi) > 9$  and  $\chi^2(KK) > 9$  and  $\chi^2(pp) < 9$  and  $m_{\text{TOF}}^2 > 0.6$  GeV →  $p\bar{p}$ 
elif  $\chi^2(\pi\pi) > 9$  and  $\chi^2(KK) < 9$  and  $\chi^2(pp) > 9$  and  $m_{\text{TOF}}^2 > 0.15$  GeV →  $K^+K^-$ 
elif  $\chi^2(\pi\pi) < 12$  →  $\pi^+\pi^-$ .
```

C8.2. Restricting fiducial cuts on K^+K^- and $p\bar{p}$ (to reduce misidentifications and assure high PID eff.):

```
if  $K^+K^-$ :  $p_T > 0.3$  GeV,  $\min(p_T^+, p_T^-) < 0.7$  GeV
if  $p\bar{p}$ :  $p_T > 0.4$  GeV,  $\min(p_T^+, p_T^-) < 1.1$  GeV
```

C9. Missing (total) momentum of TPC tracks and RP tracks $p_T^{\text{miss}} < 75$ MeV.

¹Some cuts (e.g. C3) are decomposed to constituent sub-cuts. Cut is formed by the logical AND of all its sub-cuts. Events must pass all cuts to be identified as a signal.

4.2 Description of cuts

4.2.1 (C1,C2) Primary vertex and its z -position

As it was designed in the trigger logic, we aim to perform CEP analysis in a clean, pile-up-free environment, therefore we cut on primary vertex multiplicity (Fig. 4.1) to reject events with more than one interaction per bunch crossing. We required exactly one primary vertex containing TPC tracks matched with hits in TOF (matching of the track with hit in TOF is identified with the TOF match flag being different from 0). Later in the text we refer to such events as a single “TOF vertex” events.



Figure 4.1: Primary vertex multiplicity. Red arrow marks bin with events with exactly one primary vertex (with track(s) matched with hit in TOF), which are used in physics analysis. Expectations from embedded $\pi^+\pi^-$ signal MC (normalized to the content of the single TOF vertex bin) has also been shown.

The single TOF vertex was required to be placed within a range (-80 cm, 80 cm) along the z -axis (Fig. 4.2). Events with vertices away from the nominal IP have low acceptance both for the central tracks and the forward protons (comparing to events with vertices close to nominal IP), therefore we reject them as their inclusion to analysis would naturally introduce large systematic uncertainties. See Sec. 3.2.3 in Ref. [1].

In Fig 4.3 we show comparison of the z -position of single TOF primary vertex measured in the TPC, between data and MC generated e.g. to study of detector effects present in analysis. The ratio of distributions which is compatible with unity indicates proper position, width and shape of distribution assumed at MC generation (gaussian with mean at 0 and width of 50 cm).



Figure 4.2: z -position of the primary vertex in single TOF vertex events (passing cut C1). Red dashed line indicate range of longitudinal vertex position accepted in analysis.

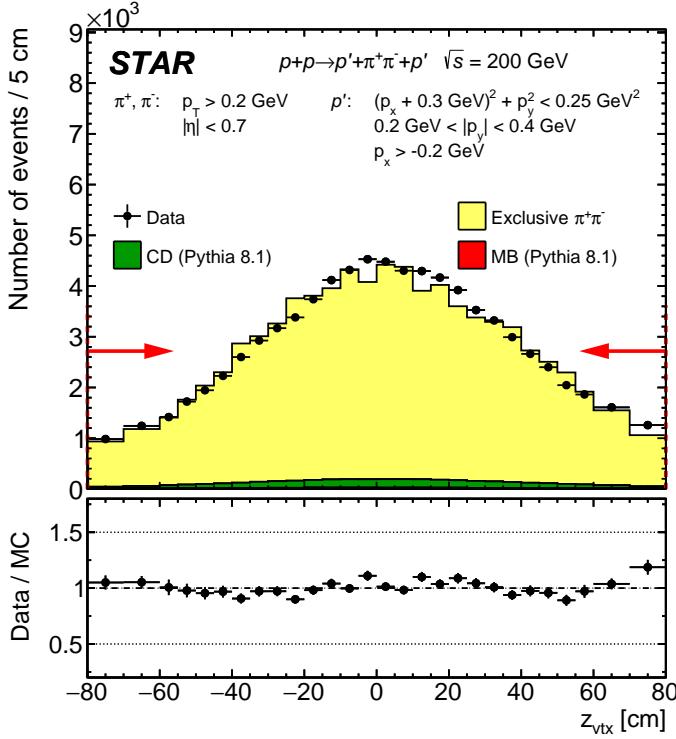


Figure 4.3: Comparison of z_{vtx} distribution between data and embedded MC after full selection. Data are represented by black points, while stacked MC predictions are drawn as histograms of different colors. Histogram from each MC process has been normalized according to prescription in Sec. 5.3. Vertical error bars represent statistical uncertainties, horizontal bars represent bin sizes. Comparison is shown for only z -vertex range corresponding to offline selection cut C2 due to such limited vertex range used in MC generation for increase of generation efficiency.

4.2.2 (C3) TPC tracks

The TPC track selection starts from the selection of events with exactly two primary tracks matched with hit in TOF (Fig. 4.4). Matching with TOF guarantee that analyzed tracks originate from the triggered bunch crossing (ensures that tracks are "in-time"). It is in accordance with the trigger logic which required at least 2 L0 TOF hits, as well as it enables more accurate particle identification with merged time-of-flight and dE/dx method, comparing to sole usage of dE/dx . Primary tracks not matched with hit in TOF, whose average multiplicity in single TOF vertex is ~ 8 , are hardly distinguished between real and fake (off-time) tracks, which is an additional reason for not analyzing events with only one TOF-matched primary TPC track (the other track might be unmatched due to TOF inefficiency).

Primary TPC tracks from the single TOF vertex which are matched with TOF are allowed to be also matched with BEMC clusters. Matching with BEMC cluster is claimed if the distance in $\eta - \phi$ space between the BEMC cluster position ($\eta_{\text{clus}}, \phi_{\text{clus}}$) and projected position of the track in BEMC ($\eta_{\text{proj}}, \phi_{\text{proj}}$), defined as

$$R = \sqrt{(\eta_{\text{clus}} - \eta_{\text{proj}})^2 + (\phi_{\text{clus}} - \phi_{\text{proj}})^2}, \quad (4.1)$$

is less than $R_{\text{max}}^{\text{match}} = 0.05$. Distribution of the distance between the primary TPC track and the closest BEMC cluster is shown in Fig. 4.5.

However, if there are any primary TPC tracks matched with BEMC cluster and not matched with TOF in the single TOF vertex with two TOF-matched tracks, an event is rejected. Such configuration implies higher-than-2 multiplicity of the real tracks in the vertex, hence an event is unlikely a Central Exclusive Production of two particles.

We apply cuts on the quantities reflecting quality of reconstructed TPC tracks similar to these typically used at STAR. We cut on number of hits used in TPC track reconstruction $N_{\text{hits}}^{\text{fit}} \geq 25$ and number of hits used in specific energy loss reconstruction $N_{\text{hits}}^{\text{dE/dx}} \geq 15$ in order to achieve good momentum and dE/dx resolution. We show distributions of aforementioned quantities together with spectrum of fraction of number of hits potentially generated by the track and finally used in the reconstruction $N_{\text{hits}}^{\text{fit}}/N_{\text{hits}}^{\text{poss}}$ in Fig. 4.6. One can see, that embedded MC simulation describes measured data well.

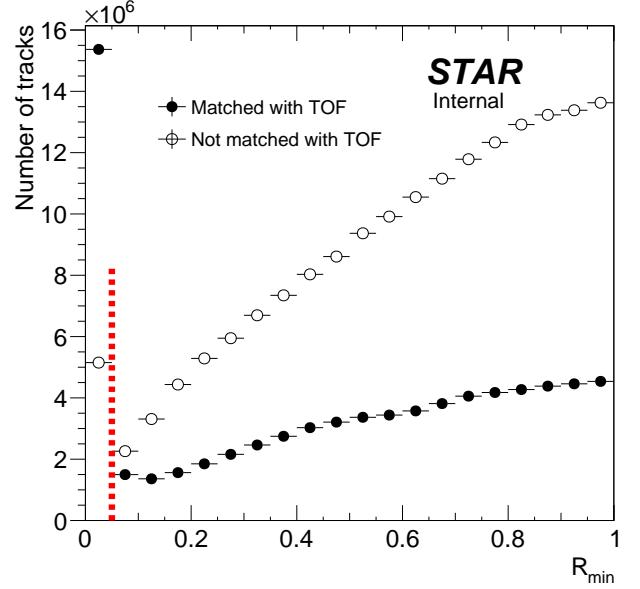
We also require that helices of global tracks associated with selected primary TOF tracks point well to the primary vertex ($DCA(R) < 1.5$ cm and $|DCA(z)| < 1$ cm), as well as the longitudinal separation of helices at the beamline (Fig. 6.14) is small and coincides with cut on $|DCA(z)|$ ($|\Delta z_0| < 2$ cm). Distributions of these quantities together with comparison against embedded MC are shown in Fig. 8.5 of Ref. [1]. In that reference one can also read how appropriate adjustment was derived needed to achieve satisfactory agreement of the d_0 , $DCA(R)$, $DCA(z)$ and $|\Delta z_0|$ in data and embedded MC.

Figure 4.7 shows comparison of the track pseudorapidity and azimuthal angle between data and embedded MC. These distributions are quite well described by MC. Large modulation in the ϕ distribution (enhancement



Figure 4.4: Multiplicity of primary TPC tracks matched with hit in TOF for single TOF vertex events. Red arrow marks bin with events with exactly two primary tracks matched with hit in TOF, which are used in physics analysis. Expectations from embedded $\pi^+\pi^-$ signal MC (normalized to the content of the bin representing 2 TOF tracks) has also been shown.

at $\phi = \pm\pi/2$) is connected with the RP acceptance mostly at $\varphi = \pm\pi/2$ - central particles pair is always back-to-back in azimuth with respect to pair of forward scattered protons, therefore pairs produced in "up" or "down" direction are preferred.



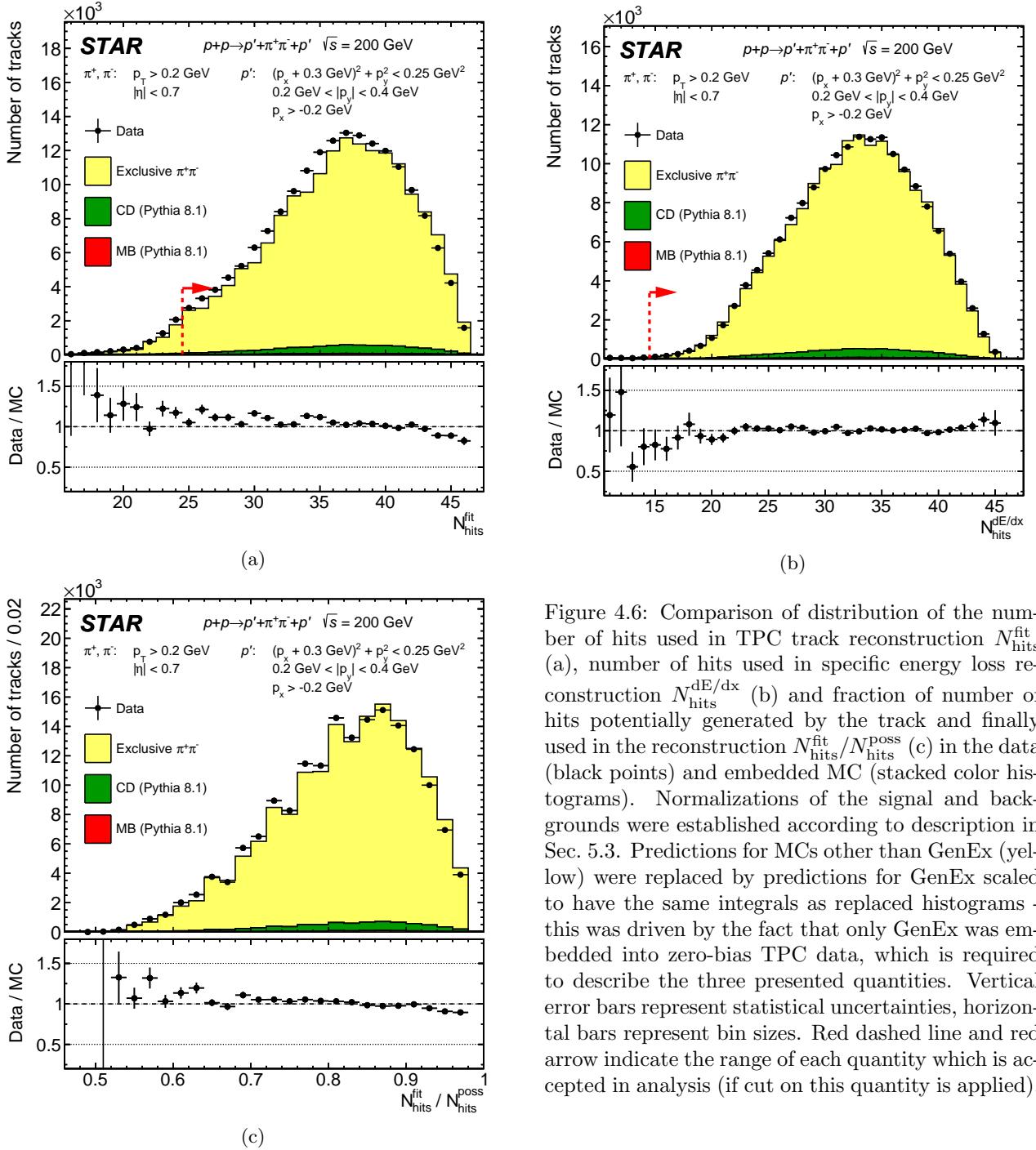


Figure 4.6: Comparison of distribution of the number of hits used in TPC track reconstruction $N_{\text{hits}}^{\text{fit}}$ (a), number of hits used in specific energy loss reconstruction $N_{\text{hits}}^{\text{dE/dx}}$ (b) and fraction of number of hits potentially generated by the track and finally used in the reconstruction $N_{\text{hits}}^{\text{fit}} / N_{\text{hits}}^{\text{poss}}$ (c) in the data (black points) and embedded MC (stacked color histograms). Normalizations of the signal and backgrounds were established according to description in Sec. 5.3. Predictions for MCs other than GenEx (yellow) were replaced by predictions for GenEx scaled to have the same integrals as replaced histograms - this was driven by the fact that only GenEx was embedded into zero-bias TPC data, which is required to describe the three presented quantities. Vertical error bars represent statistical uncertainties, horizontal bars represent bin sizes. Red dashed line and red arrow indicate the range of each quantity which is accepted in analysis (if cut on this quantity is applied).

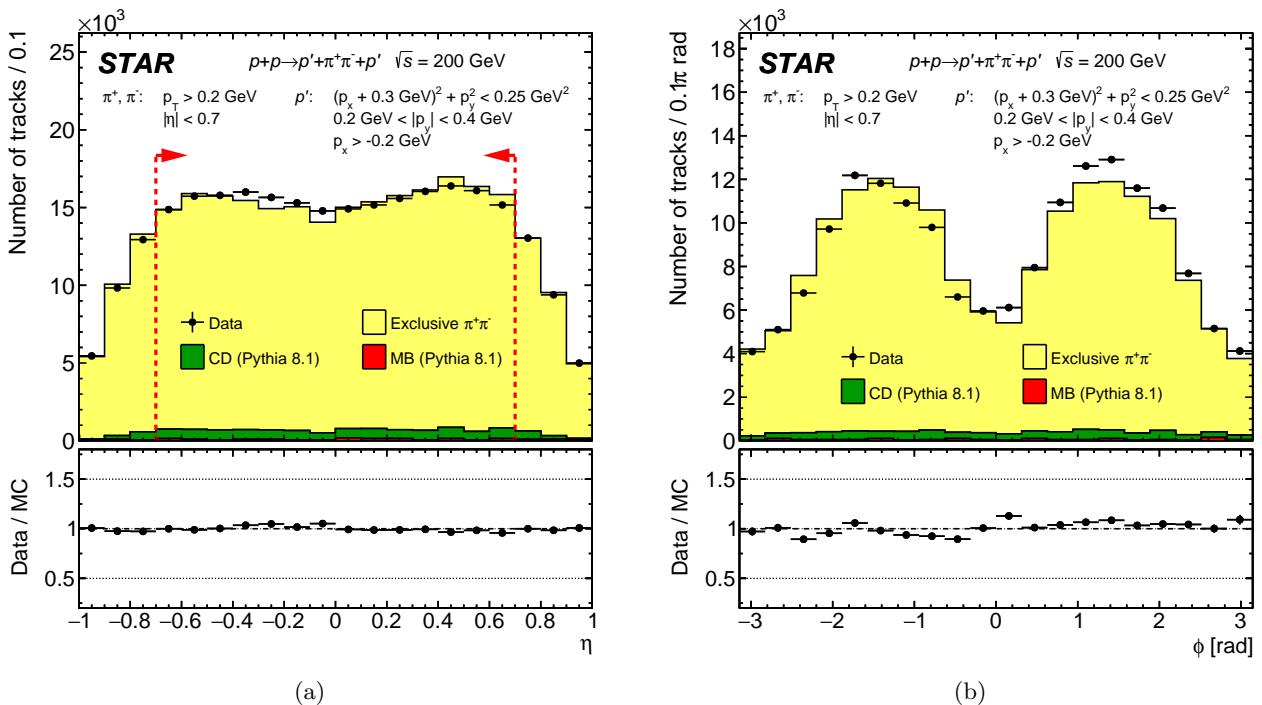


Figure 4.7: Comparison of the track pseudorapidity η (a) and the track azimuthal angle ϕ (b) in the data (black points) and embedded MC (stacked color histograms). Normalizations of the signal and backgrounds were established according to description in Sec. 5.3. Vertical error bars represent statistical uncertainties, horizontal bars represent bin sizes. Red dashed line and red arrow indicate the range of each quantity which is accepted in analysis (if cut on this quantity is applied).

4.2.3 (C4) RP tracks

In presented physics analysis the highest-level forward objects were used - RP tracks. They were obtained through the reconstruction process, starting from merging the signals (clustering) in single channels of silicon strip detectors housed inside RPs. General description of the reconstruction procedure has been given in Sec. 6.2 of the supplementary analysis note [1] and reference therein. A bit more detail description is available in elastic proton-proton scattering measurement analysis note [26].

Roman Pot data was analyzed offline as follows. First, all RP tracks which contain track points that had been formed of less than 3 hits of out 4 maximally possible (1 hit per silicon plane), were rejected. This is natural consequence of very high single plane efficiency $> 99.5\%$, and prevents including to analysis tracks with track points formed from unmatched pairs of clusters in both x - and y -coordinate (e.g. from electronics noise).

Next, preselected tracks were verified for consistency of their local angles with hypothesis of their origin being at the STAR IR. Using Geant4 simulation of RP system (see Sec. 6.3. of Ref. [1]) the impact of apertures limiting RP acceptance for the forward scattered protons generated at STAR IR was tested. The result is shown

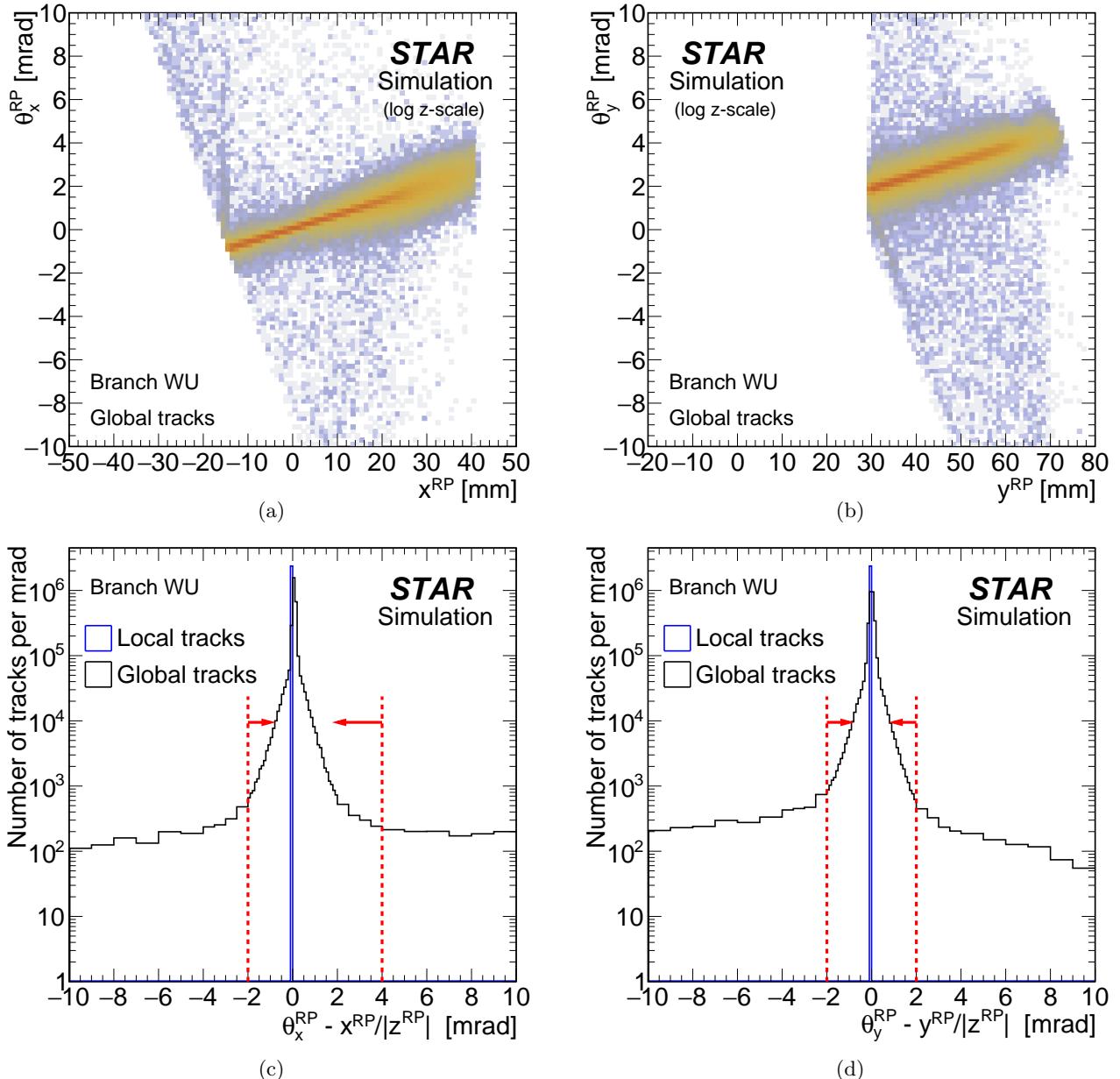


Figure 4.8: Typical correlation between local angle (y -axis) and position (x -axis) of RP tracks matched with true level primary protons for x - (a) and y -coordinate (b), here shown for branch WU. The same events are contained in c and d for x - and y -coordinate respectively, where difference between reconstructed local angle and local angle expected from the elastic track is histogrammed. Red lines and arrows visualize cuts imposed on RP tracks for final selection (cuts C4.2).

in Fig. 4.8, where density maps of reconstructed RP track local angle θ^{RP} and corresponding track coordinate in RP station are drawn (we show it only for branch WU as the picture is the same in the remaining branches). Only RP tracks matched with generated primary forward protons were used to fill the histograms. Clear bands of primary proton tracks can be distinguished in the top plots (Figs. 4.8a and 4.8b), with some very small number of tracks significantly scattered on the beampipe/DX/detector material. One-dimensional representation of the correlation between local angle and position can be obtained by constructing quantities

$$\tilde{\Delta\theta}_x^{RP} = \theta_x^{RP} - x^{RP}/|z^{RP}|, \quad (4.2)$$

$$\tilde{\Delta\theta}_y^{RP} = \theta_y^{RP} - y^{RP}/|z^{RP}|, \quad (4.3)$$

which reflect deviation of reconstructed local angle from expectation for forward proton of the beam momentum, and whose distributions are presented in Fig. 4.8c and Fig. 4.8d, respectively (black histograms). On these one-dimensional histograms we clearly see peaks from the true primary tracks. We considered optimal to restrict accepted $\tilde{\Delta\theta}_x^{RP}$ from -2 mrad to 4 mrad, and $\tilde{\Delta\theta}_y^{RP}$ from -2 mrad to 2 mrad. The upper cut on $\tilde{\Delta\theta}_x^{RP}$ equal to 4 mrad may look too inclusive, but intention was to preserve tracks of protons with very large ξ , whose local angle highly deviates from that of elastically scattered protons (DX magnets bends more protons with lower momentum) and which might have been underpopulated in MC (GenEx predictions were used). It is also worth to comment on the blue histograms in Figs. 4.8c and 4.8d, which represent local tracks (formed of single track points). These tracks are reconstructed assuming their momentum is equal to the beam momentum (angle at vertex equal to angle at RP station), therefore $\tilde{\Delta\theta}_x^{RP}$ and $\tilde{\Delta\theta}_y^{RP}$ is 0 by definition.

Once the set of cuts above was applied we required that on each side of STAR there was exactly one selected RP track. We did not allow higher number of tracks on one side because of no clear way to discriminate real tracks of primary protons.

In addition to cuts above, we restricted our measurement to the fiducial region defined as

$$0.2 < |p_y| < 0.4, \quad -0.2 < p_x, \quad (p_x + 0.3)^2 + p_y^2 < 0.5^2 \quad (\text{all in GeV}), \quad (4.4)$$

therefore both RP tracks were required to be contained within above envelope in (p_x, p_y) space. This fiducial area is drawn with black solid line on top of the (p_x, p_y) distribution of all measured CEP candidates (Fig. 4.9). It was chosen to compromise signal statistics and systematic uncertainties of the RP-related efficiencies (see e.g. Sec. 10.3 of Ref. [1]).

In the remaining part of the section we show comparisons of the track points position distributions between the data and embedded MC. In Fig. 4.10 we present side-by-side comparisons of two-dimensional hit maps from the data and embedded MC. Figures 4.11 and 4.12 show the same comparisons, but between their x - and y -projections for each RP separately. One can see, that simulation generally describes data well, both

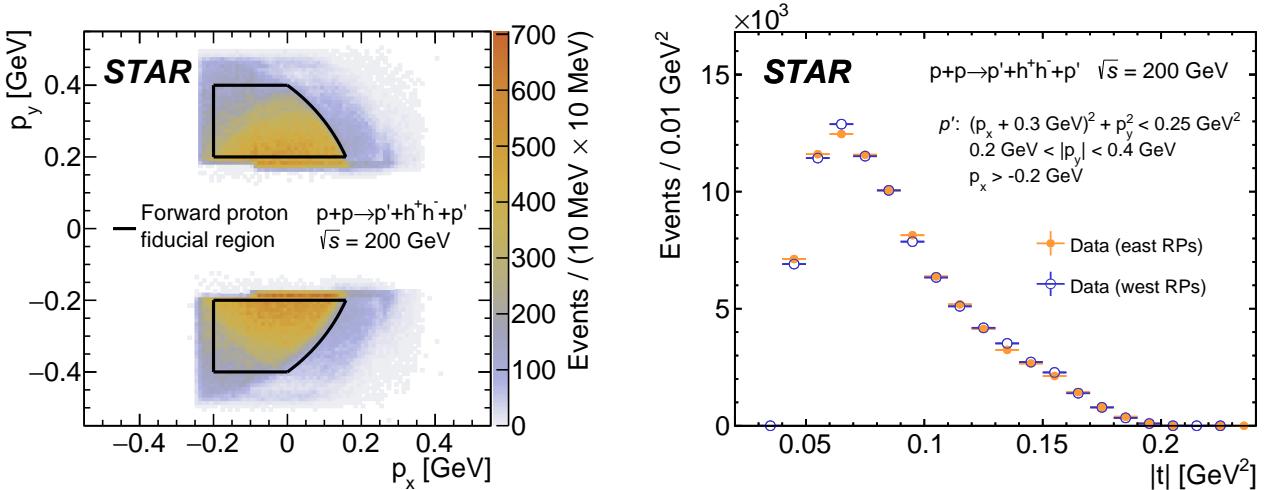


Figure 4.9: (left) Merged distributions of diffractively scattered protons momenta p_y vs. p_x in exclusive h^+h^- events reconstructed with the East and West RP stations, together with the kinematic region used in the measurement marked with the black line. (right) Distributions of measured four momenta transfers at the proton vertices for exclusive h^+h^- events with all particles in the fiducial phase space are shown for East and West stations with yellow and blue color, respectively.

in terms of shapes (which is mainly sensitive to detector alignment and geometry/apertures) and track points normalizations in various RPs (which is mainly sensitive to reconstruction efficiency).

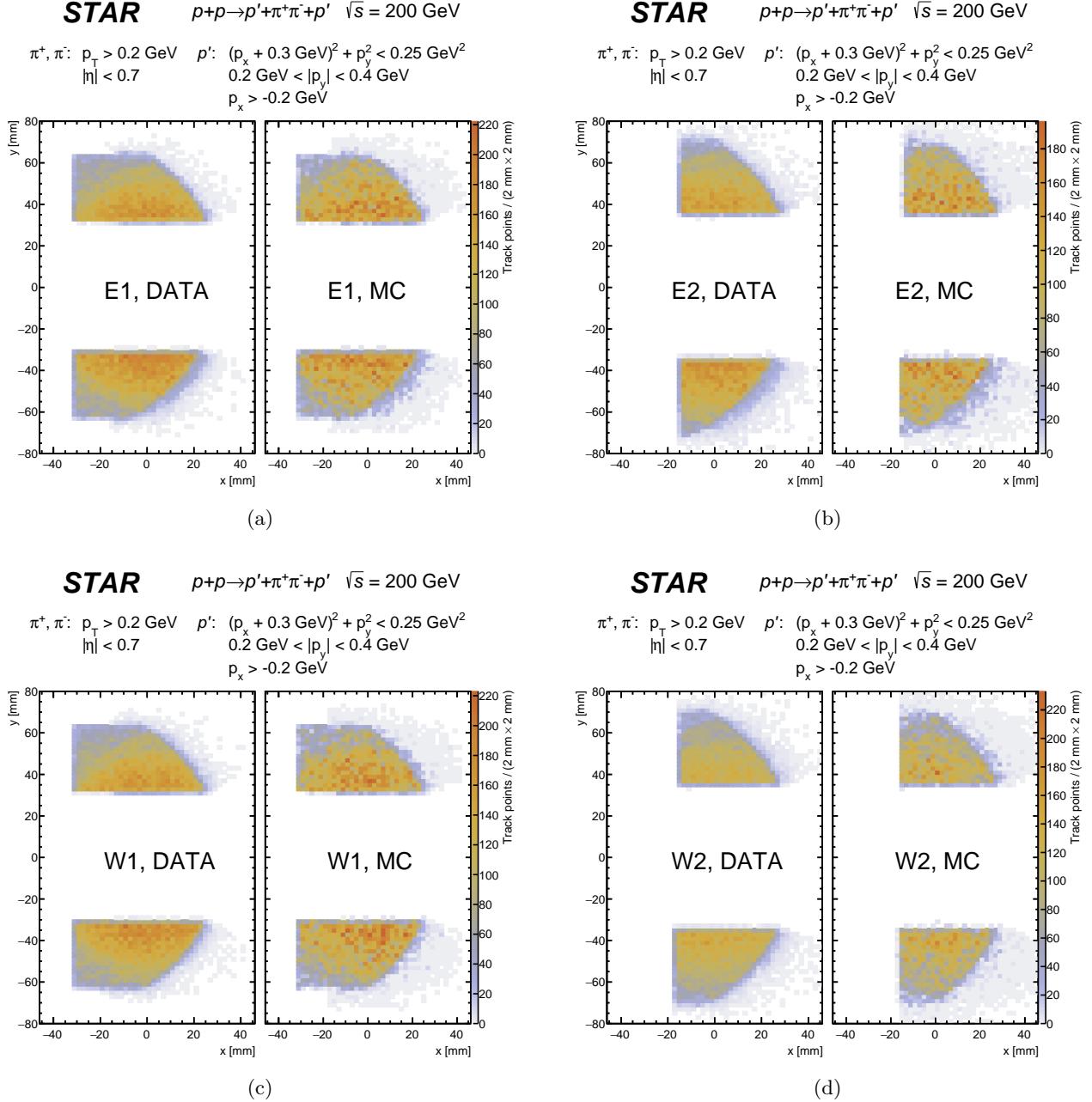


Figure 4.10: Comparison of two-dimensional track point density map in the data (left panel in subfigures) and stacked embedded MC (right panel in subfigures). Each subfigure corresponds to single RP station with position of track points measured in upper and lower RP visible at positive and negative y , respectively. Normalizations of the signal and backgrounds were established according to description in Sec. 5.3.

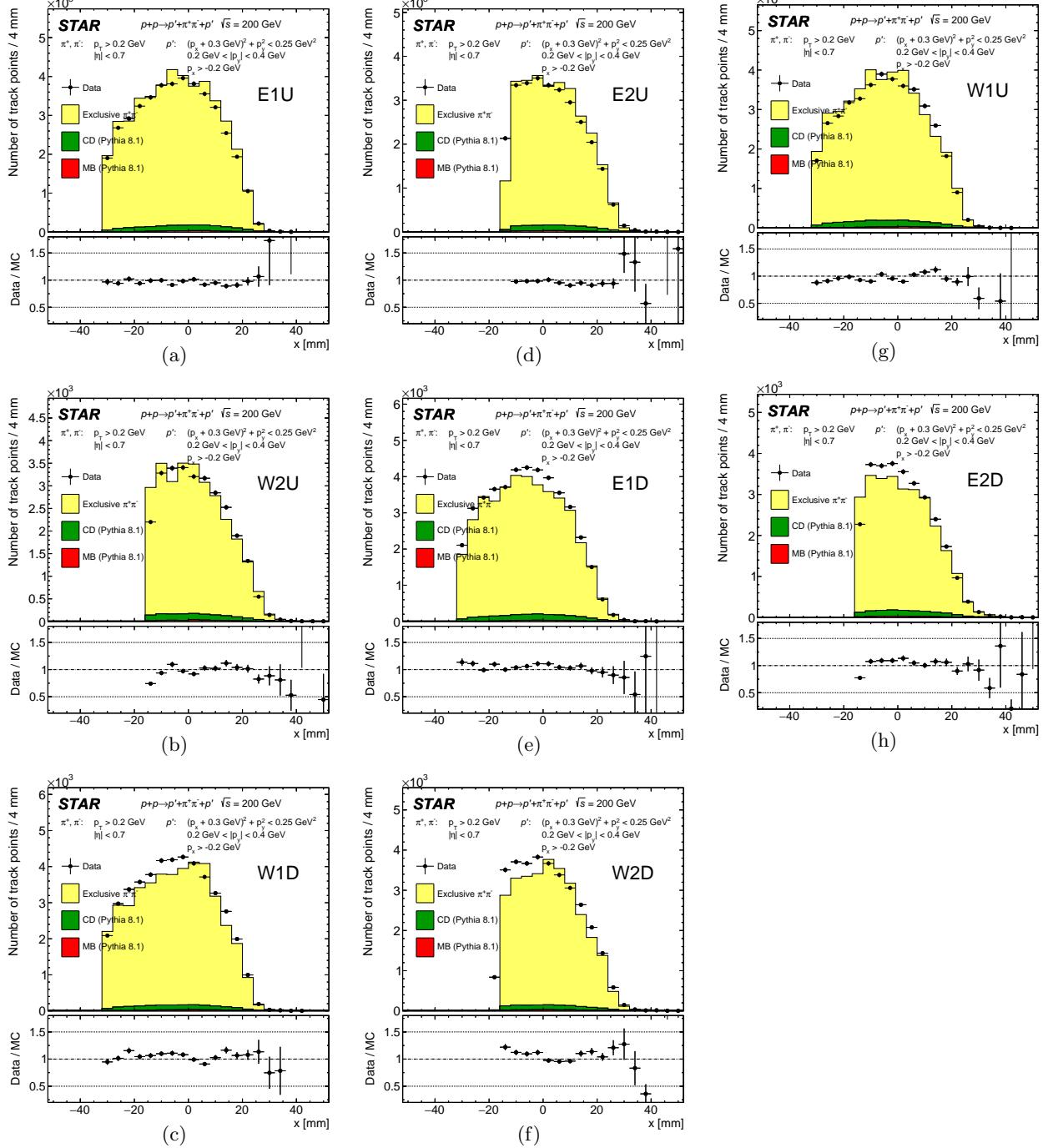


Figure 4.11: Comparison of x -position of track point between the data (black points) and stacked embedded MC (color histograms). Each subfigure corresponds to single RP station, whose name is printed in the right part subfigure. Vertical error bars represent statistical uncertainties, horizontal bars represent bin sizes. Normalizations of the signal and backgrounds were established according to description in Sec. 5.3.

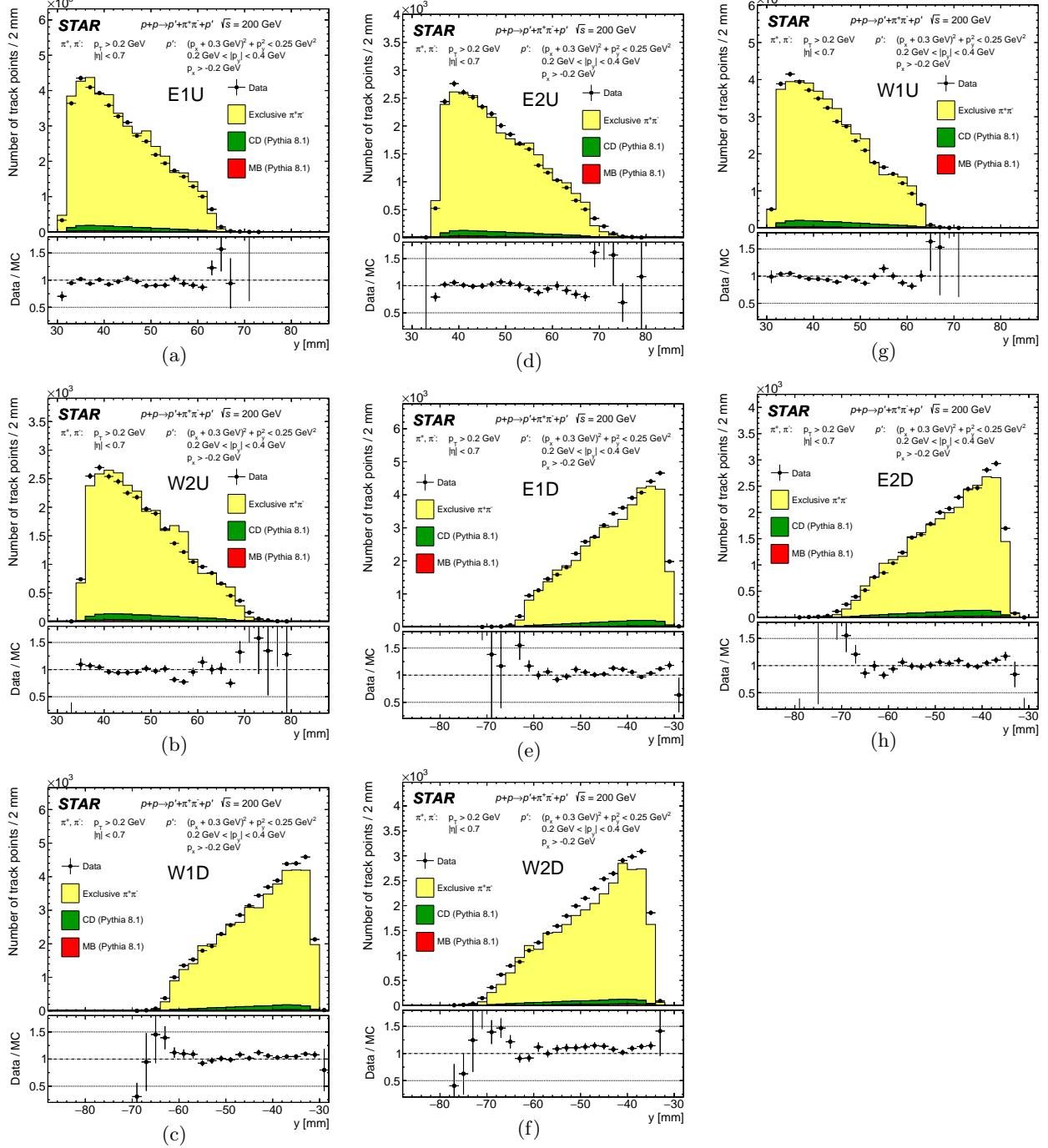


Figure 4.12: Comparison of y -position of track point between the data (black points) and stacked embedded MC (color histograms). Each subfigure corresponds to single RP station, whose name is printed in the middle of sub-figure. Vertical error bars represent statistical uncertainties, horizontal bars represent bin sizes. Normalizations of the signal and backgrounds were established according to description in Sec. 5.3.

4.2.4 (C5) TPC-RP z -vertex matching

In CEP tracks in the central detector and tracks in Roman Pots originate from the same interaction vertex. Measurement of the time of detection of forward protons in RPs gives access to reconstruction of the position of the vertex

$$z_{\text{vtx}}^{\text{RP}} = c \cdot \frac{t_{\text{W}}^{\text{RP}} - t_{\text{E}}^{\text{RP}}}{2} \quad (4.5)$$

independently from TPC, which allows their comparison and rejection of the background if the two values disagree. Time of detection of proton in RP is provided in StMuRpsTrack object - it is an average of all TAC values from PMTs in RPs used to form a track, corrected for the slewing effect and linearly transformed (scaled and shifted) to have the best correlation with the z -position of the vertex measured in TPC, translated to unit of time (all these steps are done at the level of raw data reconstruction). In Fig. 4.13 the comparisons of the $z_{\text{vtx}}^{\text{RP}}$ and $z_{\text{vtx}}^{\text{TPC}}$ are shown with some preselection cuts applied. A clear signal from the Central Diffraction (and thus CEP) process is manifesting in high correlation of the two values (diagonal in Fig. 4.13a) or significant and relatively narrow peak centered at 0 for the difference of two values (Fig. 4.13b). The sum of two Gaussian

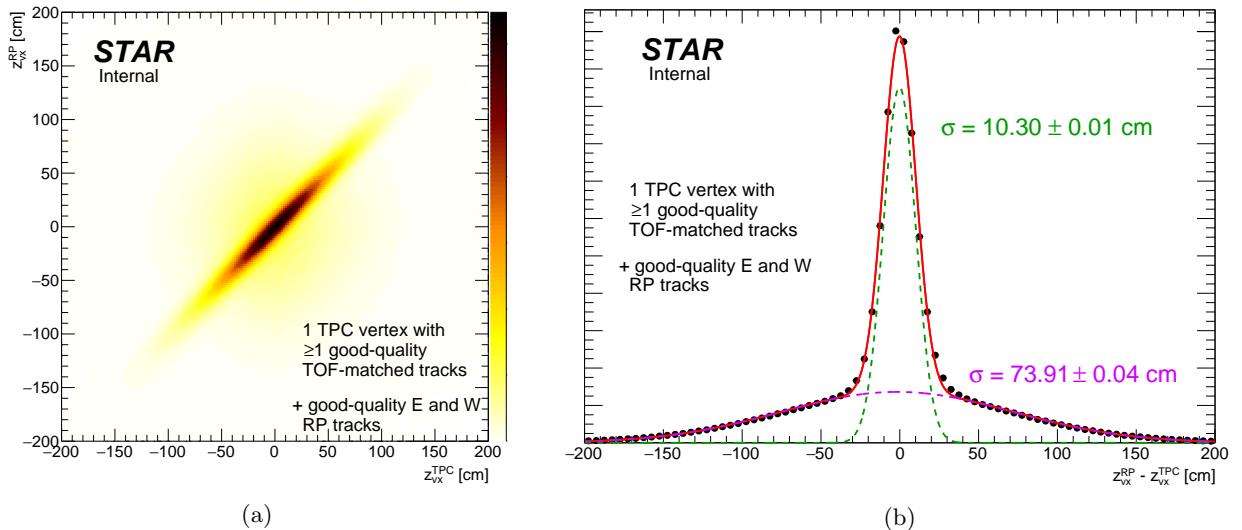


Figure 4.13: Correlation (Fig. 4.13a) and difference (Fig. 4.13b) of z -vertex position measured in Roman Pots and TPC in RP_CPT2 triggers, after preselection described in the plots.

distributions was fitted to data in Fig. 4.13b yielding good description of the distribution of Δz_{vtx} with the width parameters equal 10.3 cm (CD signal) and 73.9 cm (pile-up). The first parameter reflects the time resolution of RPs (the $z_{\text{vtx}}^{\text{RP}}$ measurement), as the TPC resolution is much better (~ 1 cm). Value of the second parameter, consistent with $\sqrt{2}\sigma_{z_{\text{vtx}}} \approx \sqrt{2} \cdot 52$ cm ≈ 73.5 cm, confirms that the wide distribution under the narrow signal peak is uncorrelated background, in other words forward protons originating from a different vertex than the central tracks. To reject this background without significant loss of the signal, we introduce $3.5\sigma_{\Delta z_{\text{vtx}}}$ cut on Δz_{vtx} ($|\Delta z_{\text{vtx}}| < 36$ cm).

4.2.5 (C6) BBC-large signal veto

At the trigger level a veto on signal in small BBC detectors was used. During offline analysis we found that the non-exclusive background can be reduced if an additional veto on signal in large BBC detectors is added. It is connected with the fact that vast majority of selected RP_CPT2 triggers were from the central diffraction process to which CEP belongs. Many of central diffraction events have particles produced in the rapidity region outside the TPC and TOF acceptance, some hitting large BBC tiles. Presence of signal in large BBC is therefore a signature of background or a pile-up interaction.

The response of large BBC tiles is different from that of small BBC tiles, as shown in sample plots in Fig. 4.14 (similar distributions for all channels can be found in Appendix B). Typically in small BBC tiles a peak visible in ADC distribution around 100 – 150 (Figs. 4.14a,4.14c), a signature of good separation of the electronics noise and signal from the ionizing particle. No such feature is observed in corresponding distribution for large BBC tile (Figs. 4.14b,4.14d), which can be explained by the difference in geometry (in size) of small and large tiles. In large BBC tiles the path that scintillation light must travel to reach PMT is much longer in comparison to small BBC tiles (multiple reflections on the main tile surface due to small thickness of the tile) therefore it is highly attenuated and extended in time. This is possible reason of lack of signal peak in the ADC distribution



Figure 4.14: Sample BBC-small (left column) and BBC-large (right column) response in zero-bias data. Top row shows TAC vs. ADC distributions, bottom row shows projection of the corresponding two-dimensional distribution on x -axis (ADC) in the TAC range quoted in the legend, for both abort gaps and colliding bunches. Red lines and arrows indicate thresholds for a signal in presented channels.

in large BBC tile spectrum (Fig. 4.14d), as well as the late-TAC ($TAC < \sim 600$, $ADC < 100$) tail in the ADC vs. TAC spectrum (slewing effect, Fig. 4.14b). Nevertheless, the above features of BBC-large response does not disqualify this detector from being used as a veto detector, as in this case lower efficiency of the detector only reduces the background rejection power.

Each channel of the BBC-large has different response to signal from ionizing particle, as well as different level of noise. We decided to set up a signal threshold for each channel based on a study of the noise in abort gaps (in zero-bias data). This noise, in principle, should be solely the electronics noise, but possible is also some signal from the off-time pile-up (from preceding bunch crossings). We checked for each channel the probability to detect a signal with ADC above certain threshold and with TAC contained within 100 and 2400 (the same window is deafult for small BBC). The result is shown in Fig. 4.15. Next, we established final ADC thresholds in each BBC-large channel by requiring that the noise in BBC-large would cause a veto in maximally 3.5% of events. Such number was chosen because it was consistent with an average ADC threshold of 40, found optimal in terms of selection efficiency and sample purity (see Appendix A), as well as it was acceptably low. To transform it to ADC_{thr} we first assumed that the noise is uncorrelated between the channels. With this assumption one can connect the probability of the veto in whole BBC-large detector (east and west) caused by noise $\mathcal{P}_{veto}^{noise}$ with the probability of the signal induced by noise in single BBC-large channel $\mathcal{P}_{i,sig}^{noise}$:

$$\mathcal{P}_{veto}^{noise} = 1 - \mathcal{P}_{!veto}^{noise} = 1 - (1 - \mathcal{P}_{i,sig}^{noise})^{N_{ch}^{BBC}}. \quad (4.6)$$

In the equation above N_{ch}^{BBC} denotes number of active channels in BBC-large. From plots contained in Appendix B one can read that there were 14 active channels in BBC-large. 2 dead channels were found on the west side (40 and 42). By transforming Eq. 4.6 to the form presented below we can calculate the threshold



Figure 4.15: Percentage of events in abort gaps from zero-bias triggers with the ADC counts larger than the ADC threshold given in the x -axis, for each BBC-large channel. Measured points with statistical uncertainties are connected with a smooth line of corresponding color for better visualization.

probability for a single BBC-large channel:

$$\mathcal{P}_{i,\text{sig}}^{\text{noise}} = 1 - \sqrt[N_{\text{ch}}^{\text{BBC}}]{1 - \mathcal{P}_{\text{veto}}^{\text{noise}}} = 1 - \sqrt[14]{1 - 0.035} \approx 0.0025. \quad (4.7)$$

In the last step we translated this number to ADC threshold for each channel of BBC-large. For this purpose we used Fig. 4.15. The x -axis projection of the crossing point of each color line with the y -axis value of 0.0025 defines ADC_{thr} for each particular channel. These numbers are listed in Tab. 4.1. The event was dropped from analysis if any of the BBC-large channels registered signal of strength $\text{ADC}_i > \text{ADC}_{i,\text{thr}}$ and $100 < \text{TAC}_i < 2400$.

Observation of high purification of CEP sample with described BBC-large veto in the data from run 15 was helpful to improve the CEP trigger for run 17. The improved trigger called RP_CPT2noBBCL was similar to RP_CPT2 with an addition of BBC-large veto using ADC threshold of 50.

4.2.6 (C7) TOF clusters limit

The TOF is mainly used to distinguish real TPC tracks from the fakes, as well as it helps to identify particles. However, we also used it to reject non-CEP events in which the TPC tracks were not reconstructed or were not successfully matched to TOF hit. For this we introduced a concept of a TOF cluster - a group of offline TOF hits close in space and time. We expect that such cluster of hits is induced by the single primary particle, eventually associated with the secondaries (e.g. delta rays). The most important is that single particle should not produce two or more clusters.

We defined a TOF cluster as a group of reconstructed TOF hits with the (ϕ, η) space distance R to neighbouring hit (defined similarly to Eq. (4.1) not larger than 0.1 and with the time distance to the same hit Δt not larger than 1.5 ns. In other words, TOF clusters were formed by the offline hits that form at least one pair with the other hit in the cluster satisfying

$$R < 0.1, \quad \Delta t < 1.5 \text{ ns}. \quad (4.8)$$

In Fig. 4.16 distribution of R and Δt is presented. From these pictures one can find justification for the limits used in Ineqs. (4.8). Clear enhancement is visible at $R < 0.1$ and $\Delta t < 1.5$ ns, which arises from the TOF hits originating from the same particle. Distribution of Δt significantly differs from the zero-bias embedded signal MC, however observed mismatch between data and MC could be assigned to imperfect TOF simulation. Data and MC are in qualitative agreement in a sense that the main part of the time signal is in both cases contained at $\Delta t < 1.5$ ns. We consider this level of description of data by MC sufficient, given that efficiency correction related to cut on $N_{\text{cltrs}}^{\text{TOF}}$ is extracted from the data themselves.

East		West	
i	ADC_{thr}	i	ADC_{thr}
16	27	40	(dead)
17	30	41	31
18	26	42	(dead)
19	37	43	14
20	25	44	29
21	55	45	30
22	43	46	33
23	27	47	22

Table 4.1: Offline ADC thresholds in BBC-large.

Comparison of data and MC in terms of multiplicity of TOF clusters is presented in Fig. 4.17. The agreement between the two is acceptable. From the comparisons one can see that higher multiplicities are features of backgrounds (e.g. TOF hits reconstructed but TPC tracks not, or matching between TPC track and TOF hit unsuccessful), hence no more than 1 additional TOF cluster was allowed per event - in total the number of reconstructed TOF clusters $N_{\text{cltrs}}^{\text{TOF}}$ could not exceed 3.

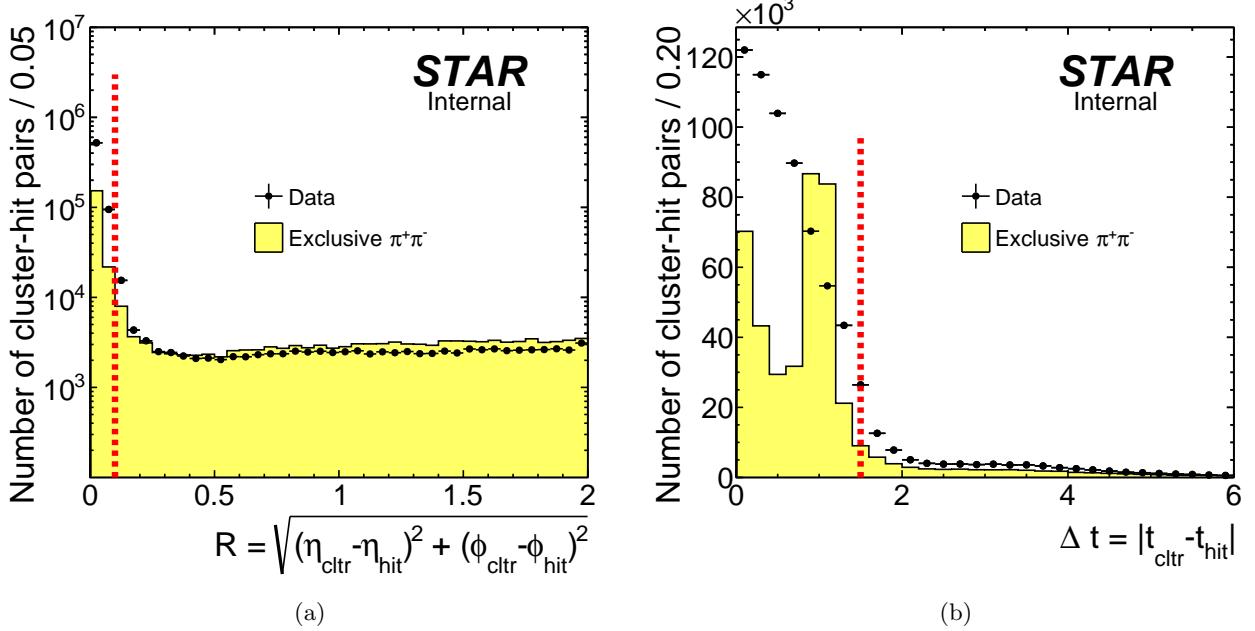


Figure 4.16: Distribution of space (a) and time (b) distance between TOF hits and existing TOF clusters in the clustering procedure. Each of distributions contains entries from cluster-hit pairs satisfying matching requirement imposed on the other quantity. Data are shown as black points with vertical error bars representing statistical uncertainties and horizontal bars representing bin sizes. Expectations from embedded $\pi^+\pi^-$ signal MC, normalized to the same integrals at $R > 0.5$ (a) or at $\Delta t > 2$ ns (b), has also been shown. Dashed red lines mark limits used in the TOF clustering algorithm.

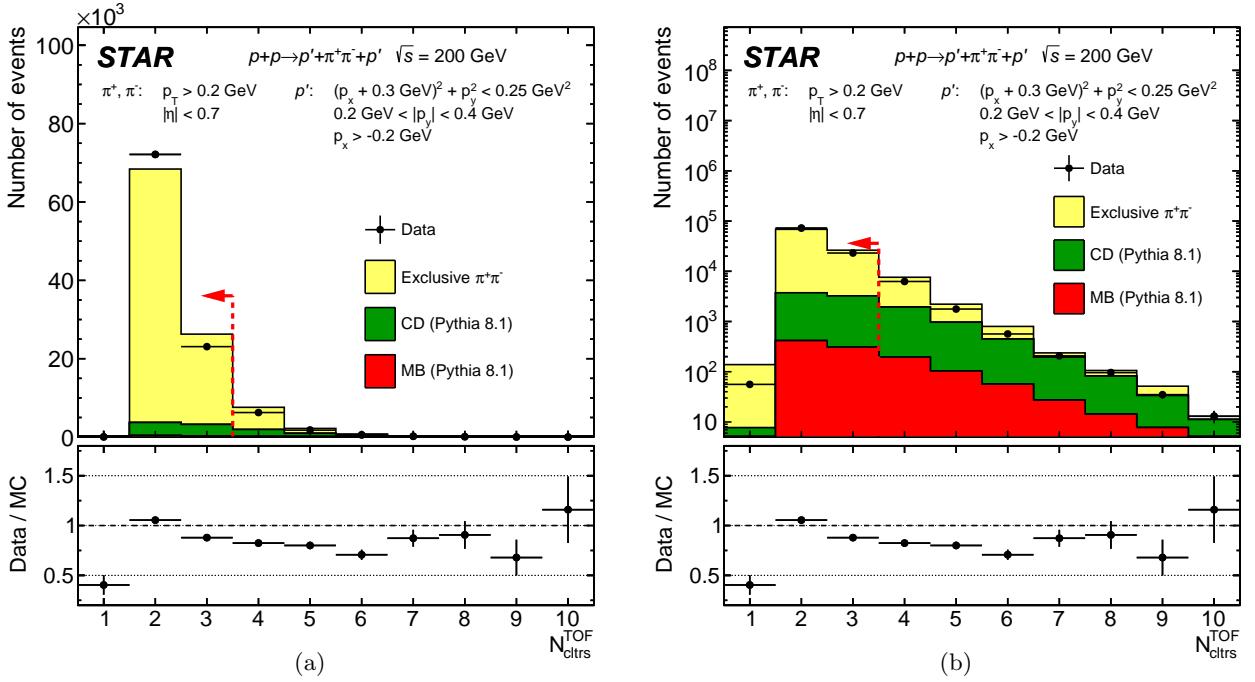


Figure 4.17: Distribution of TOF cluster multiplicity $N_{\text{cltrs}}^{\text{TOF}}$ after all selection cuts except cut C7. Left and right plot differ only in the y -axis (left: linear, right: logarithmic). Data are represented by black points, while stacked MC predictions are drawn as histograms of different colors. Histogram from each MC process has been normalized according to prescription in Sec. 5.3. Vertical error bars represent statistical uncertainties, horizontal bars represent bin sizes.

4.2.7 (C8) Particle identification

Particles were identified using combined information from the TPC (dE/dx) and TOF (time of hit detection in the TOF subsystem). Merging informations from two sources led to reduction of misidentifications, as well as gave access to higher kaon and proton momentum range where dE/dx of different species overlap.

Compatibility of track dE/dx with that expected from particle of type X was determined using the quantity $n\sigma_X$ widely used at STAR, defined as

$$n\sigma_X = \ln \left[(dE/dx)^{\text{measured}} / (dE/dx)_X^{\text{theory}} \right] / \sigma_{dE/dx}, \quad (4.9)$$

where $(dE/dx)^{\text{measured}}$ is the ionization energy loss of the TPC track, $(dE/dx)_X^{\text{theory}}$ is the Bethe-Bloch [27] expectation for the given particle type ($X = \pi, K, p$) at reconstructed track momentum, and $\sigma_{dE/dx}$ is the statistical uncertainty of $\ln(dE/dx)^{\text{measured}}$. Quantity $n\sigma_X$ is in fact a pull: $(dE/dx)^{\text{measured}}$ is (in first order) an average over Landau \otimes normal-distributed dE/dx of single TPC hits forming the track, hence the $(dE/dx)^{\text{measured}}$ is distributed log-normally and $\ln(dE/dx)^{\text{measured}}$ - normally. From $n\sigma_X$ of the two tracks the χ^2 statistic for a XX pair hypothesis was calculated:

$$\chi^2_{dE/dx}(XX) = (n\sigma_X^{\text{trk1}})^2 + (n\sigma_X^{\text{trk2}})^2. \quad (4.10)$$

Sometimes we also quote $n\sigma^{\text{pair}}$ quantity (which is no longer a Gaussian pull) connected with χ^2 through relation

$$n\sigma_X^{\text{pair}} = \sqrt{\chi^2_{dE/dx}(XX)} = \sqrt{(n\sigma_X^{\text{trk1}})^2 + (n\sigma_X^{\text{trk2}})^2}. \quad (4.11)$$

The time of detection of particle in the TOF system was used to reconstruct its squared mass m_{TOF}^2 . For this purpose the time of primary interaction is typically used ("start time"), reconstructed by detecting fragments of dissociated beam particles in VPD detectors on both sides of the interaction point². However, it is not accessible in CEP as the initial protons survive the interaction intact. We overcame this problem by assuming that both central tracks are of the same type which is natural expectation for CEP events. With this assumption the time difference between TOF hits and measured tracks' momenta and lengths of helical paths between the primary vertex and TOF then allow to calculate m_{TOF}^2 . The derivation of formula used to obtain m_{TOF}^2 is presented in Appendix C.

Particle identification involved a few steps. First, the pp hypothesis was verified:

$$\underbrace{\chi^2_{dE/dx}(pp) < 9}_{\text{likely } pp} \& \underbrace{m_{\text{TOF}}^2 > 0.6 \text{ GeV}^2}_{\text{unlikely } \pi\pi \text{ or } KK} \& \underbrace{\chi^2_{dE/dx}(\pi\pi) > 9}_{\text{unlikely } \pi\pi \text{ or } KK} \& \underbrace{\chi^2_{dE/dx}(KK) > 9}_{\text{unlikely } pp}. \quad (4.12)$$

If any of above was not satisfied, the pair was checked for compatibility with KK hypothesis:

$$\underbrace{\chi^2_{dE/dx}(KK) < 9}_{\text{likely } KK} \& \underbrace{m_{\text{TOF}}^2 > 0.15 \text{ GeV}^2}_{\text{unlikely } \pi\pi} \& \underbrace{\chi^2_{dE/dx}(\pi\pi) > 9}_{\text{unlikely } \pi\pi} \& \underbrace{\chi^2_{dE/dx}(pp) > 9}_{\text{unlikely } pp}. \quad (4.13)$$

In case the pair was neither recognized as $p\bar{p}$ or K^+K^- , it was assumed to be a $\pi^+\pi^-$ pair if the dE/dx of positive and negative charge track was consistent with pion hypothesis at 3σ level:

$$|n\sigma_\pi^{\text{trk1}}| < 3 \& |n\sigma_\pi^{\text{trk2}}| < 3. \quad (4.14)$$

In Fig. 4.18 we present two-dimensional distributions of $n\sigma^{\text{pair}}$ variables which help better understand the behaviour and aim of $n\sigma^{\text{pair}}$ (χ^2) cuts in Eqs. (4.12), (4.13). Regions of enriched population of specific pair species are appropriately labeled. Similar connections between $n\sigma^{\text{pair}}$ and m_{TOF}^2 are shown in Fig. 4.19. Distributions of $\chi^2_{dE/dx}$ and m_{TOF}^2 for CEP event candidates before PID cuts are shown in Fig. 4.20.

²Time measured from protons in the RP detectors cannot be used because RP readout runs on independent clock from that used by VPD and TOF.

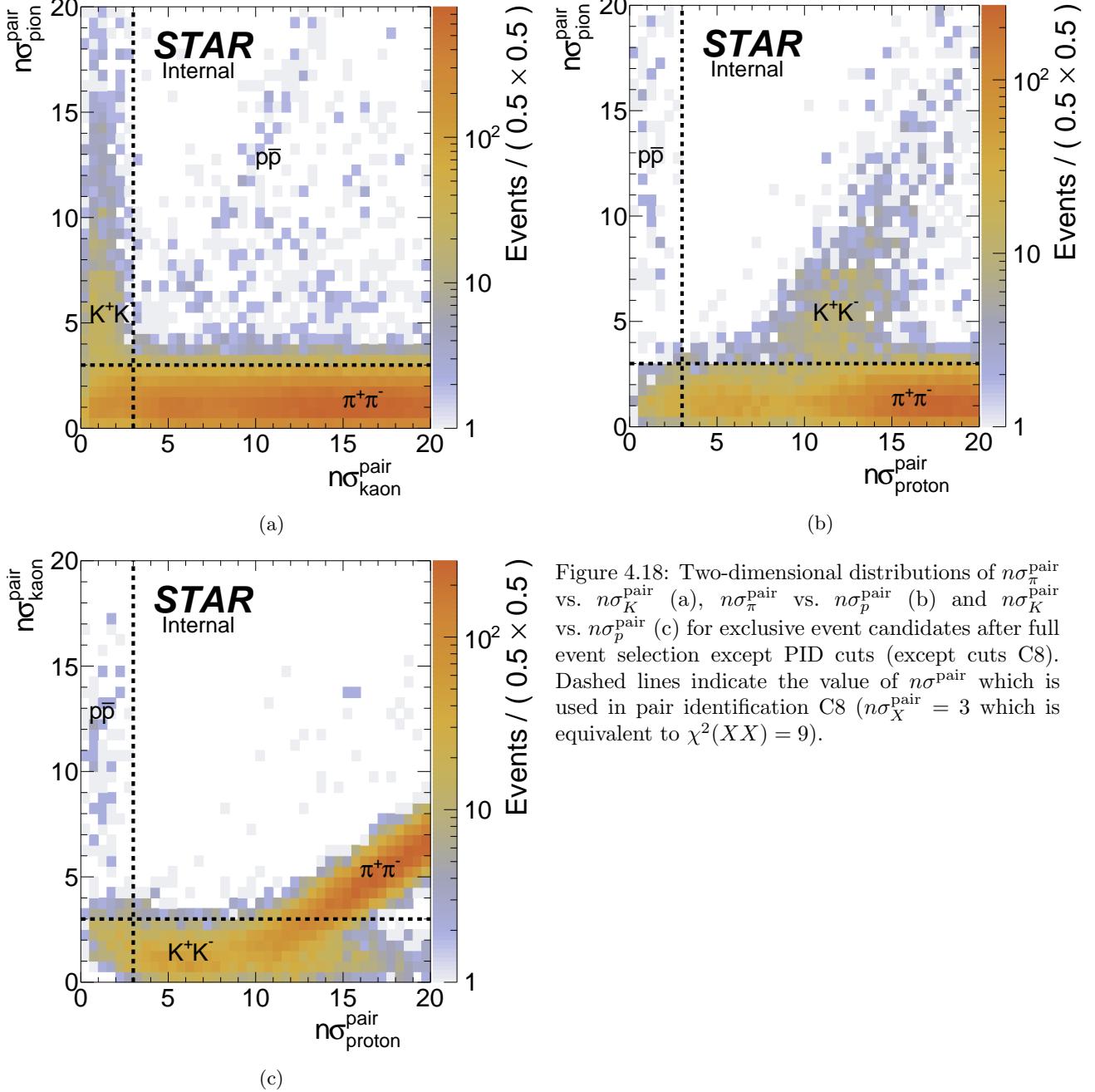


Figure 4.18: Two-dimensional distributions of $n\sigma_{\pi}^{\text{pair}}$ vs. $n\sigma_K^{\text{pair}}$ (a), $n\sigma_{\pi}^{\text{pair}}$ vs. $n\sigma_p^{\text{pair}}$ (b) and $n\sigma_K^{\text{pair}}$ vs. $n\sigma_p^{\text{pair}}$ (c) for exclusive event candidates after full event selection except PID cuts (except cuts C8). Dashed lines indicate the value of $n\sigma_{\text{X}}^{\text{pair}}$ which is used in pair identification C8 ($n\sigma_X^{\text{pair}} = 3$ which is equivalent to $\chi^2(XX) = 9$).



Figure 4.19: Two-dimensional distributions of $n\sigma_{\pi}^{\text{pair}}$ (top row), $n\sigma_K^{\text{pair}}$ (middle row) and $n\sigma_p^{\text{pair}}$ (bottom row) vs. m_{TOF}^2 . The left column contains all clean BBC-large events with single TOF vertex and two opposite sign TOF-matched tracks (in other words events passing cuts C1, C3.1, C3.2 and C6), which provides excellent statistics to see the signatures or pairs of specific ID. The right column contains exclusive event candidates after full event selection except PID cuts (except cuts C8). Dashed red line and arrow indicate the cut imposed on plotted quantities which are used to select exclusive pairs of given particle species (keep in mind that these are not the only cuts).



Figure 4.20: Raw distributions of $\chi_{dE/dx}^2$ (left column) and m_{TOF}^2 (right column) for exclusive $\pi^+\pi^-$ (top row), K^+K^- (middle row) and $p\bar{p}$ (bottom row) candidates after full event selection. Data are shown as black points, while stacked predictions for signal and backgrounds are shown as color histograms. Dashed red line and arrow indicate the value of cut imposed on plotted quantity to select exclusive pairs of given particle species. Last bins in each subplot are overflows representing an integral of the tail of distribution. Presented distributions were obtained after all the cuts were applied, except the cut on presented quantity in the last step in PID algorithm used to select pairs of given species. Non-exclusive background was determined with a method described in Sec. 5.2.1, while predictions for exclusive contributions were obtained as described in Sec. 5.2.2.

4.2.8 (C9) Exclusivity cut (missing p_T cut)

The most important cut which is used in this analysis to select events of exclusively produced pairs of particles is the missing transverse momentum, or the total transverse momentum cut. It benefits from detection and reconstruction of the forward proton in RP detectors - a rare capability among high energy physics experiments which STAR provides. The observable p_T^{miss} used to select exclusive event is defined as

$$p_T^{\text{miss}} = \left(\vec{p}_{p'}^E + \vec{p}_{h^+} + \vec{p}_{h^-} + \vec{p}_{p'}^W \right)_T = \sqrt{\left(p_x^{\text{miss}} \right)^2 + \left(p_y^{\text{miss}} \right)^2}, \quad (4.15)$$

with the other total momentum components defined analogously:

$$p_x^{\text{miss}} = \left(\vec{p}_{p'}^E + \vec{p}_{h^+} + \vec{p}_{h^-} + \vec{p}_{p'}^W \right)_x, \quad (4.16)$$

$$p_y^{\text{miss}} = \left(\vec{p}_{p'}^E + \vec{p}_{h^+} + \vec{p}_{h^-} + \vec{p}_{p'}^W \right)_y. \quad (4.17)$$

Figure 4.21 visualize the (anti-)correlation between the momentum components of the forward system (sum of two forward protons momenta) and the central system (sum of two central tracks momenta). The enhanced band at anti-diagonal restricted by dashed lines contains events balanced in momentum, a signature of exclusivity. Events outside this band are the non exclusive backgrounds, in most cases Central Diffraction events with some particles undected (due to detector inefficiency or produced outside acceptance). Slight horizontal enhancement in all distributions around $[\vec{p}_{p'}^W + \vec{p}_{p'}^E]_x = [\vec{p}_{p'}^W + \vec{p}_{p'}^E]_y = 0$ is a signature of the elastic proton-proton scattering background with some non-elastic pile-up interaction which mimics the CEP event. All these backgrounds are reasonably low after the exclusivity cut, as described in Sec. 5.1.1.

The momentum balance is shown one-dimensionally in Fig. 4.22, with the sum of x - and y -components of momentum shown respectively in the left and right column for each analyzed particle species. The sum of signal and background (both assumed to be described a Gaussian) was fitted to p_x^{miss} and p_y^{miss} distributions. Results of the fit are given in each subfigure. One can notice that the widths of Gaussian functions representing the exclusive signal are consistent among species and amount $\sigma_{p_x^{\text{miss}}} = 27.4$ MeV for the x -component of total momentum, and $\sigma_{p_y^{\text{miss}}} = 28.1$ MeV for the y -component of total momentum, taking the values of the lowest statistical uncertainty - for $\pi^+\pi^-$. These values are measures of the total momentum resolution respectively for p_x^{miss} and p_y^{miss} . Having these number it is possible to form an elliptical cut on the missing momentum:

$$\left(\frac{p_x^{\text{miss}}}{\sigma_{p_x^{\text{miss}}}} \right)^2 + \left(\frac{p_y^{\text{miss}}}{\sigma_{p_y^{\text{miss}}}} \right)^2 < n_{\text{cut}}^2 \quad (4.18)$$

where n_{cut} is the parameter denoting radius of limiting ellipsis in units of standard deviations of distributions of total momentum components (resolutions). Since these resolutions are nearly identical ($\sigma_{p_x^{\text{miss}}} = \sigma_{p_y^{\text{miss}}} = \sigma_{p_{x,y}^{\text{miss}}}$) such cut can be reduced (multiplying Ineq. 4.18 by $\sigma_{p_{x,y}^{\text{miss}}}^2$) to one-dimensional cut on a single quantity:

$$(p_x^{\text{miss}})^2 + (p_y^{\text{miss}})^2 < \left(n_{\text{cut}} \cdot \sigma_{p_{x,y}^{\text{miss}}} \right)^2 \quad \xrightarrow{\sqrt{}} \quad p_T^{\text{miss}} < n_{\text{cut}} \cdot \sigma_{p_{x,y}^{\text{miss}}} \quad (4.19)$$

In current analysis the n_{cut} was set to 2.5, which translates to threshold value 2.5×30 MeV = 75 MeV. Such value was found optimal considering study described in Appendix A.

In Fig. 4.23 the missing transverse momentum distributions are presented for the three studied CEP channels. In Sec. 5.3 a demonstration of various background contributions is given for $\pi^+\pi^-$, explaining all features of the distribution.



Figure 4.21: Two-dimensional distributions of sum of forward protons momenta (x -axis) and sum of central tracks momenta (y -axis) for exclusive $\pi^+\pi^-$ (top row), K^+K^- (middle row) and $p\bar{p}$ (bottom row) event candidates after full event selection, except the exclusivity cut C9. Left and right column shows correlation of respectively x - and y -component of tracks' momenta. Anti-diagonal representing perfect momentum balance of the central and forward system is limited with dashed lines extending by $\pm 2.5\sigma$ ($\sigma \approx 30$ MeV) around the anti-diagonal. Three distinct horizontal regions in plots on the right hand side correspond to different forward proton configurations: elastic-like (protons in branches EU&WD or ED&WU, $|[\vec{p}_p^W + \vec{p}_p^E]_y| < 0.2$ GeV) and anti-elastic configuration (protons in branches ED&WD or EU&WU, $|[\vec{p}_p^W + \vec{p}_p^E]_y| > 0.4$ GeV).

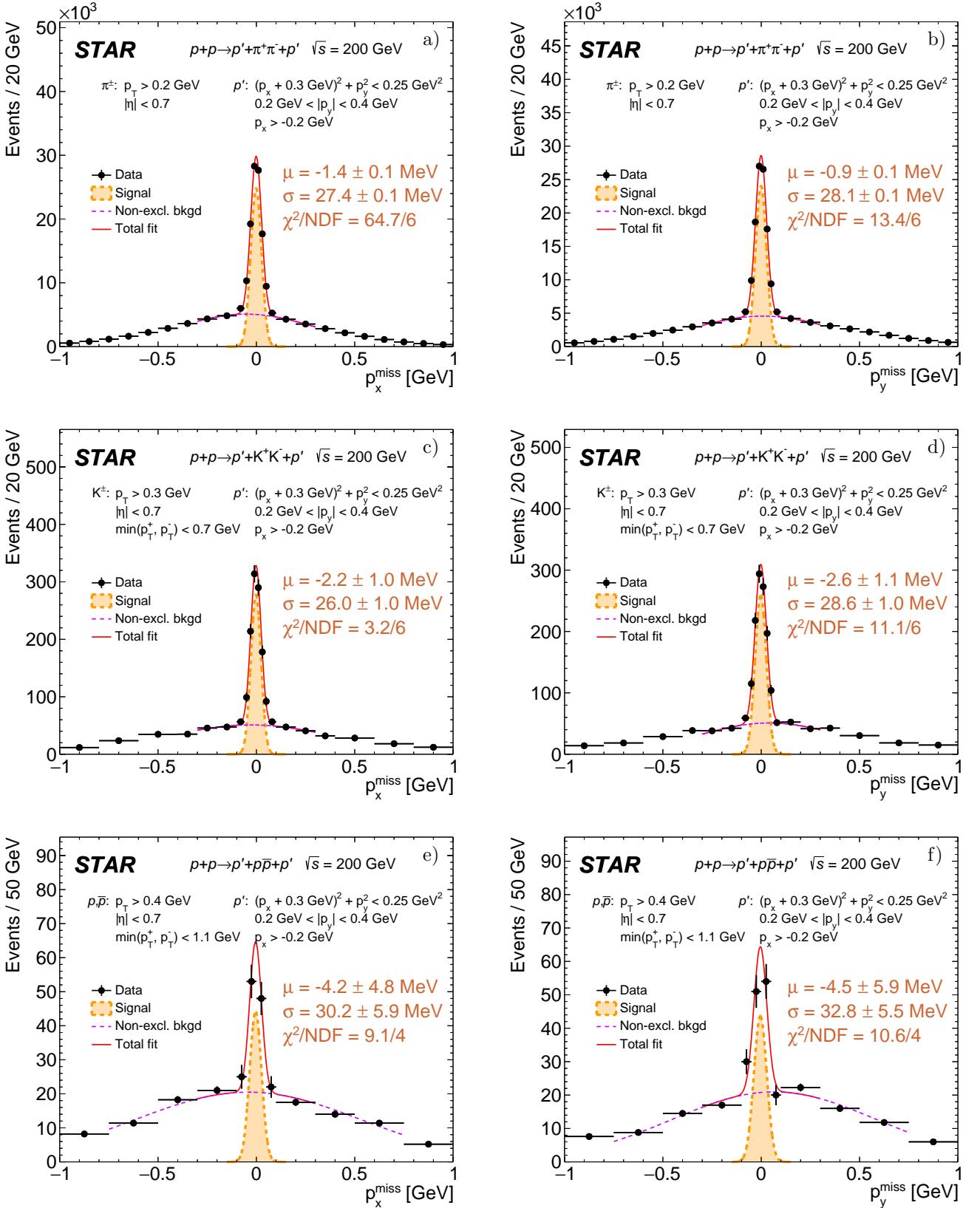


Figure 4.22: Raw distributions of $p_{\text{miss}}^{\text{x}}$ (left column) and $p_{\text{miss}}^{\text{y}}$ (right column) for exclusive $\pi^+\pi^-$ (top row), K^+K^- (middle row) and $p\bar{p}$ (bottom row) candidates after full event selection, except exclusivity cut C9. Solid red line represents the fit of sum of two Gaussian functions representing the exclusive event signal (orange) and non-exclusive background (violet). Parameters of the total momentum resolution for signal events obtained from the fit (given in the plots) roughly agree between all species.

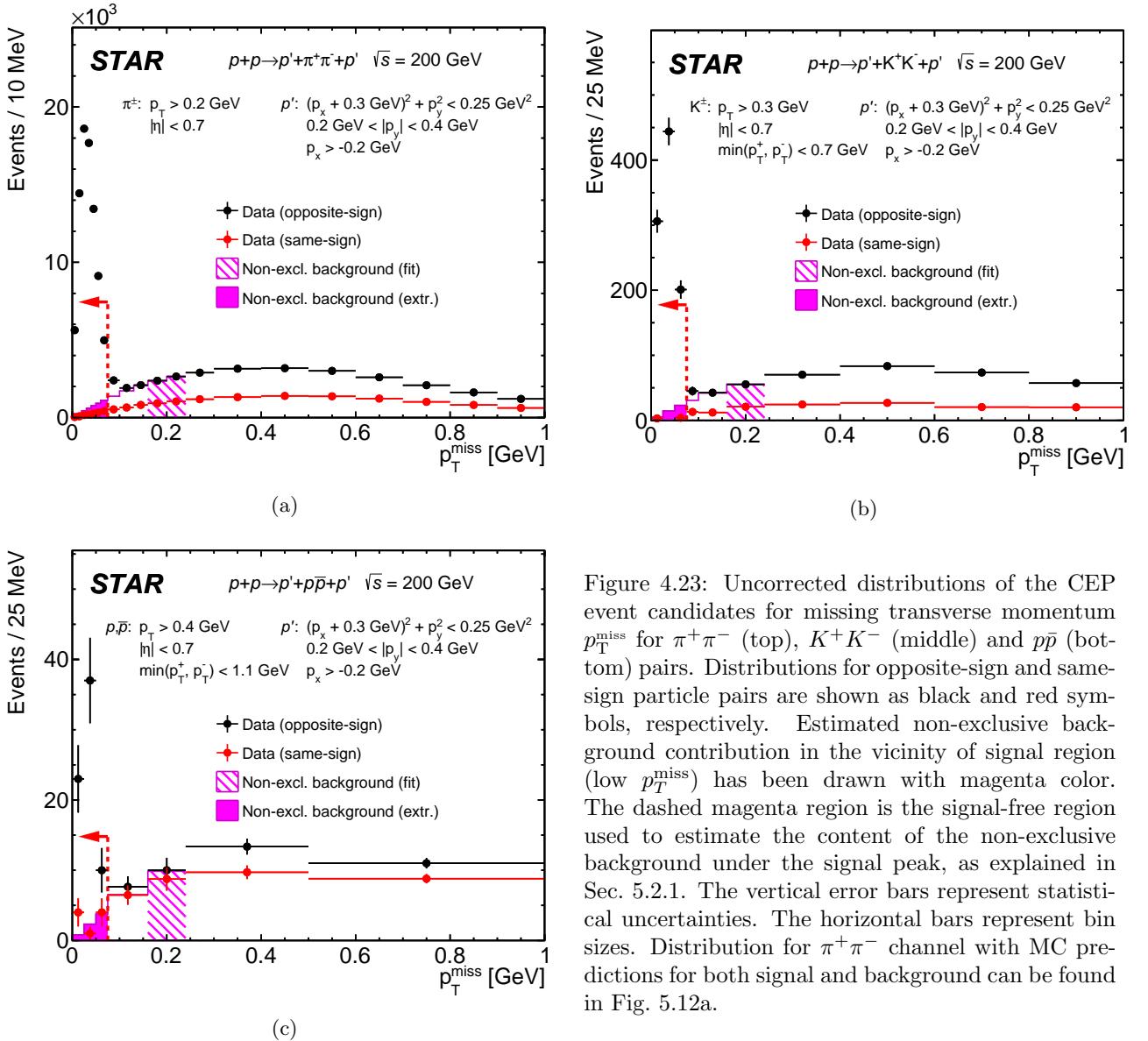


Figure 4.23: Uncorrected distributions of the CEP event candidates for missing transverse momentum p_T^{miss} for $\pi^+\pi^-$ (top), K^+K^- (middle) and $p\bar{p}$ (bottom) pairs. Distributions for opposite-sign and same-sign particle pairs are shown as black and red symbols, respectively. Estimated non-exclusive background contribution in the vicinity of signal region (low p_T^{miss}) has been drawn with magenta color. The dashed magenta region is the signal-free region used to estimate the content of the non-exclusive background under the signal peak, as explained in Sec. 5.2.1. The vertical error bars represent statistical uncertainties. The horizontal bars represent bin sizes. Distribution for $\pi^+\pi^-$ channel with MC predictions for both signal and background can be found in Fig. 5.12a.

5. Backgrounds

In this section we discuss sources of backgrounds present in data and methods of their determination. We also present studies which provide quantitative determination of relative content of various background components, which were successfully suppressed to a few % level with the set of cuts discussed in previous chapter.

5.1 Sources of background

5.1.1 Non-exclusive background

The main background present in the final exclusive $\pi^+\pi^-/K^+K^-/p\bar{p}$ sample is the non-exclusive background. There are several classes of events which mimic topology of h^+h^- CEP: two forward protons, two opposite sign central tracks and rapidity gaps. Below we list the most probable cases:

- Single physics interaction processes:
 - Central Diffraction (Fig. 5.1b) - this process differs from CEP of h^+h^- only by the number of produced particles; protons originate from the same vertex as the central tracks, hence correlation of reconstructed vertex position from RPs and TPC is still observed.
- Accidental coincidences (pile-up):
 - inelastic + elastic interaction (Fig. 5.1c) - there may be overlap of protons from elastic scattering interaction and activity in the central detector from another (inelastic) interaction; it should be suppressed by the rapidity gap veto in BBC-small (online) and BBC-large (offline); easy to identify through protons collinearity and lack of correlation of z -vertex from RPs and TPC.
 - Single Diffraction + beam halo - there may be overlap of proton from SD on one side and beam halo proton on the opposite side, and activity in the central detector from diffractive state; it should be suppressed by the rapidity gap vetos and (low) beam halo rate;
 - $2\times$ beam halo + inelastic interaction.

} negligibly low

These backgrounds are graphically presented in Fig. 5.1. In Sec. 5.2.2 data-driven method of determination of these backgrounds is presented. In Sec. 5.3 discussed background is decomposed with the use MC simulations.

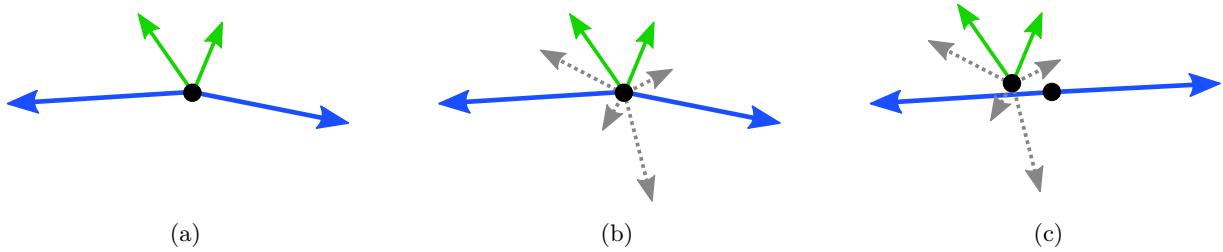


Figure 5.1: Sketches of main processes exhibiting h^+h^- CEP event topology: the exclusive h^+h^- signal itself (a), central diffraction event with some particles not detected (b) and elastic proton-proton scattering event with pile-up inelastic interaction in the central region (c). Particles represented by arrows are: forward scattered protons (blue), detected mid-rapidity particles (green) and undetected particles (dashed gray). Black dots mark primary interaction vertices.

5.1.2 Exclusive background (particle misidentification)

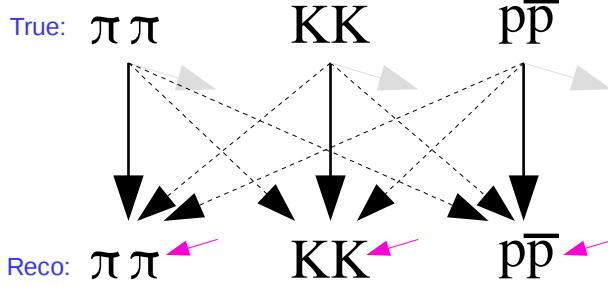


Figure 5.2: Graph illustrating the misidentification problem - the origin of exclusive background in selected samples. Gray arrows represent event rejection due to failed PID selection (C8). Magenta arrows indicate non-exclusive backgrounds described in Sec. 5.1.1. Solid black arrows represent successful identification, whereas dashed black lines show misidentification paths.

Another source of background which is connected with finite particle identification power is the exclusive background from the particle species other than species under study. This effect is schematically shown in Fig. 5.2, and written in the form of set of equations (5.1), where N_R^{XX} is number of reconstructed events identified as XX ($X = \pi, K$ or p), N_T^{XX} is true number of XX events, $N_{bkgd}^{\pi\pi}$ is number of non-exclusive events among reconstructed N_R^{XX} , ϵ^{XX} is identification efficiency for species XX , and $\lambda^{XX \rightarrow YY}$ is misidentification probability of species XX as YY (see Sec. 6.2.2.6):

$$N_R^{\pi\pi} = \underbrace{\epsilon^{\pi\pi} \cdot N_T^{\pi\pi}}_{\text{true pion pairs}} + \underbrace{\lambda^{KK \rightarrow \pi\pi} \cdot N_T^{KK}}_{\text{kaon pairs reconstructed as pion pairs}} + \underbrace{\lambda^{p\bar{p} \rightarrow \pi\pi} \cdot N_T^{p\bar{p}}}_{\text{proton pairs reconstructed as pion pairs}} + N_{bkgd}^{\pi\pi} \quad (5.1a)$$

$$N_R^{KK} = \underbrace{\lambda^{\pi\pi \rightarrow KK} \cdot N_T^{\pi\pi}}_{\text{pion pairs reconstructed as kaon pairs}} + \underbrace{\epsilon^{KK} \cdot N_T^{KK}}_{\text{true kaon pairs}} + \underbrace{\lambda^{p\bar{p} \rightarrow KK} \cdot N_T^{p\bar{p}}}_{\text{proton pairs reconstructed as kaon pairs}} + N_{bkgd}^{KK} \quad (5.1b)$$

$$N_R^{p\bar{p}} = \underbrace{\lambda^{\pi\pi \rightarrow p\bar{p}} \cdot N_T^{\pi\pi}}_{\text{pion pairs reconstructed as proton pairs}} + \underbrace{\lambda^{KK \rightarrow p\bar{p}} \cdot N_T^{KK}}_{\text{kaon pairs reconstructed as proton pairs}} + \underbrace{\epsilon^{p\bar{p}} \cdot N_T^{p\bar{p}}}_{\text{true proton pairs}} + N_{bkgd}^{p\bar{p}} \quad (5.1c)$$

We only consider three most significant possible hadronic CEP channels - next in a row would be CEP of $d\bar{d}$, but such events are not observed in the data, although reconstruction efficiency should be similar to $p\bar{p}$. Eqs. (5.1) can be written in the matrix form, as shown in Eq. (5.2), from which it is straightforward to obtain final formula for restored number of events of given ID, Eq. (5.3):

$$\begin{bmatrix} N_R^{\pi\pi} - N_{bkgd}^{\pi\pi} \\ N_R^{KK} - N_{bkgd}^{KK} \\ N_R^{p\bar{p}} - N_{bkgd}^{p\bar{p}} \end{bmatrix} = \underbrace{\begin{bmatrix} \epsilon^{\pi\pi} & \lambda^{KK \rightarrow \pi\pi} & \lambda^{p\bar{p} \rightarrow \pi\pi} \\ \lambda^{\pi\pi \rightarrow KK} & \epsilon^{KK} & \lambda^{p\bar{p} \rightarrow KK} \\ \lambda^{\pi\pi \rightarrow p\bar{p}} & \lambda^{KK \rightarrow p\bar{p}} & \epsilon^{p\bar{p}} \end{bmatrix}}_{\text{"mixing matrix" } \Lambda} \begin{bmatrix} N_T^{\pi\pi} \\ N_T^{KK} \\ N_T^{p\bar{p}} \end{bmatrix} \rightarrow \begin{bmatrix} N_T^{\pi\pi} \\ N_T^{KK} \\ N_T^{p\bar{p}} \end{bmatrix} = \Lambda^{-1} \begin{bmatrix} N_R^{\pi\pi} - N_{bkgd}^{\pi\pi} \\ N_R^{KK} - N_{bkgd}^{KK} \\ N_R^{p\bar{p}} - N_{bkgd}^{p\bar{p}} \end{bmatrix} \quad (5.2)$$

In Sec. 5.2.2 we show a semi-data-driven method of estimation of the exclusive background.

5.2 Background determination

5.2.1 Non-exclusive background

Determination of non-exclusive background makes use of the missing transverse momentum which is distributed differently for the signal and for aforementioned background. High statistics of the data allows to apply a data-driven method, which is desired as it significantly reduces impact of model-dependence to results, especially when models of diffraction do not describe physics observables. What is more, not only integrated over observables but differentially as a function of these.

It has already been demonstrated in Sec. 4.2.8 that p_T^{miss} from exclusive events is much narrower compared to background, visible as a peak near the axis origin. Additional feature of p_T^{miss} - probability density approaching to zero with p_T^{miss} moving towards the axis origin, helps performing a polynomial fit without constant component

to p_T^{miss} distribution in the background-dominated range and extrapolation of this polynomial down to $p_T^{\text{miss}} = 0$ under the peak of CEP signal. The procedure used to determine non-exclusive background content in the signal region is described below. The description assumes determination of non-exclusive background differentially in single observable X (in 1 dimension), but procedure naturally applies also to more dimensions.

1. 2-dimensional distribution of p_T^{miss} vs. X (by design without cut C9 applied) was looped over all bins in X . Projection onto p_T^{miss} axis, $\frac{dN_X}{dp_T^{\text{miss}}}$, was done for only these bins of X , in which there are signal candidates (more than 0 counts in the region $p_T^{\text{miss}} < 75$ MeV).
2. Projections of p_T^{miss} from bins with signal candidates are summed to a single histogram (like data points in Fig. 5.3):

$$\frac{dN}{dp_T^{\text{miss}}} = \sum_X \frac{dN_X}{dp_T^{\text{miss}}} \quad (5.4)$$

3. Fit of polynomial given by Eq. (5.5) was performed to $\frac{dN}{dp_T^{\text{miss}}}$ in the range $160 \text{ MeV} < p_T^{\text{miss}} < 240 \text{ MeV}$, where dominant non-exclusive background with negligibly low signal content is expected.

$$b(p_T^{\text{miss}}) = c_1 \cdot p_T^{\text{miss}} + c_2 \cdot (p_T^{\text{miss}})^2 \quad (5.5)$$

The left edge of the fitting range was chosen to be close to $p_T^{\text{miss}} = 0$, but far enough from the signal peak which could bias fitted background shape. The right edge of the fitting range was set to provide reasonable width of that range, but on the other hand be close enough to $p_T^{\text{miss}} = 0$, so that 2nd order polynomial approximation would still be valid for the background shape. Result of the fit is shown in Fig. 5.3 with semi-transparent magenta line.

4. Ratio r_{bkgd} was calculated between the integral of function b in the signal region ($p_T^{\text{miss}} < 75$ MeV)) and in the fitted region $160 \text{ MeV} < p_T^{\text{miss}} < 240 \text{ MeV}$:

$$r_{\text{bkgd}} = \frac{\int_0^{75 \text{ MeV}} b(p_T^{\text{miss}}) dp_T^{\text{miss}}}{\int_{160 \text{ MeV}}^{240 \text{ MeV}} b(p_T^{\text{miss}}) dp_T^{\text{miss}}}. \quad (5.6)$$

5. In each bin of X with any signal counts the non-exclusive background was determined as

$$N_{\text{bkgd},X}^{\text{non-excl}} = r_{\text{bkgd}} \cdot \int_0^{75 \text{ MeV}} \frac{dN_X}{dp_T^{\text{miss}}} dp_T^{\text{miss}}. \quad (5.7)$$

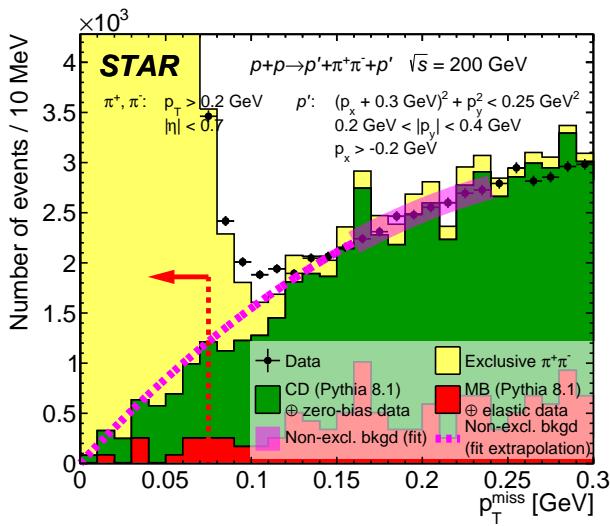


Figure 5.3: Demonstration of non-exclusive background determination method using p_T^{miss} distribution. Both data and MC predictions presented in the figure are the same as in Fig. 5.12 - here same sign events were omitted, as well as the binning was set finer and axes ranges were adjusted to focus on the background region below the signal peak. Normalization of MC components was explained in Sec. 5.3. The data are shown with black points, stacked MC predictions are shown with filled histograms, and fit of 2nd order polynomial given by Eq. (5.5) representing non-exclusive background, together with its extrapolation to $p_T^{\text{miss}} = 0$ is drawn with solid and dashed magenta line, respectively.

One can see in Fig. 5.3 that fitted polynomial extrapolated to $p_T^{\text{miss}} = 0$ matches well predictions from MC.

In Fig. 5.4 we demonstrate, that data driven method differs from MC predictions by up to 50% in both directions. Also, shape of the same-sign background is significantly different from opposite-sign estimate, which disqualifies usage of same-sign background as an estimate of non-exclusive opposite-sign background.

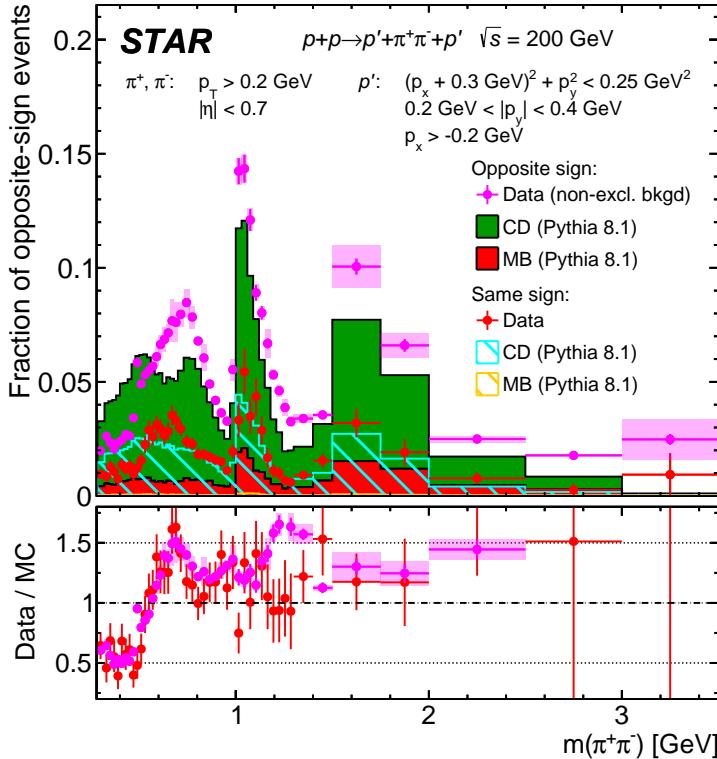


Figure 5.4: Comparison of non-exclusive background as a function of $m(\pi^+\pi^-)$ extracted from data and MC predictions. All offline selections were applied. Normalization of MC components was explained in Sec. 5.3. Opposite-sign non-exclusive background extracted from data is shown with magenta points, while stacked opposite-sign MC predictions are shown with filled histograms. Control same-sign background events are shown with red points for the data, and stacked hatched histograms for MC predictions.

5.2.2 Exclusive background

Exclusive background arising from wrong identification have been estimated with the help of semi-data-driven method. This method uses fast MC generator introduced in Sec. 6.2.2.6, in which all quantities relevant for particle identification (dE/dx and its resolution, TOF time measurement resolution etc.) were set according to their distribution/magnitude in the data. In order to determine absolute size of migrations between three measured species of particle pairs it was required to know the full distribution of particles' (transverse) momenta - especially in the regions of momentum space where the migrations are significant (regions of non-zero $\lambda^{X \rightarrow Y}$ in Fig. 6.11). There are no models of CEP of $\pi^+\pi^-$, K^+K^- and $p\bar{p}$ which describe measured data, therefore we decided to use measured distributions as an input models of (p_T^+, p_T^-) ¹. We assumed that selected CEP pairs have low contamination from the exclusive background (we know that non-exclusive is less than 7%). Such assumption was motivated by restrictive particle identification algorithm, which based on study from Sec. 6.2.2.6 provides high level of identification efficiency and low level of misidentification probability. Also, in the distributions of $\chi_{dE/dx}^2$ and m_{TOF}^2 presented in Fig. 4.20 we see clear features expected for given pair types, without signs of excessfull exclusive background. Having commented that, raw distributions of (p_T^+, p_T^-) for selected CEP events without additional lower track p_T cut C8.2 for kaon and proton pairs (Figs. 5.5a, 5.6a and 5.7a) were assumed to properly represent corresponding detected, reconstructed and identified particle species.

The following procedure was conducted to prepare (p_T^+, p_T^-) distributions finally used to determine exclusive background in all three CEP samples:

1. Distributions exhibit natural symmetry around $p_T^+ = p_T^-$ therefore corresponding mirror-image bins with respect to diagonal were averaged:

$$N_{X,avg}(p_T^+, p_T^-) = N_{X,avg}(p_T^-, p_T^+) = \frac{N_X(p_T^-, p_T^+) + N_X(p_T^+, p_T^-)}{2}. \quad (5.8)$$

Outcome for all three species is shown in Figs. 5.5b, 5.6b and 5.7b.

2. Distributions were corrected for the identification efficiency from Fig. 6.11:

$$N_{X,corr}(p_T^+, p_T^-) = \frac{N_{X,avg}(p_T^-, p_T^+)}{\epsilon^X (\max(p_T^-, p_T^+), \min(p_T^-, p_T^+))}. \quad (5.9)$$

¹ (p_T^{\max}, p_T^{\min}) could be used same well.

At this stage distributions $N_{X,corr}$ represent detected and reconstructed events before identification. They are drawn in Figs. 5.5c, 5.6c and 5.7c.

3. Last step of preparation of (p_T^+, p_T^-) distributions applies only to K^+K^- and $p\bar{p}$, as it is related with the upper cut on $\min(p_T^-, p_T^+)$. Because of this cut we do not have access to region where both-tracks' carry high p_T . We overcome this difficulty by performing an extrapolation of the distributions into the unmeasured region. This is done for the histograms binned as shown in figures mentioned earlier. In a loop over all bins in p_T^- (index i) and in p_T^+ (index j) the following prescription is used to fill empty bins, starting from the bins covering $\min(p_T^-, p_T^+)$ cuts specific for K^+K^- and $p\bar{p}$:

$$N_{X,extr}(p_T^+, p_T^-) = f_{extr} \cdot \frac{N_{X,extr}(p_T^-, i-1, p_T^+, j-1) + N_{X,extr}(p_T^-, i-2, p_T^+, j-2)}{2}. \quad (5.10)$$

In above formula factor f_{extr} determines the “steepness” of the distribution with growing track's p_T . As we observe in $\pi^+\pi^-$ channel the high- p_T tail in the distribution tends to diminish and disappears around (2 GeV, 2 GeV). We find that $f_{extr} = 0.8$ is reasonable to provide picture similar to $\pi^+\pi^-$ in the two remaining CEP channels. Final distributions for K^+K^- and $p\bar{p}$ are drawn in Figs. 5.6d and 5.7d, respectively.

Prepared (p_T^+, p_T^-) distributions were used to obtain predictions for the misidentifications. Samples of exclusive $\pi^+\pi^-$, K^+K^- and $p\bar{p}$ simulated with fast MC, with uniformly distributed (p_T^+, p_T^-) over $0.2 \text{ GeV} < p_T^+, p_T^- < 3 \text{ GeV}$, were subjected to PID algorithm C8. Each event was assigned with the weight equal to the data-extracted event density for given (p_T^+, p_T^-) , such that relative number of $\pi^+\pi^-$, K^+K^- and $p\bar{p}$ pairs was exactly the same as it resulted from (p_T^+, p_T^-) maps in Fig. 5.5c, 5.6d and 5.7d. Histograms of $\chi_{dE/dx}^2$ and m_{TOF}^2 were filled with reconstructed quantities and using aforementioned weight. There were separate histograms for different true-level PIDs and reconstructed PIDs, so that they formed 3×3 array of histograms.

The last step involved proper normalization of the histograms obtained earlier. Predictions for each true-level pair type were normalized independently, but the same normalization was preserved for all quantities and for all reconstructed pair types. Normalization F_X^{MC} of histograms representing prediction for exclusive XX was established such that the number of predicted XX events in the XX signal-dominating region (fiducial region of $\chi_{dE/dx}^2(XX) < 6$), $N_{X \rightarrow X, \text{fid}}^{\text{MC}}$, was equal to the number of measured XX events in that region ($N_{X, \text{fid}}^{\text{data}}$) less a number of non-exclusive background events in the same region ($N_{\text{bkgd}, X, \text{fid}}^{\text{non-excl}}$) extracted with a method introduced in Sec. 5.2.1. It is expressed with the formula in Eq. (5.11):

$$F_X^{\text{MC}} = \frac{N_{X, \text{fid}}^{\text{data}} - N_{\text{bkgd}, X, \text{fid}}^{\text{non-excl}}}{N_{X \rightarrow X, \text{fid}}^{\text{MC}}} \quad (5.11)$$

where all components are explicitly given in Eqs. (5.12)-(5.14):

$$N_{\text{bkgd}, X, \text{fid}}^{\text{non-excl}} = \int_0^6 \frac{dN_{\text{bkgd}, X, \text{fid}}^{\text{non-excl}}}{d\chi_{dE/dx}^2} d\chi_{dE/dx}^2, \quad N_{X, \text{fid}}^{\text{data}} = \int_0^6 \frac{dN_X^{\text{data}}}{d\chi_{dE/dx}^2} d\chi_{dE/dx}^2, \quad N_{X \rightarrow X, \text{fid}}^{\text{MC}} = \int_0^6 \frac{dN_{X \rightarrow X}^{\text{MC}}}{d\chi_{dE/dx}^2} d\chi_{dE/dx}^2. \quad (5.12) \quad (5.13) \quad (5.14)$$

The relation between resultant normalization factors $F_{\pi\pi}^{\text{MC}}/F_{KK}^{\text{MC}}/F_{pp}^{\text{MC}}$ amounts 1/1.01/0.88. Comparisons of the data with the fast MC predictions normalized according above prescription are shown in Fig. 4.20. Fast MC well reproduces measured spectra of $\chi_{dE/dx}^2$ and m_{TOF}^2 for all selected particle pair species.

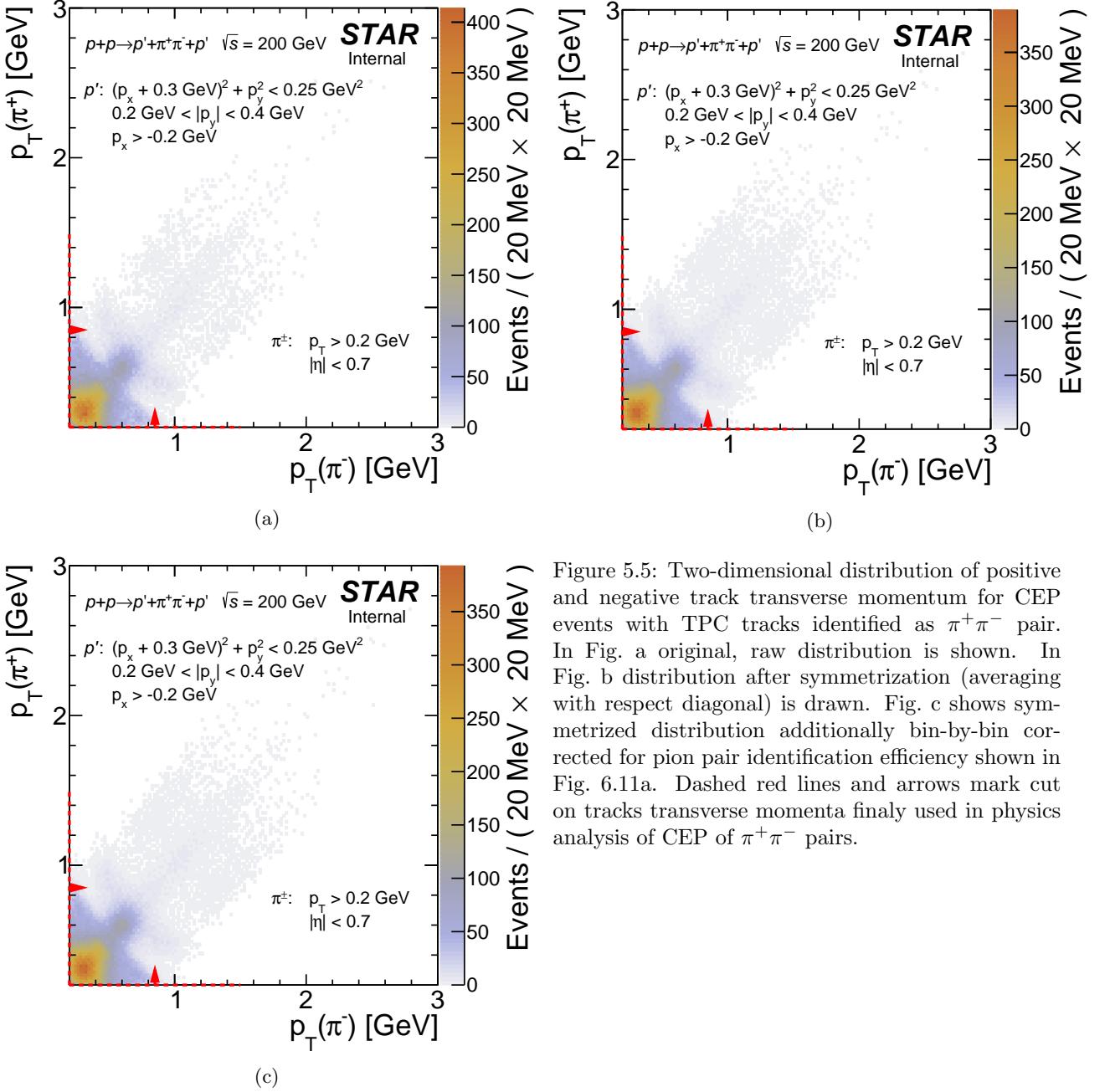


Figure 5.5: Two-dimensional distribution of positive and negative track transverse momentum for CEP events with TPC tracks identified as $\pi^+ \pi^-$ pair. In Fig. a original, raw distribution is shown. In Fig. b distribution after symmetrization (averaging with respect diagonal) is drawn. Fig. c shows symmetrized distribution additionally bin-by-bin corrected for pion pair identification efficiency shown in Fig. 6.11a. Dashed red lines and arrows mark cut on tracks transverse momenta finally used in physics analysis of CEP of $\pi^+ \pi^-$ pairs.



Figure 5.6: Two-dimensional distribution of positive and negative track transverse momentum for CEP events with TPC tracks identified as K^+K^- pair. In Fig. a original, raw distribution is shown. In Fig. b distribution after symmetrization (averaging with respect diagonal) is drawn. Fig. c shows symmetrized distribution additionally bin-by-bin corrected for pion pair identification efficiency shown in Fig. 6.11e. Last distribution in Fig. 5.6d shows pair identification-corrected distribution extrapolated to unmeasured transverse momentum region (transparent green), as described in the text. Dashed red lines and arrows mark cuts on tracks transverse momenta finally used in physics analysis of CEP of K^+K^- pairs.



Figure 5.7: Two-dimensional distribution of positive and negative track transverse momentum for CEP events with TPC tracks identified as $p\bar{p}$ pair. In Fig. a original, raw distribution is shown. In Fig. b distribution after symmetrization (averaging with respect diagonal) is drawn. Fig. c shows symmetrized distribution additionally bin-by-bin corrected for pion pair identification efficiency shown in Fig. 6.11e. Last distribution in Fig. 5.7d shows pair identification-corrected distribution extrapolated to unmeasured transverse momentum region (transparent green), as described in the text. Dashed red lines and arrows mark cut on tracks transverse momenta finally used in physics analysis of CEP of $p\bar{p}$ pairs.

5.2.3 Estimated background content

Numerical summary of the background determination is given in Tab. 5.1. One can see that the dominant source of background is non-exclusive background, which was suppressed down to 5% ($\pi^+\pi^-$, K^+K^-) and 8% ($p\bar{p}$). The exclusive background is typically not larger than 1%, except the case of misidentification of $\pi^+\pi^-$ as K^+K^- (3%).

	Selected events	Non-exclusive background	Exclusive background		
			$\pi^+\pi^-$	K^+K^-	$p\bar{p}$
$\pi^+\pi^-$	85619	4543 (5.3%)	-	653 (0.8%)	18 (0.0%)
K^+K^-	931	50 (5.4%)	28 (3.1%)	-	0 (0.0%)
$p\bar{p}$	68	8 (12.0%)	1 (1.6%)	0 (0.1%)	-

Table 5.1: Summary of backgrounds in CEP $\pi^+\pi^-$, K^+K^- and $p\bar{p}$ channel. Values in brackets are fractions calculated with respect to number of selected events.

5.3 Normalization of signal and background models

Consistency between data and MC, valuable to demonstrate good understanding of the backgrounds and data themselves, has been tested for exclusive $\pi^+\pi^-$ channel². We considered here only non-exclusive backgrounds because of negligible contribution from misidentifications.

Normalization of backgrounds was done separately for two ranges of $\Delta\varphi$. First, MB+elastic background was normalized. By definition this was done only for $\Delta\varphi$ bin representing elastic-like configuration of forward protons ($\Delta\varphi > 90^\circ$). The MB+elastic MC was scaled to have the same integral as the data in range $|\Delta z_{\text{vtx}}| > 100 cm. In this range we assumed sole presence of this type of background, which is characterized by very wide distribution of Δz_{vtx} because of TPC and RP vertices being independent. Comparison plots are contained in Figs. 5.8 and 5.9. An important cross-check for correctness of this assumption is shown in Fig. 5.10, where the data vs. MC collinearity $\Delta\theta$ is presented, defined as$

$$\Delta\theta = \sqrt{(\Delta\theta_x)^2 + (\Delta\theta_y)^2} = \sqrt{(\theta_x^W + \theta_x^E)^2 + (\theta_y^W + \theta_y^E)^2}. \quad (5.15)$$

One can notice part of distribution close to 0, with nearly perfectly collinear protons. The data is well described by MC, which would unlikely be the case without contribution from the red histogram representing MB+elastic background. An interesting observation related to this background contribution is that almost all MB+elastic events in the final plots originate from the Central Diffraction process, with the forward protons outside of RP acceptance - non-diffractive events do not pass tight CEP event selection.

In the second step the CD MC was normalized. It was scaled to have the same integral as the data (minus MB+elastic MC in $\Delta\varphi > 90^\circ$ sub-sample) in range $p_T^{\text{miss}} > 150 MeV, where no exclusive signal is expected.$

In the last step the exclusive $\pi^+\pi^-$ MC was normalized. It was scaled to have the same integral as the data (minus all considered non-exclusive backgrounds) in range $p_T^{\text{miss}} < 75$ MeV, where exclusive signal is dominant. The result of this procedure for the distribution of p_T^{miss} is given in Figs. 5.11 and 5.12. Joint distribution for each quantity - without differentiation with respect to $\Delta\varphi$ - was obtained by adding corresponding event counts from two $\Delta\varphi$ ranges.

As can be observed in the comparison plots, presented data are generally well described by MC. In case of Δz_{vtx} some imperfectness in the position and width of the simulated signal peak can be noticed, most probably arising from slightly underestimated timing resolution of the RP trigger counters in the simulation. Distribution of p_T^{miss} is very well described, for both signal and control channel. The ratio of number of opposite-sign pairs to same-sign pairs is compatible between data and MC, which was possible to achieve by rejecting in Pythia contributions from events with the central state consisting from two opposite-sign pions and at least one neutral particle. These events should be suppressed by the DIPE condition (1.5), which seem to be not taken into account in Pythia at the hadronization level. We demonstrate in Fig. 5.12c that if these events are preserved, Pythia MC cannot describe data in the background-dominating region (large p_T^{miss}).

²Other channels - K^+K^- and $p\bar{p}$ - were not subjected to similar study because of poor MC statistics. However, structure of backgrounds and level of agreement with MC is expected to be similar to that presented for $\pi^+\pi^-$.

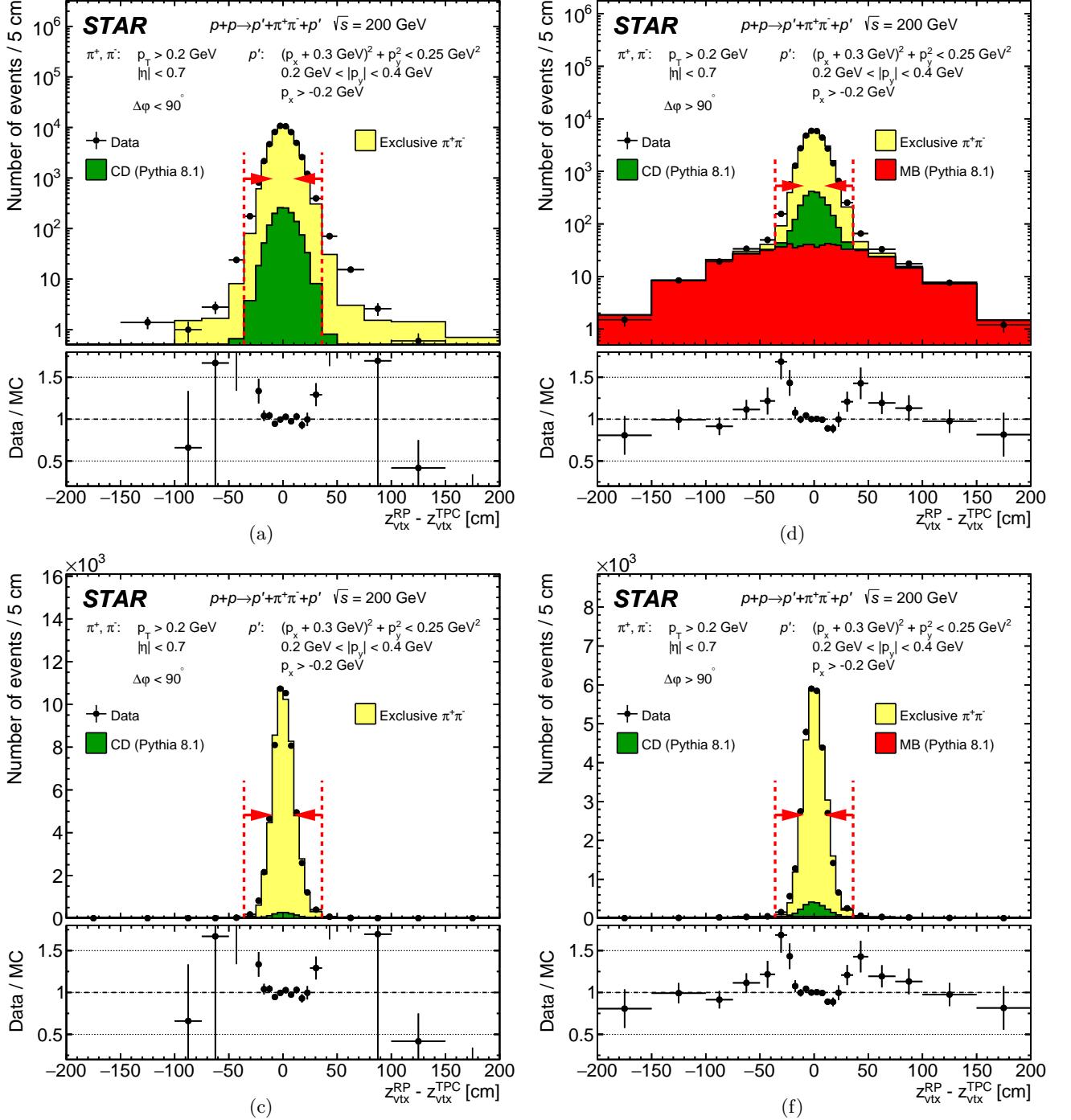
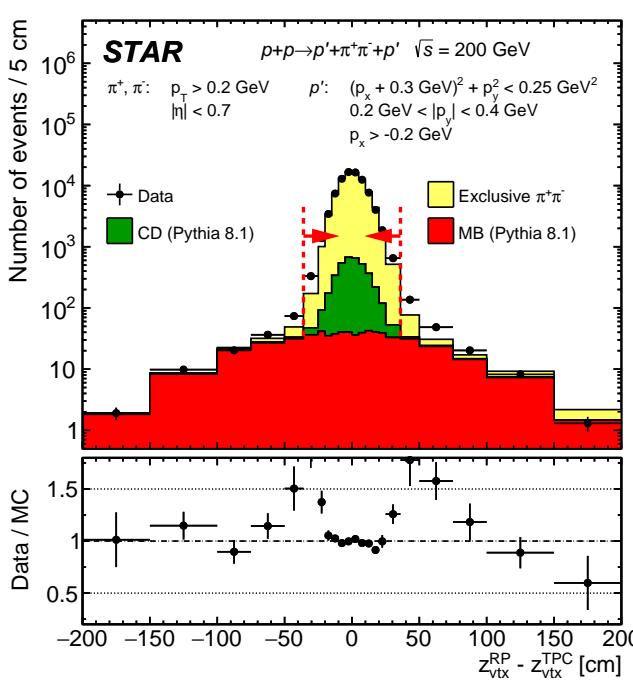
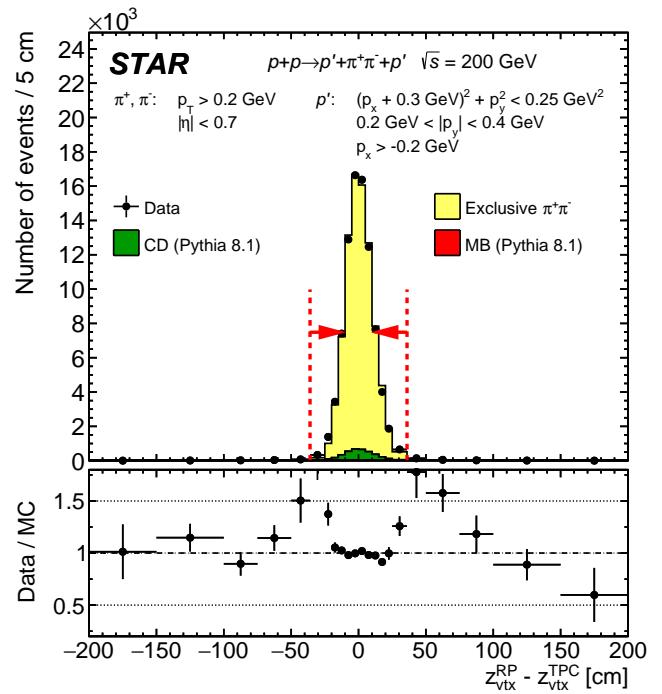


Figure 5.8: Comparison of Δz_{vtx} for CEP $\pi^+\pi^-$ events in two ranges of $\Delta\varphi$ (left: $\Delta\varphi < 90^\circ$, right: $\Delta\varphi > 90^\circ$) between data and embedded MC after full selection (except cut on presented quantity). Plots in top and bottom row differ only in the y -axis (top: logarithmic, bottom: linear). Data are represented by black points, while stacked MC predictions are drawn as histograms of different colors. Histogram from each MC process has been normalized according to prescription in the text. Vertical error bars represent statistical uncertainties, horizontal bars represent bin sizes.



(a)



(b)

Figure 5.9: Comparison of Δz_{vtx} for CEP $\pi^+\pi^-$ events between data and embedded MC after full selection (except cut on presented quantity). Left and right plot differ only in the y -axis (left: logarithmic, right: linear). Data are represented by black points, while stacked MC predictions are drawn as histograms of different colors. Histogram from each MC process has been normalized according to prescription in the text. Vertical error bars represent statistical uncertainties, horizontal bars represent bin sizes.

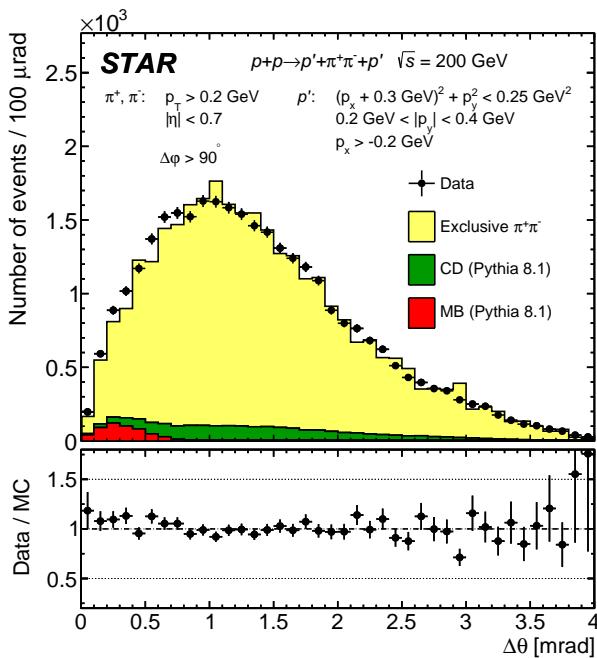


Figure 5.10: Comparison of colinearity $\Delta\theta$ for CEP $\pi^+\pi^-$ events with $\Delta\varphi > 90^\circ$ between data and embedded MC after full selection. Data are represented by black points, while stacked MC predictions are drawn as histograms of different colors. Histogram from each MC process has been normalized according to prescription in the text. Vertical error bars represent statistical uncertainties, horizontal bars represent bin sizes.

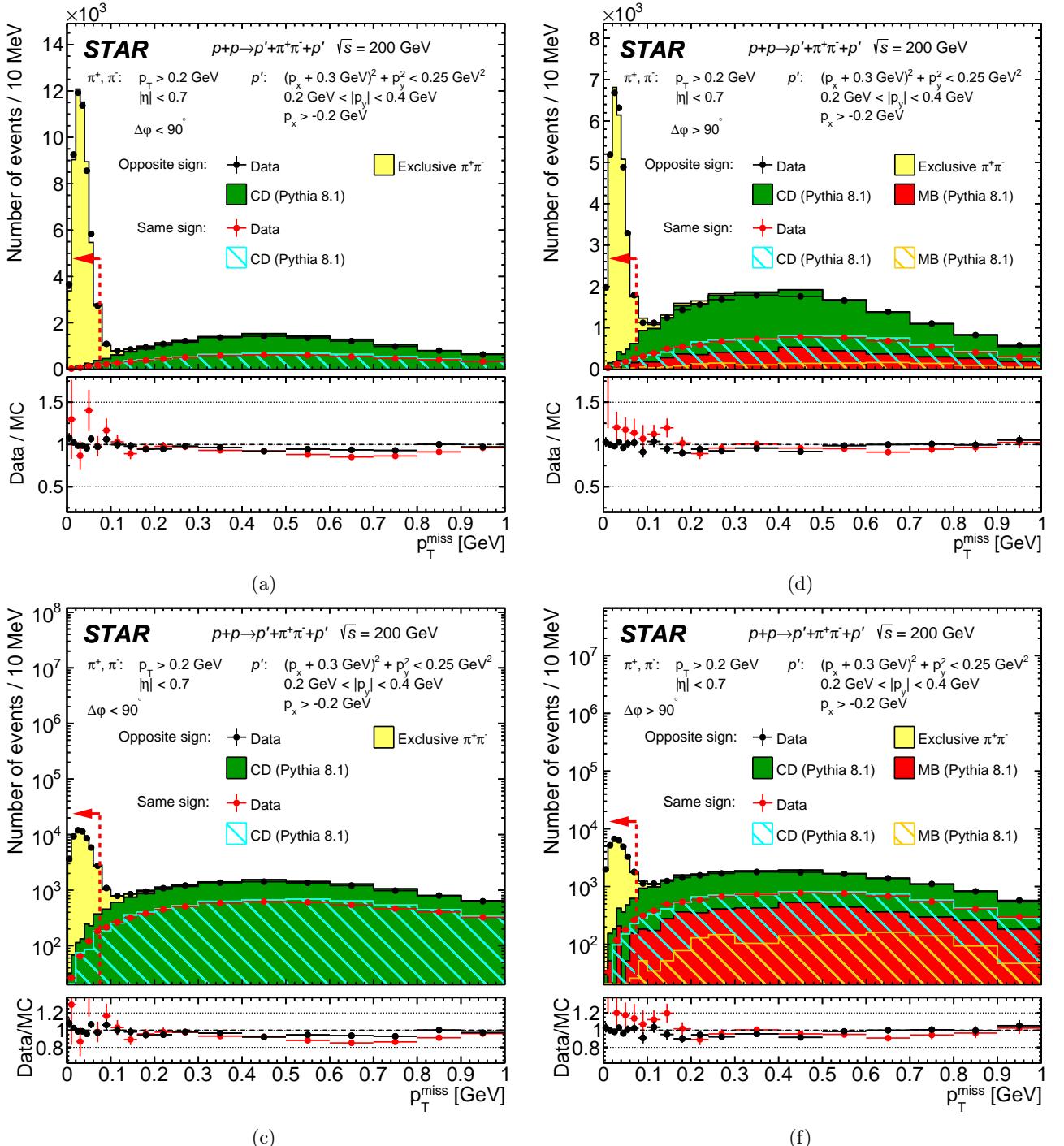


Figure 5.11: Comparison of p_T^{miss} for CEP $\pi^+\pi^-$ events in two ranges of $\Delta\varphi$ (left: $\Delta\varphi < 90^\circ$, right: $\Delta\varphi > 90^\circ$) between data and embedded MC after full selection (except cut on presented quantity). Plots in top and bottom row differ only in the y -axis (top: linear, bottom: logarithmic). In addition to signal channel (opposite-sign particles) also control background channel (same-sign particles) is contained in the plots. Data are represented by black (opposite-sign) or red (same-sign) points, while stacked MC predictions are drawn as filled (opposite-sign) or hatched (same-sign) histograms of different colors. Histogram from each MC process has been normalized according to prescription in the text. Vertical error bars represent statistical uncertainties, horizontal bars represent bin sizes.

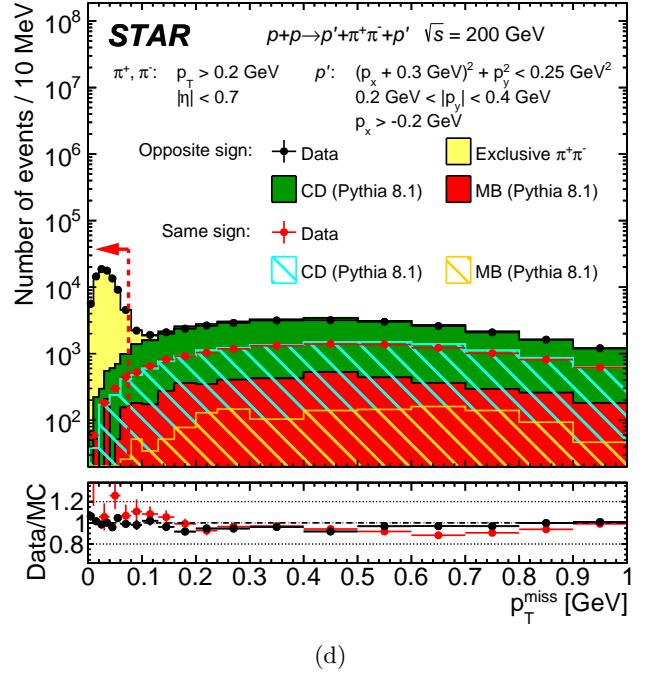
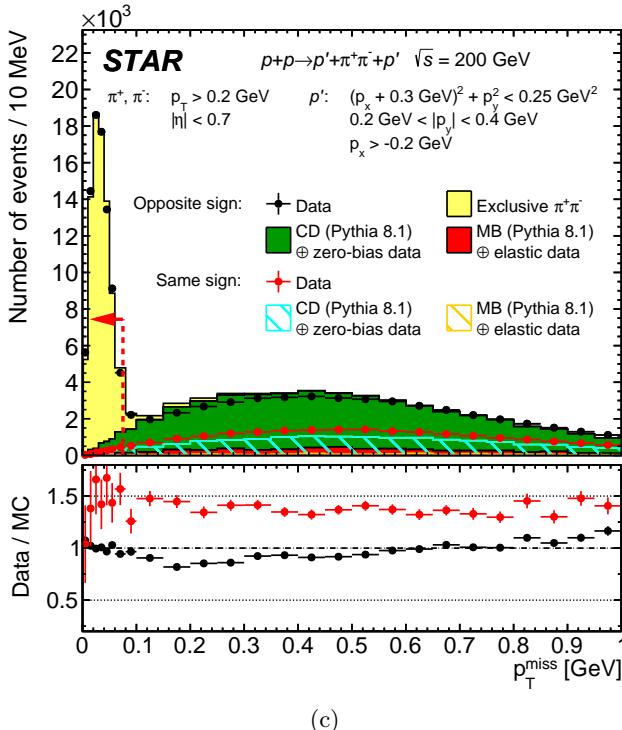
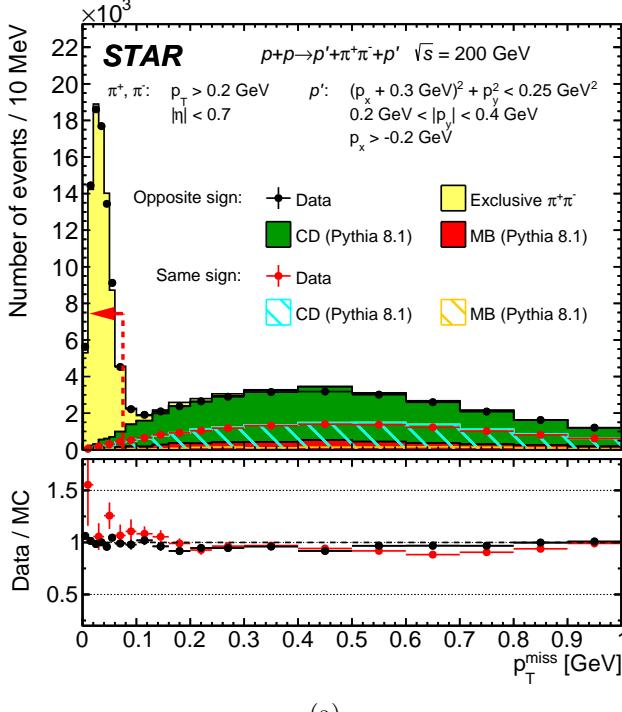


Figure 5.12: Comparison of p_T^{miss} for CEP $\pi^+\pi^-$ events between data and embedded MC after full selection (except cut on presented quantity). Top left and top right plot differ only in the y -axis (left: linear, right: logarithmic). In addition to signal channel (opposite-sign particles) also control background channel (same-sign particles) is contained in the plots. Data are represented by black (opposite-sign) or red (same-sign) points, while stacked MC predictions are drawn as filled (opposite-sign) or hatched (same-sign) histograms of different colors. Histogram from each MC process has been normalized according to prescription in the text. Vertical error bars represent statistical uncertainties, horizontal bars represent bin sizes. Left bottom plot differ from the top plots in the content of Pythia MCs - in the bottom plot events with $\pi^\pm\pi^\mp + \text{neutrals}$ in the central state were preserved, demonstrating significant inconsistency between data and MC in the ratio of opposite-sign to same-sign events if such events are not rejected.

6. Corrections

In this chapter we describe methodology of correcting the data to the hadron-level cross sections. We describe technical details of the procedure (Sec. 6.1), as well as present derivation of relevant acceptances and efficiencies (Sec. 6.2). At the end of the chapter we show the closure tests performed on MC to validate data correction procedure together with the entire set of efficiencies.

6.1 Method of corrections application

Differential cross section in every bin of measured quantity of interest q have been calculated according to Eq. (6.1):

$$\frac{d\sigma}{dq} = \frac{1}{\Delta q} \times \frac{1}{\varepsilon} \times \frac{N^w - N_{\text{bkgd}}^w}{L_{\text{int}}^{\text{eff}}}, \quad (6.1)$$

where N^w is weighted number of measured events in given bin, N_{bkgd}^w is weighted number of background events in given bin, Δq is width of the bin, ε is joint efficiency of

$$L_{\text{int}}^{\text{eff}} = \sum_{\text{run}} L_{\text{int}}^{\text{run}} \times \epsilon_{\text{veto}}(L^{\text{run}}) \quad (6.2)$$

$$\varepsilon = \epsilon_{\text{ET/IT}} \times \epsilon_{\text{vrtx}}(q) \times \epsilon_{C2} \times \epsilon_{C5} \times \epsilon_{C9} \times \epsilon_{\text{PID}}(q) \quad (6.3)$$

$$N^w = \sum_{\text{event}} w_{\text{event}} \quad (6.4)$$

$$w = \left[\prod_{\text{sign}} \epsilon_{\text{TOF}}(\text{sign}, \text{PID}, p_T, z_{vx}, \eta) \times \prod_{\text{sign}} \epsilon_{\text{TPC}}(\text{sign}, \text{PID}, p_T, z_{vx}, \eta) \times \prod_{\text{side}} \epsilon_{\text{RP}}^{\text{side}}(p_x, p_y) \right]^{-1}, \quad (6.5)$$

$\text{sign} \in \{+, -\}, \text{ side} \in \{E, W\}$

Figure ?? shows the distribution of weights for all three types of analyzed particle pairs. These correction factors are large, however they are products of many other factors which are in general close to 1.

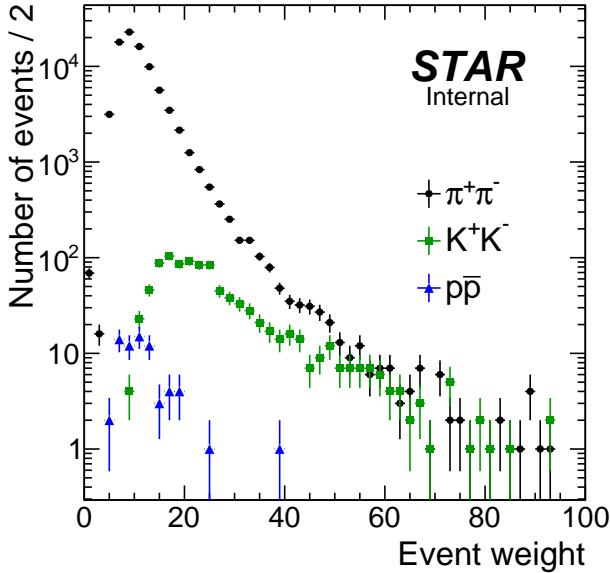


Figure 6.1: Distribution of weights assigned to selected CEP events in $\pi^+\pi^-$ (black circle), K^+K^- (red square) and $p\bar{p}$ (blue triangle) channel.

6.2 Acceptances and efficiencies

In this section we present calculation of all efficiencies except TPC track reconstruction and TOF hit reconstruction and matching efficiency, which were discussed and presented in Ref. [1].

6.2.1 Trigger efficiency

6.2.1.1 Online TOF efficiency

The efficiency of the part of the trigger related to TOF subsystem $\mathcal{E}_{\text{TOF}}^{\text{trig}}$ was calculated using the zero-bias data. Events with exactly 1 TOF vertex (cut C1), exactly 2 primary good quality TOF-matched TPC tracks (cuts C3.1, C3.4) and maximally 3 TOF clusters (cut C7) were used to calculate this efficiency defined as a probability of having at least two TOF hits on the trigger level in selected set of events:

$$\mathcal{E}_{\text{TOF}}^{\text{trig}} = \frac{\#\text{events with } \geq 2 \text{ L0 TOF multiplicity and 1 TOF vtx and 2 TOF trks and } \leq 3 \text{ TOF cltrs}}{\#\text{events with 1 TOF vtx and 2 TOF trks and } \leq 3 \text{ TOF cltrs}} \quad (6.6)$$

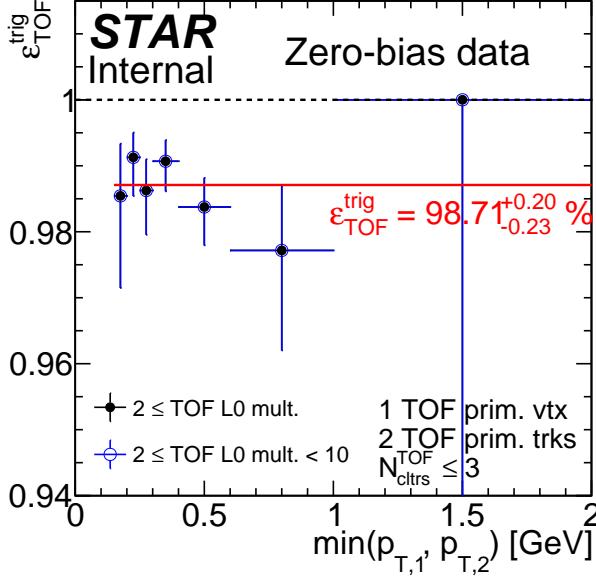


Figure 6.2: TOF trigger efficiency as a function of lower p_T of two TOF-matched tracks. Black points denote efficiency of requirement of at least 2 online TOF hits, while open blue circles represent efficiency with added upper multiplicity limit (< 10). These efficiencies are identical therefore the same efficiency (98.7%, solid red line) is used as a correction factor for all analyzed events.

It has been verified that described efficiency does not depend on the transverse momentum of two tracks. In Fig. 6.2 we show dependence of the TOF trigger efficiency in one dimension, as a function of lower p_T of two TOF-matched tracks. Data points are consistent with constant value, herefore a single number for this efficiency is used, equal to 98.7%. It is important to account for the fact that at some point of data-taking (see Tab. 2.1) an upper limit (< 10) on L0 TOF multiplicity was imposed. Study shows that with the cut on offline TOF cluster multiplicity (cut C7) the efficiency of the trigger with and without upper limit of online TOF multiplicity remains unchanged, so the same value of the efficiency is used for the entire dataset.

6.2.1.2 Online veto (BBC-small and ZDC veto)

Vetoing signal in BBC-small and ZDC detectors on both sides of STAR was implemented in the logic of RP_CPT2 trigger. Common correction of the online and offline vetoes which is used in the correction procedure explained in Sec. 6.1 is presented in Sec. 6.2.2.3. However, to help quantify effect of just the online vetoes in BBC-small and ZDCs we show the Fig. 6.3 with the efficiency of the joint BBC-small and ZDC veto as a function of the instantaneous luminosity calculated from the zero-bias data. Details of the way the efficiency was calculated as well as description of the data in the Figure is the same as explained in Sec. 6.2.2.3.



Figure 6.3: Overall efficiency of the online BBC-small and ZDC veto as a function of instantaneous luminosity.

6.2.1.3 RP triggering efficiency

Based on studies presented in Sec. 10.4 of Ref. [1] we concluded that the RP triggering efficiency is nearly 100 %, which is in agreement with the Geant4 MC simulation of RP system. Therefore we use in the correction procedure

$$\mathcal{E}(\text{TR}^E \wedge \text{TR}^W) = \mathcal{E}(\text{TR}^W) \times \mathcal{E}(\text{TR}^E) = 1. \quad (6.7)$$

6.2.1.4 Up and Down RP combination veto (due to dead material)

Probability that secondaries induced by proton with successfully reconstructed and selected RP track generate a trigger signal in the other RP branch on the same side was calculated using the embedded MC (see Sec. 6.3 in Ref. [1] for details of RP simulation in Geant4). Forward protons from CEP process provided by GenEx [20] were simultaneously generated from the interaction point spatially distributed the same as in the data. MC samples for all runs with RP_CPT2 triggers were produced to account for non-constant positions of the RP detectors throughout the run 15. Number of simulated events for each run was proportional to number of RP_CPT2 triggers in given run. The angular divergence of the beams was also simulated.

The discussed probability, $\mathcal{P}_{\text{DM veto}}^{\text{side}}$, was calculated as a probability that a MC-trigger signal is present in the branch on given side other than east and west branches where primary forward protons are expected from their initial momenta, under condition that these east and west branches detect a MC-trigger signal and there is no veto due to simultaneous ET&IT trigger bits in the overlayed data (no pile-up veto). By MC-trigger we understand the trigger signal reconstructed solely from the simulated data (not from the data embedded into).

Technically the $\mathcal{P}_{\text{DM veto}}^{\text{side}}$ was obtained in the following procedure:

1. No simultaneous ET&IT trigger bits were allowed in the data of an event that simulated signal was embedded into.
2. It was verified if there are MC-trigger signals in east and west branches that the primary forward protons were expected to reach based on their p_y ($p_y > 0$ - branch UP, $p_y < 0$ - branch DOWN). These events formed set *A*.
3. Events with the MC-trigger signal in RP branch other than the branch with MC-trigger signal expected from proton p_y on given side formed set *B*.
4. The probability was determined by the ratio of histograms from set *B* and set *A*:

$$\begin{aligned} \mathcal{P}_{\text{DM veto}}^{\text{side}}(p_x, p_y, z_{\text{vtx}}) &= \mathcal{E}^{\text{side}}(\text{Veto}^{\text{DM}} | \text{!Veto}^{\text{PU}} \wedge \text{TR}^E \wedge \text{TR}^W) = \\ &= \frac{(p_x, p_y, z_{\text{vtx}}) \text{ histogram for protons from set } B}{(p_x, p_y, z_{\text{vtx}}) \text{ histogram for protons from set } A} \end{aligned} \quad (6.8)$$

It should be noted that the momentum components (p_x, p_y) were taken from the proton with accounted effect of the beam divergence (after the original initial momentum smearing). Sample probability of a dead-material-induced veto is shown in Fig. 6.4, with all the remaining results contained in Appendix F.

The efficiency of the discussed veto which is finally used to correct the data is opposite of the veto probability, namely

$$\epsilon_{\text{DM veto}}^{\text{side}} = 1 - \mathcal{P}_{\text{DM veto}}^{\text{side}}. \quad (6.9)$$

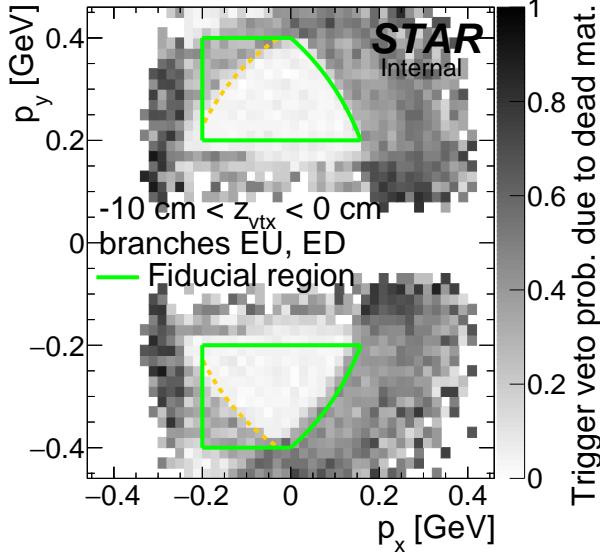


Figure 6.4: Sample probability of ET&IT trigger veto due to forward proton interaction with dead material. Results were obtained from forward proton MC simulation embedded into zero-bias data.

6.2.2 Reconstruction and selection efficiency

6.2.2.1 TPC z -vertex cut (C2)

Removing from analysis specific range of z -positions of primary vertices effectively reduces accepted luminosity with respect to that delivered by the collider. This loss of luminosity has to be accounted when calculating the cross sections, which is the goal of presented analysis. Assuming that the distribution of z_{vtx} of all primary interactions that take place when east and west beams overlap follows a normal distribution (\mathcal{N}), then the formula describing efficiency of the cut C2 has the following form:

$$\epsilon_{z_{\text{vtx}}} = \int_{z_{\text{vtx}}^{\min}}^{z_{\text{vtx}}^{\max}} \mathcal{N}(z_{\text{vtx}}; \mu, \sigma) dz_{\text{vtx}} = \frac{1}{2} \left[\text{Erf} \left(\frac{z_{\text{vtx}}^{\max} - \mu}{\sqrt{2}\sigma} \right) - \text{Erf} \left(\frac{z_{\text{vtx}}^{\min} - \mu}{\sqrt{2}\sigma} \right) \right], \quad (6.10)$$

where z_{vtx}^{\min} and z_{vtx}^{\max} are respectively minimum and maximum value of the longitudinal position of the vertex accepted in analysis (in our case these are -80 cm and 80 cm), and parameters μ and σ are respectively the mean and standard deviation of the normal distribution:

$$\mu = \langle z_{\text{vtx}} \rangle, \quad \sigma = \sigma(z_{\text{vtx}}).$$

Real parameters of z_{vtx} distribution were studied separately for every single fill of the collider. It is motivated by the fact that each fill of the machine is nearly independent from the previous thus the shape and position of z_{vtx} may vary on fill by fill basis. We neglect possible changes within the fill (e.g. widening of the distribution due to intrabeam scattering etc.) arguing that this effect if expected to be smaller than the systematic uncertainties related to determination of position and width of z_{vtx} distribution.

For every fill of RHIC the distribution of z_{vtx} of single TOF vertices was prepared, as shown in Fig. 6.5. This distribution was fitted with the Gaussian function in a range $z_{\text{vtx}} \in [-120 \text{ cm}, 120 \text{ cm}]$. The output parameters of all fits were plotted as a function of the fill number, as shown in Fig. 6.6. The efficiency used in the correction procedure was calculated independently for each fill using presented values of $\langle z_{\text{vtx}} \rangle$ and $\sigma(z_{\text{vtx}})$. Typical numerical value of this efficiency equals $\sim 88\%$.

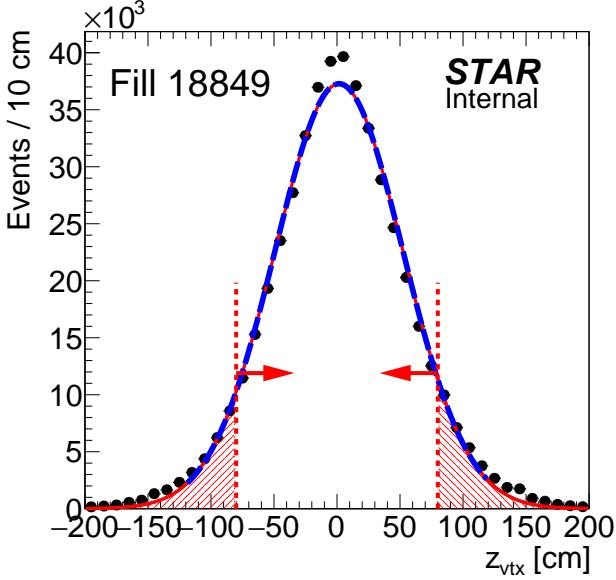


Figure 6.5: Sample distribution of z_{vtx} of single TOF vertices together with the fit of normal distribution (dashed blue) extended outside the range of the fit (solid red). Hashed red area represents part of the distribution rejected by cut C2 with the cut value marked with dashed red vertical lines and arrows.

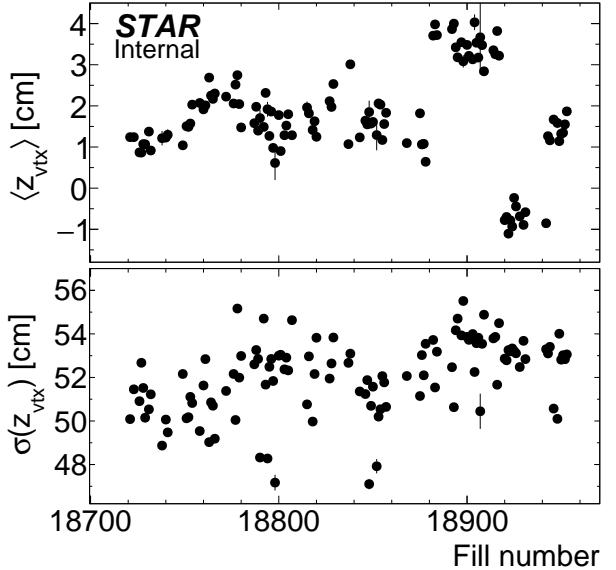


Figure 6.6: Mean (top panel) and width (bottom panel) parameters of the normal distribution obtained from a fit of normal distribution to z_{vtx} distribution in a range $[-120 \text{ cm}, 120 \text{ cm}]$ for each RHIC fill as a function of the fill number.

6.2.2.2 TPC-RP z -vertex matching (C5)

This cut was safely set to $3.5\sigma_{\Delta z_{\text{vtx}}}$, therefore the correction for the introduced inefficiency is negligible.

6.2.2.3 Primary vertices limit (C1), BBC-large veto (C6), TOF clusters limit (C7) and Up and Down RP combination veto (due to pile-up)

Combined efficiency of the online veto in BBC-small and ZDC (Sec. 6.2.1.2) and offline cuts (vetoes) on extra TPC-TOF vertices, extra TOF clusters, signal in BBC-large and simultaneous signal in Up and Down RPs, was calculated using the zero-bias data. For each run a fraction of events (for colliding bunches) was calculated in which all mentioned cuts would be satisfied in case of the CEP $\pi^+\pi^-/K^+K^-/p\bar{p}$ event (event would not be vetoed). One can transform this prescription to simple formula below:

$$\epsilon_{b_E b_W}^{\text{veto}} = \frac{\# \text{events in the run without TOF vertices, without signal in BBC-S, BBC-L, ZDC, RP branches other than } b_E, b_W, \text{ and with no more than 1 reconstructed TOF cluster}}{\# \text{events in the run}} \quad (6.11)$$

In Fig. 6.7 this efficiency is presented as a function instantaneous luminosity delivered by the machine, for each combination of east and west RP branches. Result for each combination is nearly identical as the effect of ET&IT trigger veto in RPs is not dominant, as well as trigger in all branches had similar acceptance. The data points were fitted with the exponential function (of the form contained in the figure) which reflects the fact that this efficiency should behave similar to the probability of lack of any interaction in the bunch crossing given by the Poisson distribution:

$$\text{Pois}(0; \mu) = \frac{\mu^0}{0!} \times e^{-\mu} = e^{-\mu}. \quad (6.12)$$

Comparison of the μ in Eq. (6.12) with the fit parameters in Fig. 6.7 leads to approximate determination of the average interaction probability per bunch crossing equal $0.2 - 0.9$. The result of the fit, $\epsilon_{b_E b_W}^{\text{veto}}(\mathcal{L})$, is finally used to correct measured data as described in Sec. 6.1.

Comparison of efficiencies in Fig. 6.7 with similar efficiency in Fig. 6.3 demonstrates that offline selection has much smaller impact on the loss of signal events than online selection. It has to be underlined that online vetoes were necessary to set trigger purity to satisfactory level, as well as reduce prescale of the trigger.

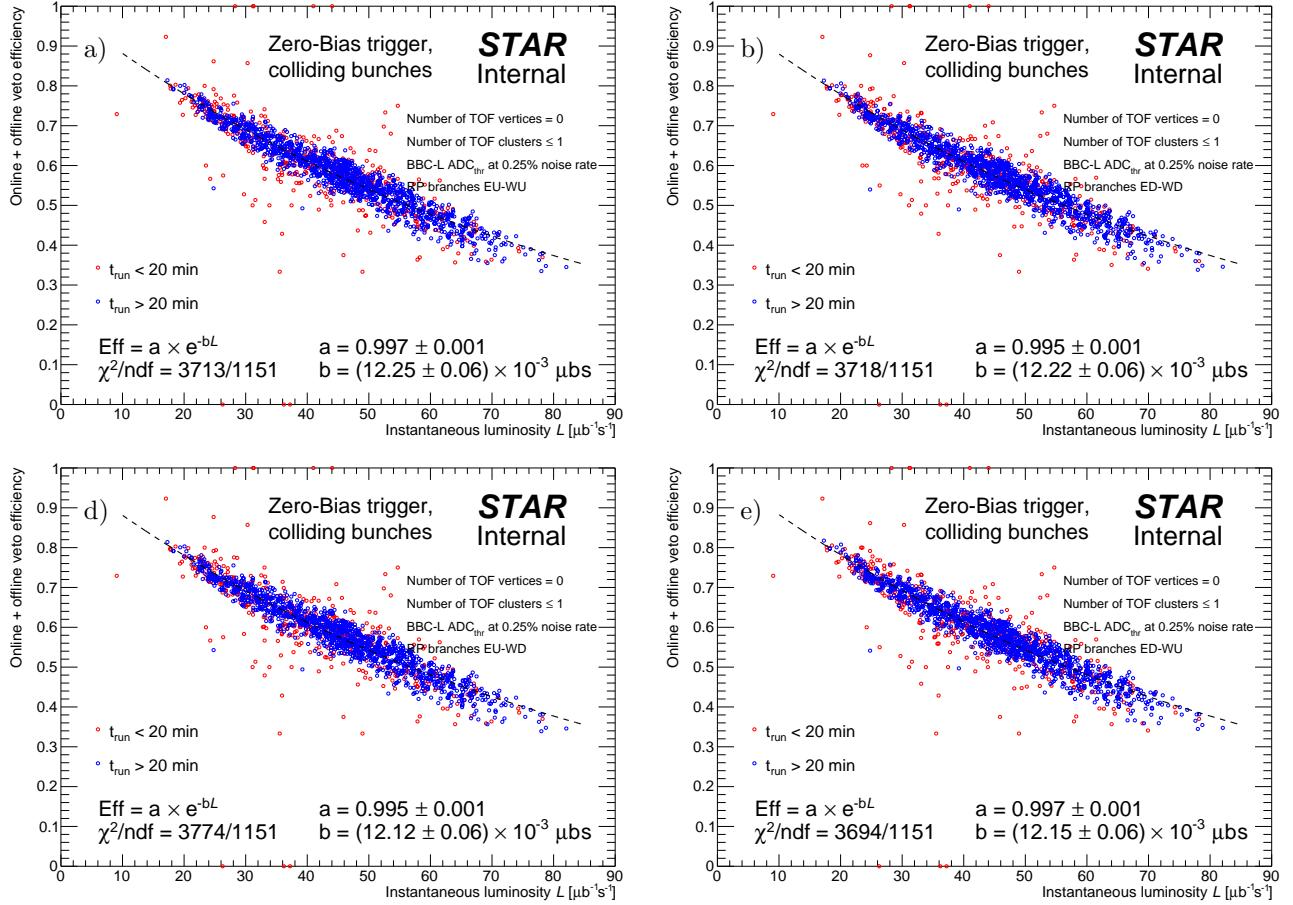


Figure 6.7: Overall efficiency of the online BBC-small, ZDC and ET&IT trigger veto, primary vertices limit (C1), BBC-large veto (C6) and TOF clusters limit (C7) as a function of instantaneous luminosity for all possible combinations of east and west RP branches. Red and blue points represent runs lasting for less and more than 20 minutes, respectively. Black dotted lines represent fits of exponential functions to blue points.

6.2.2.4 TOF clusters limit (C7)

Correction described in previous section (Sec. 6.2.2.3) covers inefficiency related to the pile-up interactions. It is also possible that a higher multiplicity of TOF clusters is generated in the exclusive h^+h^- signal event. Therefore, the upper limit on the number of TOF clusters equal to 3 introduces some inefficiency. To study this effect a no-pile-up signal MC was analyzed (pure STARsim without embedding into zero-bias data).

In Fig. 6.8 the multiplicity of TOF clusters is shown for the signal MC. One can clearly notice that with cut on $N_{\text{cltrs}}^{\text{TOF}} \leq 3$ some part of the signal is truncated. The level of truncation is presented in Fig. 6.9 as a function of the invariant of the $\pi^+\pi^-$. No significant mass dependence is observed hence we use a single efficiency correction number equal to 95.7%, which results from the fit of a constant to efficiency points.

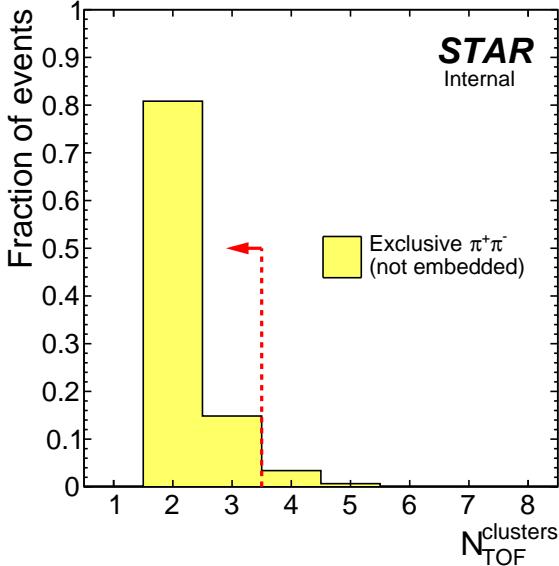


Figure 6.8: Multiplicity of $N_{\text{cltrs}}^{\text{TOF}}$ in CEP $\pi^+\pi^-$ events passed through STAR detector simulation without embedding into zero-bias data. Red dashed line and arrow mark the limit on number of TOF clusters accepted in analysis.

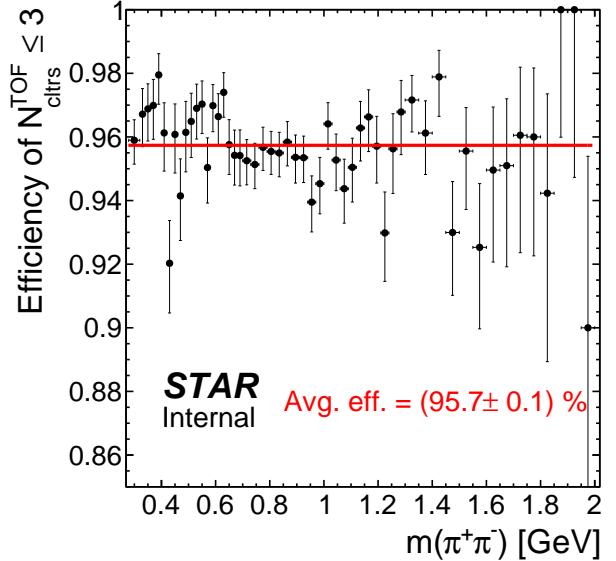


Figure 6.9: Efficiency of upper limit of $N_{\text{cltrs}}^{\text{TOF}}$ as a function of the invariant mass of the $\pi^+\pi^-$, based on the STAR simulation of exclusive $\pi^+\pi^-$ without embedding into zero-bias data. Red line shows the fit of a constant to all efficiency points.

6.2.2.5 Missing p_T cut (C9)

The resolution of the total transverse momentum is in general determined by the angular divergence of the proton beams. Based on known parameters of the beams in run 15 (see Ref. [28]) expected divergence for a single beam amounts $180 \mu\text{rad}$. In forward proton track reconstruction the direction of the incoming proton is assumed to be the same in each event (aligned with nominal z -axis), hence effectively the transverse components of reconstructed forward protons momenta are smeared by this amount. One can check the comparison of the collinearities of elastically scattered protons in the data and embedded MC (Fig. 10.19 of Ref. [1]) to see the satisfactory agreement between the two with assumed MC angular divergence equal to $180 \mu\text{rad}$. For 100 GeV beam such divergence results in smearing of the transverse momentum components for (elastically) scattered protons equal $100 \text{ GeV} \times 180 \cdot 10^{-6} = 18 \text{ MeV}$. Using this value to calculate the resolution of total $p_x(p_y)$ momentum of two forward protons we get $\sqrt{2} \times 18 \text{ MeV} = 25.5 \text{ MeV}$. One can compare it with the output of fits to distributions of $p_x^{\text{miss}}(p_y^{\text{miss}})$ and find that indeed the angular beam divergence dominates the resolution of the total transverse momentum in CEP events.

There is, however, another ingredient to the total transverse momentum resolution, namely the momentum resolution of the central tracks, whose significance rises up together with increasing track p_T . Most of CEP events is characterized by low invariant mass of the central tracks pair ($\lesssim 1.5 \text{ GeV}$) which is inextricably linked with low momentum of tracks ($\lesssim 0.7 \text{ GeV}$), therefore an effect of p_T^{miss} widening is barely visible in the missing momentum distribution integrated over mass (e.g. Fig. 4.22). Nevertheless one can calculate the efficiency of the exclusivity cut as a function of the central tracks momenta to directly see this effect.

Physics model of the CEP process from GenEx was used in embedded signal MC, therefore there was no sufficient statistics (too low population of high- p_T tracks) to calculate the efficiency of p_T^{miss} cut as a function of central tracks momenta. In such case the efficiency of this cut was calculated using simplified MC method described below.

A simple CEP event generator was used to produce large sample of CEP events (kinematics of protons and pions) in the fiducial phase space of the measurement. For each event the hadronic level momenta of positive and negative central tracks were smeared according to resolution function obtained from the embedded MC (6 MeV if $p_T < 0.3 \text{ GeV}$, $2.4 \text{ MeV} + 1.2\% \times p_T$ if $p_T > 0.3 \text{ GeV}$). Next, the p_x^{miss} and p_y^{miss} were calculated from these smeared pions momenta and hadronic level forward protons momenta. Both p_x^{miss} and p_y^{miss} were added the Gaussian component corresponding to the experimental resolution extracted in Figs. 4.22a and 4.22b (means and standard deviations printed in the plots were used). At the end, p_T^{miss} was calculated with the use of Eq. (4.15). The efficiency of the exclusivity cut was defined as a following ratio:

$$\epsilon_{p_T^{\text{miss}}} (p^{\max}, p^{\min}) = \frac{N_{p_T^{\text{miss}}} (p^{\max}, p^{\min})}{N_{\text{all}} (p^{\max}, p^{\min})}, \quad (6.13)$$

where N_{all} is a number of all generated CEP events and $N_{p_T^{\text{miss}}}$ is number of events passing exclusivity cut C9. The result is shown in Fig. 6.10. The cut efficiency for very low tracks momenta (low pair invariant mass) obtained from simple MC (96.8%) agrees perfectly with the efficiency calculated using embedded MC sample for the same momenta range (96.4%), which validates presented efficiency. Clearly, the deterioration of the central track momentum resolution starts to play significant role in efficiency of p_T^{miss} cut at about 1 GeV track momentum.

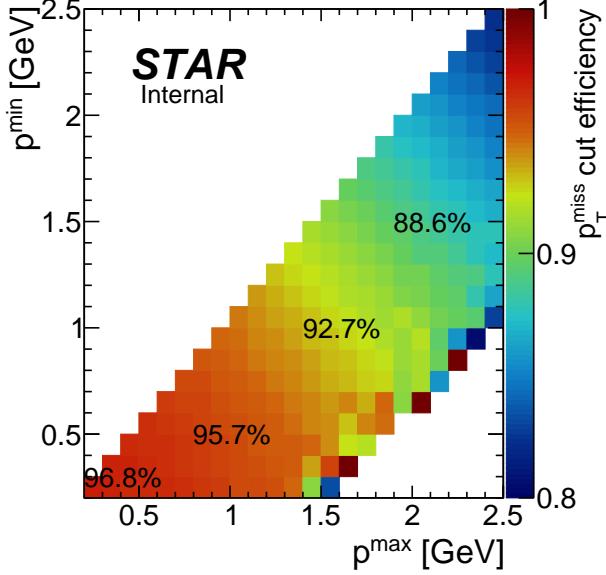


Figure 6.10: Efficiency of p_T^{miss} cut as a function of higher (x -axis) and lower (y -axis) momentum of the central tracks, calculated with MC method described in the text of this Section. Efficiency in a few points of $(p^{\text{min}}, p^{\text{max}})$ space is printed on top of the plot. Lower right corner has no entries/low statistics due to kinematic constraints in the fiducial phase space; this region is not populated with events in the data.

6.2.2.6 Particle identification (C8)

The identification efficiency/misidentification probability was studied in two dimensions - as a function of particles' momenta. Because of that the shape of momentum distribution for PID efficiency study was not required to match the data and was defined flat, spanning between 0.2 GeV and 3 GeV, to provide low statistical uncertainties over full momentum space. We considered particles' momenta as the best quantities to study pair identification because $n\sigma_X$ and m_{TOF}^2 and their resolutions depend nearly solely on magnitude of momentum.

The identification efficiency ϵ^X and misidentification probability $\lambda^{X \rightarrow Y}$ were calculated for each species using the pair selection cuts C8.1 described in more detail in Sec. 4.2.7, following the definitions provided in Eqs. (6.14) and (6.15):

$$\epsilon^X(p^{\text{max}}, p^{\text{min}}) = \frac{N_{\text{true}X}^{\text{reco}X}(p^{\text{max}}, p^{\text{min}})}{N_{\text{true}X}(p^{\text{max}}, p^{\text{min}})}, \quad (6.14) \quad \lambda^{X \rightarrow Y}(p^{\text{max}}, p^{\text{min}}) = \frac{N_{\text{true}X}^{\text{reco}Y}(p^{\text{max}}, p^{\text{min}})}{N_{\text{true}X}(p^{\text{max}}, p^{\text{min}})}, \quad (6.15)$$

where $N_{\text{true}X}$ is number of XX pairs, $N_{\text{true}X}^{\text{reco}X}$ is number of XX pairs correctly recognized as XX , $N_{\text{true}X}^{\text{reco}Y}$ is number of XX pairs misidentified as YY and p^{max} and p^{min} are respectively higher and lower momentum of particles in the pair. The results as a function of unsmeared true-level $(p^{\text{max}}, p^{\text{min}})$ are presented in Fig. D.1 (Appendix D). Here in Fig. 6.11 we show the result presented as a function of higher and lower transverse momentum of particles in the pair $(p_T^{\text{max}}, p_T^{\text{min}})$. This result clearly indicated necessity of adding a cut on the lower transverse momentum of particle in the pair for K^+K^- and $p\bar{p}$, as above certain p_T^{min} the identification efficiency drops to a very low level (< 10%). The cuts (C8.2) are $p_T^{\text{min}} > 0.7$ GeV for kaons and $p_T^{\text{min}} > 1.1$ GeV for protons, indicated with dashed blue lines and arrows.

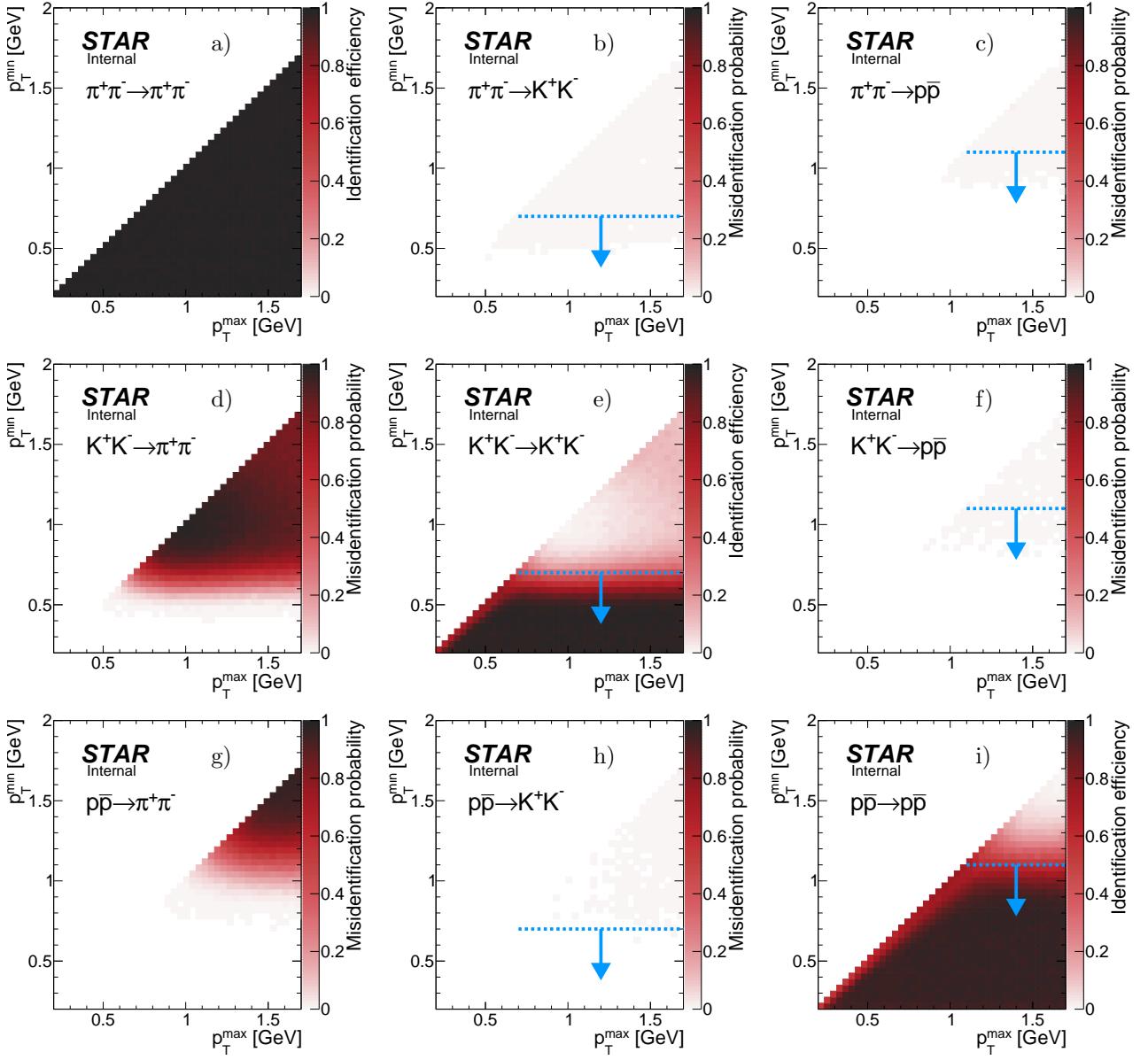


Figure 6.11: Pair identification efficiency (diagonal) and misidentification probability (off-diagonal) as a function of tracks' p_T for $\pi^+\pi^-$, K^+K^- and $p\bar{p}$ pairs. The results were obtained from the dedicated MC simulation described in the text. Blue lines and arrows mark the cut value on lower of the track p_T 's for kaons and protons.

6.2.3 RP track acceptance and reconstruction efficiency

To calculate RP acceptance and track reconstruction efficiency the embedded MC technique was used. The same sample was used as that described in Sec. 6.2.1.4, used for calculation of the dead-material related trigger veto.

The joint RP acceptance and track reconstruction efficiency for a given STAR side, $\epsilon_{RP}^{\text{side}}$, was calculated as a probability that a single good quality RP track (satisfying cuts C4.1-C4.2) matched with true-level primary forward proton is reconstructed on given side in the branch expected based on sign of p_y of the proton, under condition that there is a trigger signal in that branch and there is no trigger signal in the other branch on the same side.

Technically the $\epsilon_{RP}^{\text{side}}$ was obtained in the following procedure:

1. It was verified if there is a trigger signal in the branch that the primary forward proton is expected to reach based on its p_y ($p_y > 0$ - branch UP, $p_y < 0$ - branch DOWN). Additionally required lack of trigger signal in the other branch on the same side. These events formed set *A*.
2. The nominal RP track selection algorithm was used to find a single good quality track (cuts C4.1-C4.2) on given side. If exactly one such track was found, it was additionally checked if it is matched with true-level

primary proton. These events formed *set B*.

3. The efficiency was determined by the ratio of histograms from *set B* and *set A*:

$$\epsilon_{\text{RP}}^{\text{side}}(p_x, p_y, z_{\text{vtx}}) = \mathcal{E} \left(\text{RP}^{\text{side}} \mid \text{TR}^{\text{side}} \wedge !\text{TR}^{\text{side}} \right) = \frac{(p_x, p_y, z_{\text{vtx}}) \text{ histogram for protons from set } B}{(p_x, p_y, z_{\text{vtx}}) \text{ histogram for protons from set } A} \quad (6.16)$$

It should be noted that the momentum components (p_x, p_y) were taken from the proton with accounted effect of the beam divergence (after the original initial momentum smearing).

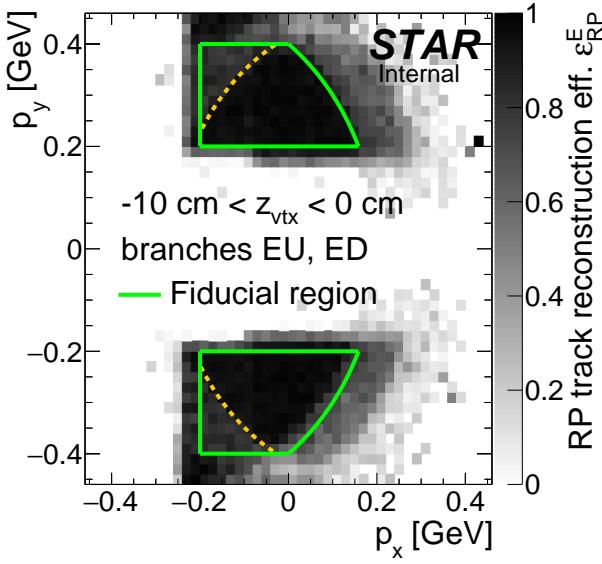


Figure 6.12: Sample RP track reconstruction efficiency in a single z -vertex bin on the east STAR side. The efficiency was calculated using forward proton MC simulation embedded into zero-bias data. Green envelopes mark the fiducial region of the measurement, while dashed yellow lines mark the part of the fiducial region with a data-driven efficiency correction needed, as explained in Sec. 10.3.1 of Ref. [1].

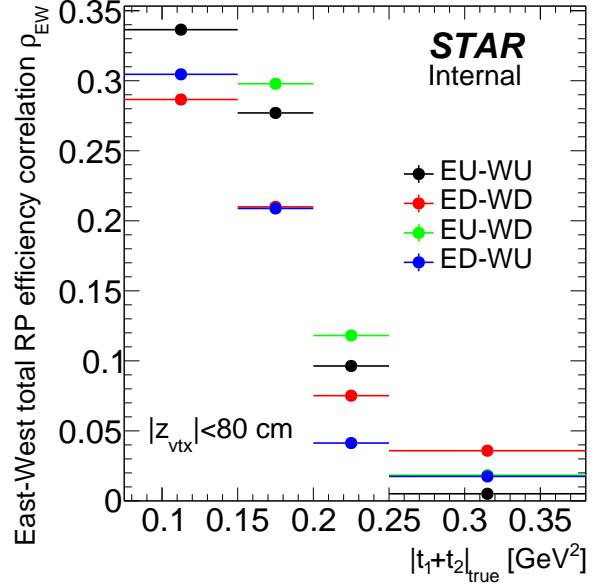


Figure 6.13: Correlation between joint RP track reconstruction and trigger efficiency (no dead material veto) in east and west RPs calculated from the CEP MC embedded into zero-bias data. The result for protons within the fiducial region and with vertex position $|z_{\text{vtx}}| < 80$ cm in four different combinations of east and west branches are presented as a function of the total squared four-momentum transfer.

The efficiency calculated in the way described above is, by design, the acceptance, reconstruction and selection efficiency for a single proton on one side of the IP. In CEP event there are two independent forward protons which may be simultaneously not reconstructed or rejected by the selection algorithm due to e.g. elastic pile-up interaction providing additional good quality proton tracks on both sides of IP. One could, in principle, calculate 5-dimensional efficiency for both forward protons (in variables $p_x^E, p_y^E, p_x^W, p_y^W$ and z_{vtx}) which would ultimately account for the simultaneous east and west inefficiency, however this would require orders of magnitude larger statistics of MC to provide reasonably low statistical uncertainty of the efficiency. Instead, on top of the 3-dimensional reconstruction and selection efficiencies for east and west RPs we calculate (from embedded MC) correlation between these efficiencies, as defined in Eq. (E.2) of appendix E. It is shown in Fig. 6.13 for all four combinations of east and west RP branches. A need to account for this correlation was found based on the closure tests performed on the MC sample.

6.2.4 TPC vertex reconstruction efficiency

The definition of vertex reconstruction efficiency (ϵ_{vtx}) established in this analysis is the probability that two global tracks, both associated with true-level primary particles from the kinematic region of the measurement, both satisfying kinematic and quality criteria (cuts C3.3 and C3.4) and both matched with hits in TOF, form a vertex listed in the collection of reconstructed primary vertices and DCA(R) and DCA(z) of both global tracks calculated w.r.t. this vertex is contained within the limits of cut C3.5.

We calculated this efficiency as a function of the longitudinal separation between two tracks (global helices) Δz_0 . Illustration of this quantity is given in Fig. 6.14. We consider this a natural quantity to present the vertexing efficiency - the closer to each other the helices are on the beamline, the more probable it is that two tracks will form a common primary vertex. It is in accordance with the way the vertexing algorithm works.

The vertexing efficiency was calculated from the data in the following way:

1. Data from RP_CPT2 trigger were used. Events were selected with nearly the same cuts as in nominal CEP analysis (Sec. 4.1). The requirement of exactly one primary vertex with exactly two primary TOF tracks was dropped. Instead, analysis utilized only global TOF tracks - exactly two global TOF tracks were required (cut C3.1 without primary track requirement), passing also cuts C3.2-C3.4. In this case the position of the vertex was reconstructed as

$$z_{\text{vtx}} = \frac{z_0^+ + z_0^-}{2}, \quad (6.17)$$

where z_0^+ and z_0^- are longitudinal impact parameters (z -coordinates of points of closest approach to the beamline) of positive and negative charge particle tracks, respectively. The vertex position was normally required to satisfy cut C2. Events after full selection, classified as exclusive $\pi^+\pi^-$ candidates, formed set *A*.

2. The two global TOF tracks were checked if they have associated primary tracks, and the two primary tracks are assigned to the same primary vertex. If yes, the tracks were additionally subjected to cut C3.5. Events passing described selection formed set *B*.
3. The efficiency was determined by the ratio of histograms from set *B* and set *A*:

$$\epsilon_{\text{vtx}}(|\Delta z_0|) = \frac{|\Delta z_0| \text{ histogram for events from set } B}{|\Delta z_0| \text{ histogram for events from set } A}. \quad (6.18)$$

Distribution of $|\Delta z_0|$ between two CEP global track candidates after full selection (*setA*) is presented in Fig. 6.15. The vertexing efficiency obtained with described method is shown in Fig. 6.16. Solid green points represent efficiency calculated with the non-exclusive background preserved, while open black points represent efficiency with this background subtracted. Since the vertexing efficiency does not depend on the physics process and background is purely of physics origin the black and green points should overlap. Such picture emerges from presented comparison. We have calculated the same efficiency using CEP MC embedded into zero-bias data, the result is shown in Fig. 6.16 with red points. There is very good agreement between vertexing efficiency in the data and embedded MC for $|\Delta z_0| < 1$ cm, where most ($\sim 80\%$) of the signal is present. The differences in high- $|\Delta z_0|$ tail are understood as a result of the imperfect description of the pointing resolution (here: the transverse resolution) of TPC tracks in STARsim. Although the pointing resolution is adjusted to gain more accurate description of the data by MC simulation as described in Chapter 8 of Ref. [1], this does not help with the vertexing which is performed at the level of raw data (MC) processing to MuDst. Another reason could be different p_T (thus also d_0) spectrum of CEP tracks in the data and MC (GenEx).

Based on the width of $|\Delta z_0|$ distribution, the background content as a function of $|\Delta z_0|$, and the value of ϵ_{vtx} as a function of $|\Delta z_0|$, we decided to accept in analysis only tracks which satisfy $|\Delta z_0| < 2$ cm. This assures that the vertexing efficiency does not drop below $\approx 30\%$, as well as it coincides with the primary tracks requirement of $|\text{DCA}(z)| < 1$ cm. In the correction procedure we nominally use the vertexing efficiency represented by open black points in Fig. 6.16 (to correct the MC e.g. in closure tests we use red points instead). The additional correction factor connected with the cut on maximum $|\Delta z_0|$ (2 cm) was calculated from the data and equals 2.4% (Fig. 6.15). This correction is used as an additional normalization correction factor, which is different from $\epsilon_{\text{vtx}}(|\Delta z_0|)$ applied in form of a weight to each selected CEP event.

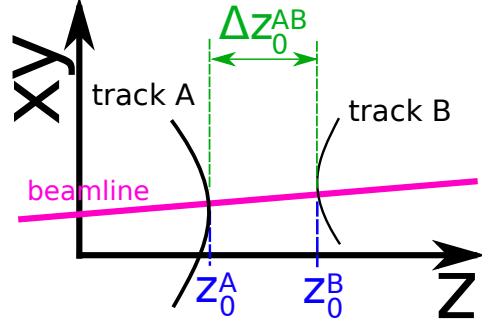


Figure 6.14: Sketch with definition of the longitudinal separation of two tracks (helices) Δz_0 .

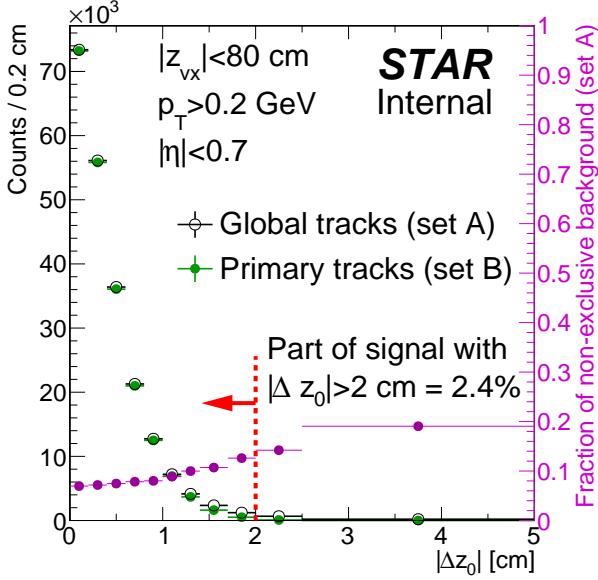


Figure 6.15: Distribution of Δz_0 between two CEP-candidate global tracks (green and black points) together with fraction of non-exclusive background in black distribution as a function of Δz_0 (violet points).

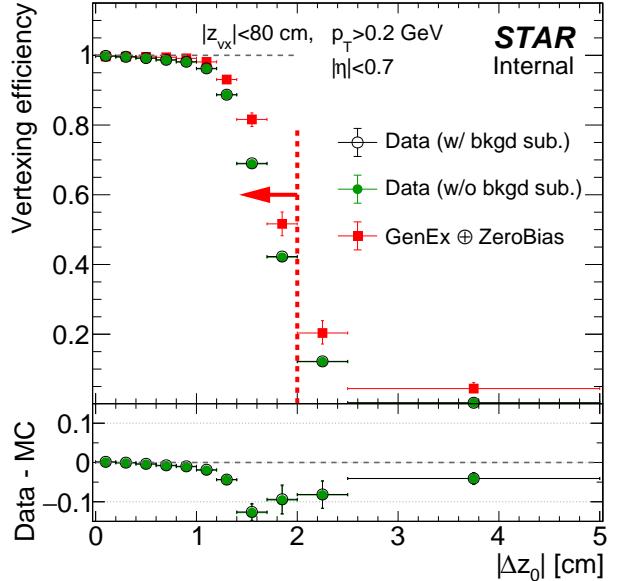


Figure 6.16: Vertexing efficiency calculated from the data (open black and full green points) and from embedded MC (red points) as a function of Δz_0 between two CEP-candidate global tracks.

6.3 Particle energy loss

Energy loss correction as a function of reconstructed particle p_T in bins of z -position of reconstructed vertex has been calculated and presented in Chapter 5 of Ref. [1] for all analyzed particle species and both positive and negative charges. The correction was applied independently for each particle in the following procedure:

1. After central particles were identified (cut C8) an absolute value of the particle transverse momentum correction ($-\Delta p_T = p_T^{\text{meas}} - p_T^{\text{true}}$) was read from the histogram corresponding to reconstructed z_{vtx} and to assigned particle ID (Appendix C of Ref. [1]).
2. The momentum correction factor f_p^{corr} was calculated:

$$f_p^{\text{corr}} = \frac{p_T^{\text{meas}} + \Delta p_T}{p_T^{\text{meas}}}. \quad (6.19)$$

3. New, corrected momentum \vec{p}^{corr} was assigned to the particle:

$$\vec{p}^{\text{corr}} = f_p^{\text{corr}} \cdot \vec{p}^{\text{meas}}. \quad (6.20)$$

In this way all three components of particle momentum are corrected so that the pseudorapidity of a particle remains unchanged.

This new momentum was further used in determination of total transverse momentum of all reconstructed particles, p_T^{miss} , as well as in applying TPC and TOF efficiency corrections and preparing histograms (cross sections) of physics quantities (e.g. invariant mass, rapidity of a pair of central tracks).

6.4 Fake tracks and migrations into and out of fiducial region

Finite resolutions play non-negligible role in presented analysis. Smearing of reconstructed quantities with respect to their true value at the hadron level makes some tracks from outside of the fiducial phase space migrating/leaking into it, as well as some tracks from inside the fiducial region escaping from it.

Correction related to migrations and fake tracks was calculated using quantities described in the listing below. It applies to both TPC and RP tracks.

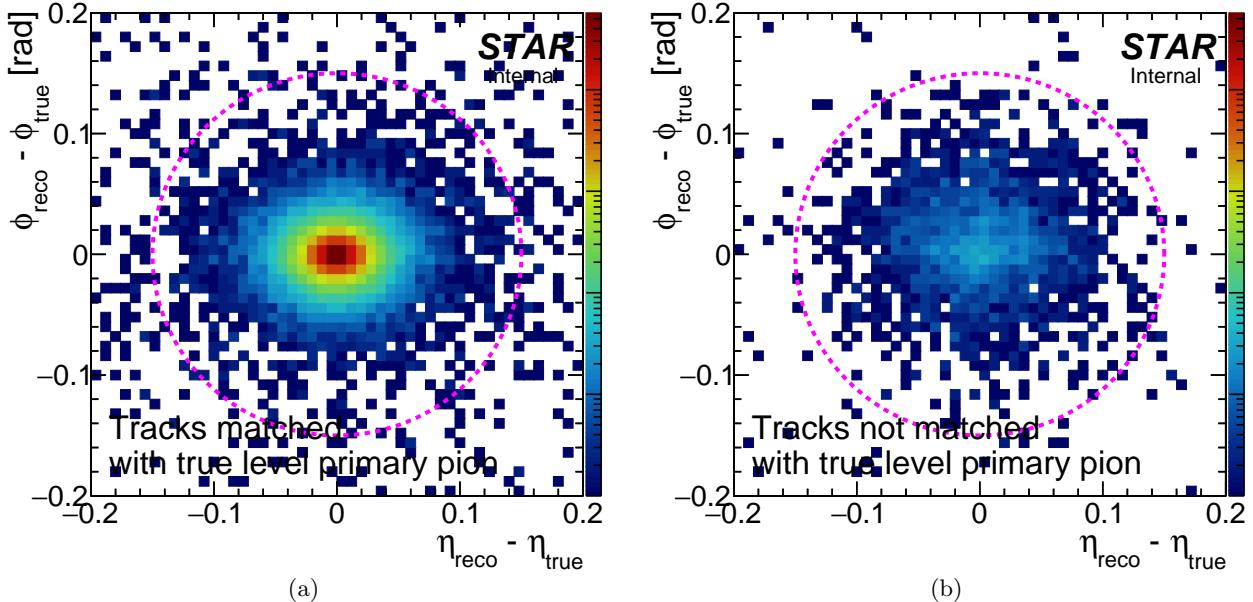


Figure 6.17: Difference between reconstructed and true parameters of the TPC tracks. Magenta circle of radius 0.15 drawn on top of distributions represent cut on maximum difference between true and reconstructed η and φ of tracks used for determination of fake tracks fraction, as explained in the text. The same z -axis (color) scale has been set up for both plots to better visualize relative content of true and fake tracks.

- N_{reco} - number of true level-matched tracks reconstructed inside fiducial region,
- $N_{\text{migr.}}^{\text{in}}$ - number of true level-matched tracks from outside of fiducial region (at the hadron level), reconstructed inside fiducial regions,
- $N_{\text{migr.}}^{\text{out}}$ - number of true level-matched tracks from inside of fiducial region (at the hadron level), reconstructed outside fiducial region,
- N_{fakes} - number of tracks not matched with true level primary but consistent with it, reconstructed inside fiducial region.

All quantities above are represented as a function of reconstructed values (TPC tracks: p_T and η , RP tracks: p_x and p_y), except $N_{\text{migr.}}^{\text{out}}$, for which true (hadron) level values are used. Definitions of fraction of migrations into and out of fiducial region, as well as fraction of fake tracks inside the fiducial region, are provided in Eqs. (6.21)-(6.23) in the same order:

$$f_{\text{migr.}}^{\text{in}} = \frac{N_{\text{migr.}}^{\text{in}}}{N_{\text{reco}}}, \quad (6.21) \quad f_{\text{migr.}}^{\text{out}} = \frac{N_{\text{migr.}}^{\text{out}}}{N_{\text{reco}}}, \quad (6.22) \quad f_{\text{fakes}} = \frac{N_{\text{fakes}}}{N_{\text{reco}}}. \quad (6.23)$$

Definition of number of fake tracks requires some elaboration. The necessary condition to claim a track being fake is that it is not matched with a true level primary particle. However, such tracks should typically have momentum significantly different from that of unmatched primary, therefore total momentum cut C9 would not be satisfied and thus these tracks should not be subtracted. For this reason, an additional condition to assign a track as fake is that its reconstructed momentum is consistent with that of primary particle. In case of TPC tracks we use cut on the distance δ between true and reconstructed (η, ϕ) , $\delta < 0.15$, introduced in Sec. 3.2.2 of Ref. [1]. For the RP tracks we use cut on the difference between true and reconstructed transverse momentum not greater than 70 MeV. Such value, somewhat arbitrary, is driven by the value used in cut C9. We do not consider any systematic effect connected with the fake RP track definition as this effect is believed to be much smaller than most of other systematic uncertainties. In Figs. 6.17 and 6.18 we present distributions of quantities for matched and not matched tracks with magenta circles drawn on top marking the conditions used in fake track definitions.

Fraction of tracks, for both TPC and RP detectors, migrating from/to fiducial region and being fake, is shown in Figs. 6.19 and 6.20. Clearly, all mentioned effects are dominant for RP tracks.

Multiplicative correction factor (per track) that takes into account all migrations and fakes can be formed

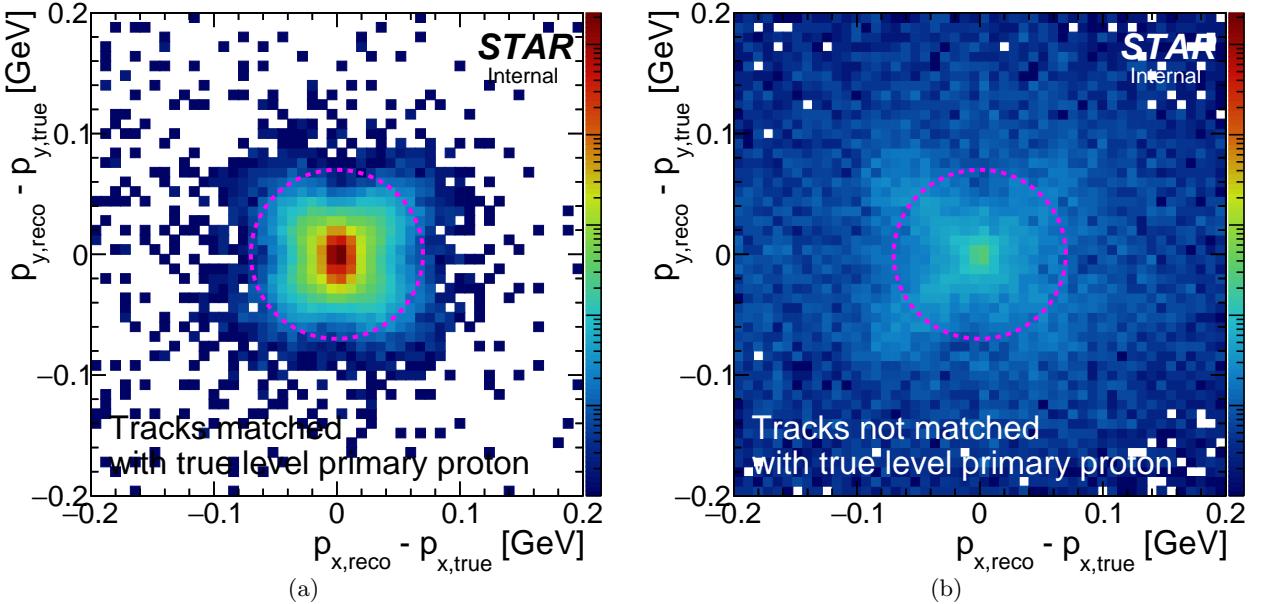


Figure 6.18: Difference between reconstructed and true momentum components of RP tracks matched (a) and not matched (b) with true level primary forward protons. Magenta circle of radius 70 MeV drawn on top of distributions represent cut on maximum difference between true and reconstructed transverse momentum used for determination of fake tracks fraction, as explained in the text. The same z -axis (color) scale has been set up for both plots to better visualize relative content of true and fake tracks.

as

$$C_{m,f} = \frac{N_{\text{reco}} + N_{\text{migr.}}^{\text{out}} - N_{\text{migr.}}^{\text{in}} - N_{\text{fakes}}}{N_{\text{reco}}} = 1 + f_{\text{migr.}}^{\text{out}} - f_{\text{migr.}}^{\text{in}} - f_{\text{fakes}}. \quad (6.24)$$

This correction is graphically represented in Fig. 6.21 for both TPC (6.21a) and RP (6.21b) tracks. One can easily notice that most important role plays correction related to migrations at the edge of fiducial region defining accepted forward scattered protons, reaching as much as 25% correction for tracks at the corners of allowed (p_x, p_y) . This is a direct consequence of sizeable angular divergence of proton beams.

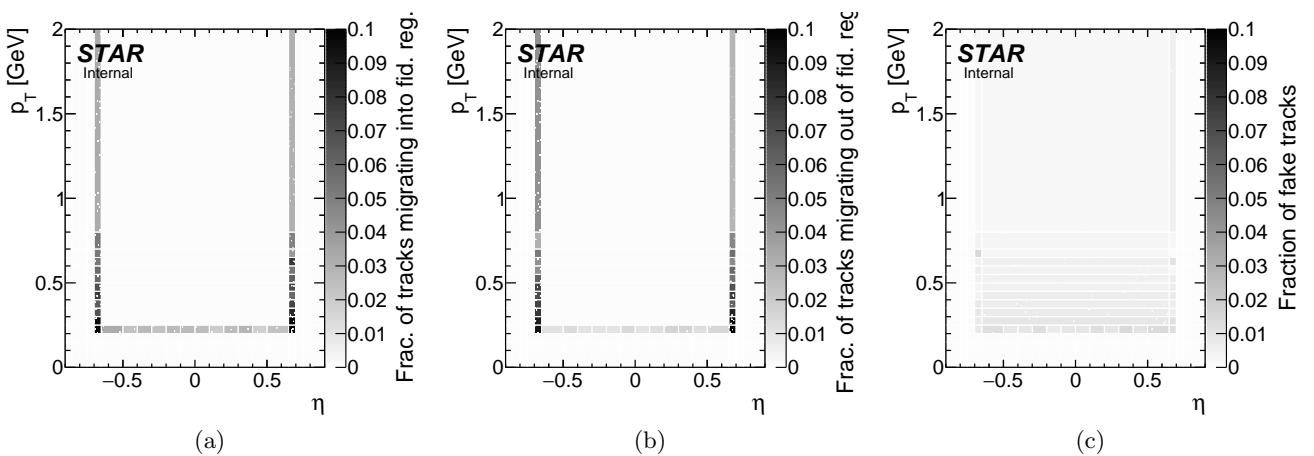


Figure 6.19: Fraction of TOF-matched TPC tracks migrating into the fiducial central tracks phase space from outside of it (a), migrating outside the fiducial phase space from inside of it (b), and fraction of fake TOF matched TPC tracks reconstructed in the fiducial phase space (c). In case of reconstructed (p_T, η) escaping the fiducial phase space (b) the true value of p_T and η is used; otherwise reconstructed values are plotted.

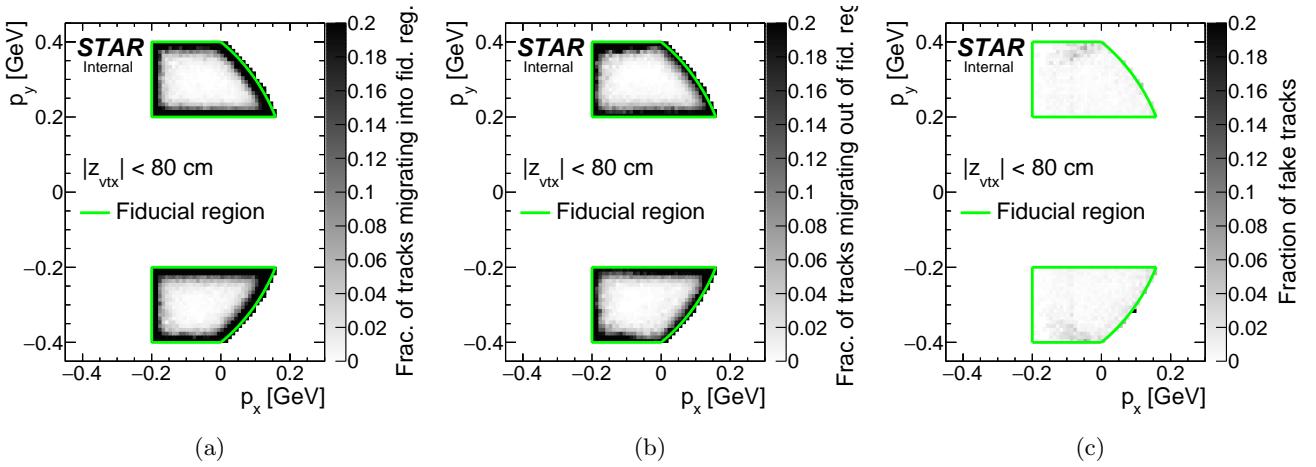


Figure 6.20: Fraction of RP tracks migrating into the fiducial forward proton momentum area from outside of it (a), migrating outside the fiducial area from inside of it (b), and fraction of fake RP tracks reconstructed in the fiducial area (c). In case of reconstructed tracks momentum escaping the fiducial area (b) the true value of p_x and p_y is used; otherwise reconstructed momentum components are plotted.

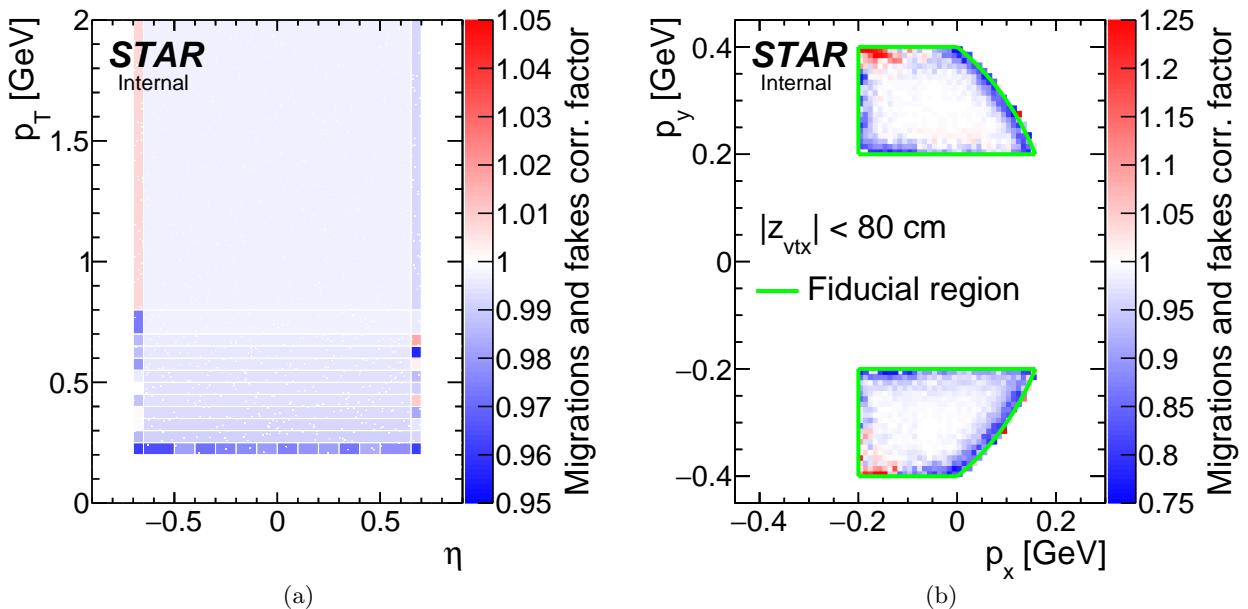


Figure 6.21: Joint correction factors for migrations and fake tracks for TOF-matched TPC tracks (6.21a) and RP tracks (6.21b).

6.5 Detector resolutions

In this section we present studies of detector resolutions of quantities relevant in the physics analysis. These resolutions were used to establish proper binning of the measured differential cross sections.

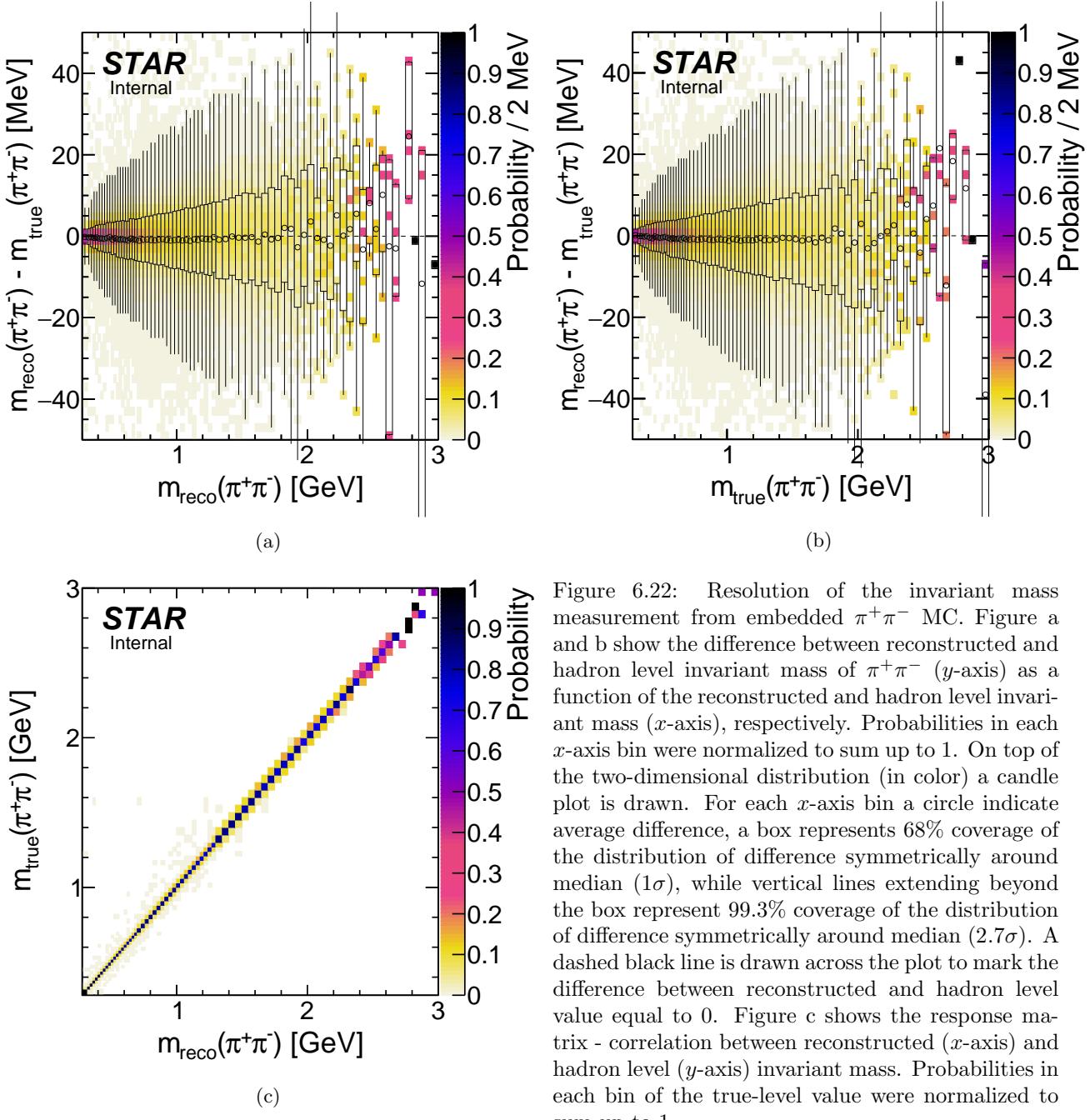


Figure 6.22: Resolution of the invariant mass measurement from embedded $\pi^+\pi^-$ MC. Figure a and b show the difference between reconstructed and hadron level invariant mass of $\pi^+\pi^-$ (y -axis) as a function of the reconstructed and hadron level invariant mass (x -axis), respectively. Probabilities in each x -axis bin were normalized to sum up to 1. On top of the two-dimensional distribution (in color) a candle plot is drawn. For each x -axis bin a circle indicate average difference, a box represents 68% coverage of the distribution of difference symmetrically around median (1σ), while vertical lines extending beyond the box represent 99.3% coverage of the distribution of difference symmetrically around median (2.7σ). A dashed black line is drawn across the plot to mark the difference between reconstructed and hadron level value equal to 0. Figure c shows the response matrix - correlation between reconstructed (x -axis) and hadron level (y -axis) invariant mass. Probabilities in each bin of the true-level value were normalized to sum up to 1.

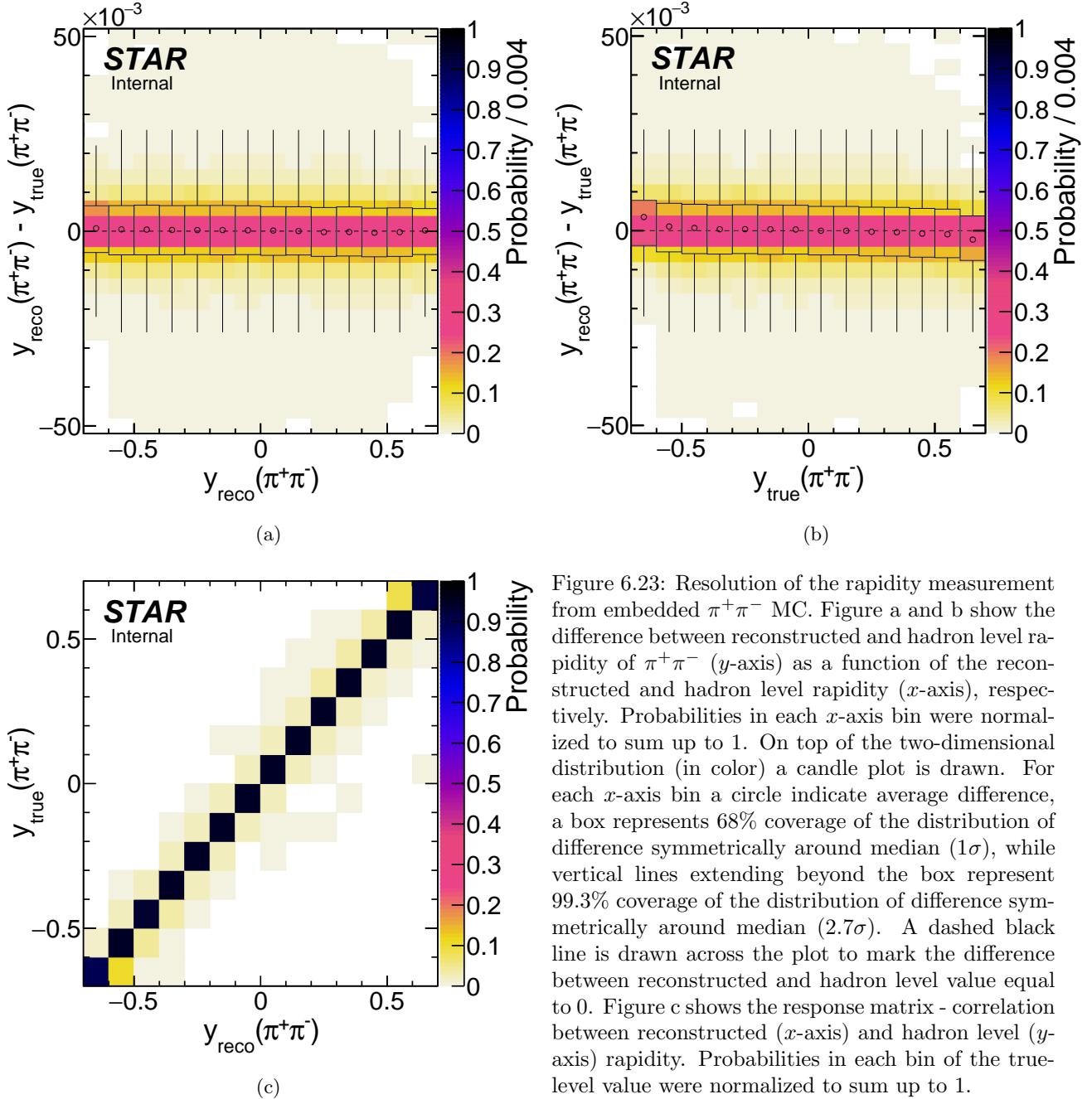


Figure 6.23: Resolution of the rapidity measurement from embedded $\pi^+\pi^-$ MC. Figure a and b show the difference between reconstructed and hadron level rapidity of $\pi^+\pi^-$ (y -axis) as a function of the reconstructed and hadron level rapidity (x -axis), respectively. Probabilities in each x -axis bin were normalized to sum up to 1. On top of the two-dimensional distribution (in color) a candle plot is drawn. For each x -axis bin a circle indicate average difference, a box represents 68% coverage of the distribution of difference symmetrically around median (1σ), while vertical lines extending beyond the box represent 99.3% coverage of the distribution of difference symmetrically around median (2.7σ). A dashed black line is drawn across the plot to mark the difference between reconstructed and hadron level value equal to 0. Figure c shows the response matrix - correlation between reconstructed (x -axis) and hadron level (y -axis) rapidity. Probabilities in each bin of the true-level value were normalized to sum up to 1.

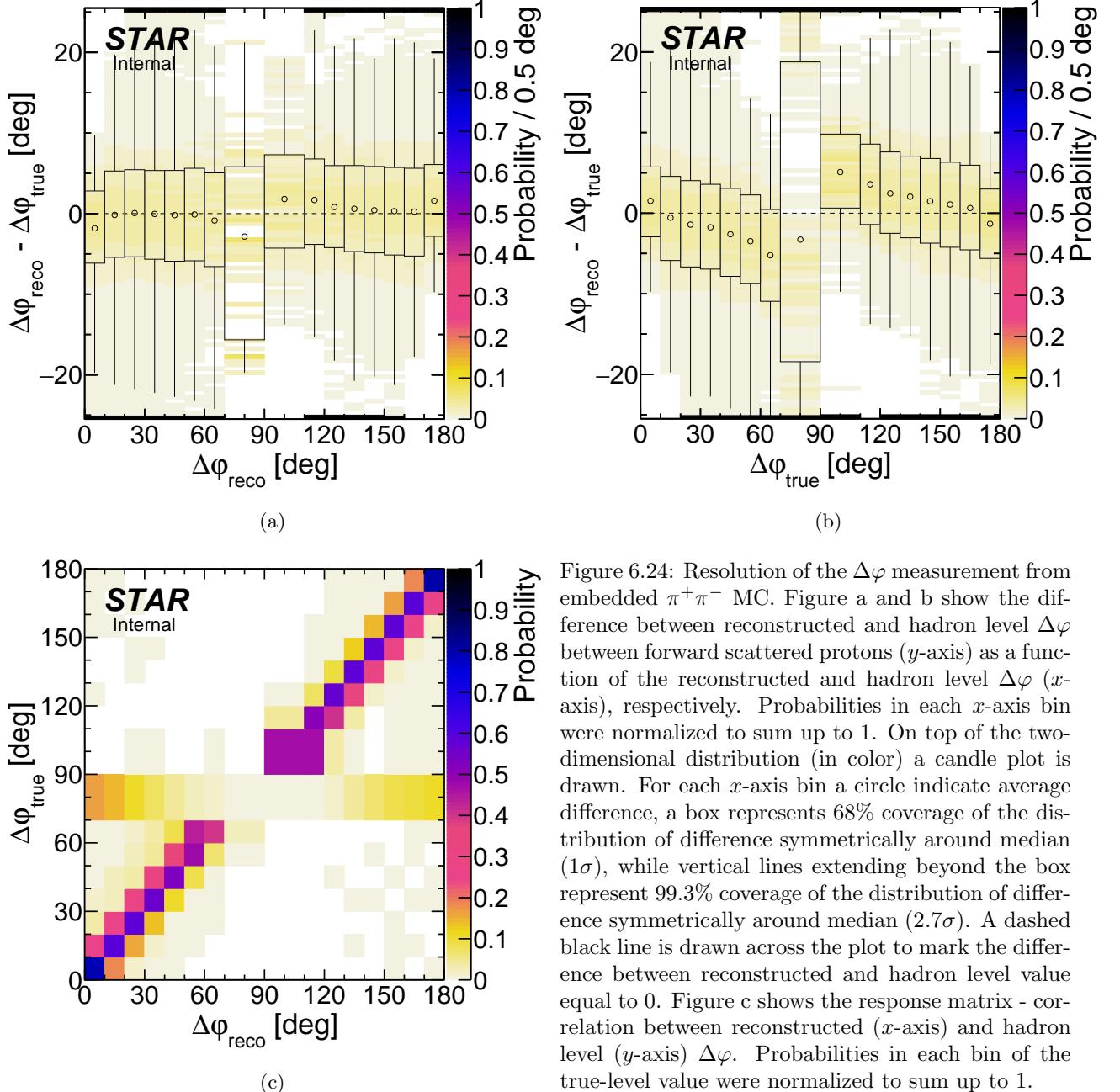
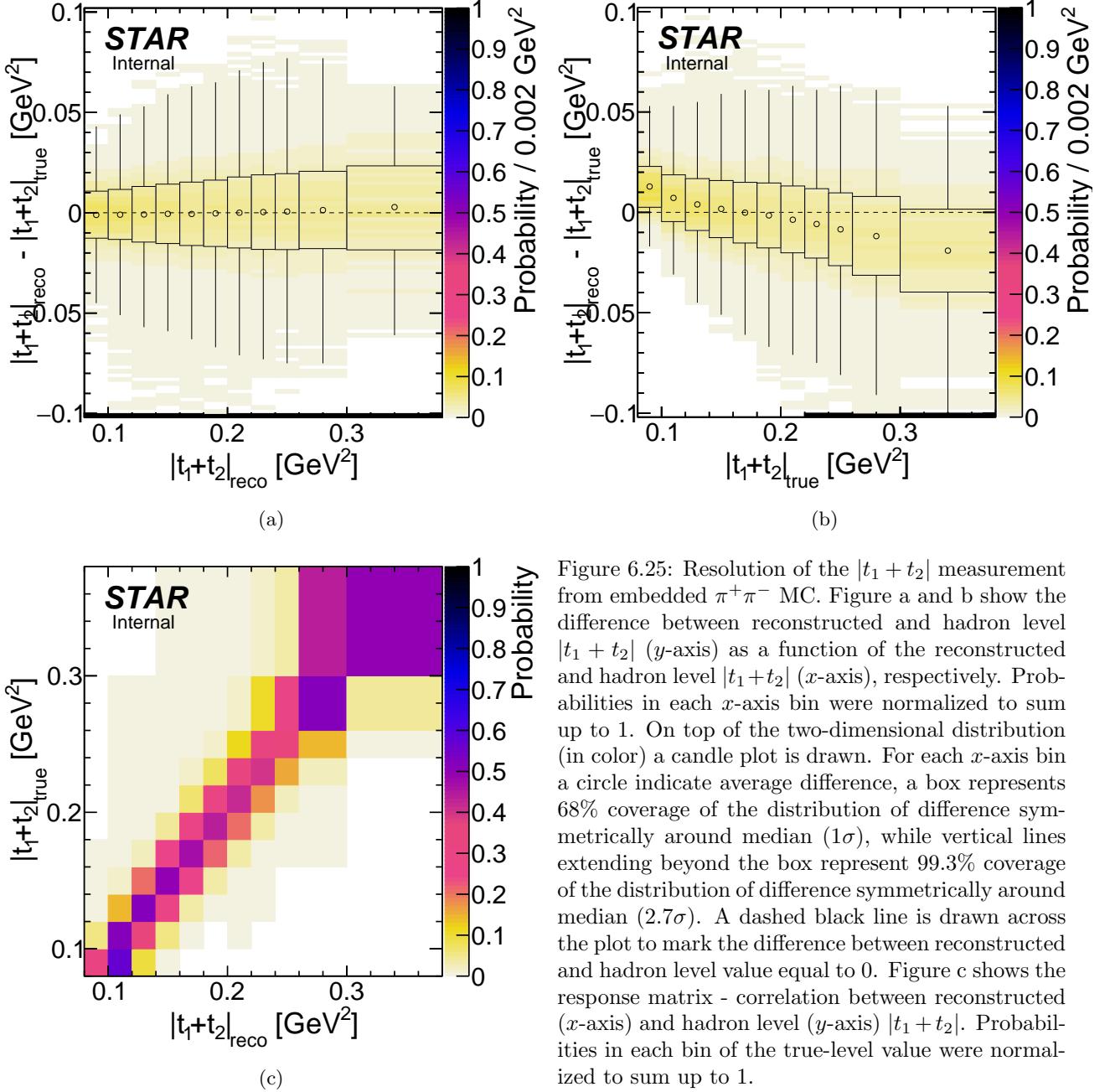


Figure 6.24: Resolution of the $\Delta\varphi$ measurement from embedded $\pi^+\pi^-$ MC. Figure a and b show the difference between reconstructed and hadron level $\Delta\varphi$ between forward scattered protons (y-axis) as a function of the reconstructed and hadron level $\Delta\varphi$ (x-axis), respectively. Probabilities in each x-axis bin were normalized to sum up to 1. On top of the two-dimensional distribution (in color) a candle plot is drawn. For each x-axis bin a circle indicate average difference, a box represents 68% coverage of the distribution of difference symmetrically around median (1σ), while vertical lines extending beyond the box represent 99.3% coverage of the distribution of difference symmetrically around median (2.7σ). A dashed black line is drawn across the plot to mark the difference between reconstructed and hadron level value equal to 0. Figure c shows the response matrix - correlation between reconstructed (x-axis) and hadron level (y-axis) $\Delta\varphi$. Probabilities in each bin of the true-level value were normalized to sum up to 1.



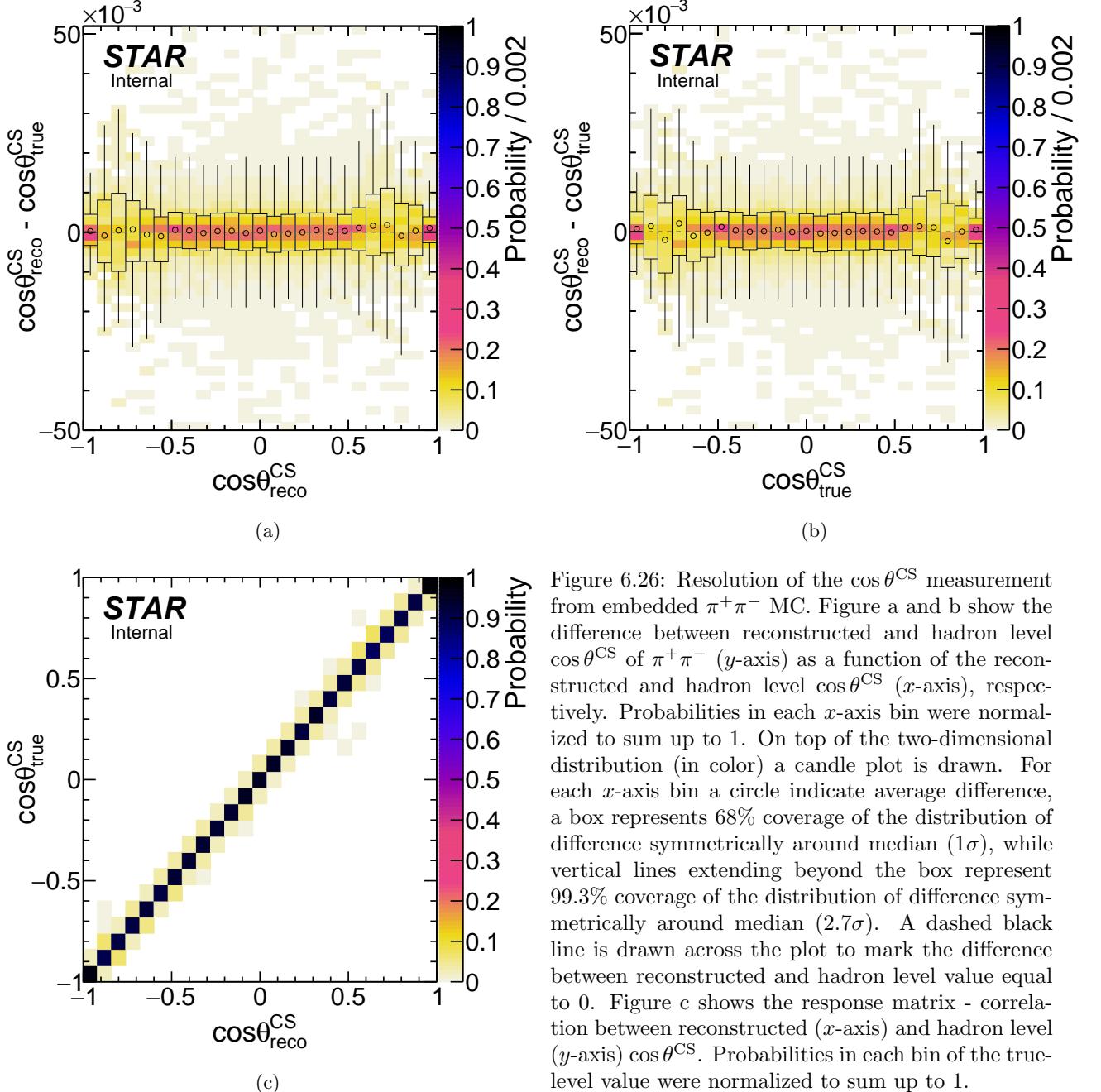


Figure 6.26: Resolution of the $\cos\theta^{\text{CS}}$ measurement from embedded $\pi^+\pi^-$ MC. Figure a and b show the difference between reconstructed and hadron level $\cos\theta^{\text{CS}}$ of $\pi^+\pi^-$ (y -axis) as a function of the reconstructed and hadron level $\cos\theta^{\text{CS}}$ (x -axis), respectively. Probabilities in each x -axis bin were normalized to sum up to 1. On top of the two-dimensional distribution (in color) a candle plot is drawn. For each x -axis bin a circle indicate average difference, a box represents 68% coverage of the distribution of difference symmetrically around median (1σ), while vertical lines extending beyond the box represent 99.3% coverage of the distribution of difference symmetrically around median (2.7σ). A dashed black line is drawn across the plot to mark the difference between reconstructed and hadron level value equal to 0. Figure c shows the response matrix - correlation between reconstructed (x -axis) and hadron level (y -axis) $\cos\theta^{\text{CS}}$. Probabilities in each bin of the true-level value were normalized to sum up to 1.

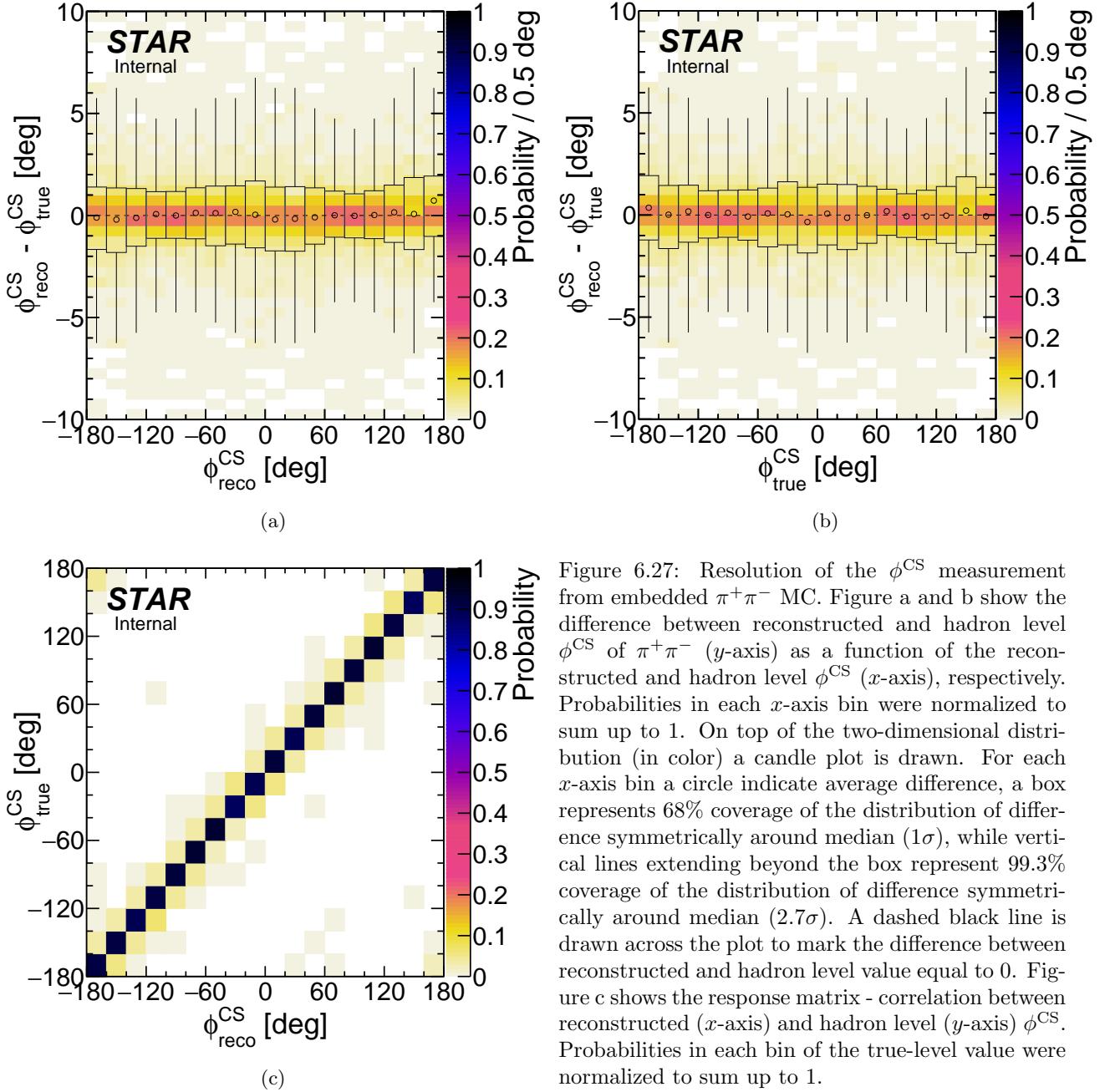


Figure 6.27: Resolution of the ϕ^{CS} measurement from embedded $\pi^+\pi^-$ MC. Figure a and b show the difference between reconstructed and hadron level ϕ^{CS} of $\pi^+\pi^-$ (y -axis) as a function of the reconstructed and hadron level ϕ^{CS} (x -axis), respectively. Probabilities in each x -axis bin were normalized to sum up to 1. On top of the two-dimensional distribution (in color) a candle plot is drawn. For each x -axis bin a circle indicate average difference, a box represents 68% coverage of the distribution of difference symmetrically around median (1σ), while vertical lines extending beyond the box represent 99.3% coverage of the distribution of difference symmetrically around median (2.7σ). A dashed black line is drawn across the plot to mark the difference between reconstructed and hadron level value equal to 0. Figure c shows the response matrix - correlation between reconstructed (x -axis) and hadron level (y -axis) ϕ^{CS} . Probabilities in each bin of the true-level value were normalized to sum up to 1.

6.6 Closure tests

6.6.1 Data pull

Sanity of the data after applied corrections was verified by preparing a pull histogram of the number of reconstructed and selected CEP events per unit of integrated luminosity (in other words - an integrated cross section). The pull quantity was calculated per run, defined as

$$\text{Pull}_i = \begin{cases} \frac{\sigma_i - \langle \sigma \rangle}{u^-(\sigma_i)}, & \text{if } \sigma_i - \langle \sigma \rangle \geq 0, \\ \frac{\sigma_i - \langle \sigma \rangle}{u^+(\sigma_i)}, & \text{if } \sigma_i - \langle \sigma \rangle < 0, \end{cases} \quad (6.25)$$

where σ_i is an integrated cross section calculated for i -th run with statistical uncertainty equal to $u^-(\sigma_i)$ or $u^+(\sigma_i)$ (lower or upper 68% confidence level interval), and $\langle \sigma \rangle$ is an expectation value of integrated cross section. For each run the integrated cross section was calculated as

$$\sigma_i = \frac{N_i}{L_i}. \quad (6.26)$$

where N_i is a number of CEP events in i -th run and L_i is a luminosity collected during i -th run. The expectation value $\langle \sigma \rangle$ was calculated using an estimator from Eq. (6.27):

$$\langle \sigma \rangle = \frac{\sum_i \sigma_i \times u^{-2}(\sigma_i)}{\sum_i u^{-2}(\sigma_i)} \quad (6.27)$$

which is simply an average integrated cross section calculated with full dataset, weighted by the uncertainties (by reciprocal of variance).

Final pull histogram is shown in Fig. 6.28 for raw event counts (open circles) and efficiency-corrected events weighted according to prescription from Eq. (6.5) (filled circles). Parameters of the Gaussian fits to data points show some deviation of the mean value from 0, and significant improvement of the width of distribution after appliance of corrections, which should be consistent with 1, as observed.

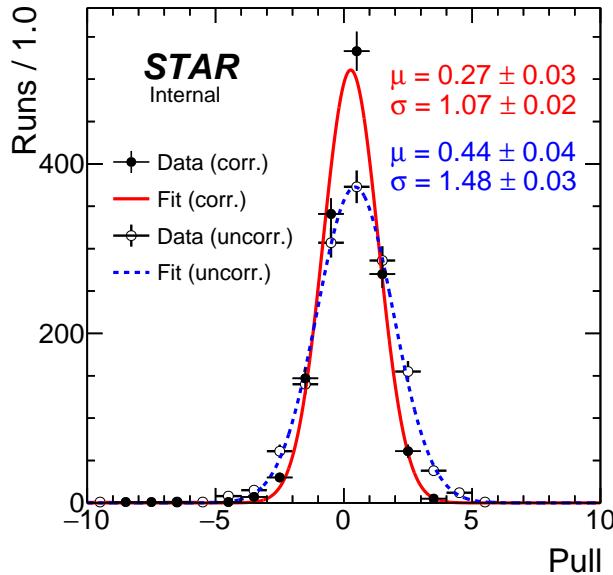


Figure 6.28: Pull histogram of number of events per unit of integrated luminosity. Open circles fitted with dashed blue Gaussian mark uncorrected data, whereas black dots fitted with red curve denote corrected (weighthed) data. Parameters obtained from the fit are provided in the plot.

6.6.2 Monte Carlo closure tests

To verify that corrections are properly applied and reconstructed+corrected distributions reproduce these at the true-level, the closure tests are performed. Monte Carlo events are subjected to the same analysis flow as the data, and the corrected observables are compared with the MC input.

In the closure tests presented below, distributions at the true level are assumed to be known with infinite statistical precision (count uncertainties are assumed to be equal to 0). This enables statistical comparison of the reconstructed and corrected distributions with those at the true level.

6.6.2.1 TPC and TOF efficiency correction validation

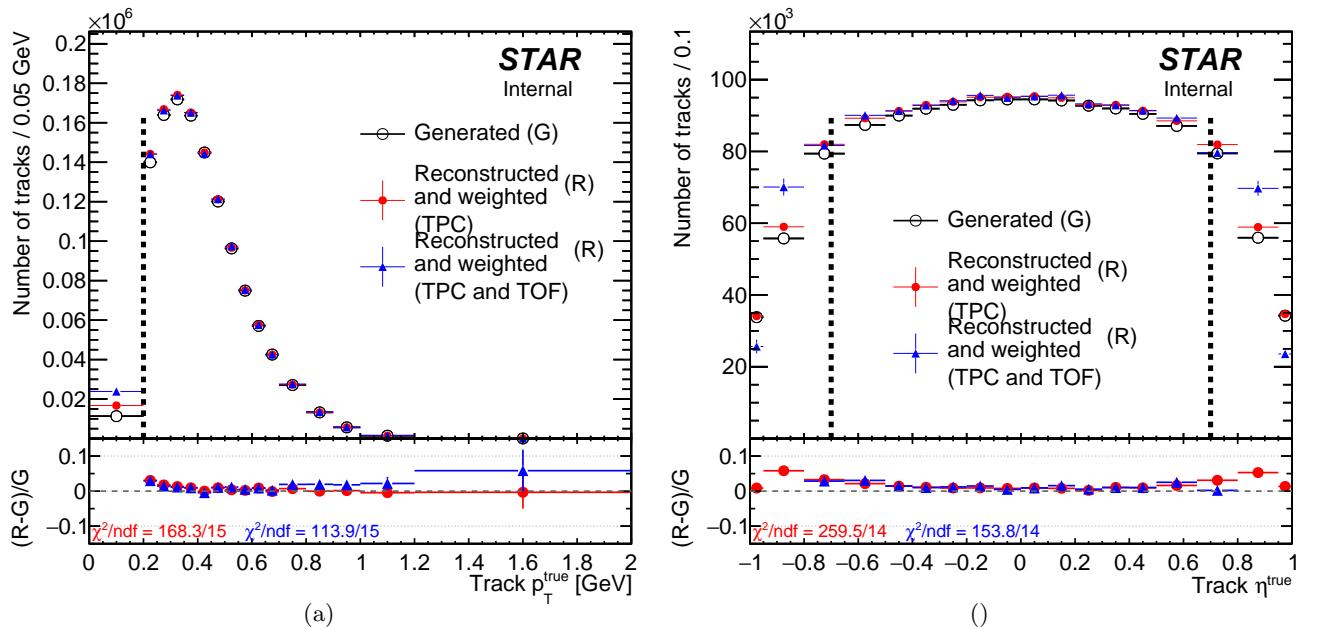


Figure 6.29: Results of TPC and TOF single-track efficiency correction closure test on embedded signal MC sample. Distributions of the true-level track p_T and true-level η corrected for single-particle TPC efficiency (red points) and single-particle TPC and TOF efficiency (blue points) are compared with the true-level distributions of corresponding observables (black points).

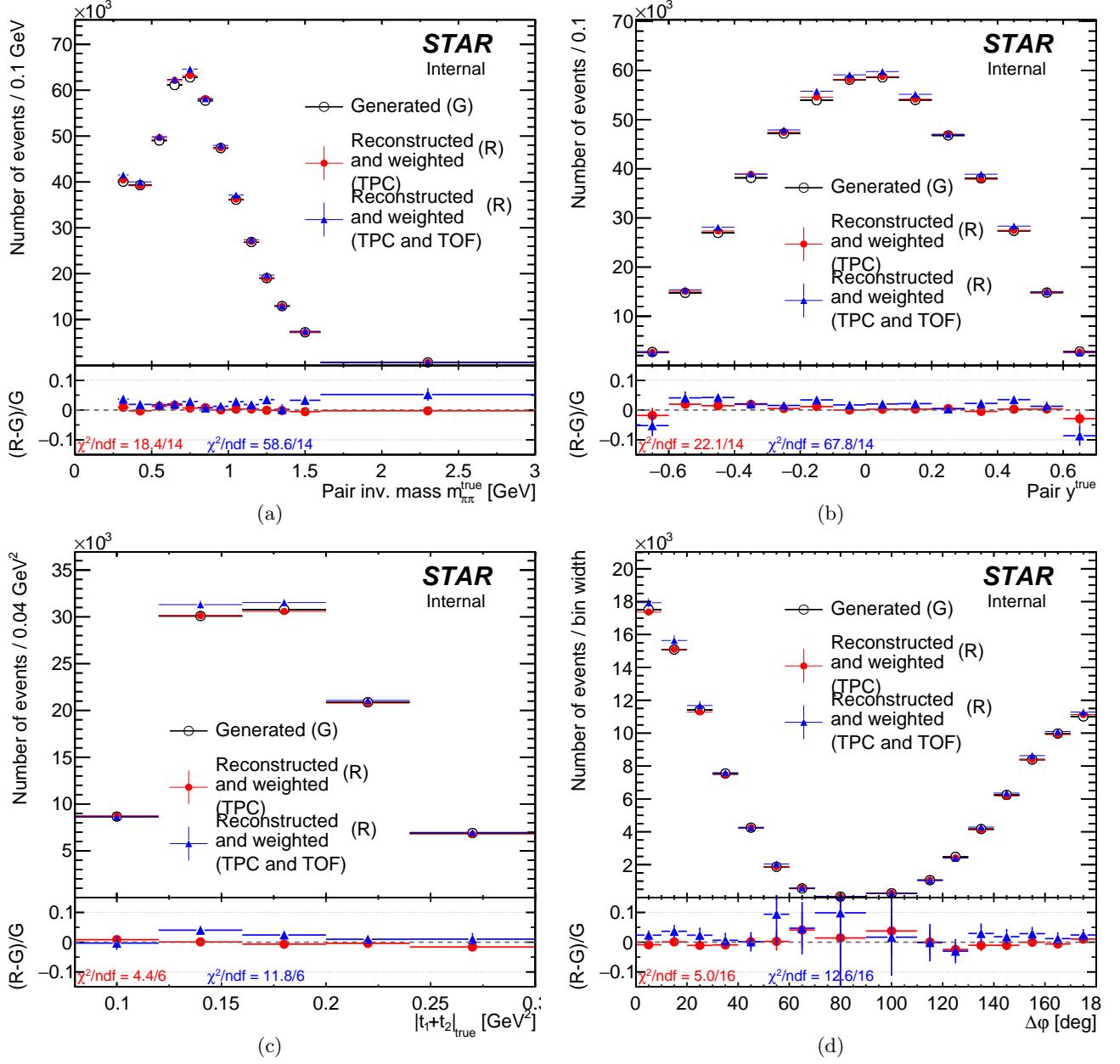


Figure 6.30: Results of TPC and TOF efficiency correction closure test on embedded signal MC sample. Distributions of the true-level pion pair invariant mass a and rapidity b, as well as forward proton total squared four-momentum transfer c and azimuthal separation d for events with both central state pion TPC tracks reconstructed (red points) and additionally matched with TOF (blue points), are compared with the true level distributions of corresponding observables (black points). All events were required to be contained within the fiducial region of the measurement.

6.6.2.2 RP efficiency correction validation

The joint RP track reconstruction and selection efficiency and the dead-material-induced veto efficiency is tested here.

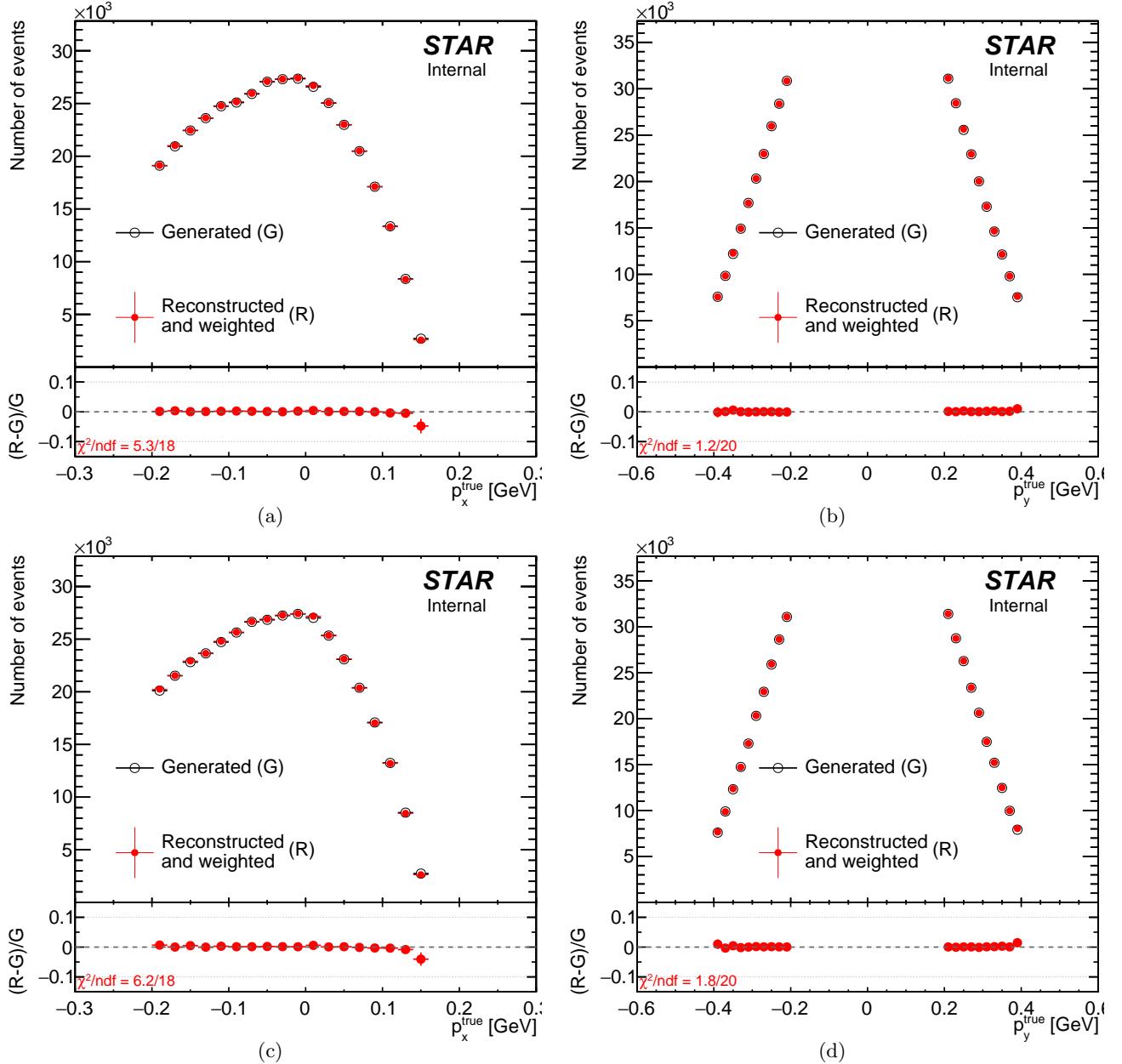


Figure 6.31: Results of RP single-track efficiency correction closure test on embedded signal MC sample. Distributions of the true-level track p_x (left) and p_y (right) for East (top) and West (bottom) RPs corrected for single-particle RP efficiency (red points) are compared with the true-level distributions of corresponding observables (black points). The true-level quantities here are taken after the angular beam divergence being applied.

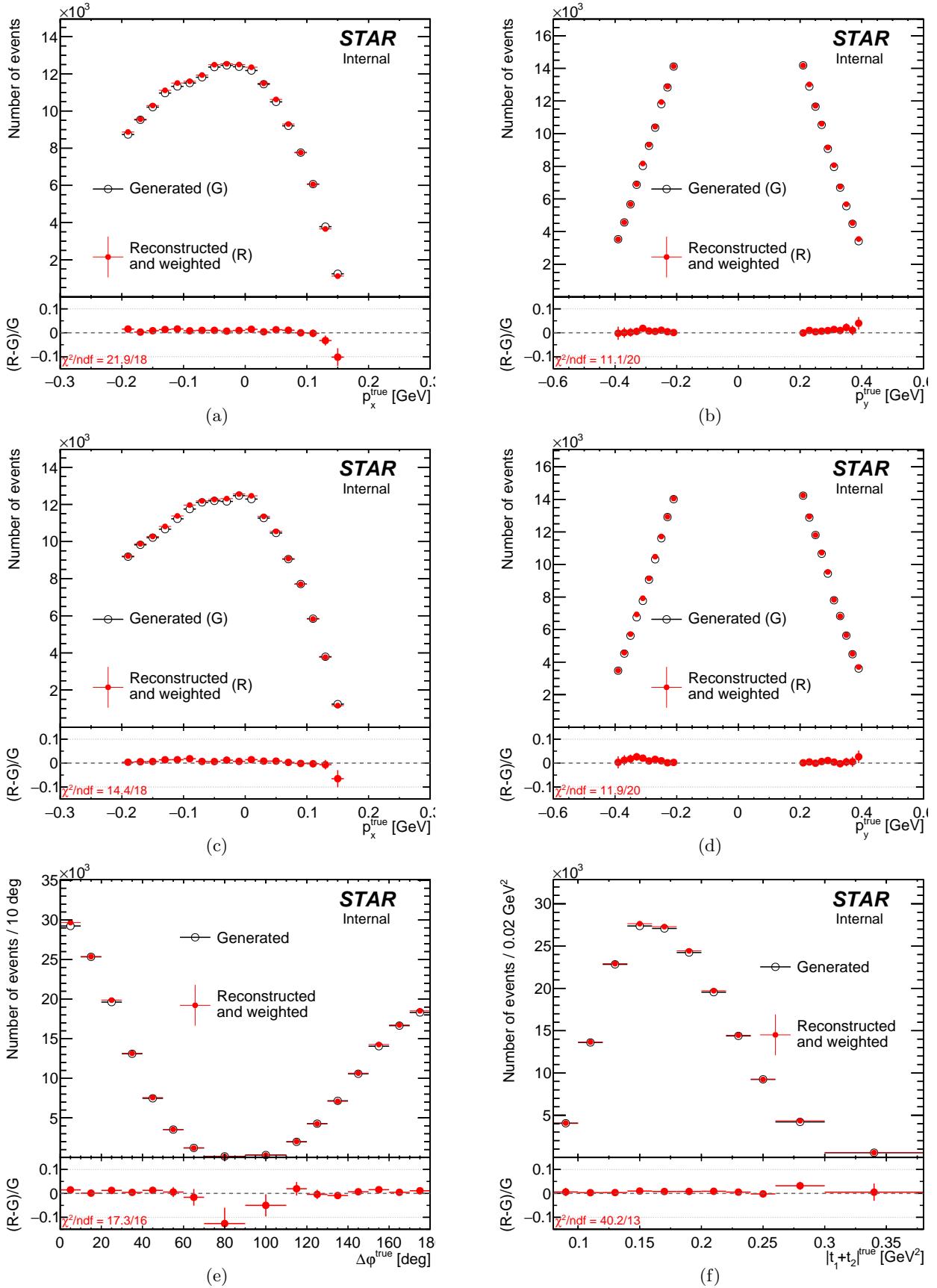


Figure 6.32: Results of RP efficiency correction closure test on embedded signal MC sample. Distributions of the true-level track p_x , p_y , as well as $\Delta\varphi$ and $|t_1 + t_2|$ corrected for full two-proton RP efficiency (red points) are compared with the true-level distributions of corresponding observables (black points). The true-level quantities here are taken after the angular beam divergence being applied.

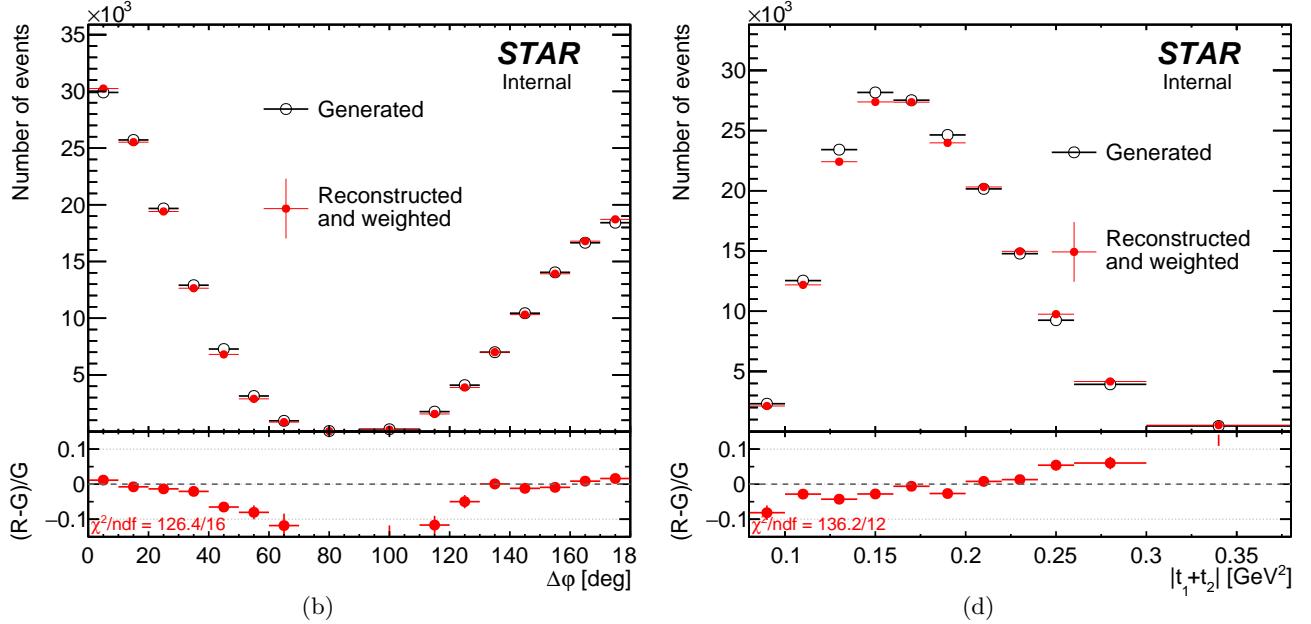


Figure 6.33: Results of RP efficiency, migrations and fakes correction closure test on embedded signal MC sample. Distributions of the reconstructed and corrected $\Delta\varphi$ and $|t_1 + t_2|$ corrected for full two-proton RP efficiency (red points) are compared with the true generator-level distributions of corresponding observables (black circles). By definition, both forward protons were required to be contained within the fiducial region of the measurement, either at the generator level (black) or reconstructed level (red).

6.6.2.3 Total correction validation

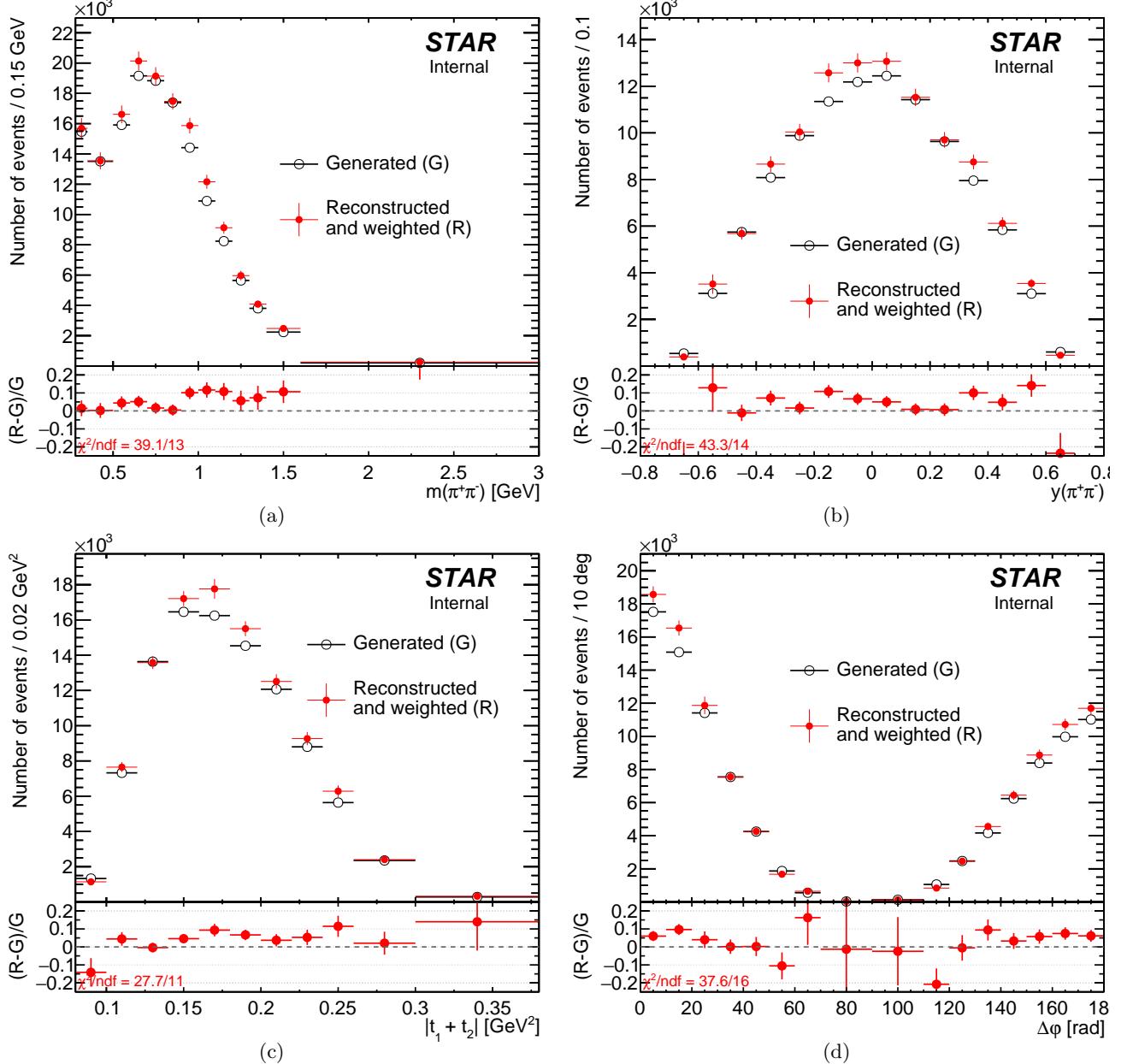


Figure 6.34: Results of full closure test on embedded signal MC sample. Reconstructed and corrected distributions of the pion pair invariant mass a and rapidity b, as well as forward proton total squared four-momentum transfer c and azimuthal separation d after CEP event selection, are compared with the true generator-level distributions of corresponding observables. By definition, all events were required to be contained within the fiducial region of the measurement, either at the generator level (black) or reconstructed level (red).

6.7 Geometrical correction

One of the goals of the analysis is to obtain information about the production of resonances in CEP process. Invariant mass distributions in the fiducial region of the measurement can not be directly used to extract and quantitatively describe possible resonances without extrapolation to the full kinematic region of the central pions pair, given by $p_T \rightarrow 0$ and $|\eta| \rightarrow \infty$ (full solid angle in the central system rest frame). Extrapolation to unmeasured region is always model dependent. Here we present corrections to the full phase-space obtained with various assumptions (models). To limit size of the corrections, the measurement is restricted to $|y(\pi^+\pi^-)| < 0.4$. In the correction calculation factorization of the central system and forward protons phase space is assumed. For the forward protons phase space a uniform distributions of the azimuthal angles are assumed while polar

angles are generated according to exponential t distribution with t -slope of 6 GeV^{-2} .

The measurement is extrapolated from the part of the fiducial region given by Eq. (4.4) covering $0.05 \leq -t_1, -t_2 \leq 0.16 \text{ GeV}^2$ to such defined Lorentz invariant t interval and full azimuthal angle of forward protons. The measurement is further restricted to two regions of $\Delta\varphi < 45^\circ$ and $\Delta\varphi > 135^\circ$ which reduces size of acceptance corrections and related systematic uncertainties.

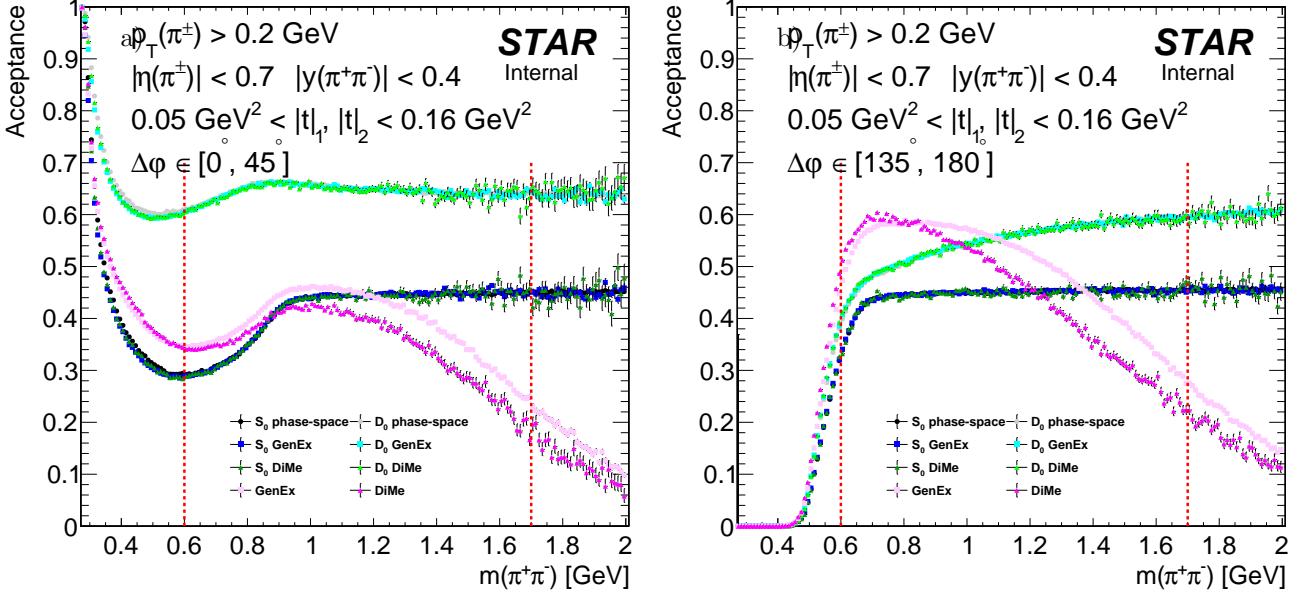


Figure 6.35: Geometrical acceptance for the $\pi^+\pi^-$ being in the fiducial region of the measurement ($|\eta(\pi^\pm)| < 0.7$, $p_T(\pi^\pm) > 0.2 \text{ GeV}$) if forward protons separated in azimuth by (left) $\Delta\varphi < 45^\circ$ and (right) $\Delta\varphi > 135^\circ$. Dashed red lines limit the $m(\pi^+\pi^-)$ region in which the fit is performed, as described in Sec. 8.3.

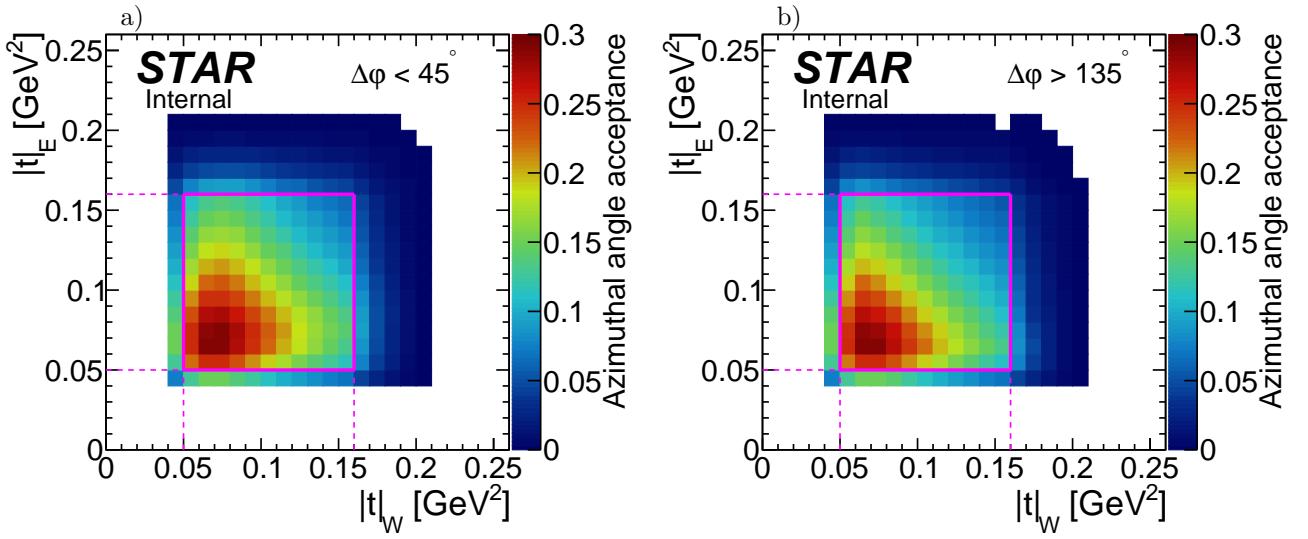


Figure 6.36: Geometrical acceptance for the forward protons being both in the fiducial region given by Eq. (4.4) if separated in azimuth by (left) $\Delta\varphi < 45^\circ$ and (right) $\Delta\varphi > 135^\circ$. Phase-space MC assuming flat distribution of azimuthal angle of the forward protons φ has been used for determination of this acceptance. Solid magenta lines limit the region selected for the measurement, which provides reasonably high geometrical acceptance.

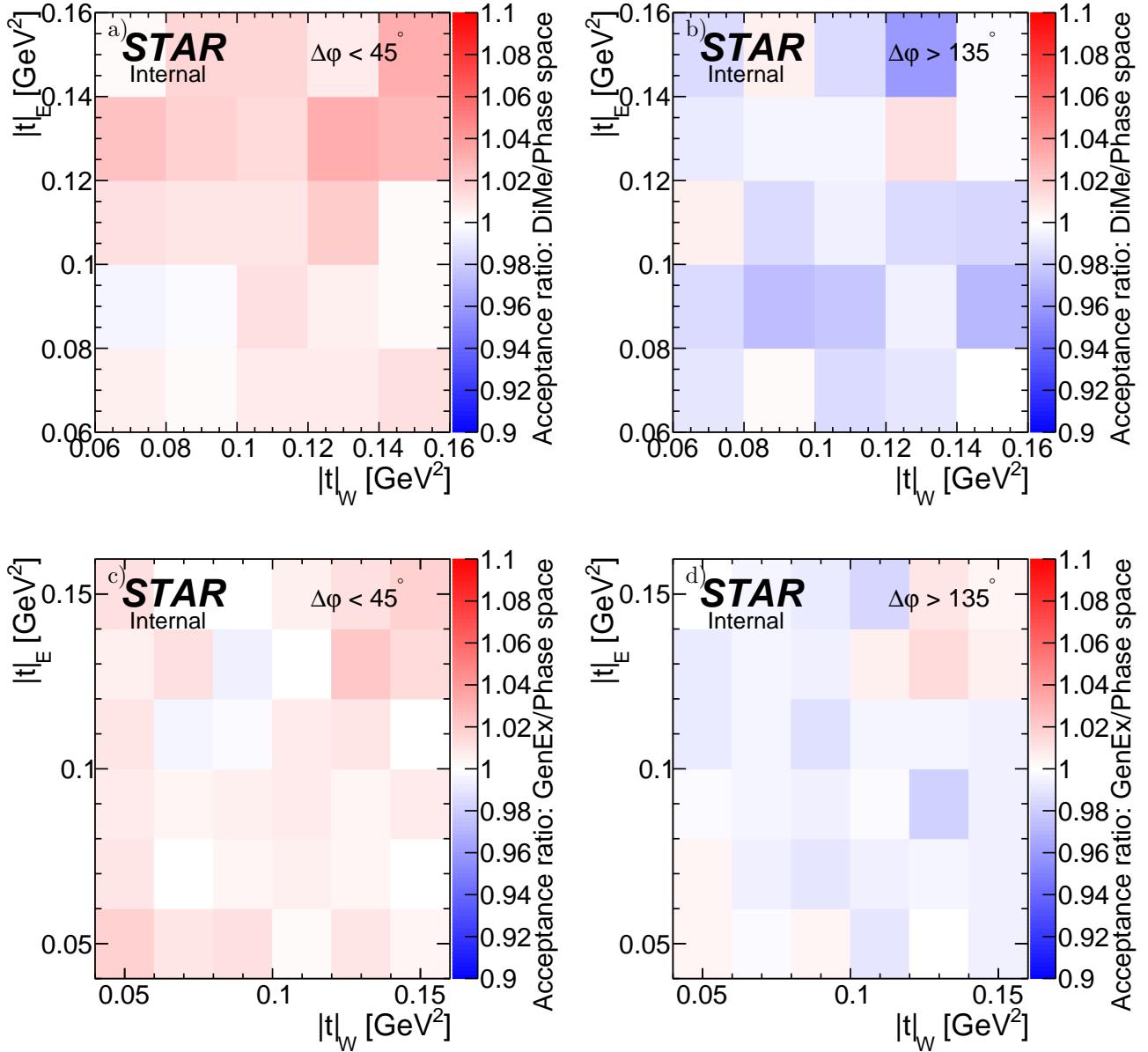


Figure 6.37: Geometrical acceptance comparison between DiMe and phase-space MC (top) and GenEx and phase-space MC (bottom) for (left) $\Delta\varphi < 45^\circ$ and (right) $\Delta\varphi > 135^\circ$.

7. Systematic uncertainties

7.1 Luminosity

Relative luminosity at STAR is determined by the coincidence rate in ZDC detectors at both beam directions. Absolute calibration is given by a special Van der Meer scan [29]. For determination of the systematic uncertainty of the integrated luminosity we use the results of a dedicated study of data from Van der Meer scans [30] performed during fill #18915. These scans were targeted on providing a precise calculation of the luminosity and an estimate of its uncertainty for the elastic proton-proton scattering measurement [26]. From this study we learn that the effective cross-section visible in the ZDC detectors is equal to 0.294 mb with 4% systematic uncertainty. The number is different from the effective ZDC cross-section used in the initial calculation of the luminosity at STAR, equal to 0.264 mb. The ratio of these numbers is 1.114. One concludes that the initial calculations of the luminosity based on the comparison of the coincidence rate of the East and West ZDC detectors, were overestimated by factor 1.114. Therefore, for the cross-section calculation we use a corrected integrated luminosity - a nominal integrated luminosity divided by aforementioned factor.

To account for possible fill-by-fill dependence in the luminosity measurement an additional 4% uncertainty was assigned to the luminosity. It was determined by comparing variations of the effective cross-sections for elastic scattering process relative to the measurement done solely based on data collected during the fill #18915 (Fig. 7.1). This effective cross-section was determined from the elastic proton-proton scattering events reconstructed with the same proton track selection as in the CEP analysis. For this purpose fiducial region for elastically-scattered proton tracks was chosen to correspond to area matching the rectangular ($|t|, \varphi$) window of 100% geometrical acceptance. This window is determined by $0.04 < |t| < 0.1$ GeV² and $1.3 < |\varphi| < 1.9$.

The overall luminosity uncertainty of 6.0% was estimated by the quadratic sum of the two uncertainty sources described above.

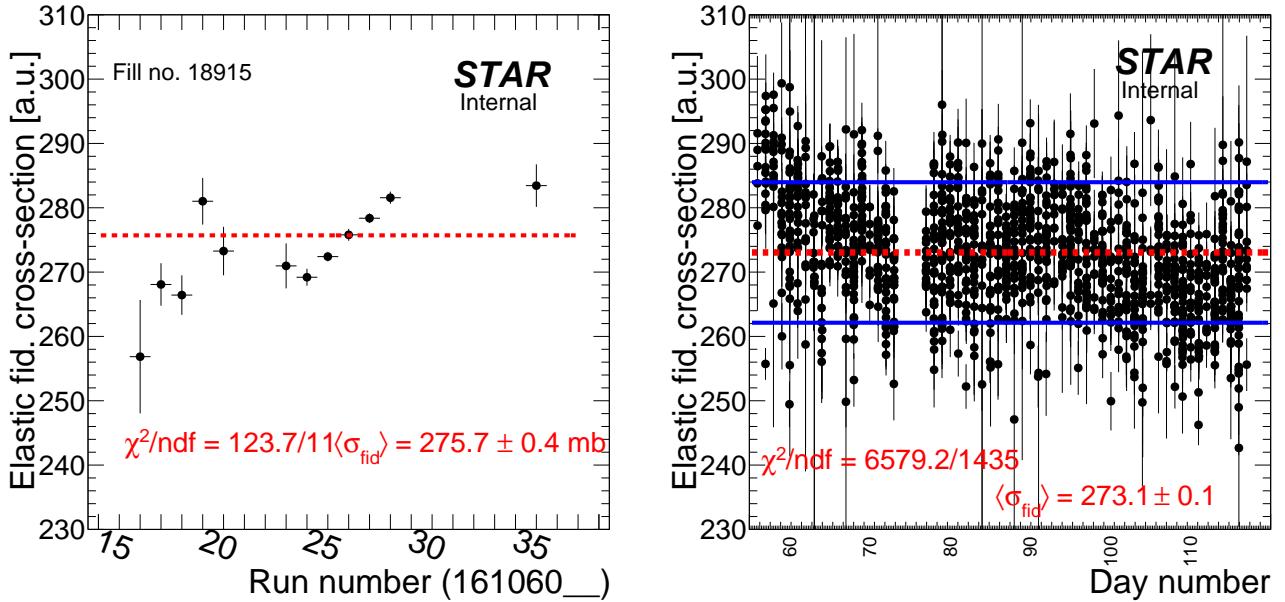


Figure 7.1: Integrated fiducial elastic proton-proton scattering cross-section for runs from fill #18915 (left) and for all runs (right). Dashed red lines mark an average fiducial cross-section within displayed run range. Solid blue lines mark $\pm 4\%$ uncertainty bands assigned to the luminosity to account to fill-by-fill variations.

7.2 Trigger veto effect (due to dead material)

Systematic uncertainty related to the trigger veto correction (Sec. 6.2.1.4) has been studied with elastic scattering events, in a way similar to analyses presented in Sec. 10.3 (and following) of Ref. [1].

Triggers dedicated for elastic scattering process (RP_ET triggers) have been studied. The trigger required signal in at least one PMT (out of four) in two RP branches opposite to each other with respect to interaction region. In addition to trigger selection, vetoes were imposed offline on any activity in other STAR detectors, such as BBC (small and large), ZDC, TOF and VPD - it reduced probability of a non-elastic pile-up interaction.

It has been demonstrated in Sec. 10.3.1 of Ref. [1] that once the single good quality RP track is required on one side, such sample consists only of elastic proton-proton scattering events.

Each side (branch) was analyzed independently; when single good quality RP track, in addition of $|\xi| < 0.01$, was found on the east side, the systematics for west side was investigated (and vice versa). Two histograms were filled per event. The first histogram was filled with all selected events. The second histogram was filled only if there was no simultaneous signal in upper and lower RP on studied side (no ET and IT trigger bits fired at the same time) - just the same, as it was implemented in RP_CPT2 trigger. However, the second histogram was filled with weight equal to inverse efficiency of the veto, $1/\epsilon_{\text{DM veto}}^{\text{side}}$. The ratio of the second to first histogram,

$$R_{\text{DM veto}} = \frac{\text{histogram of events with satisfied veto, filled with weight } 1/\epsilon_{\text{DM veto}}^{\text{side}}}{\text{histogram of all events, filled with unit weight}}, \quad (7.1)$$

has been presented in Fig. 7.2 as a function of p_x and p_y of elastically scattered proton on studied side. If single good quality proton track was reconstructed in studied branch, parameters of that track were histogrammed. Otherwise, transverse components of momentum of unreconstructed elastic proton (e.g. due to induced shower) were estimated as $-p_x$ and $-p_y$ of elastic proton track on the opposite side.

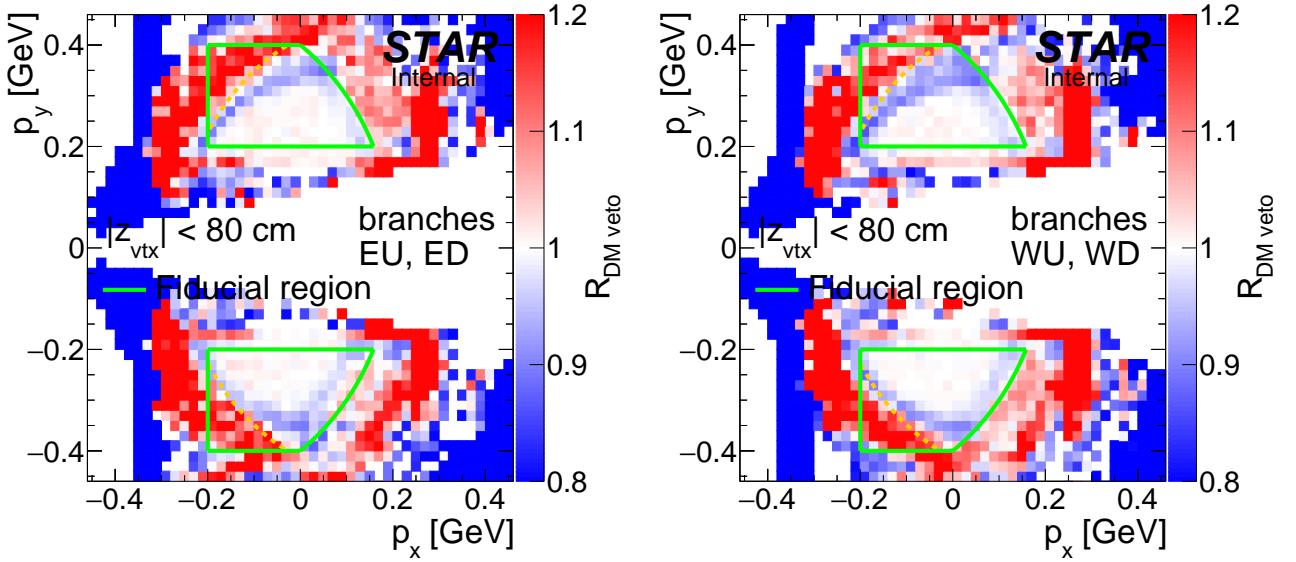


Figure 7.2: Ratio $R_{\text{DM veto}}$ illustrating systematic uncertainty of the dead material trigger veto correction in east (left) and west (right) Roman Pots.

Results presented in Fig. 7.2 indicate imperfect description of the dead material of the elements surrounding RPs (DX-D0 chamber, RF shield), which has been also overed in studies of systematic uncertainties related to RP track reconstruction efficiency, presented in Ref. [1]. Based on current study, the correction and systematic uncertainty of the dead material veto efficiency $\epsilon_{\text{DM veto}}^{\text{side}}$ are assumed to have the following form:

- multiplicative correction is applied to $\epsilon_{\text{DM veto}}^{\text{side}}$, equal to $1 + \frac{1}{2}(R_{\text{DM veto}} - 1)$,
- systematic uncertainty is assumed to be equal to $1 + \frac{1}{2}|R_{\text{DM veto}} - 1|$, therefore propagation of this systematic effect is done by variating the efficiency $\epsilon_{\text{DM veto}}^{\text{side}}$ by the multiplicative factor equal to $\pm [1 + \frac{1}{2}|R_{\text{DM veto}} - 1|]$.

7.3 TPC track quality cuts variation

We have tested sensitivity of the fiducial cross-sections on the variation of the quality cuts used in TPC track selection. Any change of these cuts requires re-calculation of the TPC track reconstruction and TOF matching efficiencies (the latter is conditional w.r.t. the former). We have checked two working points, 'loose' and 'tight', with different set of cuts on d_0 , $N_{\text{fit}}^{\text{hits}}$ and $N_{\text{DE}/\text{dx}}^{\text{hits}}$ compared to nominal working point. Definition of 'loose' and 'tight' cuts is provided in Sec. 3.2.4 of Ref. [1], together with depiction of resulted changes of the efficiencies.

Observed ratios of the cross-sections obtained with modified cuts and accordingly redefined TPC and TOF efficiencies, to the nominal cross-section, are shown in Fig. 7.3. The upward and downward relative changes of the cross-sections were added in quadrature. The resulting systematic uncertainty of the cross-section related to TPC track quality cuts is estimated to be $\pm 1.5\%$.

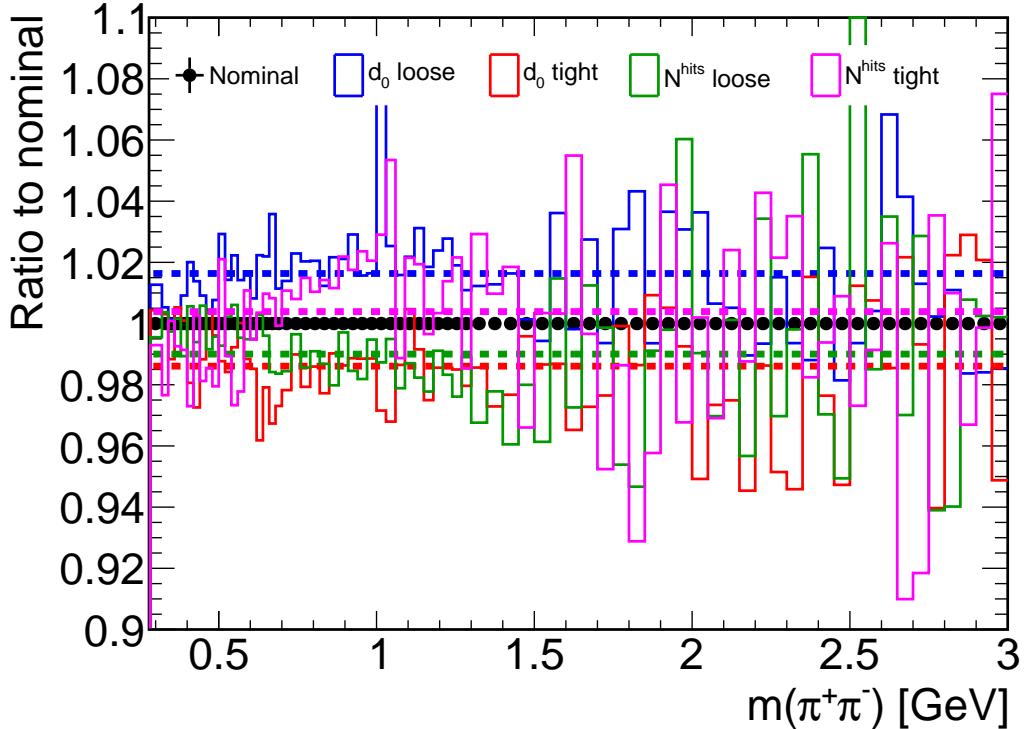


Figure 7.3: Result of variation of the TPC track quality cuts on the fiducial differential exclusive $\pi^+\pi^-$ production cross-section as a function of the invariant mass of $\pi^+\pi^-$. Dashed horizontal lines represent an average ratio for a modified cut marked with the same color.

7.4 Discussion of systematic effects

The following contributions to the overall systematic uncertainty have been studied. Influence of each systematic effect on measured cross sections has been tested by changing amount of the quantity that the systematic effect refers to and comparing the result with that obtained using nominal values.

1. Representativeness of the embedding sample ($\Delta\epsilon_{\text{TPC}}$ (embed. stat.)).

Zero-bias data available for the MC embedding is only a fraction of all zero-bias triggers, therefore physics data may be not fully represented in MC events used for determination of the TPC track reconstruction efficiency. This effect was studied by comparing estimated average levels of pile-up in the data and embedded MC. The difference was found to be of the order of 1%, which we establish as a symmetric systematic uncertainty on the TPC track reconstruction efficiency (per track). See the last paragraph of Sec. 10.1.1 of Ref. [1] for more details.

2. Embedding procedure/off-time pile-up effect ($\Delta\epsilon_{\text{TPC}}$ (pile-up)).

Reliability and precision of the embedding technique was verified and quantitatively estimated in the procedure described in Sec. 10.1.1 of Ref. [1]. Embedded MC samples were divided into sub-samples representing different levels of off-time pile-up/density of hit points in TPC. With dedicated analysis it was possible to verify if the TPC track reconstruction efficiency is compatible between all sub-samples when the effect of pile-up (changing number of hits forming a track) is reduced. The average systematic uncertainty related to the embedding procedure is < 1% (per track, Fig. 10.5 of Ref. [1]).

3. Modelling of the dead material in front of the TPC ($\Delta\epsilon_{\text{TPC}}$ (dead mat.)).

Not all detector elements are fully modeled in the MC simulation, quite often some simplifications are used. This leads to inaccuracies in efficiencies derived from the simulation. We estimated systematic uncertainty related to amount of simulated material between the primary vertex and STAR TPC to be 25% which translates to $\approx 0.5\%$ of uncertainty of the TPC track reconstruction efficiency. See Chap. 9 of Ref. [1] for details.

4. Modelling of TPC track quality parameters in embedded MC (N^{hits} and $d_0/\text{DCA}(R)$).

We have checked the impact of variation of the track quality cuts on the obtained cross-sections. It reflects systematic uncertainty related to the quality of modeling of the quantities used to select the primary TPC tracks. The estimated uncertainty on the fiducial cross-section amounts $^{+2.0}_{-1.5}\%$. See Sec. 7.3.

5. Vertexing ($\Delta\epsilon_{\text{vtx}}$).

Vertexing efficiency has been obtained using data-driven method presented in Sec. 6.2.4, thus systematic uncertainty related to this efficiency has been significantly reduced. Systematic uncertainty has been estimated as a difference between efficiency with and without subtracted background.

6. Modelling of the TOF system and validity of derived efficiency corrections ($\Delta\epsilon_{\text{TOF}}$).

The efficiency of matching TOF hits with the TPC tracks has been extracted from embedded MC sample. It has been confronted with TOF efficiency extracted from the data using two independent techniques: tag&probe (Sec. 4.1 of Ref. [1]) and HFT-tagging (Sec. 10.2.2 of Ref. [1]). Average difference between the data and MC efficiency has been used as a correction to MC efficiency, while half of the difference between data-extracted efficiencies has been treated as a systematic uncertainty (Fig. 10.16, Ref. [1]). This amounts 1%-3% (per track), depending on particle species.

7. Modelling of the RP system and validity of derived efficiency corrections ($\Delta\epsilon_{\text{RP}}$, $\Delta\epsilon_{\text{RP}}^{\text{trig.}}$ and $\Delta\epsilon_{\text{RP}}^{\text{DM veto}}$).

Reliability of RP simulation which was used to extract efficiency corrections with MC embedded into zero-bias data, has been verified and quantitatively estimated in the procedure described in Sec. 10.3 of Ref. [1]. For this purpose elastic proton-proton scattering events have been used. The same analysis has been performed on embedded elastic scattering MC and the data, leading to estimates of the RP acceptance and track reconstruction efficiency. The differences between two results has been considered as a measure of the systematic uncertainty that covers RP track reconstruction efficiency itself, detectors alignment, embedding technique. Similar studies have been performed to determine systematic uncertainty related to the trigger veto efficiency correction, as presented in Sec. 7.2.

8. Pile-up veto correction ($\Delta\epsilon_{\text{veto}}$).

Luminosity-dependent correction related to veto of pile-up interactions is derived from the zero-bias data on run by run basis. Residual systematic uncertainty has been estimated as a difference between the correction factor calculated for particular run, and correction factor obtained from the exponential fit to all points representing correction factors as a function of instantaneous luminosity.

9. Longitudinal shape and position of the primary vertex distribution ($\Delta\langle z_{\text{vtx}}$ and $\Delta\sigma(z_{\text{vtx}})$).

Comparison of the z_{vtx} distribution as seen in the TPC and in RPs leads to conservative estimate of the uncertainty of central position of the vertex equal 2 cm, and the spread (standard deviation) of vertex equal 3 cm.

10. Non-exclusive background estimate ($\Delta N_{\text{bkgd}}^{\text{non-excl}}$).

As explained in Sec. 5.2.1, estimated systematic difference between real level of non-exclusive background, and level determined with a data-driven method, may be as high as 10%. We apply such variation of the non-exclusive background and assign resulting differences of cross sections as their systematic uncertainty related to non-exclusive background determination method.

11. Luminosity determination ($\Delta\mathcal{L}$).

Uncertainty of the integrated luminosity has been estimated to 6%, which is still subject to change.

7.5 Graphical representation of systematic uncertainties

In this section we present relative contributions of effects listed in Sec. 7.4 to the total systematic uncertainties on differential fiducial cross sections presented in Chap. 8. Numbering of figures is preserved with respect to corresponding cross section results in the next chapter. The color code is the same in all figures, with the legend explaining the meaning of each color attached at the bottom of Fig. 7.4.

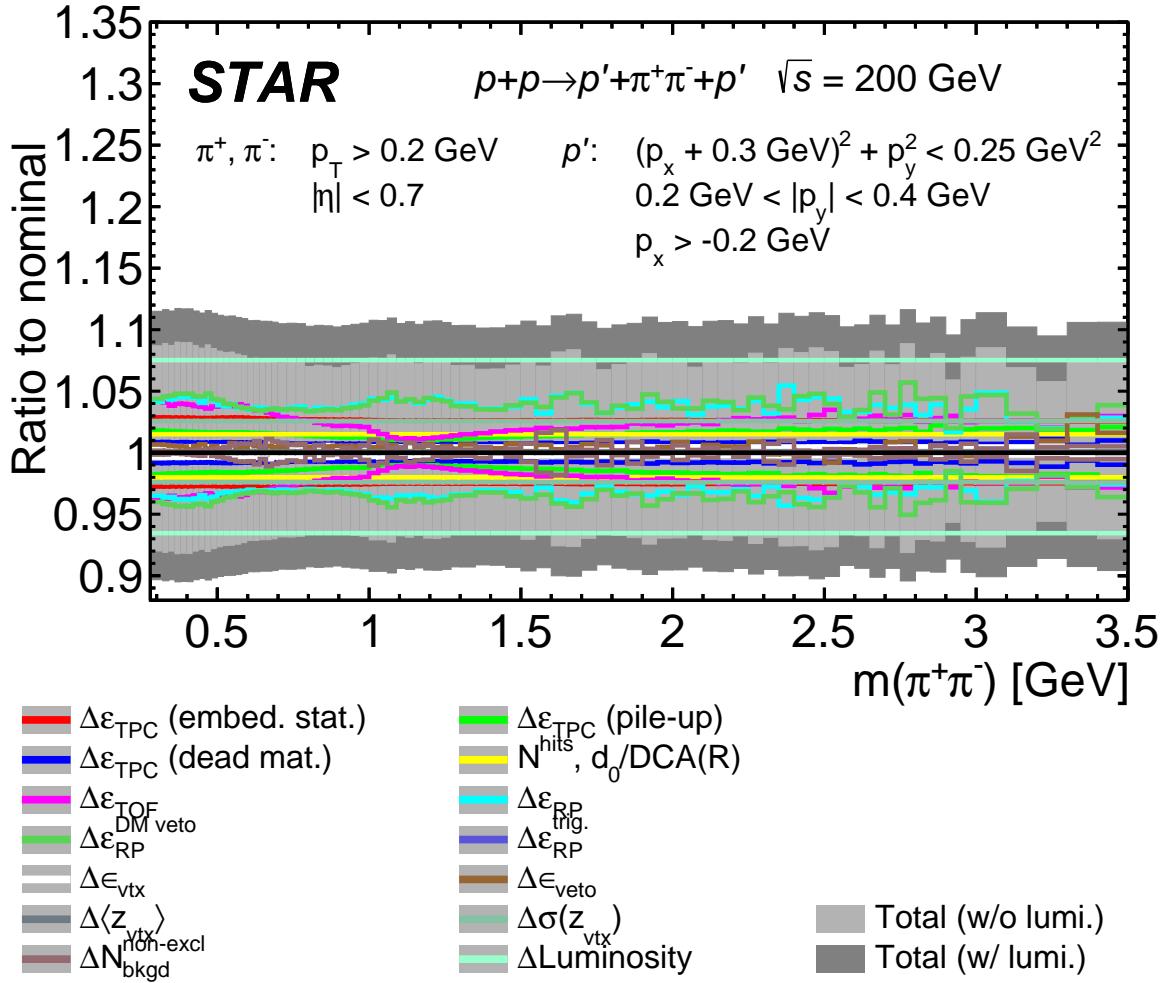


Figure 7.4: Systematic uncertainties of the differential cross sections for CEP of charged particle pairs $\pi^+\pi^-$ as a function of the invariant mass of the pair in the fiducial region explained on the plots.

	$\delta_{\text{syst}}/\sigma_{\text{fid}} [\%]$					
	TOF	TPC	RP	Other	Lumi.	Total
$\pi^+\pi^-$	-3.1 -2.9	3.3 -3.1	7.3 -6.1	2.6 -2.4		11.4 -10.5
K^+K^-	10.0 -8.6	6.6 -6.1	7.4 -6.2	2.7 -2.4	7.5 -6.5	16.0 -14.3
$p\bar{p}$	5.4 -4.9	3.6 -3.4	8.4 -6.9	2.9 -2.4		13.0 -11.8

Table 7.1: Typical systematic uncertainties of integrated fiducial cross sections for CEP of $\pi^+\pi^-$, K^+K^- and $p\bar{p}$. Provided numbers are decomposed into major components. Single number in a cell indicates symmetric uncertainty, while positive and negative number denotes asymmetric uncertainty.

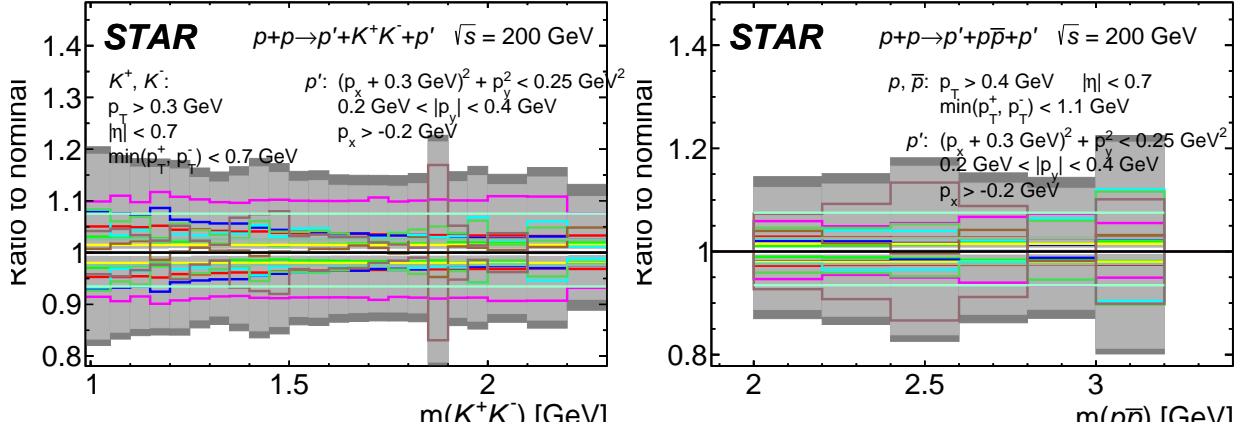


Figure 7.5: Systematic uncertainties of the differential cross sections for CEP of charged particle pairs K^+K^- (left) and $p\bar{p}$ (right) as a function of the invariant mass of the pair in the fiducial region explained on the plots.

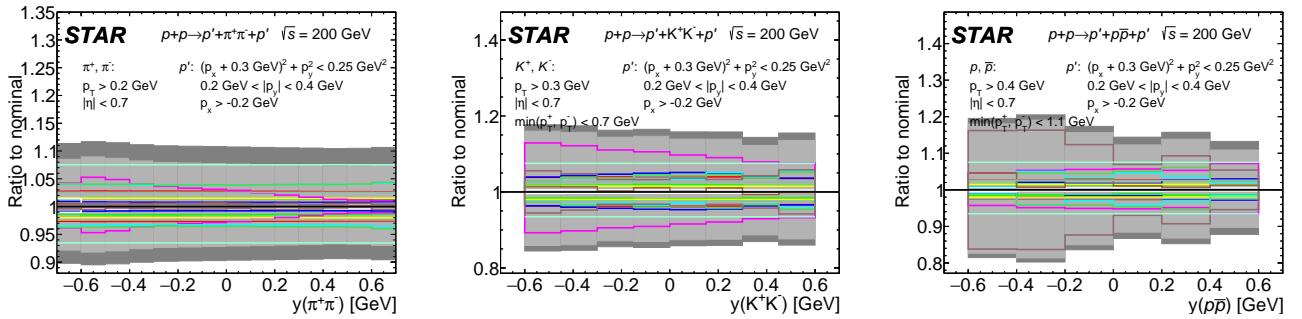


Figure 7.6: Systematic uncertainties of the differential cross sections for CEP of charged particle pairs $\pi^+\pi^-$ (left), K^+K^- (middle) and $p\bar{p}$ (right) as a function of the pair rapidity measured in the fiducial region explained on the plots.

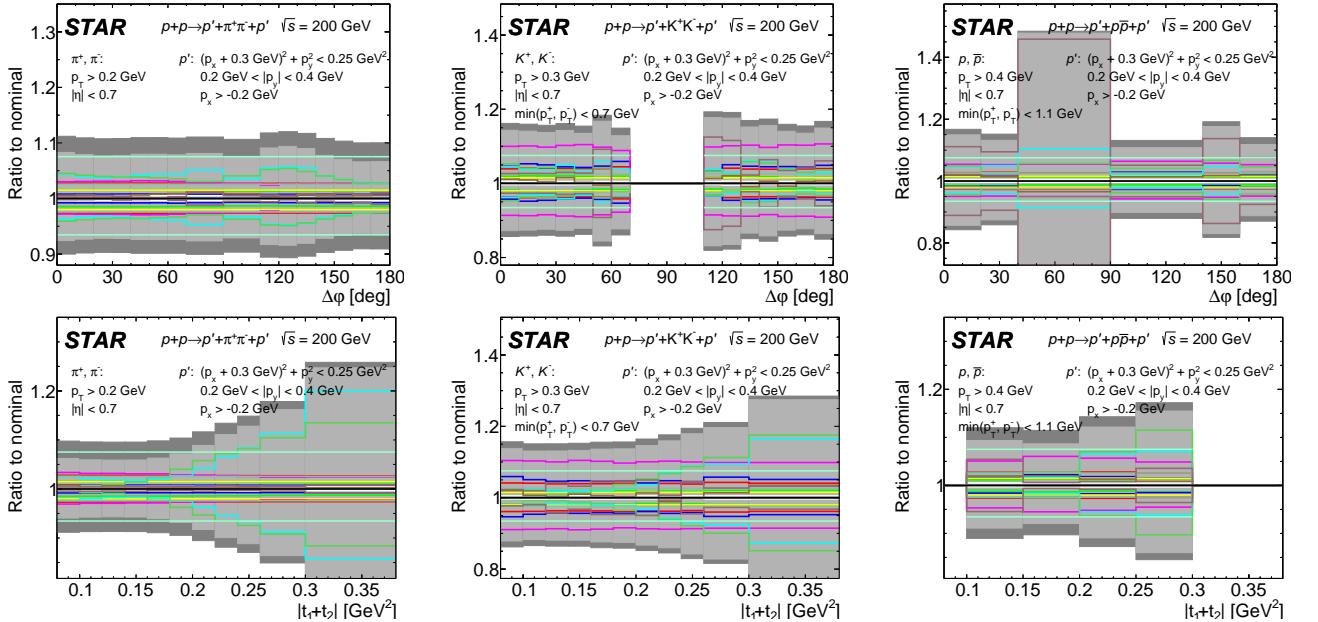


Figure 7.7: Systematic uncertainties of the differential cross sections for CEP of charged particle pairs $\pi^+\pi^-$ (left column), K^+K^- (middle column) and $p\bar{p}$ (right column) as a function of the difference of azimuthal angles of the forward scattered protons (top) and of the sum of the squares of the four-momenta losses in the proton vertices (bottom) measured in the fiducial region explained on the plots.

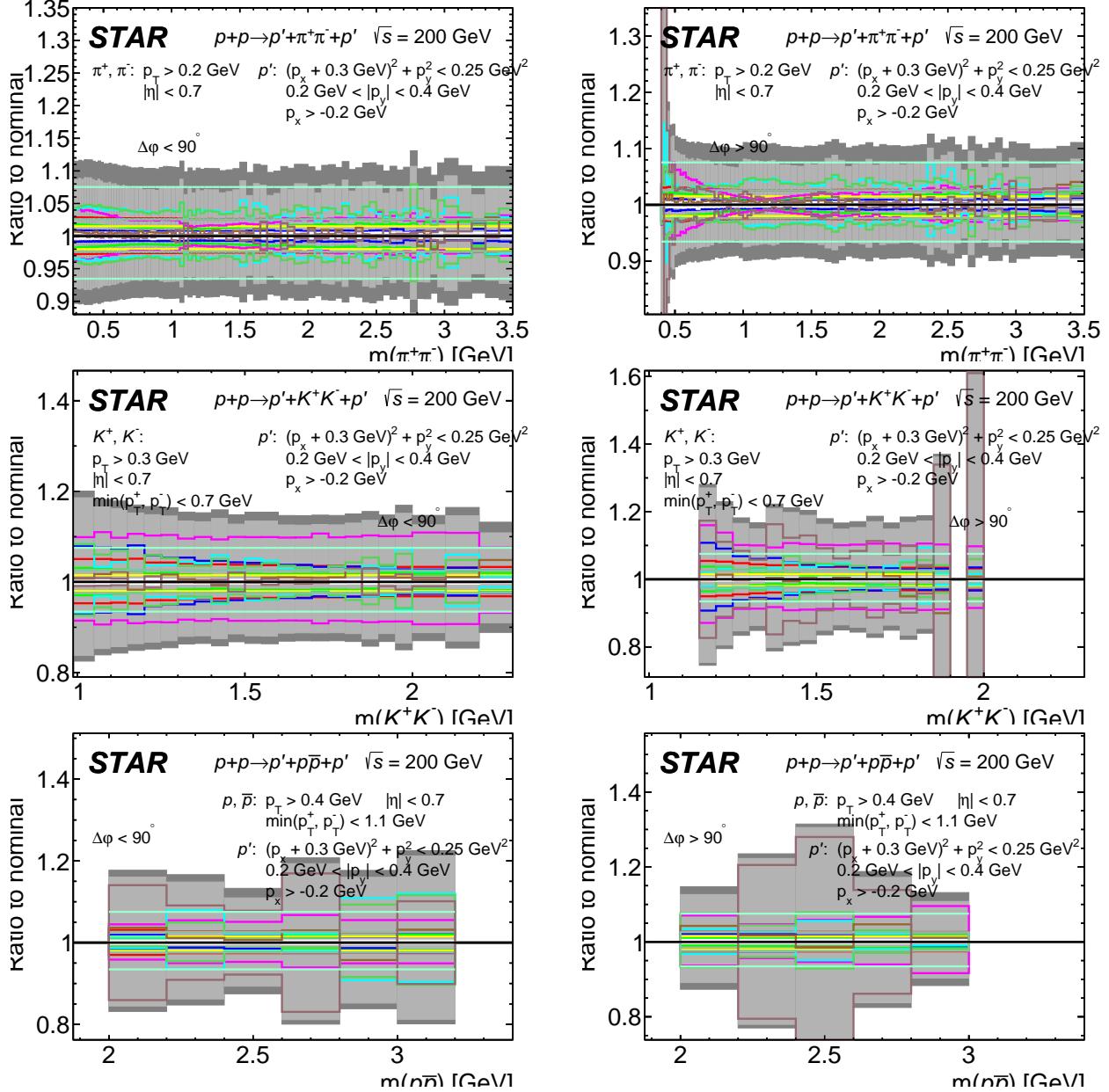


Figure 7.8: Systematic uncertainties of the differential cross sections for CEP of charged particle pairs $\pi^+\pi^-$ (top), K^+K^- (middle) and $p\bar{p}$ (bottom) as a function of the invariant mass of the pair in two $\Delta\phi$ regions: $\Delta\phi < 90$ degree (left column) and $\Delta\phi > 90$ degree (right column) measured in the fiducial region explained on the plots.

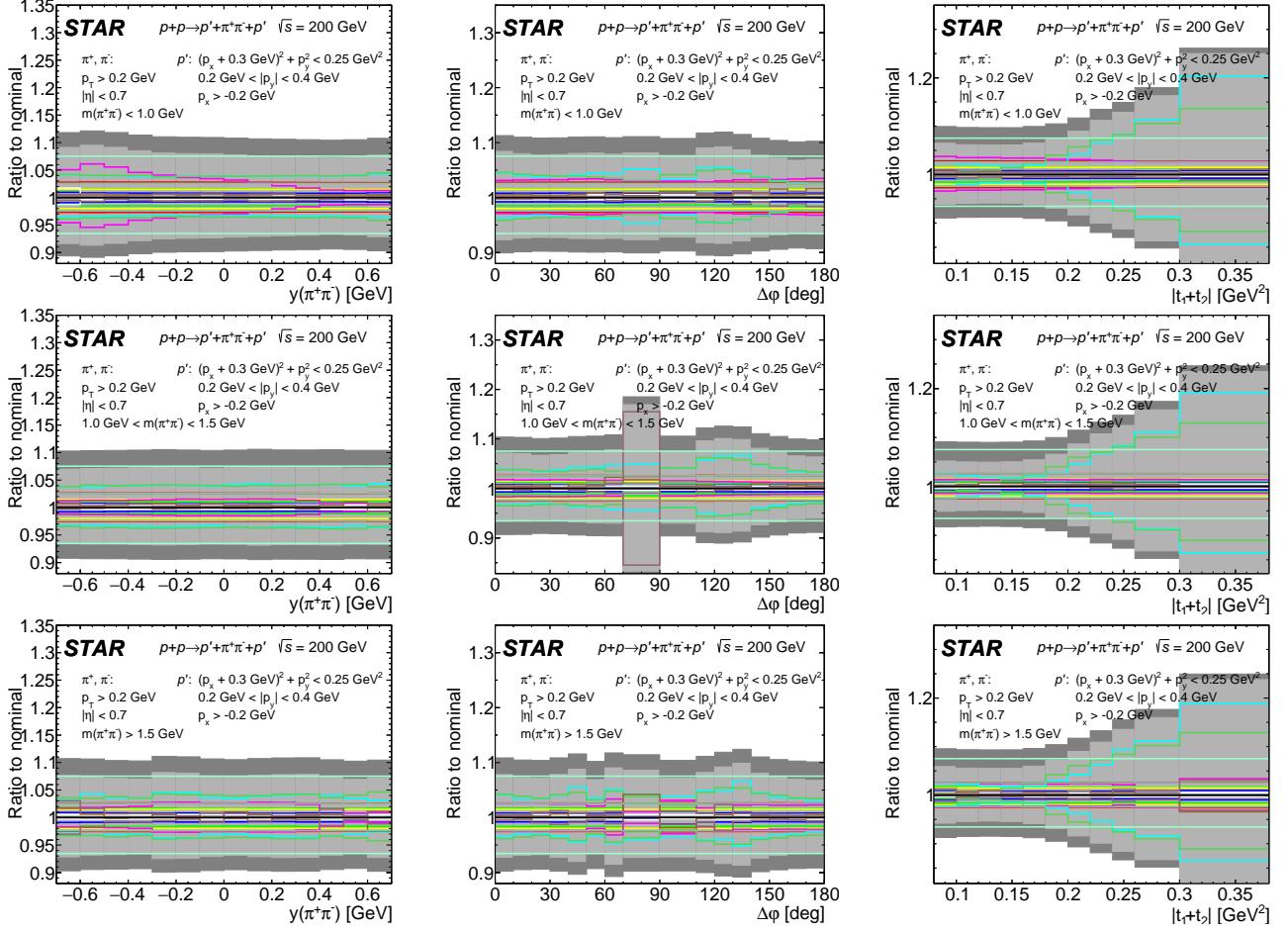


Figure 7.9: Systematic uncertainties of the differential cross sections for CEP of $\pi^+\pi^-$ pairs as a function of the rapidity of the pair (left column) difference of azimuthal angles of the forward scattered protons (middle column) and of the sum of the squares of the four-momenta losses in the proton vertices (right column) measured in the fiducial region explained on the plots, separately for three ranges of the $\pi^+\pi^-$ pair invariant mass: $m < 1$ GeV (top), $1 < m < 1.5$ GeV (middle) and $m > 1.5$ GeV (bottom).

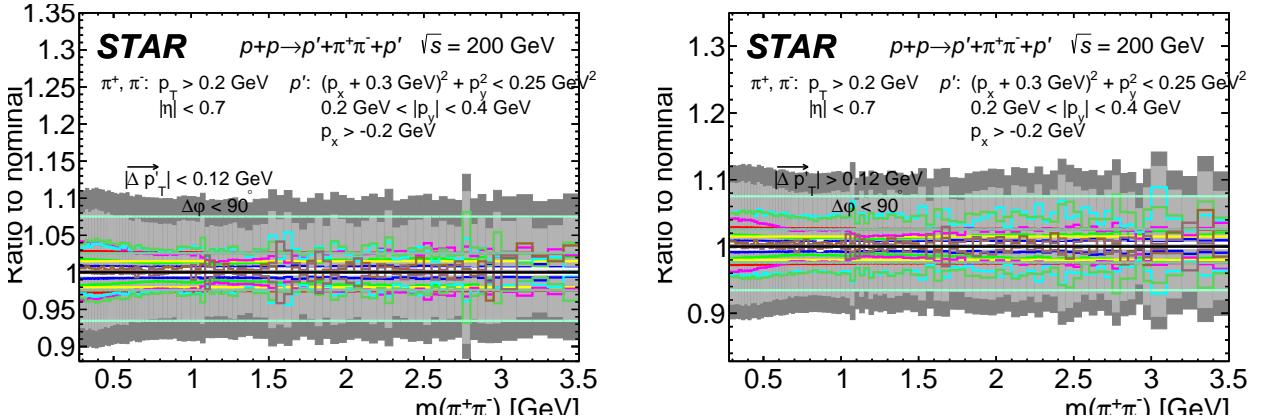


Figure 7.10: Systematic uncertainties of the differential cross sections $d\sigma/dm(\pi^+\pi^-)$ for CEP of $\pi^+\pi^-$ pairs in two $|\vec{p}'_{1,T} - \vec{p}'_{2,T}|$ regions: $|\vec{p}'_{1,T} - \vec{p}'_{2,T}| < 0.12$ GeV (left) and $|\vec{p}'_{1,T} - \vec{p}'_{2,T}| > 0.12$ GeV (right) in the fiducial region and $\Delta\phi < 90$ degree.

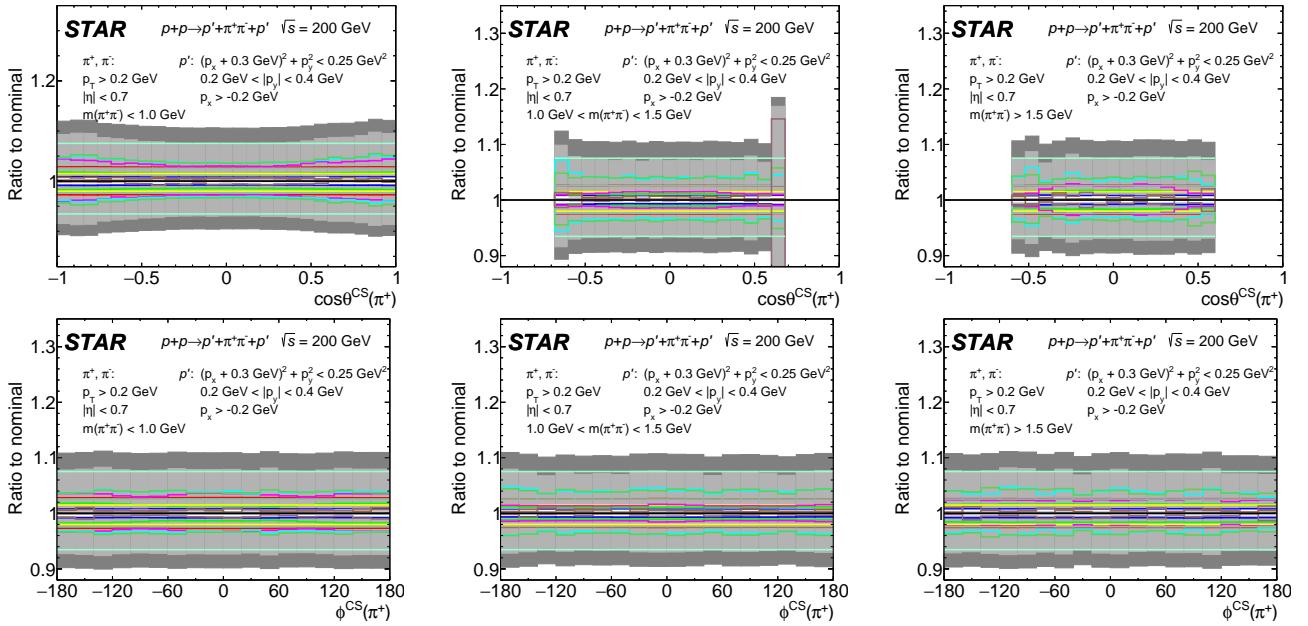


Figure 7.11: Systematic uncertainties of the differential cross sections for CEP of $\pi^+\pi^-$ pairs as a function of $\cos\theta^{\text{CS}}$ (top) and of ϕ^{CS} (bottom) measured in the fiducial region explained on the plots, separately for three ranges of the $\pi^+\pi^-$ pair invariant mass: $m < 1 \text{ GeV}$ (left column), $1 < m < 1.5 \text{ GeV}$ (middle column) and $m > 1.5 \text{ GeV}$ (right column).

8. Physics results

8.1 Differential cross sections

In this subsection we present differential fiducial cross sections.

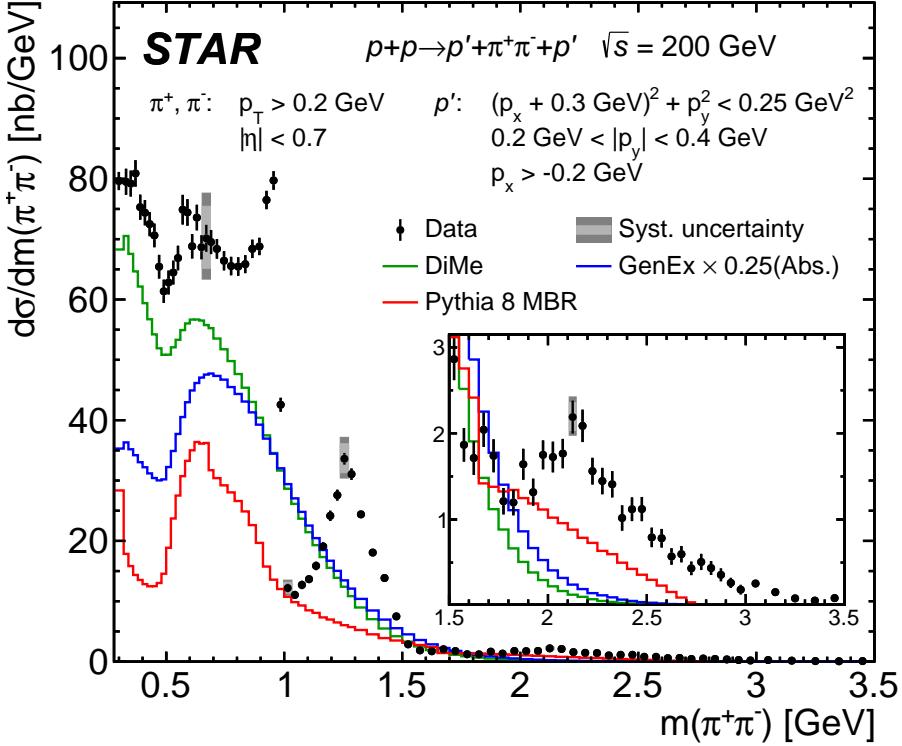


Figure 8.1: Differential cross sections for CEP of charged particle pairs $\pi^+\pi^-$ as a function of the invariant mass of the pair in the fiducial region explained on the plots. Data are shown as solid points with error bars representing the statistical uncertainties. The typical systematic uncertainties are shown as gray boxes for only few data points as they are almost fully correlated between neighboring bins. Predictions from MC models GenEx, DiMe and MBR are shown as histograms. In the lower panels in the bottom plots the ratios of the MC predictions scaled to data and the data are shown.

$\sigma_{\text{fid}} \pm \delta_{\text{stat}} \pm \delta_{\text{syst}}$			
PID	unit	$\Delta\varphi < 90^\circ$	$\Delta\varphi > 90^\circ$
$\pi^+\pi^-$	nb	$38.2 \pm 0.2^{+4.5}_{-3.9}$	$18.5 \pm 0.1^{+2.0}_{-1.8}$
K^+K^-	pb	$971 \pm 50^{+160}_{-140}$	$528 \pm 38^{+89}_{-78}$
$p\bar{p}$	pb	$16.2 \pm 4.1^{+3.0}_{-2.8}$	$30.3 \pm 5.7^{+4.7}_{-4.3}$

Table 8.1: Integrated fiducial cross sections for CEP of $\pi^+\pi^-$, K^+K^- and $p\bar{p}$ pairs in two ranges of azimuthal angle difference $\Delta\varphi$ between forward scattered protons. Statistical and systematic uncertainties are provided for each cross section.

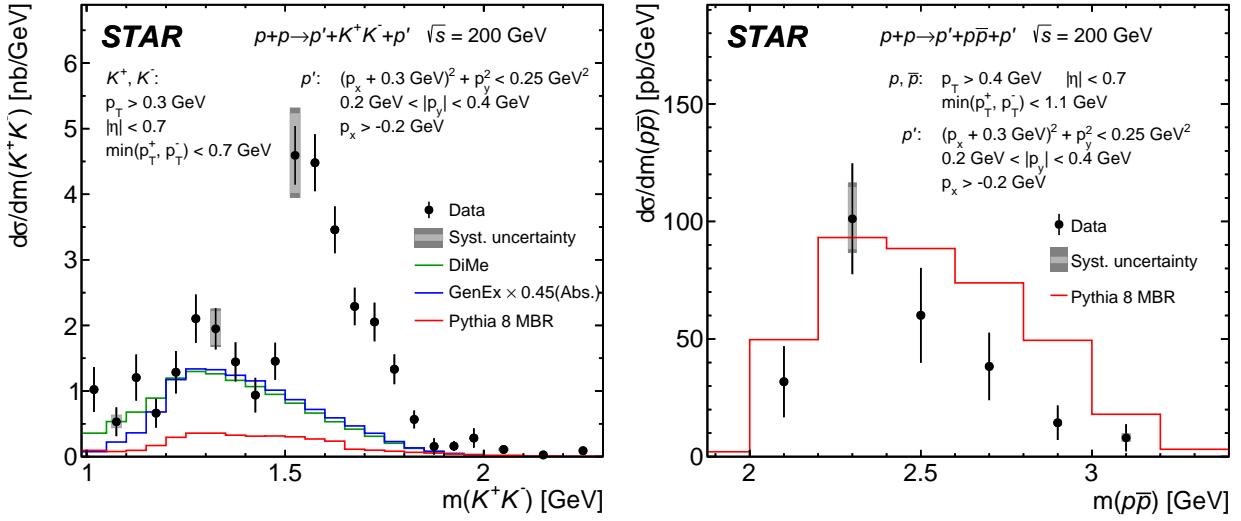


Figure 8.2: Differential cross sections for CEP of charged particle pairs K^+K^- (left) and $p\bar{p}$ (right) as a function of the invariant mass of the pair in the fiducial region explained on the plots. Data are shown as solid points with error bars representing the statistical uncertainties. The typical systematic uncertainties are shown as gray boxes for only few data points as they are almost fully correlated between neighboring bins. Predictions from MC models GenEx, DiMe and MBR are shown as histograms. In the lower panels in the bottom plots the ratios of the MC predictions scaled to data and the data are shown.

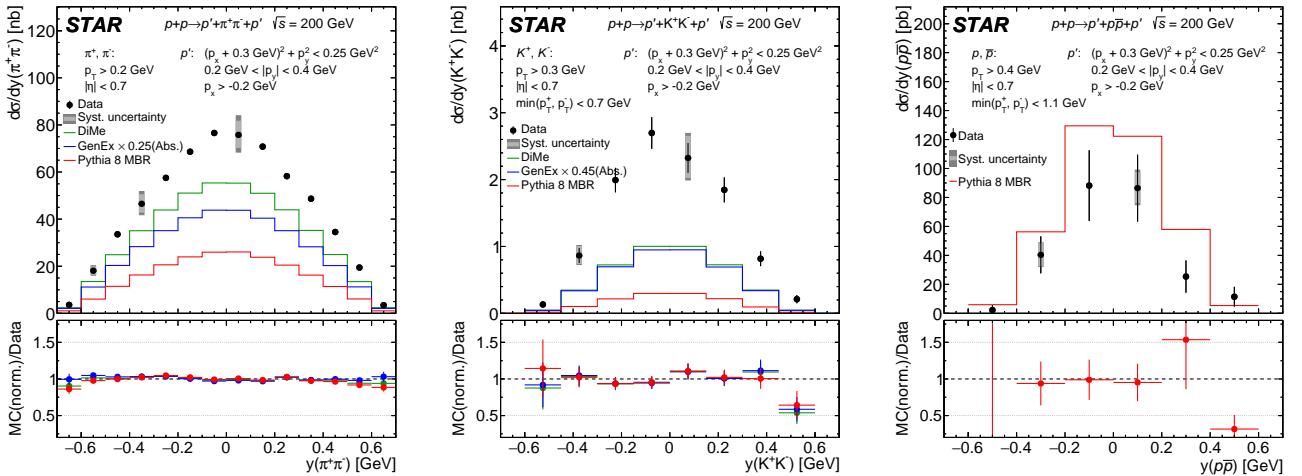


Figure 8.3: Differential cross sections for CEP of charged particle pairs $\pi^+\pi^-$ (left), K^+K^- (middle) and $p\bar{p}$ (right) as a function of the pair rapidity measured in the fiducial region explained on the plots. Data are shown as solid points with error bars representing the statistical uncertainties. The typical systematic uncertainties are shown as gray boxes for only few data points as they are almost fully correlated between neighboring bins. Predictions from MC models GenEx, DiMe and MBR are shown as histograms. In the lower panels in the bottom plots the ratios of the MC predictions scaled to data and the data are shown.

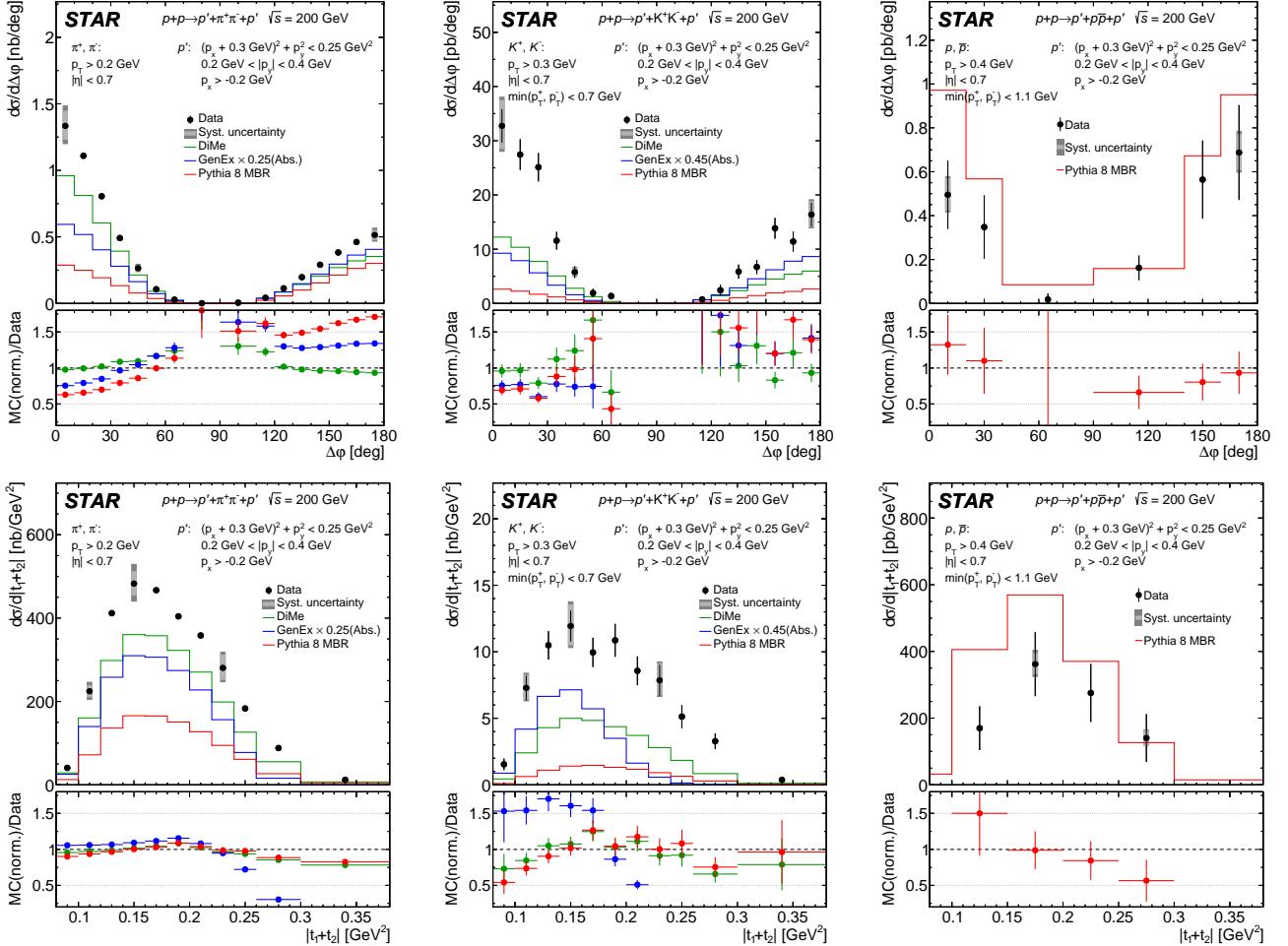


Figure 8.4: Differential cross sections for CEP of charged particle pairs $\pi^+\pi^-$ (left column), K^+K^- (middle column) and $p\bar{p}$ (right column) as a function of the difference of azimuthal angles of the forward scattered protons (top) and of the sum of the squares of the four-momenta losses in the proton vertices (bottom) measured in the fiducial region explained on the plots. Data are shown as solid points with error bars representing the statistical uncertainties. The typical systematic uncertainties are shown as gray boxes for only few data points as they are almost fully correlated between neighboring bins. Predictions from MC models GenEx, DiMe and MBR are shown as histograms. In the lower panels the ratios of the MC predictions scaled to data and the data are shown.

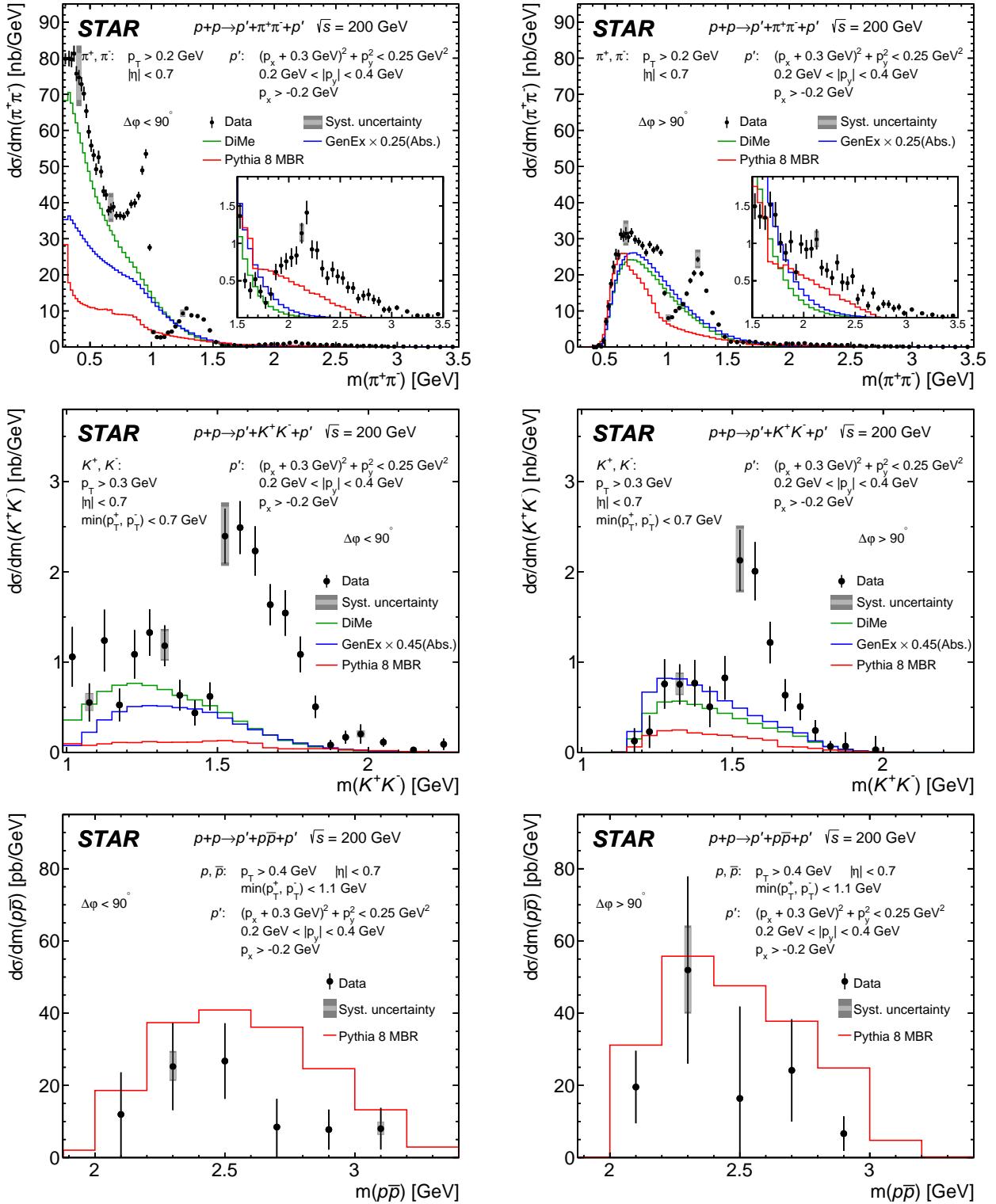


Figure 8.5: Differential cross sections for CEP of charged particle pairs $\pi^+\pi^-$ (top), K^+K^- (middle) and $p\bar{p}$ (bottom) as a function of the invariant mass of the pair in two $\Delta\phi$ regions: $\Delta\phi < 90$ degree (left column) and $\Delta\phi > 90$ degree (right column) measured in the fiducial region explained on the plots. Data are shown as solid points with error bars representing the statistical uncertainties. The typical systematic uncertainties are shown as gray boxes for only few data points as they are almost fully correlated between neighboring bins. Predictions from MC models GenEx, DiMe and MBR are shown as histograms.

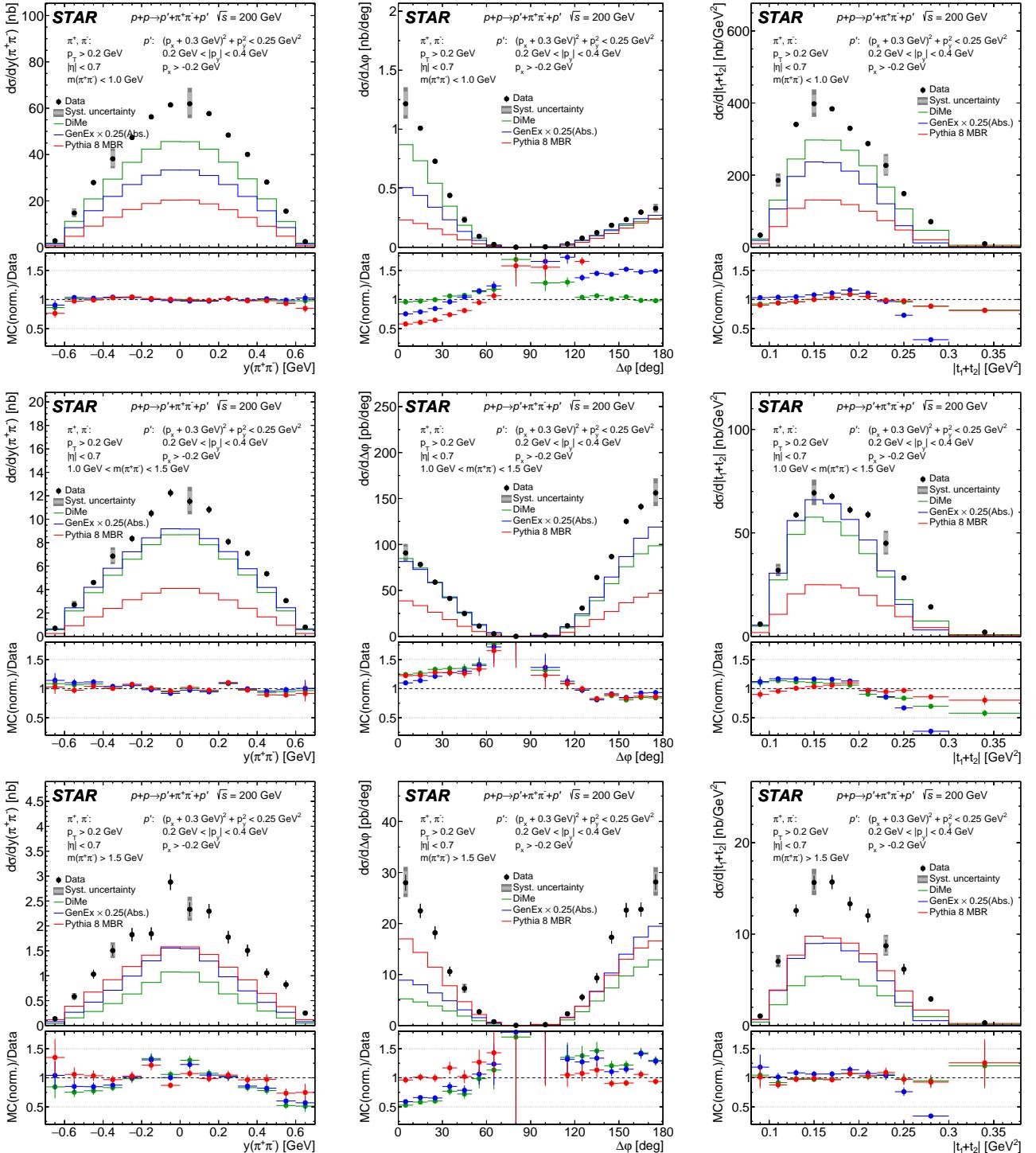


Figure 8.6: Differential cross sections for CEP of $\pi^+\pi^-$ pairs as a function of the rapidity of the pair (left column) difference of azimuthal angles of the forward scattered protons (middle column) and of the sum of the squares of the four-momenta losses in the proton vertices (right column) measured in the fiducial region explained on the plots, separately for three ranges of the $\pi^+\pi^-$ pair invariant mass: $m < 1 \text{ GeV}$ (top), $1 < m < 1.5 \text{ GeV}$ (middle) and $m > 1.5 \text{ GeV}$ (bottom). Data are shown as solid points with error bars representing the statistical uncertainties. The typical systematic uncertainties are shown as gray boxes for only few data points as they are almost fully correlated between neighboring bins. Predictions from MC models GenEx, DiMe and MBR are shown as histograms. In the lower panels the ratios of the MC predictions scaled to data and the data are shown.

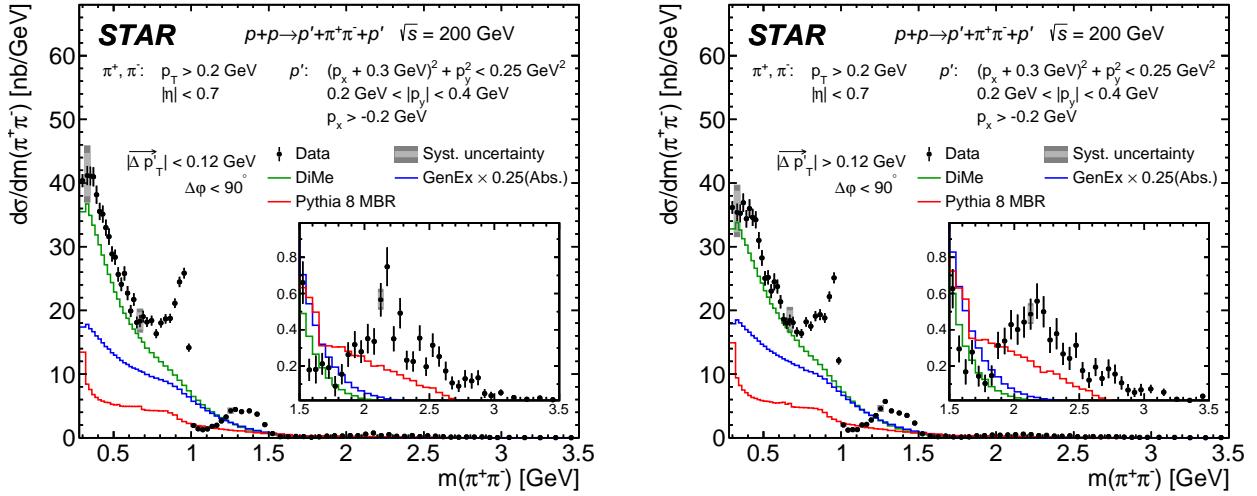


Figure 8.7: Differential cross sections $d\sigma/dm(\pi^+\pi^-)$ for CEP of $\pi^+\pi^-$ pairs in two $|\vec{p}'_{1,T} - \vec{p}'_{2,T}|$ regions: $|\vec{p}'_{1,T} - \vec{p}'_{2,T}| < 0.12$ GeV (left) and $|\vec{p}'_{1,T} - \vec{p}'_{2,T}| > 0.12$ GeV (right) in the fiducial region and $\Delta\phi < 90$ degree. There is no difference for two $|\vec{p}'_{1,T} - \vec{p}'_{2,T}|$ regions. Data are shown as solid points with error bars representing the statistical uncertainties. The typical systematic uncertainties are shown as gray boxes for only few data points as they are almost fully correlated between neighboring bins. Predictions from MC models GenEx, DiMe and MBR are shown as histograms.

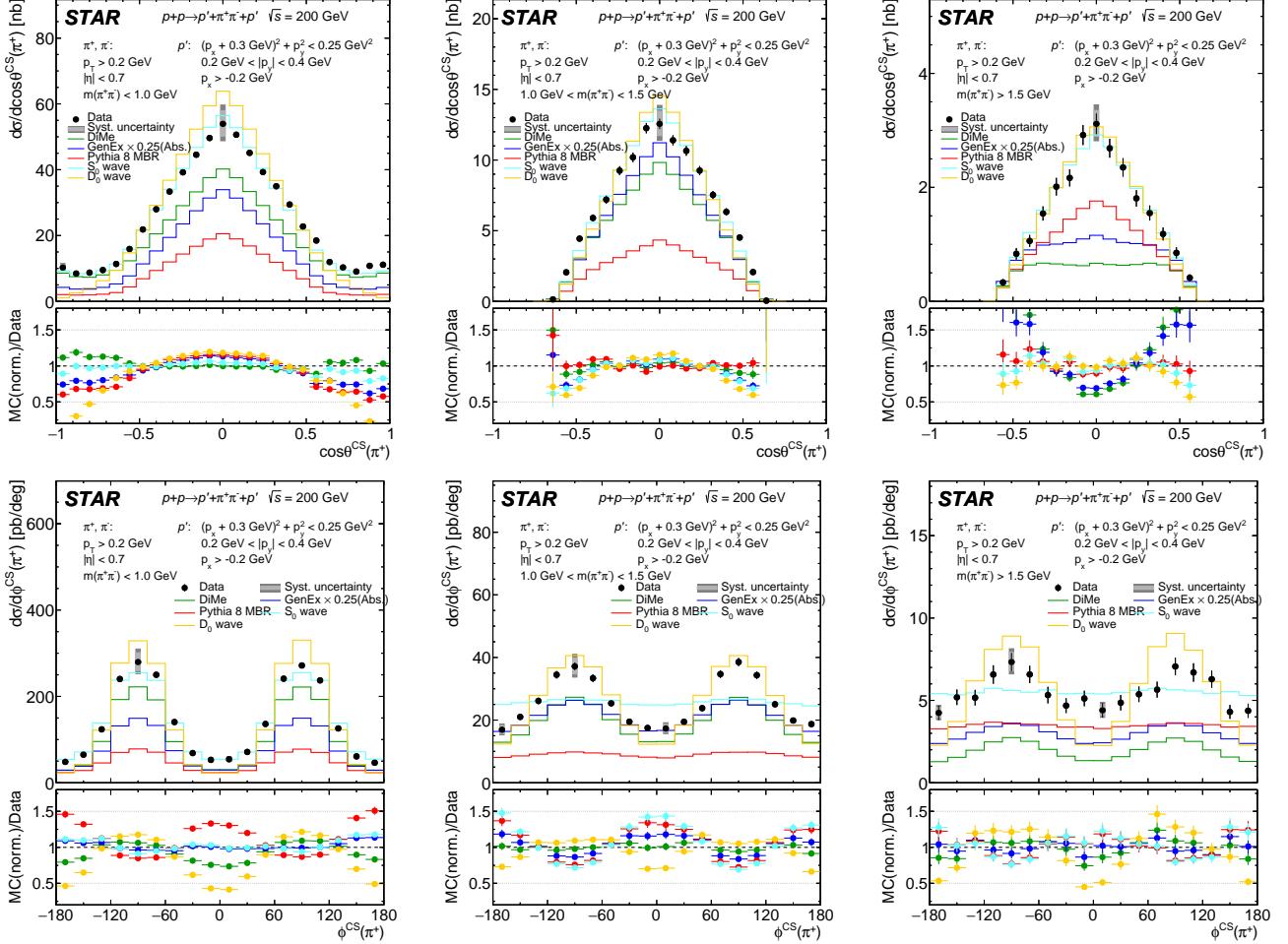


Figure 8.8: Differential cross sections for CEP of $\pi^+\pi^-$ pairs as a function of $\cos\theta^{\text{CS}}$ (top) and of ϕ^{CS} (bottom) measured in the fiducial region explained on the plots, separately for three ranges of the $\pi^+\pi^-$ pair invariant mass: $m < 1 \text{ GeV}$ (left column), $1 < m < 1.5 \text{ GeV}$ (middle column) and $m > 1.5 \text{ GeV}$ (right column). Data are shown as solid points with error bars representing the statistical uncertainties. The typical systematic uncertainties are shown as gray boxes for only few data points as they are almost fully correlated between neighboring bins. Predictions from MC models GenEx, DiMe and MBR are shown as histograms. In the lower panels the ratios of the MC predictions scaled to data and the data are shown.

8.2 Invariant mass spectrum modelling

We make an attempt to fit extrapolated (using acceptance corrections from Sec. 6.7) differential cross-section with a simplified model of the $\pi^+\pi^-$ invariant mass spectrum. In this model we assume contributions from the direct pair production and three resonances in the mass range of $0.6 - 1.7$ GeV: $f_0(980)$, $f_2(1270)$ and $f_0(1500)$. It is important to note, that in the fit only $f_2(1270)$ has fixed mass and width and thus is explicitly assumed. For the other two resonances the masses and widths are left free, however their fitted masses and widths are compatible with $f_0(980)$ and $f_0(1500)$, therefore we use such labeling from the very beginning.

The total amplitude for the exclusive $\pi^+\pi^-$ production is given by:

$$A(m) = A_{\text{cont}} \times f_{\text{cont}(m)} + \\ A_{f_0(980)} \times \mathcal{R}_F(m; M_{f_0(980)}, \Gamma_{f_0(980)}) + \\ A_{f_2(1270)} \times \mathcal{R}_{BW}(m; M_{f_2(1270)}, \Gamma_{f_2(1270)}) + \\ A_{f_0(1500)} \times \mathcal{R}_{BW}(m; M_{f_0(1500)}, \Gamma_{f_0(1500)}), \quad (8.1)$$

thus all states are added coherently (interfere with each other). The amplitude for continuum production is chosen to be real while multiplicative amplitude factors for resonances are allowed to be complex:

$$A_{\text{cont}} \in \mathbb{R}, \quad A_{f_0(980)}, A_{f_2(1270)}, A_{f_0(1500)} \in \mathbb{C} \quad \rightarrow \quad A_f = |A_f| e^{i\phi_f}. \quad (8.2)$$

The shape of the continuum amplitude is assumed to have the form

$$f_{\text{cont}}(m) = \sqrt{\frac{q}{m}} \times e^{-\frac{B}{2} \cdot q} \quad (8.3)$$

with the break-up momentum q equal to

$$q(m) = \frac{1}{2} \sqrt{m^2 - 4m_\pi^2}. \quad (8.4)$$

For $f_2(1270)$ and $f_0(1500)$ resonances we use relativistic Breit-Wigner form of the production amplitude with mass-dependent width:

$$\mathcal{R}_{BW}(m; M, \Gamma_0) = \frac{M\sqrt{\Gamma_0}\sqrt{\Gamma(m)}}{M^2 - m^2 - iM\Gamma(m)}, \quad \Gamma(m) = \Gamma_0 \frac{q}{m} \frac{M}{q_0} \left(\frac{B_J(q^2 R^2)}{B_J(q_0^2 R^2)} \right)^2. \quad (8.5)$$

The centrifugal effects in Eq. (8.5) are accounted through the Blatt-Weisskopf barrier factors B_J [31] with the empirical interaction radius R set to 1 fm and $q_0 = q(M)$. Naturally $J = 2$ and $J = 0$ is used for $f_2(1270)$ and $f_0(1500)$, respectively.

Meson $f_0(980)$ requires different treatment due to large branching ratio to $K\bar{K}$ channel which opens in the vicinity of the mass peak. This changes the resonance shape and is accounted for in the parametrisation of the amplitude via the Flatté formula [32]:

$$\mathcal{R}_F(m; M, \Gamma_0) = \frac{M\sqrt{\Gamma_0}\sqrt{\Gamma_\pi(m)}}{M^2 - m^2 - iM(\Gamma_\pi(m) + \Gamma_K(m))} \quad (8.6)$$

with the partial width Γ_j ($j = \pi, K$) described by the product of the coupling parameter g_j and the break-up momentum q (Eq. (8.4)) for particle j :

$$\Gamma_j(m) = g_j q_j(m) = \frac{g_j}{2} \sqrt{m^2 - 4m_j^2}. \quad (8.7)$$

and the partial width in $\pi^+\pi^-$ channel at the resonance mass equal to

$$\Gamma_0 = g_\pi q_\pi(M). \quad (8.8)$$

In the fit the ratio g_K/g_π is fixed to 4.21, the value well constrained experimentally through the measurement of J/ψ decay into ϕ and $\pi^+\pi^-/K^+K^-$ [33].

Squared amplitude from Eq. (8.1), $|A|^2$, is convoluted for the purpose of the fit with the normal distribution $\mathcal{N}(m; \sigma_{\text{res}})$ representing finite resolution of reconstructed invariant mass of the pion pair. The resolution parameter σ_{res} is provided to the fitting algorithm; it is set to grow linearly with increasing invariant mass according to MC simulation of the STAR TPC detector. The $m(\pi^+\pi^-)$ resolution at the lower and upper limit

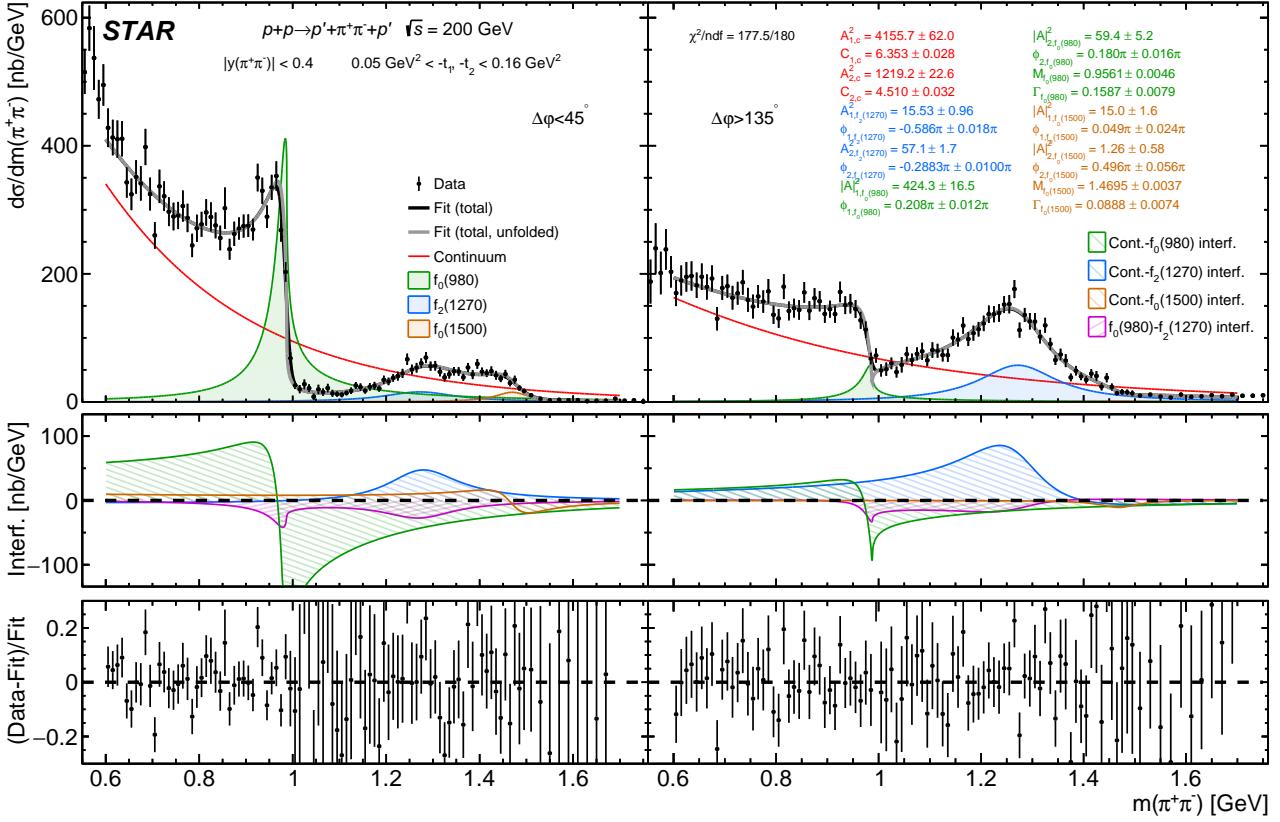


Figure 8.9: Differential cross-section $d\sigma/dm(\pi^+\pi^-)$ extrapolated from the fiducial region to the Lorentz invariant phase space given by the central state rapidity $|y(\pi^+\pi^-)| < 0.4$ and squared four-momentum transferred in forward proton vertices $0.05 \text{ GeV}^2 < -t_1, -t_2 < 0.16 \text{ GeV}^2$. Left and right parts of the figure show cross-sections for $\Delta\phi < 45^\circ$ and $\Delta\phi > 135^\circ$, respectively. The data are shown as black points with error bars representing statistical uncertainties. Result of the fit $\mathcal{F}(m)$ is drawn with solid black line. The squared amplitudes for continuum and resonance production are drawn with lines of different colors, as explained in the legend. The most significant interference terms are plotted in the middle panels, while the relative difference between each data point and fitted model is drawn in the bottom panel.

of the fit range is equal to 4 MeV and 13 MeV, respectively. The final form of function fitted to extrapolated $d\sigma/dm(\pi^+\pi^-)$ is given by

$$\mathcal{F}(m) = \int_{m-3.5 \cdot \sigma_{\text{res}}(m)}^{m+3.5 \cdot \sigma_{\text{res}}(m)} dm' \mathcal{N}(m' - m; \sigma_{\text{res}}(m')) |A(m')|^2. \quad (8.9)$$

The fitting is performed using Minuit2 toolkit [34] within the ROOT analysis software [35]. The standard-defined χ^2 is minimized simultaneously in two $\Delta\phi$ ranges with the masses and widths of both f_0 's forced to be equal, while phases and absolute values of f_2 and f_0 's amplitudes left independent in the two $\Delta\phi$ subsets. The mass and width of $f_2(1270)$ resonance is fixed to the well known Particle Data Group values [36]. Experimental systematic uncertainties of the model parameters are estimated through the independent fits to extrapolated $d\sigma/dm(\pi^+\pi^-)$ (Appendix G) with applied each of the systematic variations described in Sec. 7.4. In addition to this we take into consideration sensitivity of the fit result related to the modelling of extrapolation to full kinematic region. We check the effect of extrapolation to full solid angle in $\pi^+\pi^-$ rest frame assuming smooth transition from the angular distributions for pure S_0 wave up to 1 GeV, to the angular distributions for pure D_0 -wave starting from 1.2 GeV. We also check the effect of using extrapolation calculated with predictions from DiMe and GenEx generators, for both the central state and for the forward scattered protons. Also, we check the result of the fit with the ratio g_K/g_π varied within its uncertainties. At the end, systematic uncertainty on a parameter is calculated as a quadratic sum of the differences between the nominal fit result and the result of the fit to $d\sigma/dm(\pi^+\pi^-)$ with each systematic effect considered except differences related to the extrapolation which are separated from experimental uncertainties and quoted as the largest deviation from nominal result.

The extrapolated cross-sections are shown in Fig. 8.9 together with the result of the fit described above. The model parameters providing minimum χ^2 are listed in Tab. 8.2. The fit with the total of 20 free parameters

		unit	$\Delta\varphi < 45^\circ$	$\Delta\varphi > 135^\circ$
Continuum	A	$(\text{nb}/\text{GeV})^{\frac{1}{2}}$	$64.5 \pm 0.5 {}^{+4.0}_{-3.7} {}^{+0.8}_{-11.6}$	$34.9 \pm 0.3 {}^{+2.8}_{-2.6} {}^{+1.7}_{-8.6}$
	B	GeV^{-1}	$6.4 \pm 0.0 {}^{+0.1}_{-0.1} {}^{+0.1}_{-0.9}$	$4.5 \pm 0.0 {}^{+0.2}_{-0.2} {}^{+0.3}_{-1.1}$
$f_0(980)$	σ	nb	$37.2 \pm 1.3 {}^{+4.0}_{-3.4} {}^{+2.3}_{-3.8}$	$5.2 \pm 0.5 {}^{+0.5}_{-0.5} {}^{+0.2}_{-1.5}$
	ϕ	rad	$0.65 \pm 0.04 {}^{+0.02}_{-0.02} {}^{+0.02}_{-0.06}$	$0.57 \pm 0.05 {}^{+0.01}_{-0.01} {}^{+0.01}_{-0.09}$
	M	MeV		$956.1 \pm 4.6 {}^{+1.1}_{-0.9} {}^{+4.1}_{-5.3}$
	Γ_0	MeV		$158.7 \pm 7.9 {}^{+3.6}_{-3.8} {}^{+16.1}_{-19.1}$
$f_2(1270)$	σ	nb	$4.2 \pm 0.3 {}^{+0.5}_{-0.5} {}^{+0.3}_{-1.8}$	$15.6 \pm 0.5 {}^{+1.7}_{-1.5} {}^{+0.2}_{-4.5}$
	ϕ	rad	$-1.84 \pm 0.06 {}^{+0.01}_{-0.01} {}^{+0.04}_{-0.12}$	$-0.91 \pm 0.03 {}^{+0.03}_{-0.03} {}^{+0.06}_{-0.22}$
$f_0(1500)$	σ	nb	$2.1 \pm 0.3 {}^{+0.2}_{-0.2} {}^{+1.0}_{-0.6}$	$0.2 \pm 0.1 {}^{+0.0}_{-0.0} {}^{+0.1}_{-0.0}$
	ϕ	rad	$0.16 \pm 0.08 {}^{+0.03}_{-0.04} {}^{+0.03}_{-0.14}$	$1.56 \pm 0.18 {}^{+0.04}_{-0.05} {}^{+0.04}_{-0.08}$
	M	MeV		$1469.5 \pm 3.7 {}^{+1.0}_{-1.3} {}^{+2.0}_{-2.8}$
	Γ_0	MeV		$88.8 \pm 7.4 {}^{+2.1}_{-1.8} {}^{+3.5}_{-2.6}$

Table 8.2: Results of the fit described in the text in two ranges of azimuthal angle difference $\Delta\varphi$ between forward scattered protons. Statistical and systematic uncertainties are provided for each parameter.

gives $\chi^2/\text{ndf} = 178/180$ which shows that the data and the model are in excellent agreement in the fit region. Alternative extrapolation models show similar fit quality, although some parameters change significantly as can be noted from the model-related uncertainties in Tab. 8.2. The fitted model shows small deviation from the extrapolated data around 1.37 GeV. This might result from the presence of $f_0(1370)$, which is however not necessary to describe the data. The cross-section for $f_0(1500)$ production differs by 7 and 2 standard deviations from zero in $\Delta\varphi < 45^\circ$ and $\Delta\varphi > 135^\circ$ regions, respectively. Removing of $f_0(1500)$ (Fig. 8.11) makes χ^2/ndf change to 355/186, a 7.1 standard deviations effect. From the above we infer that the shape of $d\sigma/dm(\pi^+\pi^-)$ around 1.4-1.6 GeV - the high-mass part of the $f_2(1270)$ region, is determined by the presence of $f_0(1500)$ interfering mainly with $\pi^+\pi^-$ continuum.

Since the masses and widths of $f_0(980)$ and $f_0(1500)$ are free parameters it is allowed to confront their fitted values with the PDG data [36]. In the case of $f_0(980)$ the mass and width is found to be respectively $M_{f_0(980)} = 956 \pm 5(\text{stat.}) {}^{+1.1}_{-0.9}(\text{syst.}) {}^{+4}_{-5}(\text{mod.})$ MeV and $\Gamma_{0,f_0(980)} = 159 \pm 8(\text{stat.}) \pm 4(\text{syst.}) {}^{+16}_{-19}(\text{mod.})$ MeV. Such numbers differ from the PDG estimates of mass (990 ± 20 MeV) and width (from 10 MeV to 100 MeV), nonetheless PDG emphasizes strong dependence of the resonance parameters on the model of amplitude. Some measurements listed in Ref. [36] are in reasonable agreement with obtained numbers. In addition to this, mass and width of $f_0(980)$ resulting from the fit with the Breit-Wigner form of amplitude (Fig. 8.10) gives result $M_{f_0(980)} = 974 \pm 1(\text{stat.}) \pm 1(\text{syst.})$ MeV and $\Gamma_{0,f_0(980)} = 65 \pm 3(\text{stat.}) \pm 1(\text{syst.})$ MeV, albeit with notably worse χ^2/ndf of 225/180 being an evidence for significant branching fraction for the decay into $K\bar{K}$ which needs to be accounted in the resonance parametrization. These values are in excellent agreement with PDG estimates and $f_0(980)$ parameters from other measurements assuming Breit-Wigner resonance shape [36].

For $f_0(1500)$ we obtain from the fit $M_{f_0(1500)} = 1469 \pm 4(\text{stat.}) \pm 1(\text{syst.}) {}^{+2}_{-3}(\text{mod.})$ MeV and $\Gamma_{0,f_0(1500)} = 89 \pm 7(\text{stat.}) \pm 2(\text{syst.}) {}^{+4}_{-3}(\text{mod.})$ MeV. These numbers also deviate from the PDG averages: 1505 ± 6 MeV for the mass and 109 ± 7 MeV for the width. However, numerous measurements on $f_0(1500)$ referenced in PDG (and not used for averages calculation) report masses below 1500 MeV and widths below 100 MeV, which are consistent with our result.

We have tested a possibility of existence of an additional resonance produced in the mass range $1.2 - 1.5$ GeV (Fig. 8.12). With f_0 -like component added to the model from Eq. (8.1) the best fit is achieved for $M_{f_0} = 1367 \pm 25(\text{stat.})$ MeV and $\Gamma_{0,f_0} = 53 \pm 25(\text{stat.})$ MeV. In that case the χ^2/ndf is somewhat improved and equals 161/174 - the dip in $d\sigma/dm(\pi^+\pi^-)$ at 1.32 GeV for $\Delta\varphi < 45^\circ$ is better described compared to the nominal fit. Other parameters in the fit change slightly and remain compatible with their original values. Noteworthy is increase of the statistical uncertainty of $f_0(1500)$ width - $\Gamma_{0,f_0(1500)} = 93 \pm 30(\text{stat.})$ MeV, which makes it consistent with the PDG average. The fitted content of additional resonance f_0 at $\Delta\varphi < 45^\circ$ is several times lower than extracted yield of $f_0(1500)$, while for $\Delta\varphi > 135^\circ$ it is consistent with 0. The value of mass agrees with that of $f_0(1370)$ resonance, however the obtained width is much lower than PDG estimates of about 200-500 MeV.

We also calculated ratios of total cross sections $\sigma_{f_0(980)}/\sigma_{f_2(1270)}$ and $\sigma_{f_0(1500)}/\sigma_{f_2(1270)}$ in two $\Delta\varphi$ regions as

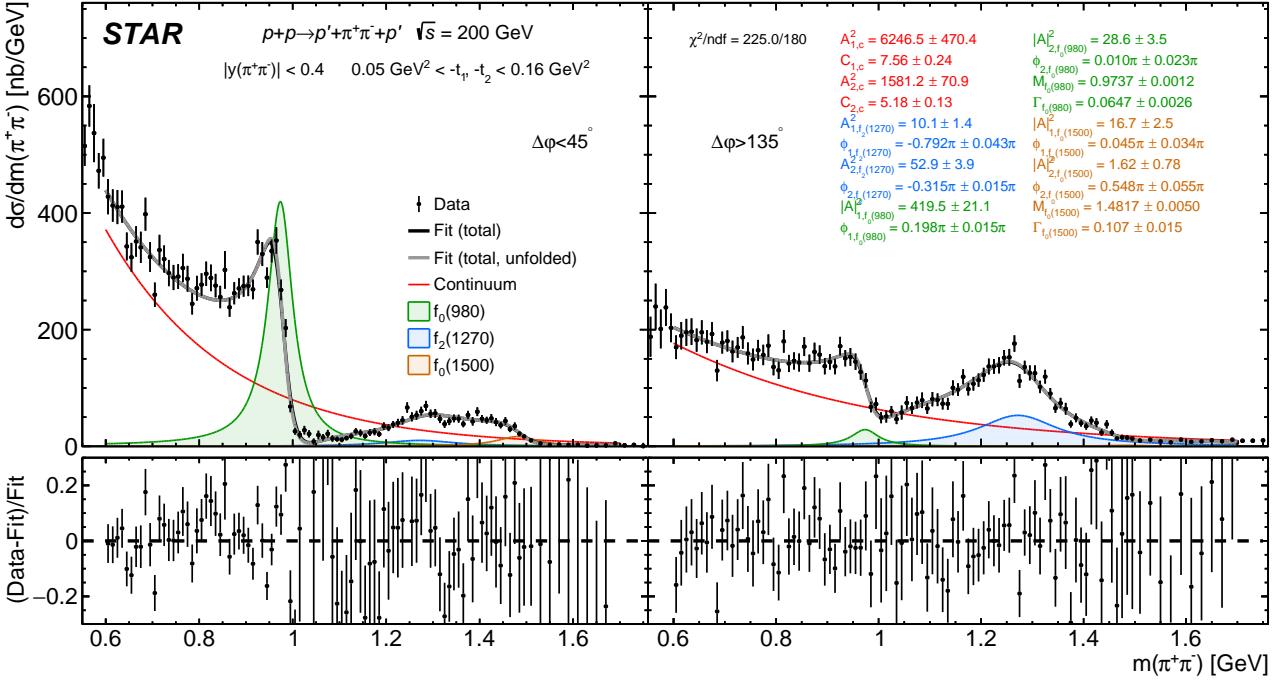


Figure 8.10: Extrapolated $d\sigma/dm(\pi^+\pi^-)$ with the fit assuming Breit-Wigner amplitude for $f_0(980)$.

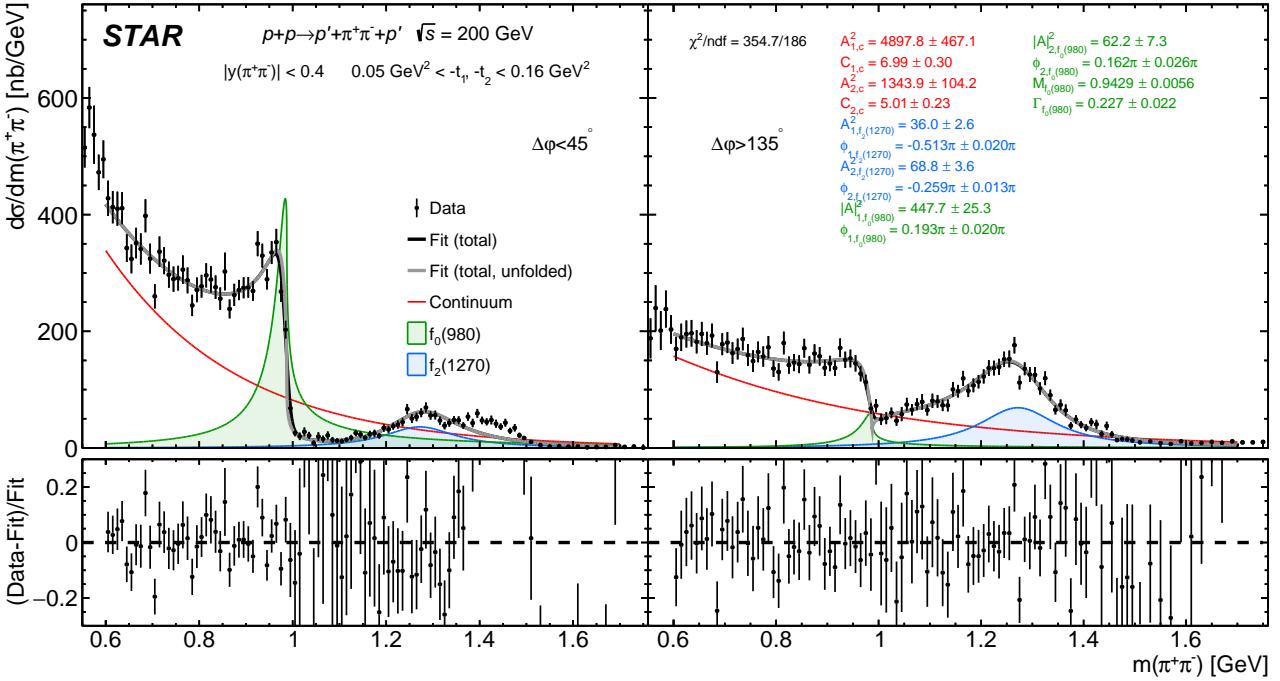


Figure 8.11: Extrapolated $d\sigma/dm(\pi^+\pi^-)$ with the fit ignoring $f_0(1500)$ component.

	$\frac{\sigma}{\sigma_{f_2(1270)}}$	$\frac{\sigma(\Delta\varphi < 45^\circ)}{\sigma(\Delta\varphi > 135^\circ)}$
$f_0(980)$	$8.77 \pm 0.62^{+0.58}_{-0.40} {}^{+7.16}_{-0.23}$	$0.33 \pm 0.03^{+0.01}_{-0.01} {}^{+0.13}_{-0.08}$
$f_2(1270)$	1	1
$f_0(1500)$	$0.49 \pm 0.08^{+0.04}_{-0.02} {}^{+0.25}_{-0.05}$	$0.01 \pm 0.01^{+0.00}_{-0.00} {}^{+0.00}_{-0.00}$
		$7.14 \pm 0.66^{+0.18}_{-0.18} {}^{+2.25}_{-0.21}$
		$0.27 \pm 0.02^{+0.01}_{-0.01} {}^{+0.02}_{-0.05}$
		$11.87 \pm 5.76^{+0.83}_{-0.67} {}^{+2.09}_{-3.40}$

Table 8.3: Ratios of integrated cross-sections on resonance production. For each ratio a statistical, systematic and model uncertainties are provided, in that order.

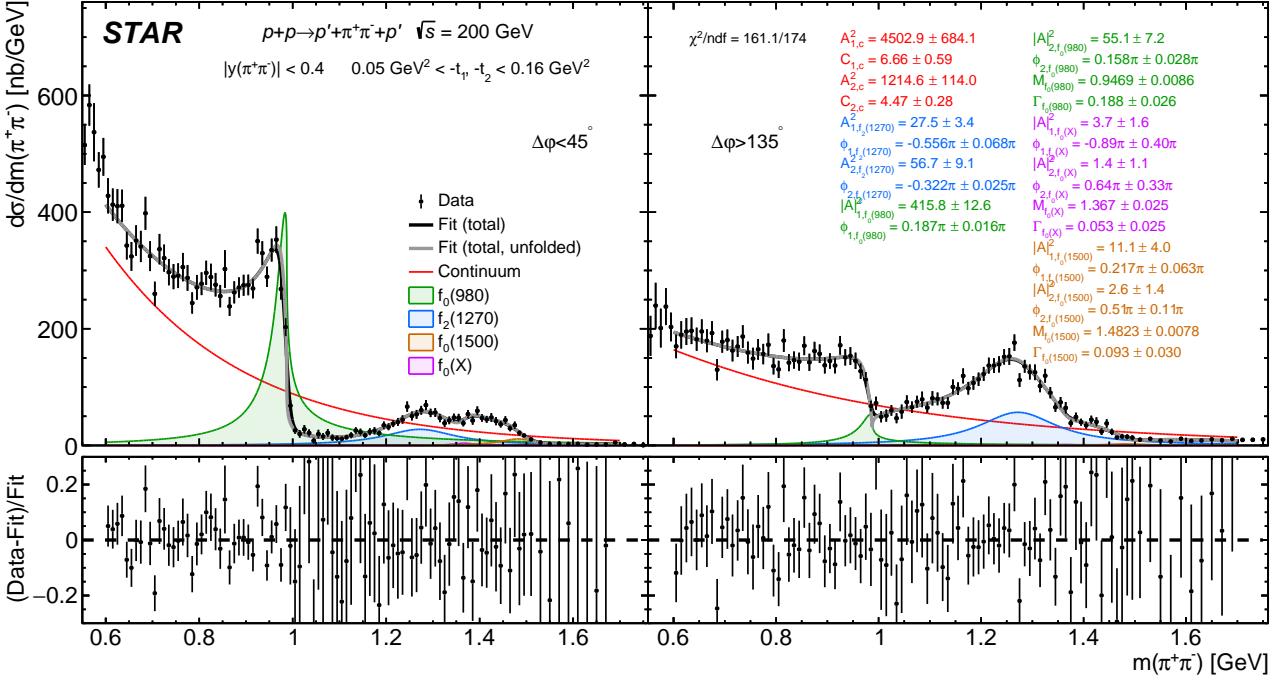


Figure 8.12: Extrapolated $d\sigma/dm(\pi^+\pi^-)$ with the fit accounting for an additional $f_0(X)$ component.

well as $\sigma(\Delta\varphi < 45^\circ)/\sigma(\Delta\varphi > 135^\circ)$ for all resonances, as listed in Tab. 8.3. In the ratios many of the systematic uncertainties cancelled out. We observe a significant dependence of the resonance production cross-sections on the azimuthal separation of the forward scattered protons. The two scalar mesons $f_0(980)$ and $f_0(1500)$ are dominantly produced at $\Delta\varphi < 45^\circ$, whereas the tensor meson $f_2(1270)$ at $\Delta\varphi > 135^\circ$. This $\Delta\varphi$ dependence is consistent with the observation made by WA102 Collaboration [37].

8.3 Extraction of exponential slope parameter of $d\sigma/dt$

Apart from the extrapolation and modelling of the $\pi^+\pi^-$ invariant mass cross-section we have also applied geometrical corrections to the $d\sigma/dt_1 dt_2$ in the same Lorentz invariant phase-space given by $|y(\pi^+\pi^-)| < 0.4$ and $0.05 \leq -t_1, -t_2 \leq 0.16 \text{ GeV}^2$ and two $\Delta\varphi$ ranges ($\Delta\varphi < 45^\circ$ and $\Delta\varphi > 135^\circ$). These cross-sections were fitted in two dimensions with the exponent $\propto \exp[\beta t_1] \cdot \exp[\beta t_2]$ separately in three selected ranges of $m(\pi^+\pi^-)$ (Figs. 8.13 and 8.14). Obtained β values are provided in Tab. 8.4. We do not separate modelling uncertainties since they are generally much smaller than experimental uncertainties. This is the consequence of uniform φ distribution in all the models and rather weak dependence of the cross-sections within measured $\Delta\varphi$ ranges. Such approximation is well founded and in good agreement with the data. Variations of the slope β with $m(\pi^+\pi^-)$ and $\Delta\varphi$ can give important constraints for model developers.

	$\Delta\varphi < 45^\circ$	$\Delta\varphi > 135^\circ$
0.6 GeV < $m < 1 \text{ GeV}$	$8.65 \pm 0.28^{+0.91}_{-0.69}$	$13.95 \pm 0.47^{+0.57}_{-0.95}$
1 GeV < $m < 1.5 \text{ GeV}$	$9.78 \pm 0.65^{+0.70}_{-0.74}$	$4.34 \pm 0.40^{+0.73}_{-0.77}$
$m > 1.5 \text{ GeV}$	$8.00 \pm 1.16^{+0.75}_{-0.79}$	$4.67 \pm 0.97^{+0.78}_{-0.84}$

Table 8.4: Slope β (in GeV^{-2}) of the $-t$ distribution in three ranges of $m(\pi^+\pi^-)$ and two two ranges of $\Delta\varphi$. For each number a statistical and systematic uncertainties are provided, in that order.

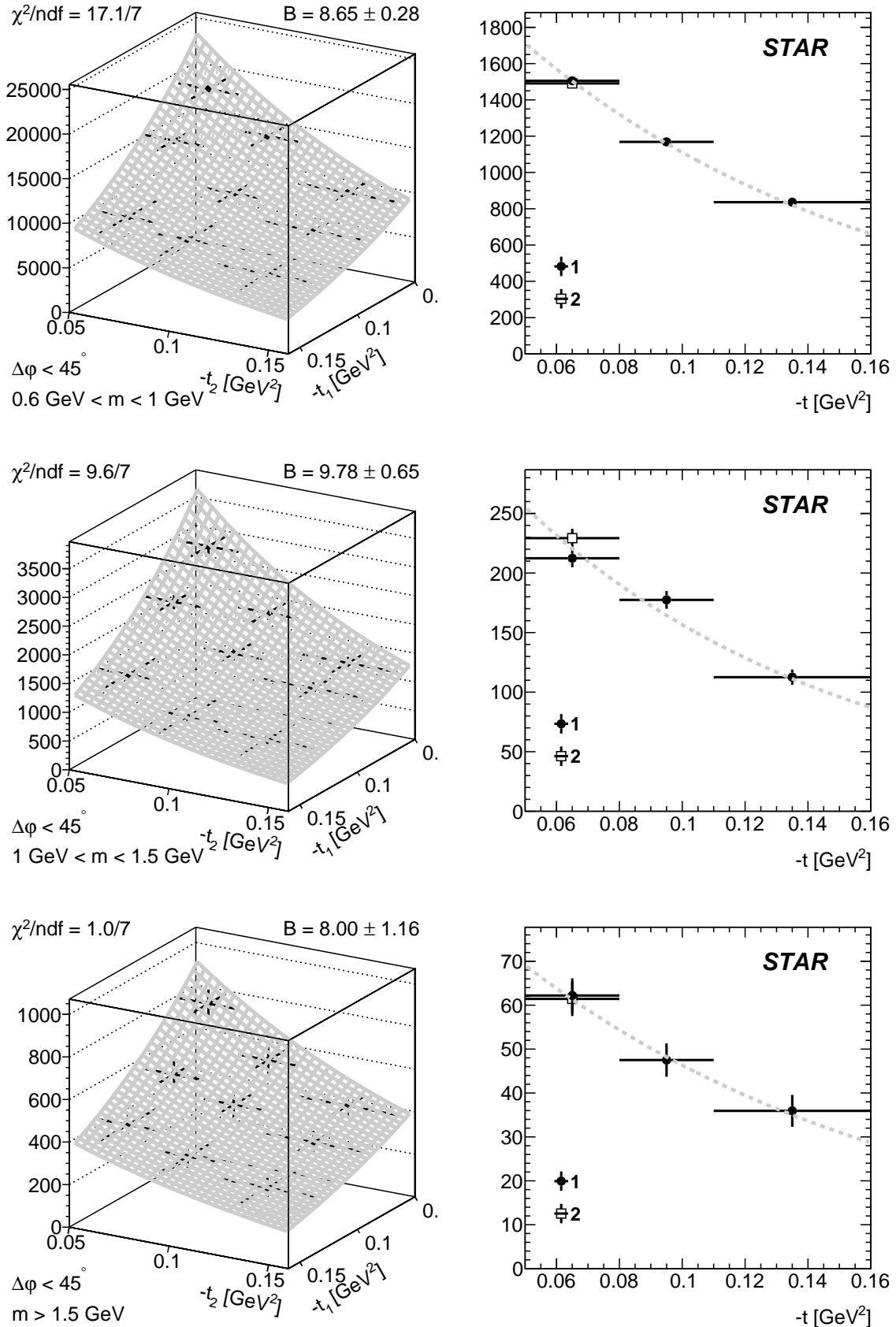


Figure 8.13: Extrapolated $d^2\sigma/dt_1 dt_2$ for $\Delta\varphi < 45^\circ$ with the exponential fit (left) and projections on the t_1 and t_2 axes (right) in three mass ranges provided in the plots.

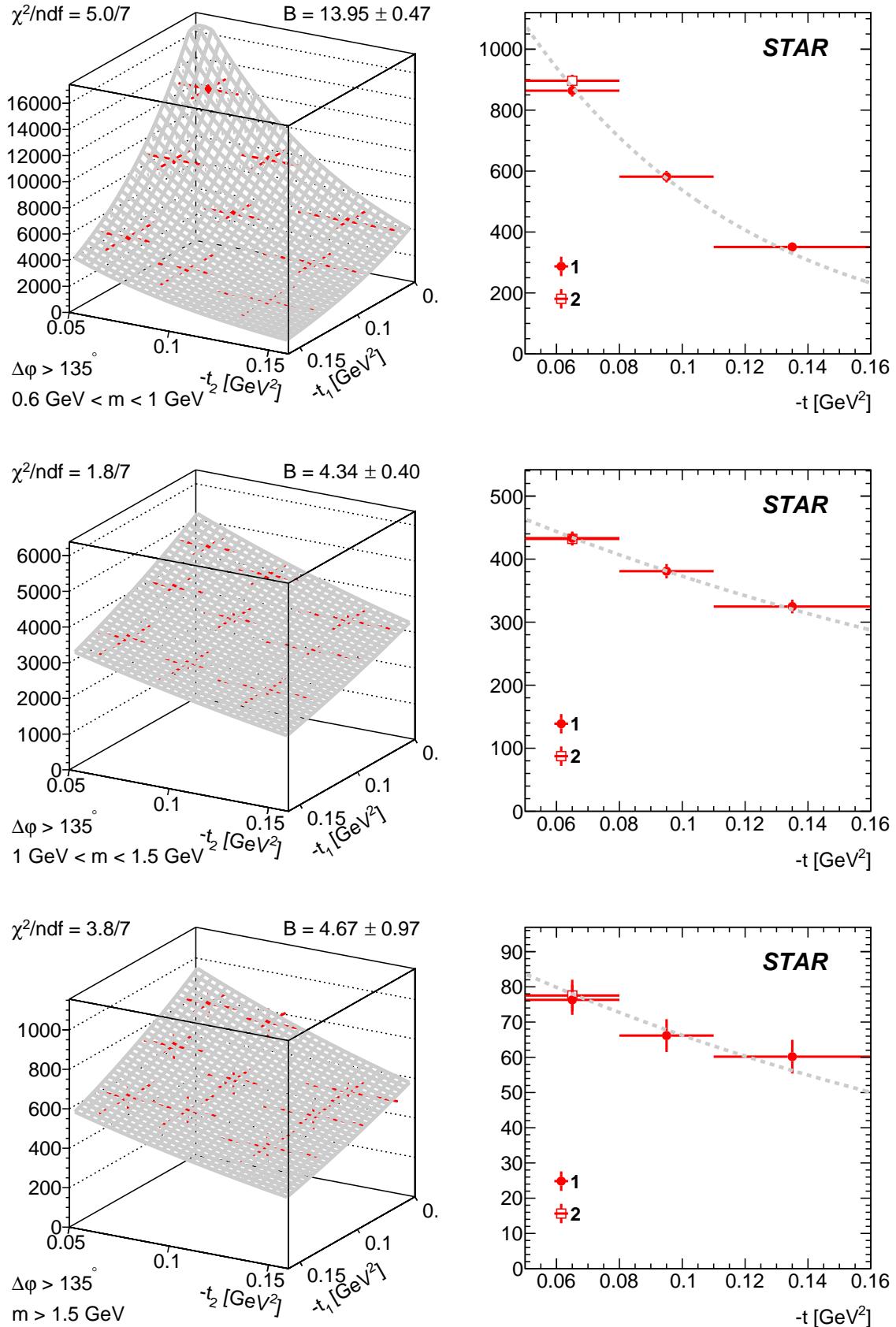


Figure 8.14: Extrapolated $d^2\sigma/dt_1 dt_2$ for $\Delta\varphi > 135^\circ$ with the exponential fit (left) and projections on the t_1 and t_2 axes (right) in three mass ranges provided in the plots.

A. Working points optimization for cuts C6, C7 and C9

The described study has been done at an early stage of analysis with some of cuts and the fiducial region defined differently from that finally established, therefore it has not been contained in the main part of this note. However, we consider it helpful to justify the cut thresholds in three significant cuts given in the title of this appendix. For aforementioned reason final numbers (for nominal fiducial region and nominal cuts) slightly differ from these presented in Fig. A.1, but the general picture remains unchanged.

We define significance, efficiency, and purity of the three cuts: C6, C7 and C9, according to equations shown below.

$$\text{Significance} = \frac{N_{\text{signal}}^{\text{cut}}}{\sqrt{N_{\text{signal}}^{\text{cut}} + N_{\text{bkgd}}^{\text{cut}}}}, \quad (\text{A.1}) \quad \text{Efficiency} = \frac{N_{\text{signal}}^{\text{cut}}}{N_{\text{signal}}^{\text{no cut}}}, \quad (\text{A.2}) \quad \text{Purity} = \frac{N_{\text{signal}}^{\text{cut}}}{N_{\text{signal}}^{\text{cut}} + N_{\text{bkgd}}^{\text{cut}}}, \quad (\text{A.3})$$

In these equations $N_{\text{signal}}^{\text{cut}}$ is number of signal events in finally selected CEP $\pi^+\pi^-$ events, $N_{\text{bkgd}}^{\text{cut}}$ is number of

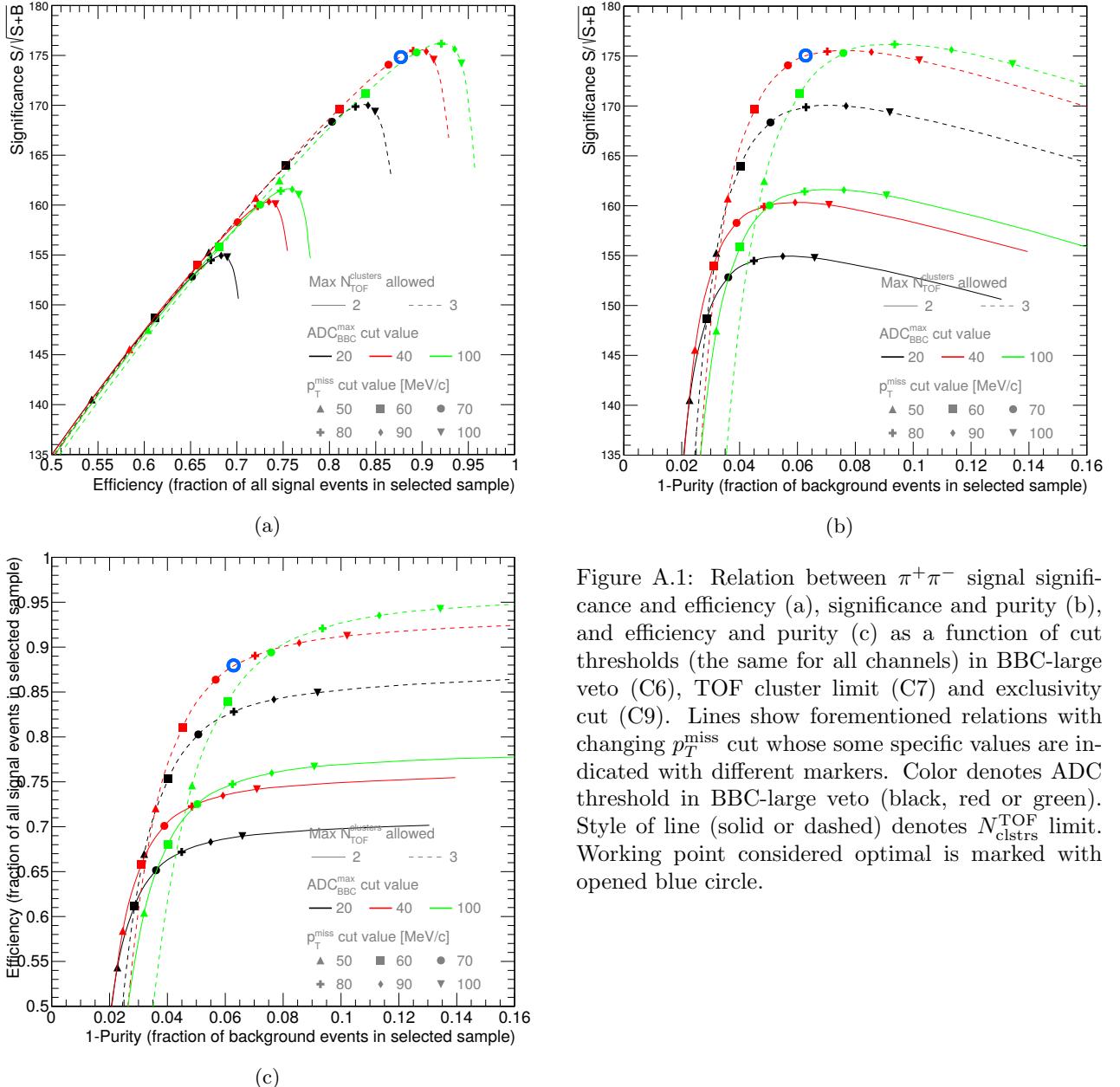


Figure A.1: Relation between $\pi^+\pi^-$ signal significance and efficiency (a), significance and purity (b), and efficiency and purity (c) as a function of cut thresholds (the same for all channels) in BBC-large veto (C6), TOF cluster limit (C7) and exclusivity cut (C9). Lines show forementioned relations with changing p_T^{miss} cut whose some specific values are indicated with different markers. Color denotes ADC threshold in BBC-large veto (black, red or green). Style of line (solid or dashed) denotes $N_{\text{clstrs}}^{\text{TOF}}$ limit. Working point considered optimal is marked with opened blue circle.

non-exclusive background events in selected sample, and $N_{\text{signal}}^{\text{no cut}}$ is number of signal events in sample after all cuts except the three studied cuts. These numbers were estimated using method described in Sec. 5.2.1.

Relations between defined quantities are shown in Fig. A.1. The first important observation was that allowing 3 TOF clusters instead of 2 (at fixed cuts C6 and C9) gives increase to selection efficiency by about 0.2, with only 0.01-0.02 decrease of the purity. We therefore decided to use condition $N_{\text{clstrs}}^{\text{TOF}} \leq 3$ in cut C7.

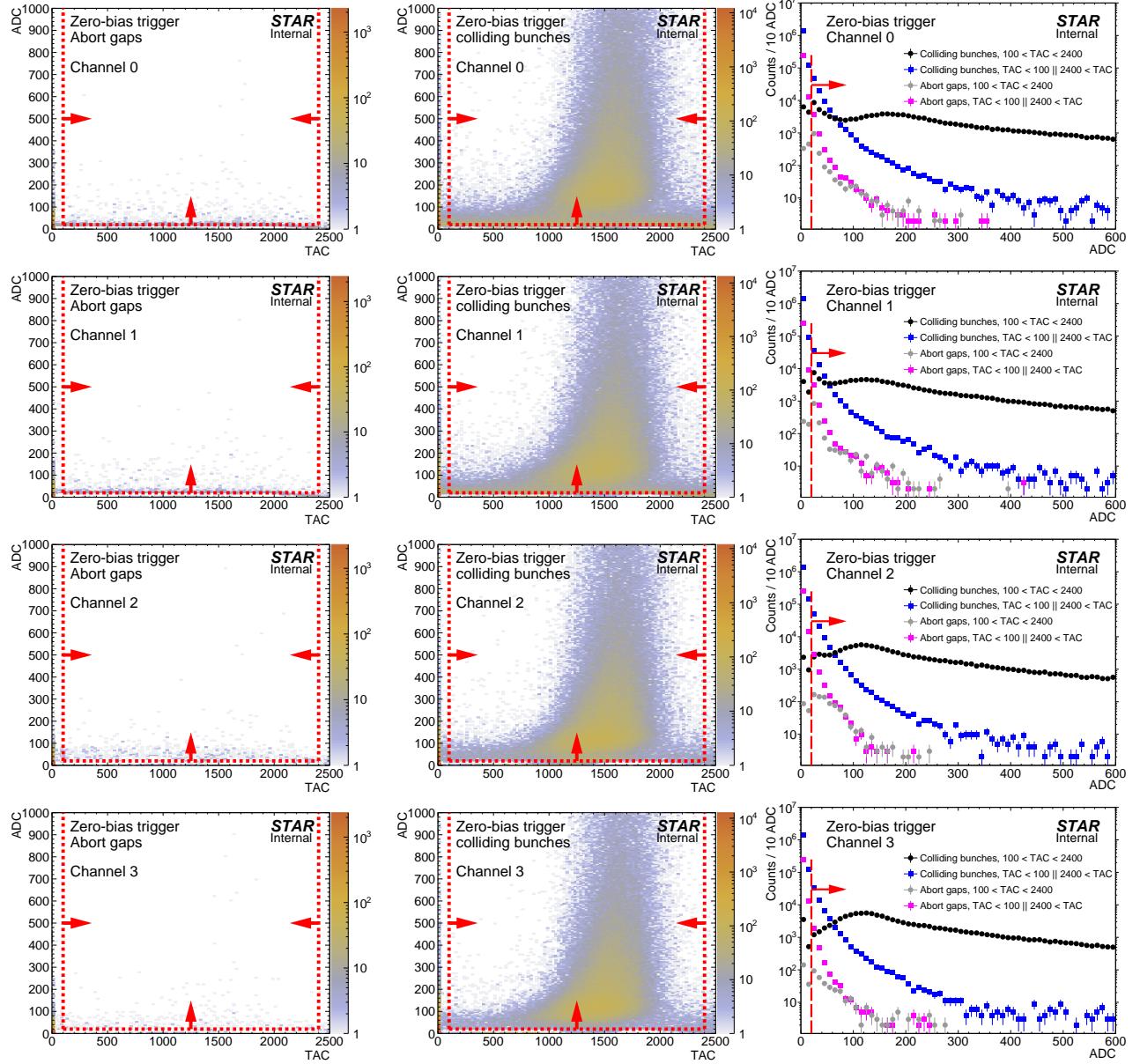
In the next step the value of maximum p_T^{miss} was found. From Fig A.1 one can read that with $N_{\text{clstrs}}^{\text{TOF}} \leq 3$ (dashed lines) the best balance between efficiency and purity is found for p_T^{miss} cut value ranging between 60 MeV (rectangle) and 80 MeV (cross). We considered optimal threshold value of total transverse momentum p_T^{miss} at 75 MeV which corresponds to 2.5σ , as elaborated in section devoted to exclusivity cut (C9, Sec. 4.2.8).

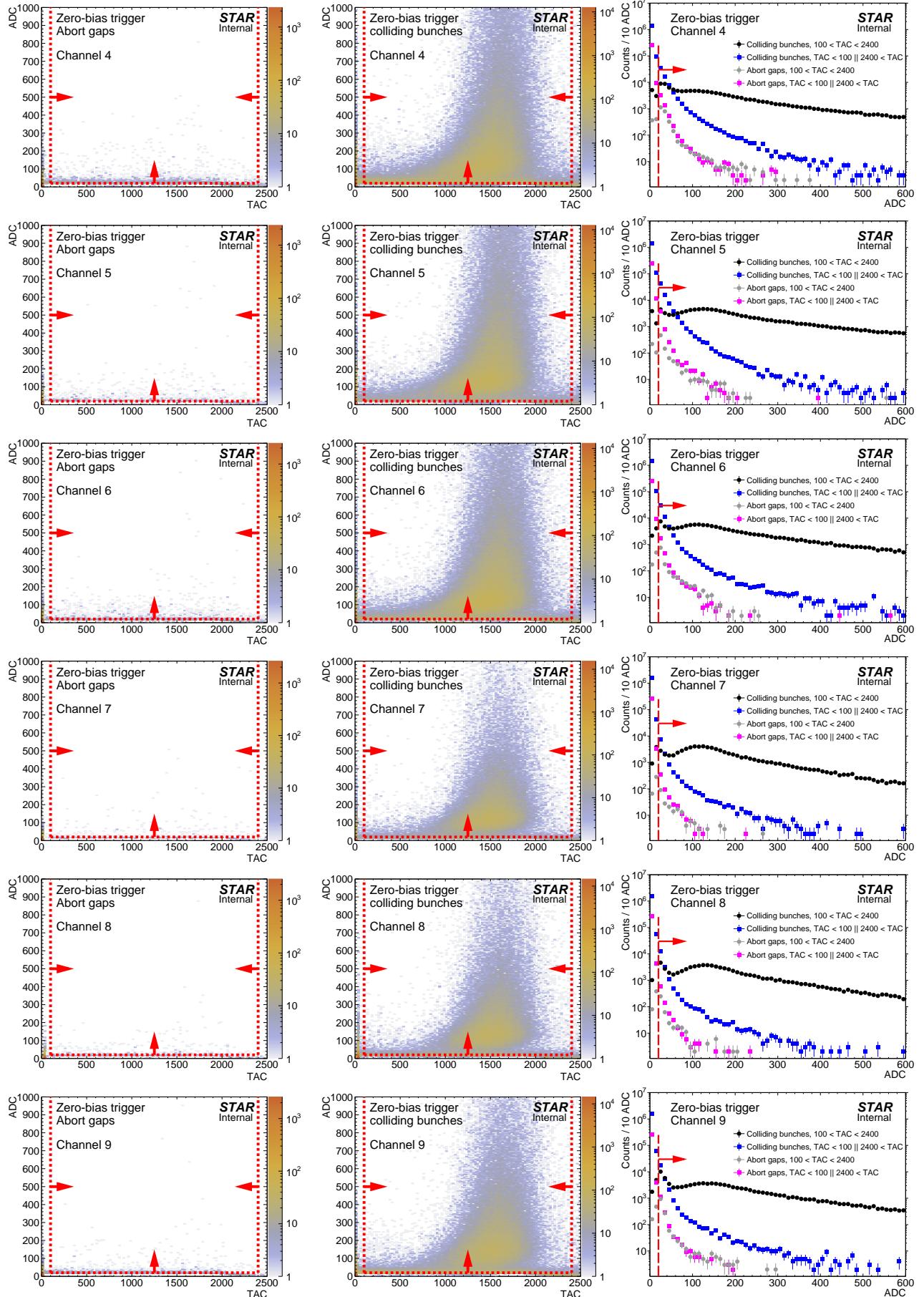
With fixed maximum number of TOF clusters and maximum p_T^{miss} the maximum ADC in BBC-large was established. Similarly to previous paragraph, the best balance between efficiency and purity was found for ADC threshold of 40.

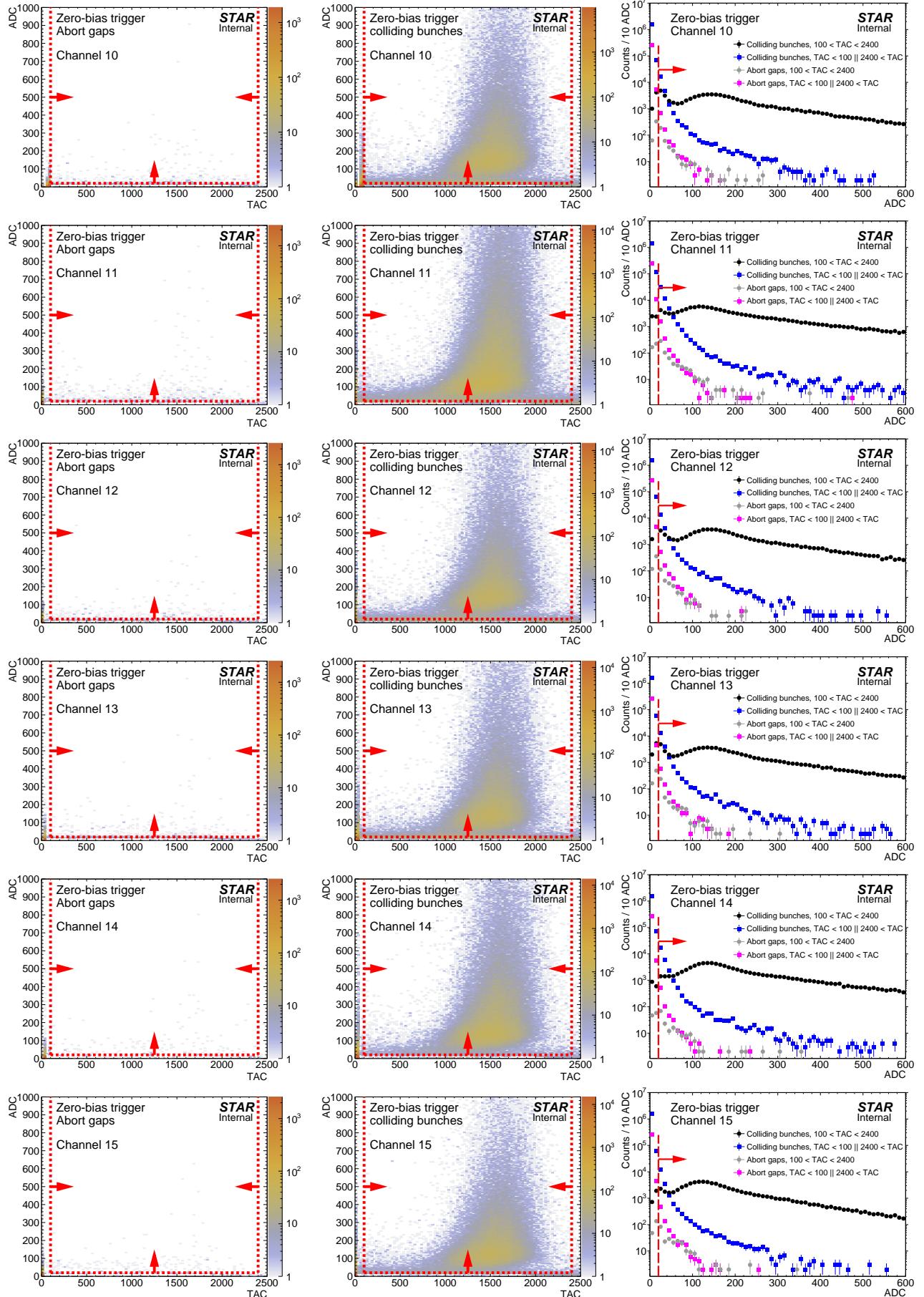
Certainly, not only factors considered here should be studied to find optimum working point, also e.g. size of systematic uncertainties for each cut value should be checked. Nonetheless, systematics related to these cuts are minor comparing to leading systematic uncertainties, therefore it was safe to omit it.

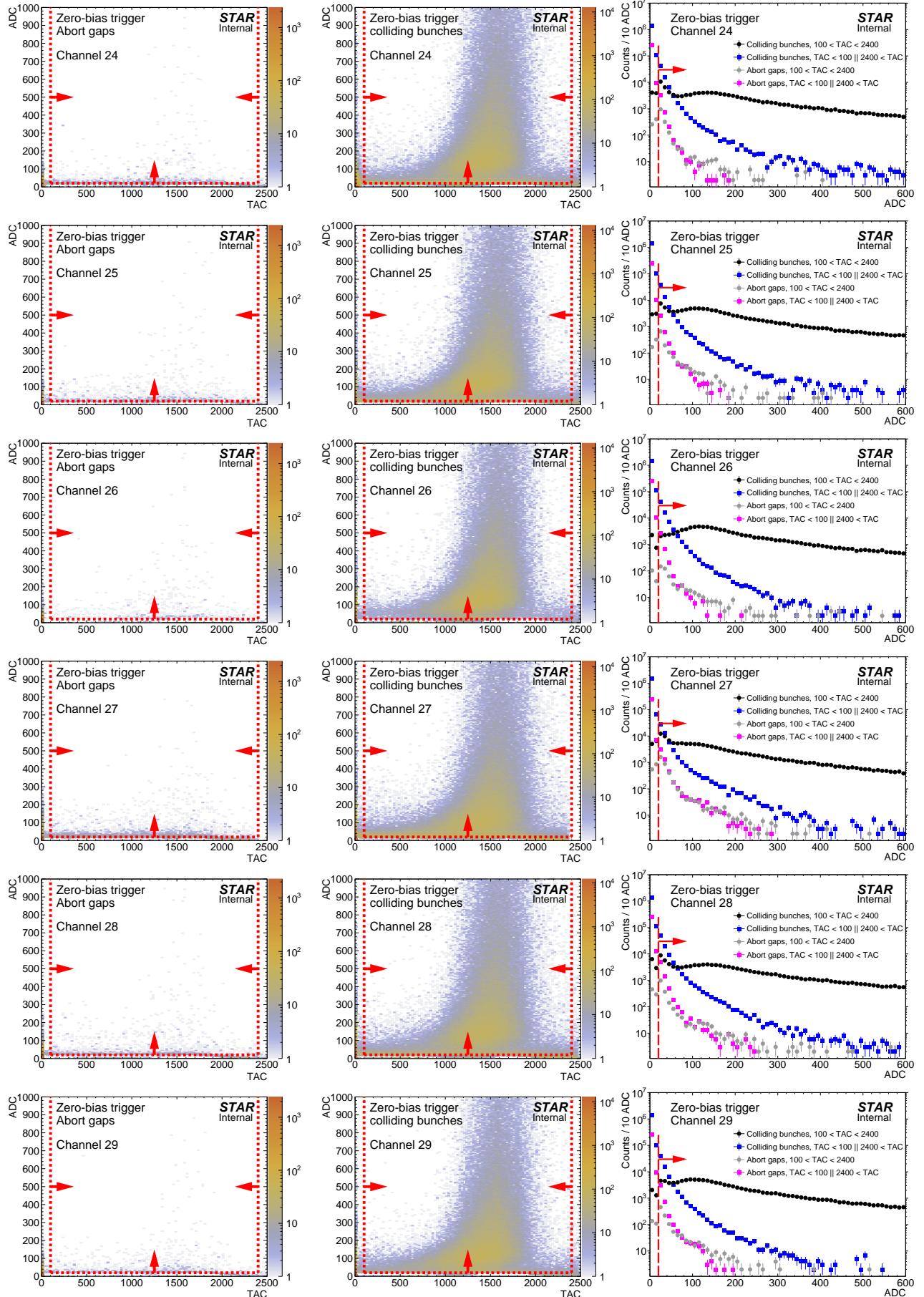
B. BBC response

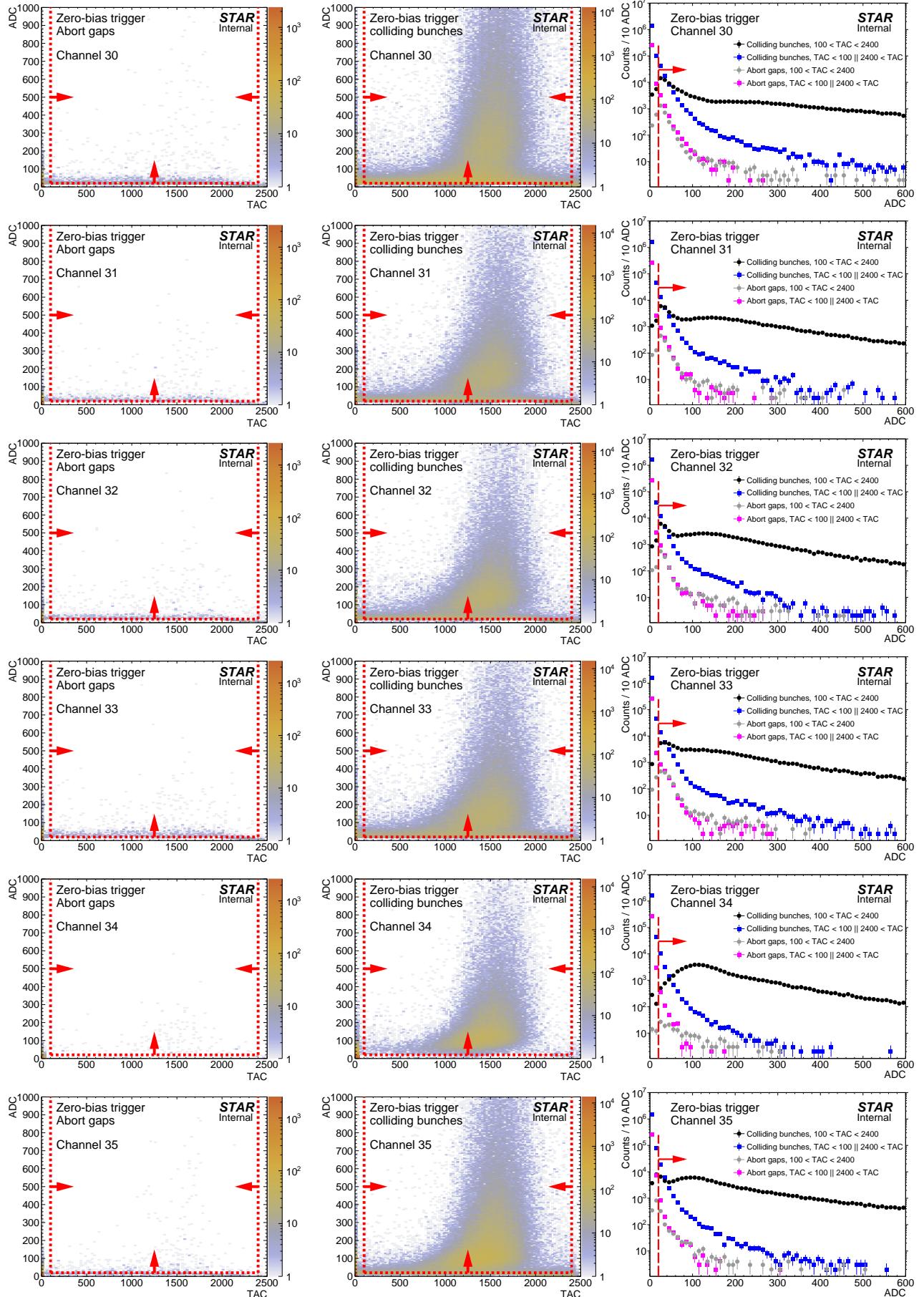
Figure B.1: Two-dimensional distribution of ADC vs. TAC counts per BBC-small channel in abort gaps (left) and colliding bunches (middle), and one-dimensional projection on x -axis (ADC) for selected ranges of TAC for colliding bunches and abort gaps (right). Each row represents single channel (small BBC tile). Red lines and arrows indicate thresholds for a signal in given channel.











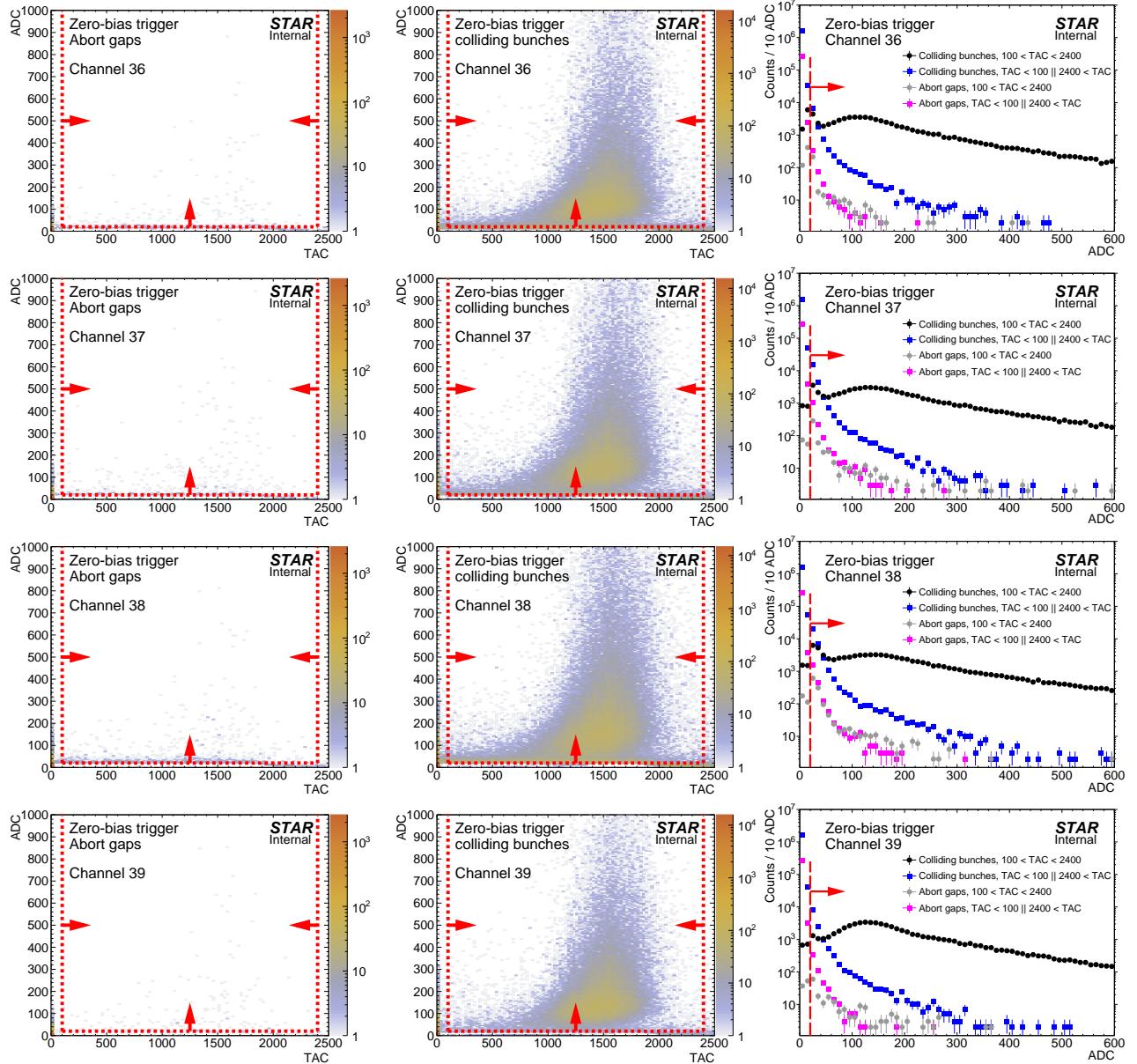
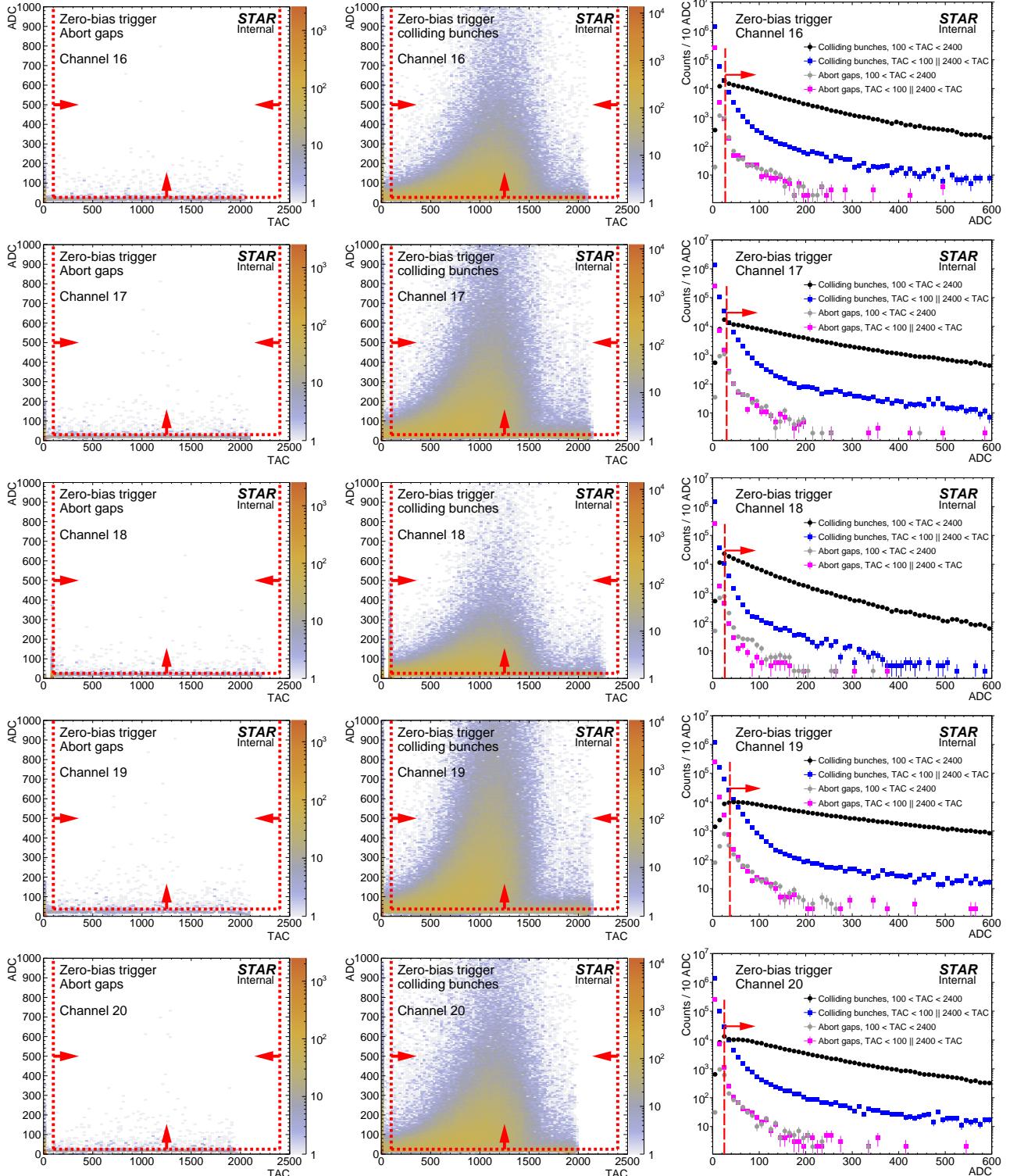
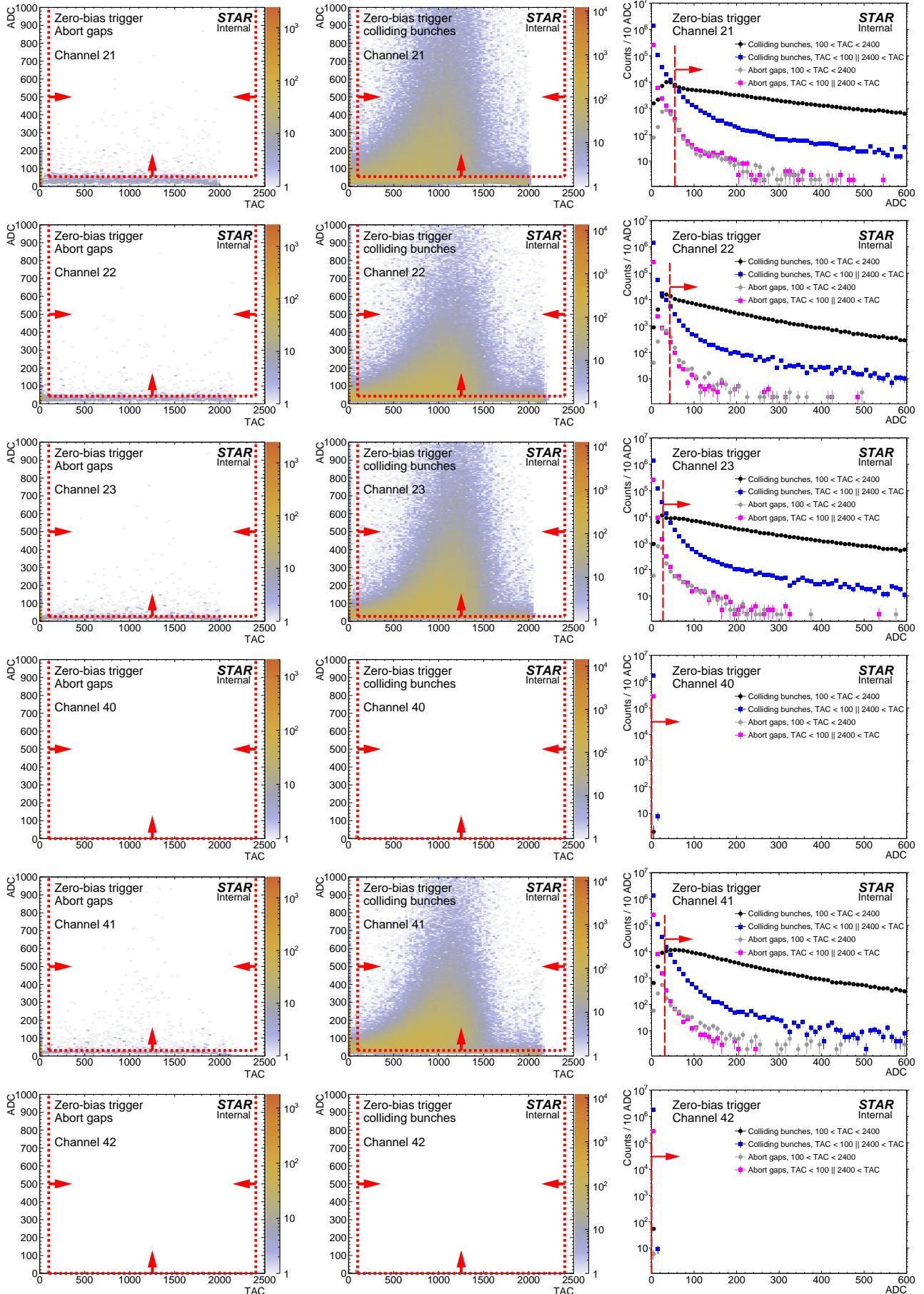
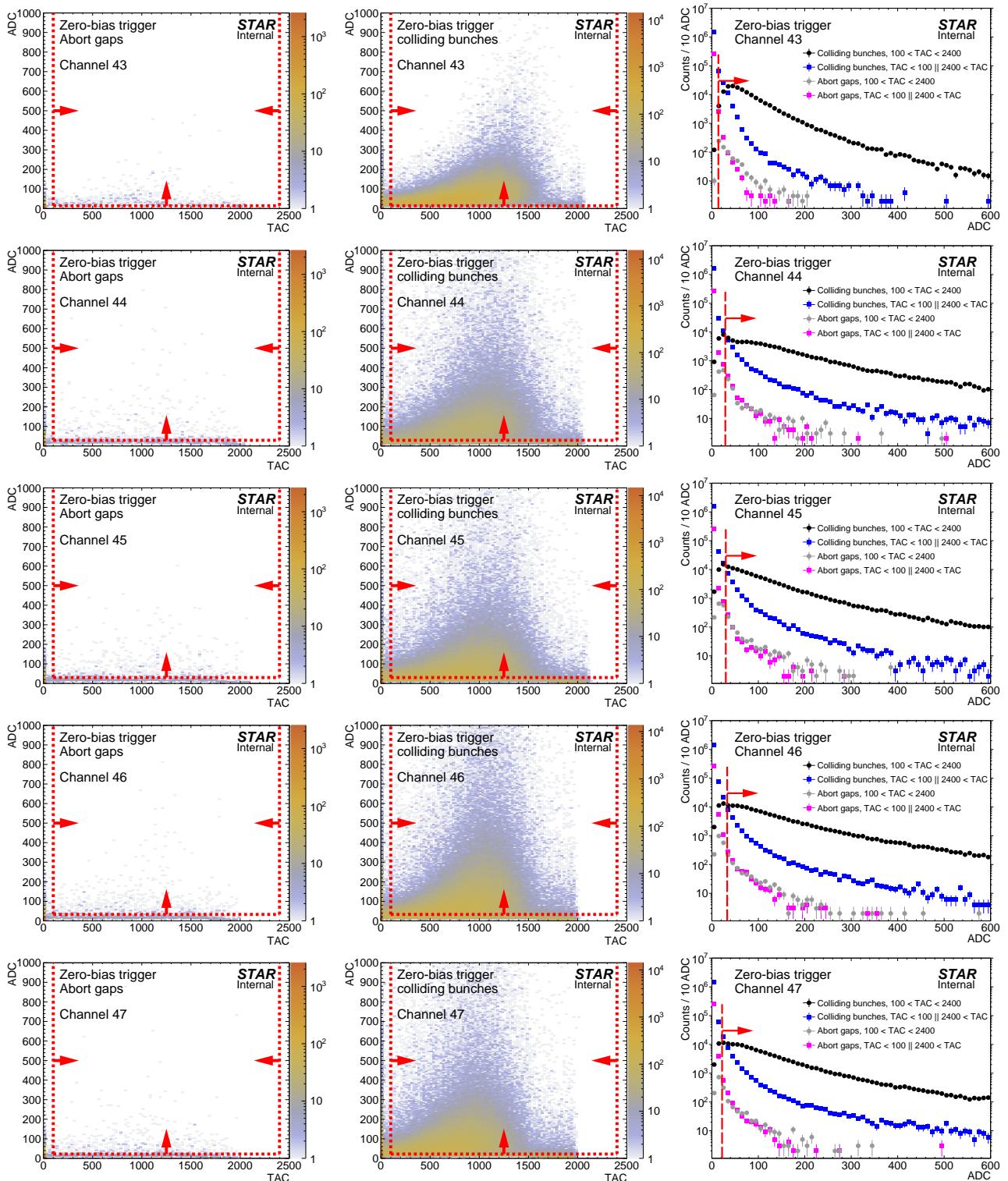


Figure B.2: Two-dimensional distribution of ADC vs. TAC counts per BBC-large channel in abort gaps (left) and colliding bunches (middle), and one-dimensional projection on x -axis (ADC) for selected ranges of TAC for colliding bunches and abort gaps (right). Each row represents single channel (large BBC tile). Red lines and arrows indicate thresholds for a signal in given channel.







C. Reconstruction of m_{TOF}^2

Definitions:

- t_0 - time of the primary pp interaction
- $t_{1,2}$ - time of detection of the hit in TOF by particle 1(2)
- $L_{1,2}$ - helical path of the particle 1(2) from the interaction vertex to the TOF cell with reconstructed hit,
- $p_{1,2}$ - magnitude of momentum of particle 1(2),
- $m_{1,2}$ - mass of particle 1(2),

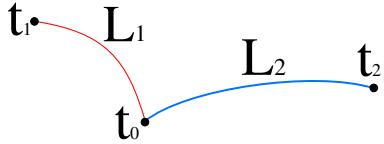


Figure C.1: Scheme of two central tracks of lengths L_1 and L_2 , produced in common vertex in moment t_0 , hitting cells in TOF detector in moments t_1 and t_2 .

From the simple algebra below which describes relation between track lengths, momenta and times of hit detection one can derive formula for the squared mass of two particles, assuming that their masses are equal (particles are of the same type).

Below we assume $c = 1$. We can write a set of two equations connecting the time that it takes for each particle to reach the TOF, starting from the interaction vertex:

$$\begin{cases} t_1 - t_0 = L_1 \sqrt{1 + \frac{m_1^2}{p_1^2}}, \\ t_2 - t_0 = L_2 \sqrt{1 + \frac{m_2^2}{p_2^2}}. \end{cases} \quad (\text{C.1})$$

By adding the two equations above we get

$$\Delta t = t_1 - t_2 = L_1 \sqrt{1 + \frac{m_1^2}{p_1^2}} - L_2 \sqrt{1 + \frac{m_2^2}{p_2^2}}. \quad (\text{C.2})$$

In CEP of two opposite-sign particles always the same species of particles are produced, therefore

$$m_1 = m_2 = m. \quad (\text{C.3})$$

If we substitute m_1 and m_2 with m in Eq. (C.2) and transform the equation to remove the square roots we get a quadratic equation of the form

$$\mathcal{A} \times (m_{\text{TOF}}^2)^2 + \mathcal{B} \times m_{\text{TOF}}^2 + \mathcal{C} = 0. \quad (\text{C.4})$$

Parameters of the Eq. (C.4) are given below:

$$\mathcal{A} = -2 \frac{L_1^2 L_2^2}{p_1^2 p_2^2} + \frac{L_1^4}{p_1^4} + \frac{L_2^4}{p_2^4}, \quad (\text{C.5})$$

$$\mathcal{B} = -2 L_1^2 L_2^2 \left(\frac{1}{p_1^2} + \frac{1}{p_2^2} \right) + \frac{2 L_1^4}{p_1^2} + \frac{2 L_2^4}{p_2^2} - 2 (\Delta t)^2 \left(\frac{L_1^2}{p_1^2} + \frac{L_2^2}{p_2^2} \right), \quad (\text{C.6})$$

$$\mathcal{C} = (\Delta t)^4 - 2 (\Delta t)^2 (L_1^2 + L_2^2) + L_1^4 + L_2^4 - 2 L_1^2 L_2^2, \quad (\text{C.7})$$

together with the final formula for a physical root of the quadratic equation which is used in the m_{TOF}^2 reconstruction:

$$m_{\text{TOF}}^2 = \frac{-\mathcal{B} + \sqrt{\mathcal{B}^2 - 4\mathcal{A}\mathcal{C}}}{2\mathcal{A}}. \quad (\text{C.8})$$

D. Particle identification efficiency

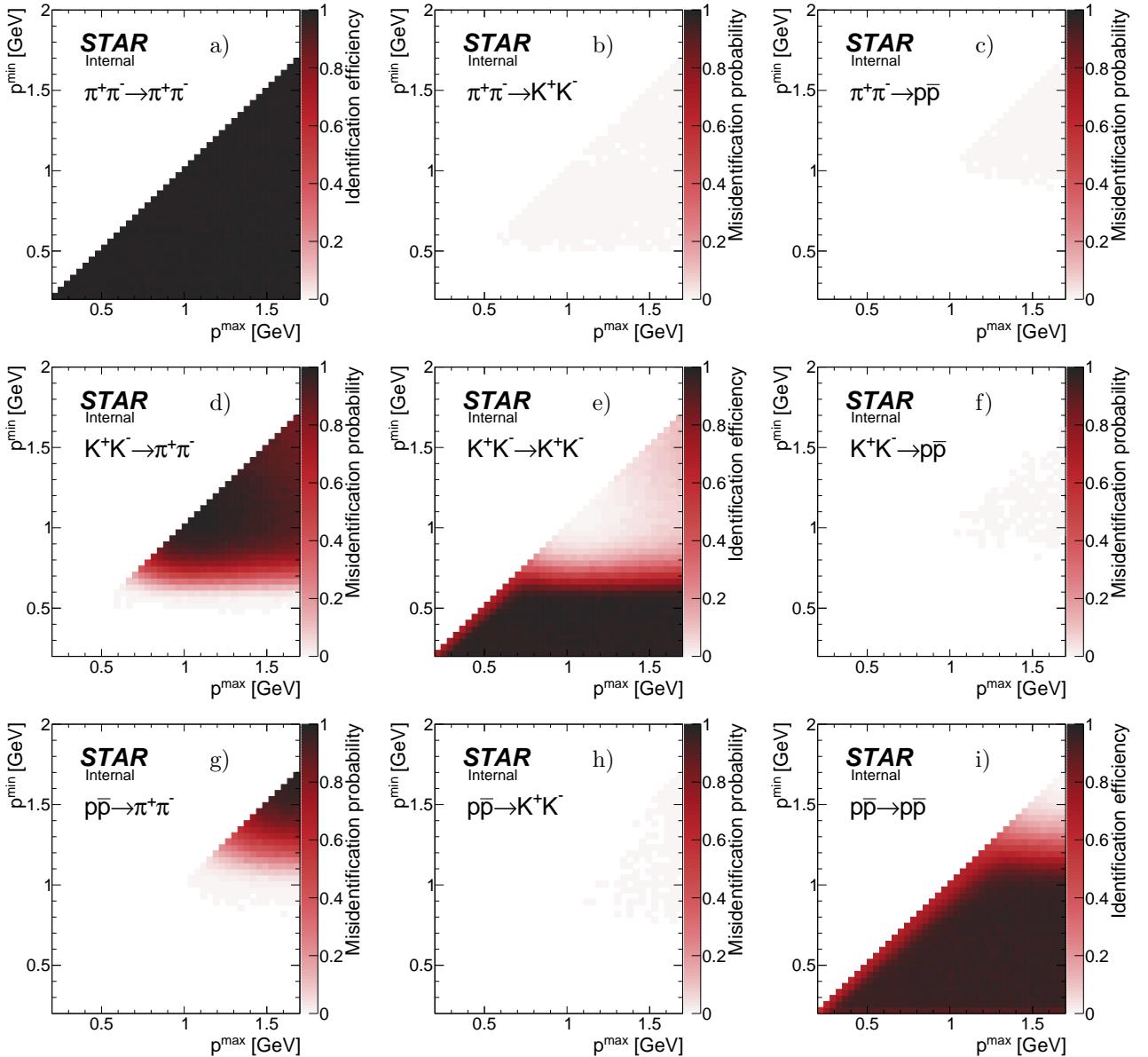


Figure D.1: Pair identification efficiency (diagonal) and misidentification probability (off-diagonal) as a function of tracks' momentum (higher, x -axis, and lower, y -axis) for $\pi^+\pi^-$, K^+K^- and $p\bar{p}$ pairs. The results were obtained from the dedicated MC simulation described in Sec. 6.2.2.6.

E. Formulation of total RP efficiency

Definitions:

- RP^E - single good quality track (satisfying cuts C4.1-C4.2) on the east side,
- RP^W - single good quality track (satisfying cuts C4.1-C4.2) on the west side,
- TR^E - trigger signal in the RP branch with single good track on the east side,
- $TR^{\neq E}$ - trigger signal in the RP branch other than branch with single good track on the east side,
- TR^W - trigger signal in the RP branch with single good track on the west side,
- $TR^{\neq W}$ - trigger signal in the RP branch other than branch with single good track on the west side,
- Veto - trigger veto on the simultaneous trigger signal in Up and Down RPs (ET&IT),
- $Veto^{PU}$ - trigger veto on ET&IT (Veto) due to pile-up interactions,
- $Veto^{DM}$ - trigger veto on ET&IT (Veto) due to forward proton interaction with dead material.

The total efficiency related to both east and west forward protons in CEP event has the following form:

$$\mathcal{E}(RP^E \wedge RP^W \wedge TR^E \wedge TR^W \wedge !Veto) = \mathcal{E}(RP^E \wedge RP^W | TR^E \wedge TR^W \wedge !Veto) \times \mathcal{E}(TR^E \wedge TR^W \wedge !Veto), \quad (E.1)$$

where the r.h.s. part of the equation is factorized using the rules of conditional probability to two components describing reconstruction and selection efficiency (first) and trigger efficiency (second).

The reconstruction and selection efficiency part can be represented as a product of single-proton reconstruction and selection efficiencies described in Sec. 6.2.3 with an additional component that accounts for the correlation between east and west efficiencies. This correlation is defined in Eq. (E.2):

$$\rho_{EW} = \frac{\mathcal{E}_{EW} - \mathcal{E}_E \times \mathcal{E}_W}{\sqrt{\mathcal{E}_E \times (1 - \mathcal{E}_E) \times \mathcal{E}_W \times (1 - \mathcal{E}_W)}}, \quad (E.2)$$

where

$$\begin{aligned} \mathcal{E}_E &= \mathcal{E}(RP^E | TR^E \wedge !TR^{\neq E}), & \mathcal{E}_W &= \mathcal{E}(RP^W | TR^W \wedge !TR^{\neq W}), \\ \mathcal{E}_{EW} &= \mathcal{E}(RP^E \wedge RP^W | TR^E \wedge TR^W \wedge !Veto). \end{aligned}$$

From that we get

$$\mathcal{E}(RP^E \wedge RP^W | TR^E \wedge TR^W \wedge !Veto) = \mathcal{E}_E \times \mathcal{E}_W + \rho_{EW} \times \sqrt{\mathcal{E}_E \times (1 - \mathcal{E}_E) \times \mathcal{E}_W \times (1 - \mathcal{E}_W)}. \quad (E.3)$$

The correlation coefficient ρ_{EW} governs information about simultaneous unsuccessful reconstruction/selection of RP track on the east and west side in the same event. This can be a result of e.g. a pile-up interaction, typically of elastic proton-proton scattering, producing additional tracks/showers simultaneously in east and west RPs and thus introducing simultaneous east and west RP inefficiency. Also, some corruption of the data stream might lead to unsuccessful reconstruction of the entire event. With the above correlation taken into account we are able to properly reconstruct the yield of true-level events and shape of distributions from the measured events, as shown in the closure test in Sec. 6.6.2.2.

In the component of RP efficiency related to the trigger we can use again the conditional probability and factorize it to part connected with the trigger veto (first) and the efficiency of detecting a signal of both forward protons by the trigger system (second):

$$\mathcal{E}(TR^E \wedge TR^W \wedge !Veto) = \mathcal{E}(!Veto | TR^E \wedge TR^W) \times \mathcal{E}(TR^E \wedge TR^W). \quad (E.4)$$

Efficiency of the triggering $\mathcal{E}(TR^E \wedge TR^W)$ is much above 99% (see the Ref. [1]). Efficiency of the (lack of) veto if forward protons are triggering in east and west RPs can be decomposed to efficiency of the veto induced by the pile-up interaction in the same bunch crossing ($Veto^{PU}$) and efficiency of the veto induced by the interaction of the CEP protons with the material of the accelerator and detectors ($Veto^{DM}$):

$$\begin{aligned} \mathcal{E}(!Veto | TR^E \wedge TR^W) &= \left| Veto = Veto^{PU} \vee Veto^{DM} \right| = \mathcal{E}(!Veto^{PU} \wedge !Veto^{DM} | TR^E \wedge TR^W) = \\ &= \mathcal{E}(!Veto^{DM} | !Veto^{PU} \wedge TR^E \wedge TR^W) \times \mathcal{E}(!Veto^{PU} | TR^E \wedge TR^W). \end{aligned} \quad (E.5)$$

The first term of the last part of Eq. (E.5) described in Sec. 6.2.1.3 can be safely factorized as the probability of veto induced by the primary CEP proton on the east side is totally independent from the similar probability on the west side:

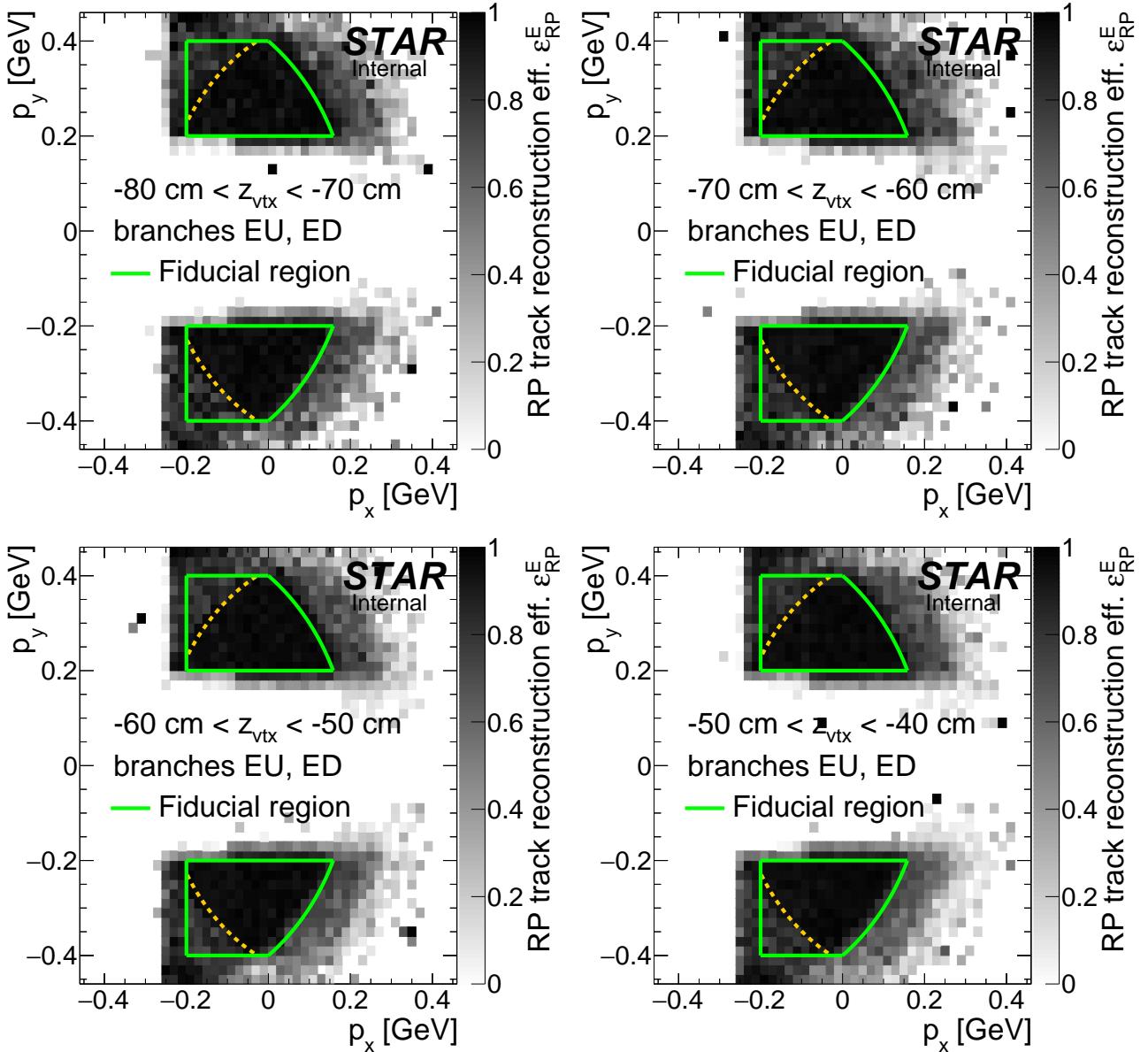
$$\begin{aligned} \mathcal{E} (!\text{Veto}^{\text{DM}} | !\text{Veto}^{\text{PU}} \wedge \text{TR}^{\text{E}} \wedge \text{TR}^{\text{W}}) &= \\ &= \mathcal{E}^{\text{E}} (!\text{Veto}^{\text{DM}} | !\text{Veto}^{\text{PU}} \wedge \text{TR}^{\text{E}} \wedge \text{TR}^{\text{W}}) \times \mathcal{E}^{\text{W}} (!\text{Veto}^{\text{DM}} | !\text{Veto}^{\text{PU}} \wedge \text{TR}^{\text{E}} \wedge \text{TR}^{\text{W}}) \end{aligned} \quad (\text{E.6})$$

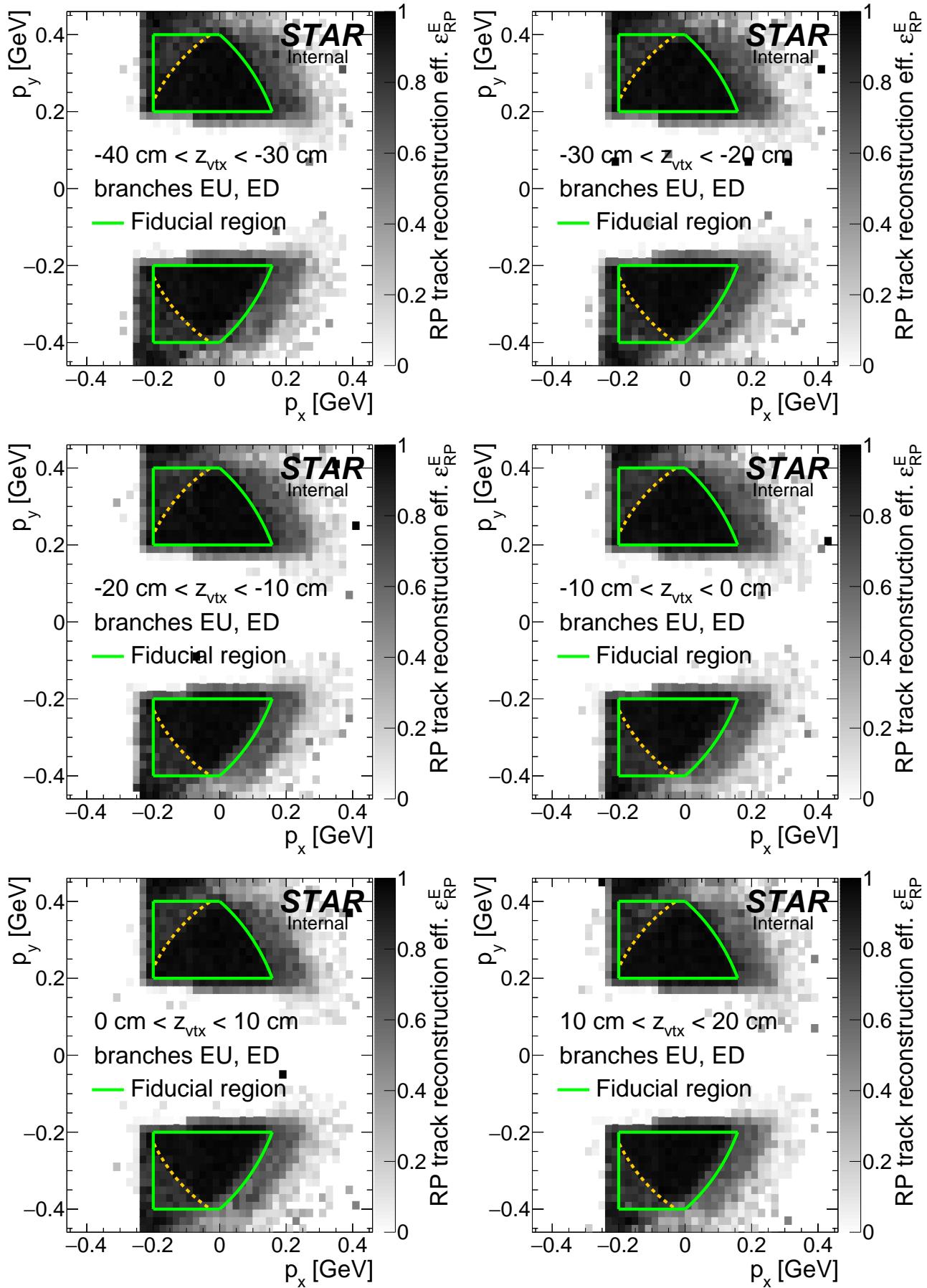
The second term of the last part of Eq. (E.5) related with the pile-up is incorporated to overall efficiency of online and offline vetoes described in Sec. 6.2.2.3 - this is required by the correlation of vetoes, the possibility that vetoes in independent subdetectors take place in the same bunch crossing. This could happen if e.g. single diffraction event occurs on top of the CEP event, yielding a BBC signal and RP signal, both vetoing RP_CPT2 trigger.

F. RP efficiency

F.1 RP track acceptance, reconstruction and selection efficiency

Figure F.1: RP track acceptance, reconstruction and selection efficiency on the east side obtained from MC simulation embedded into zero-bias data. Each plot corresponds to z -vertex range given in the plot.





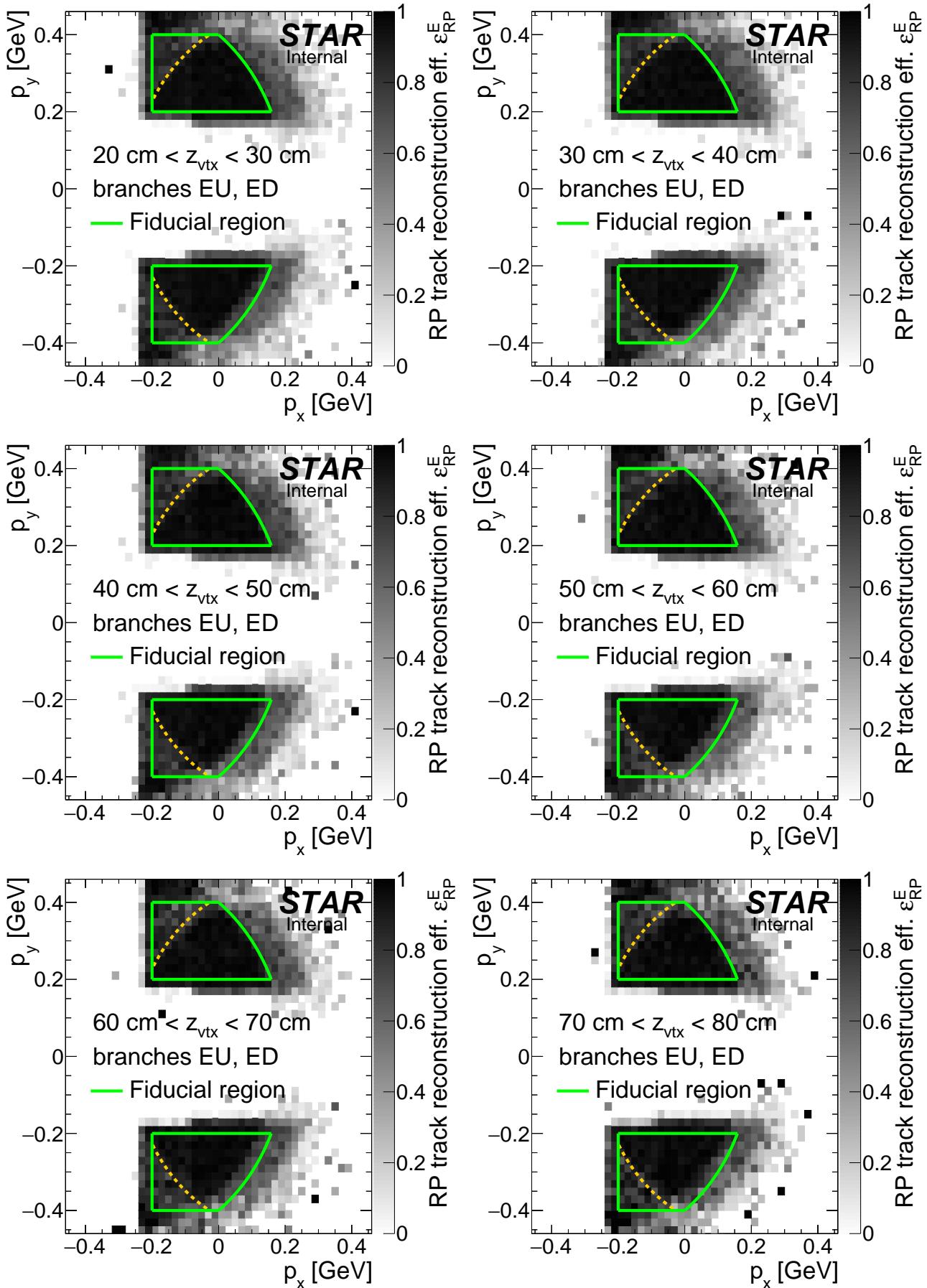
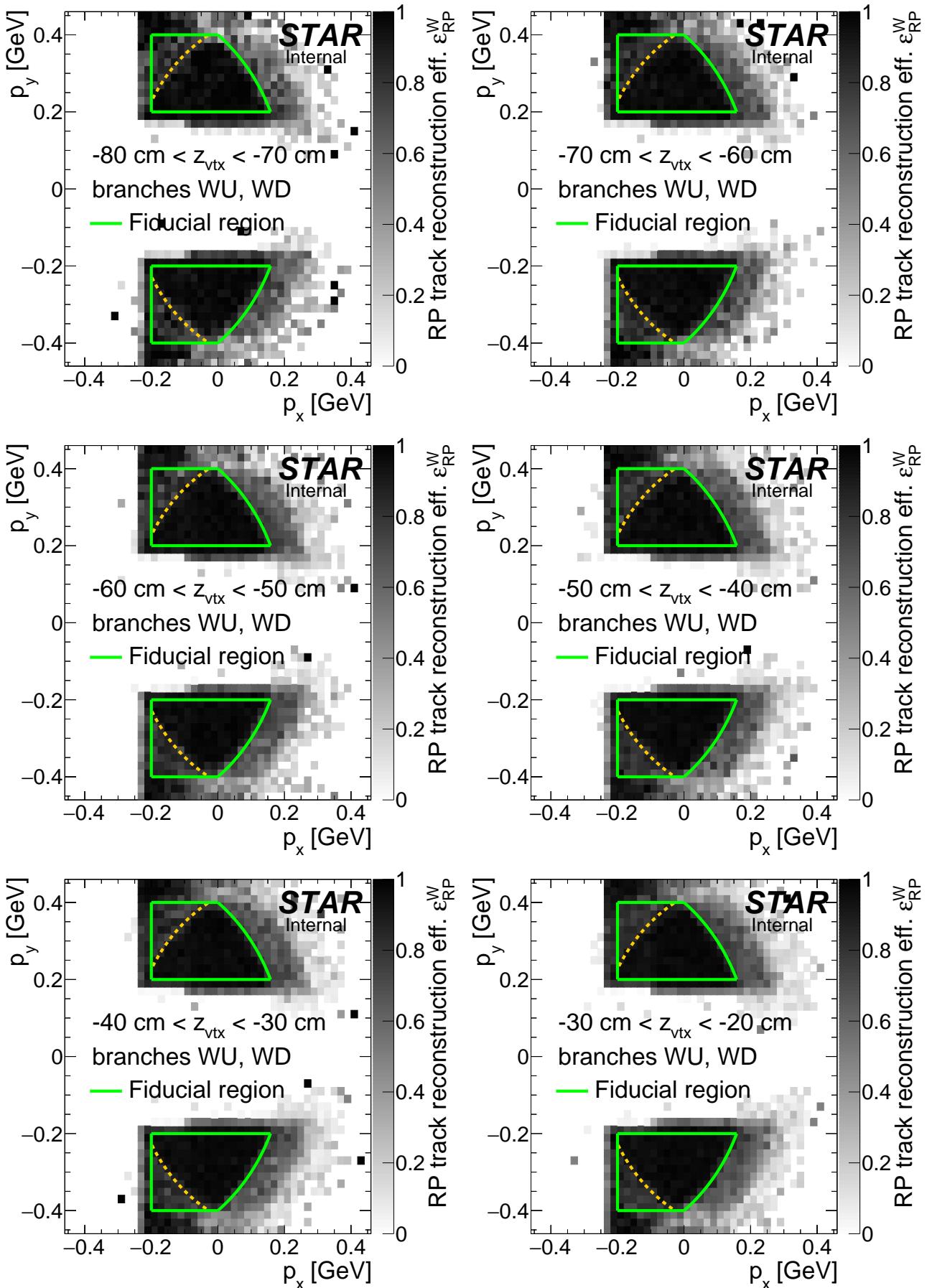
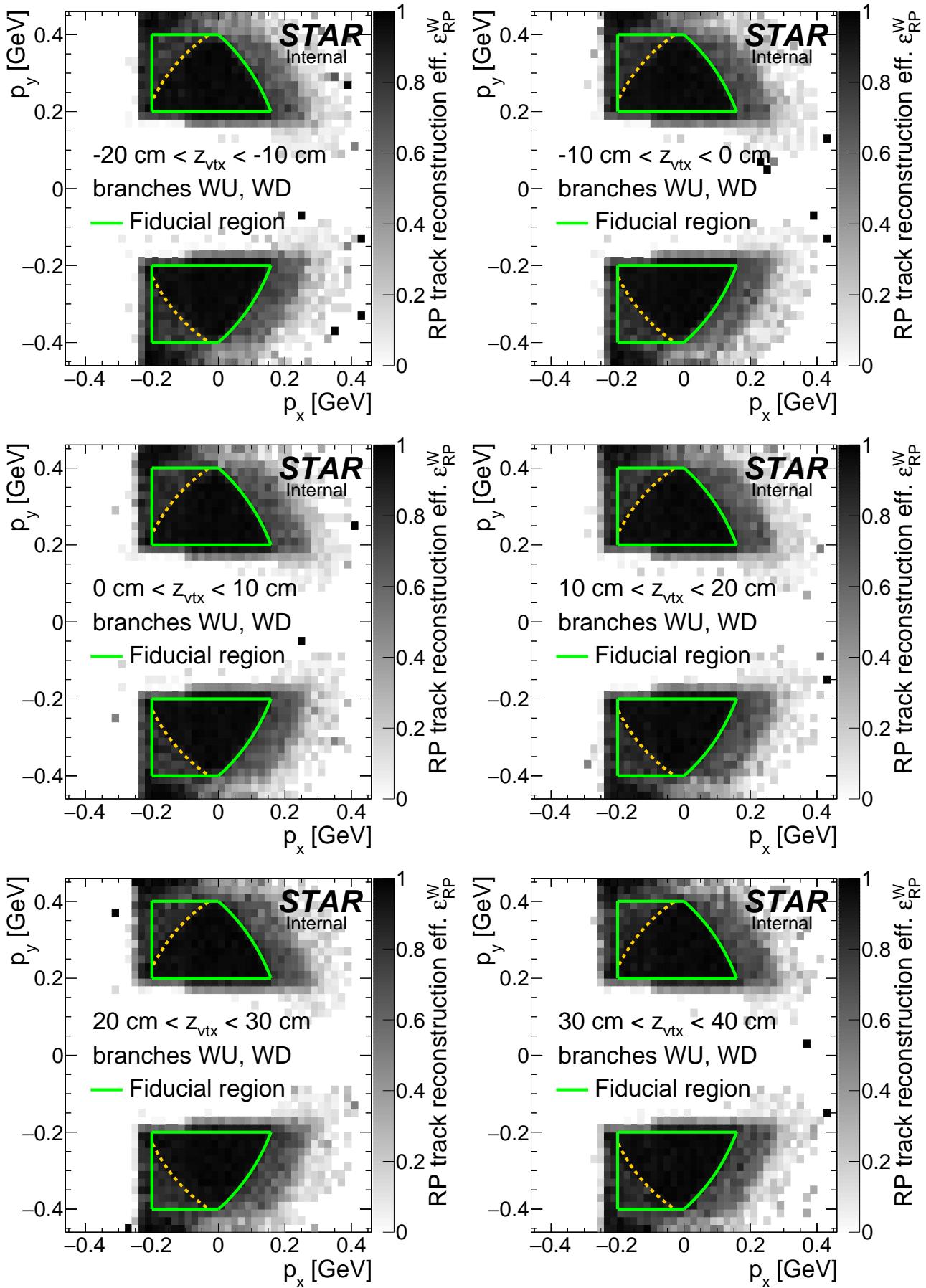
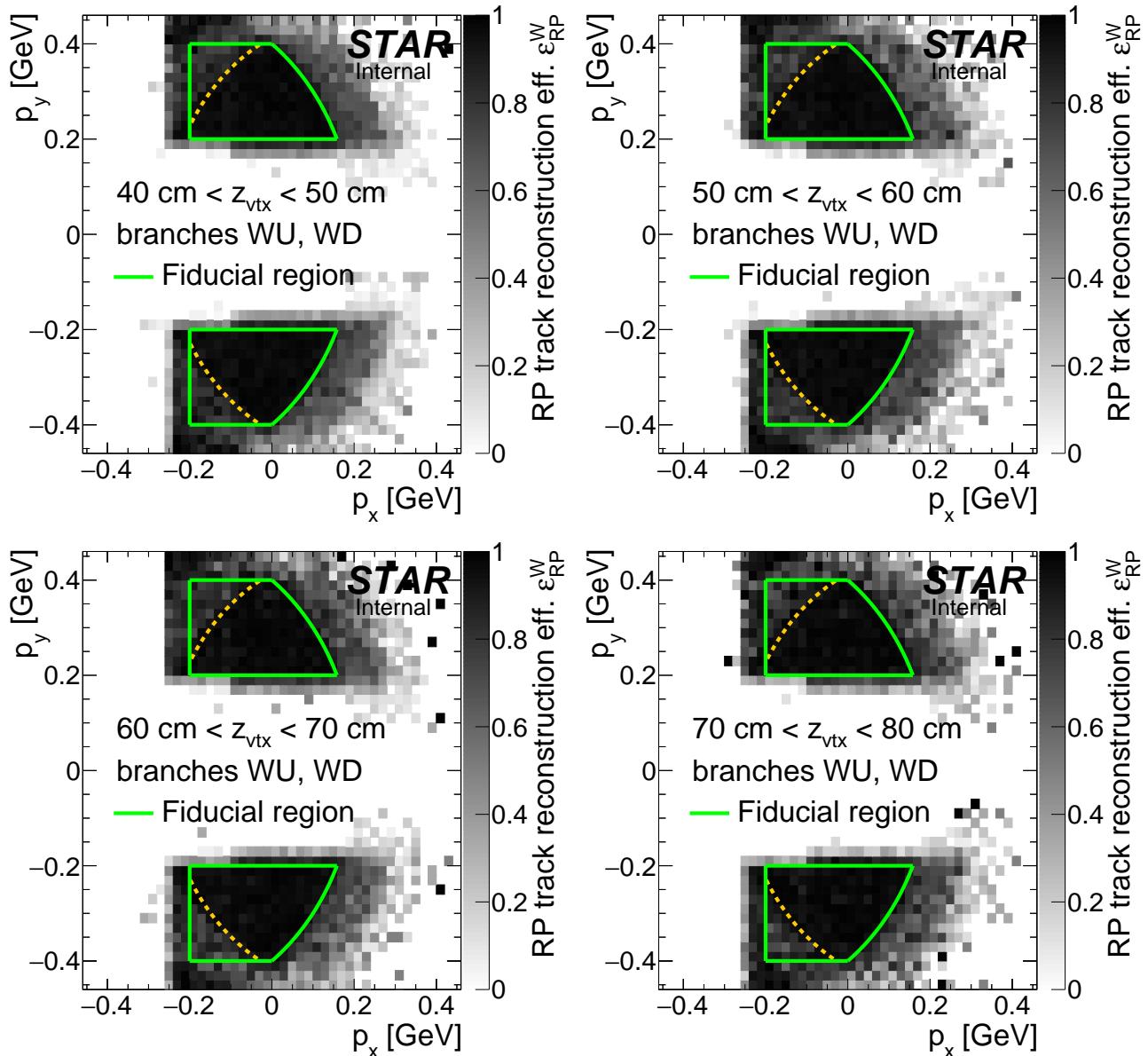


Figure F.2: RP track acceptance, reconstruction and selection efficiency on the west side obtained from MC simulation embedded into zero-bias data. Each plot corresponds to z -vertex range given in the plot.

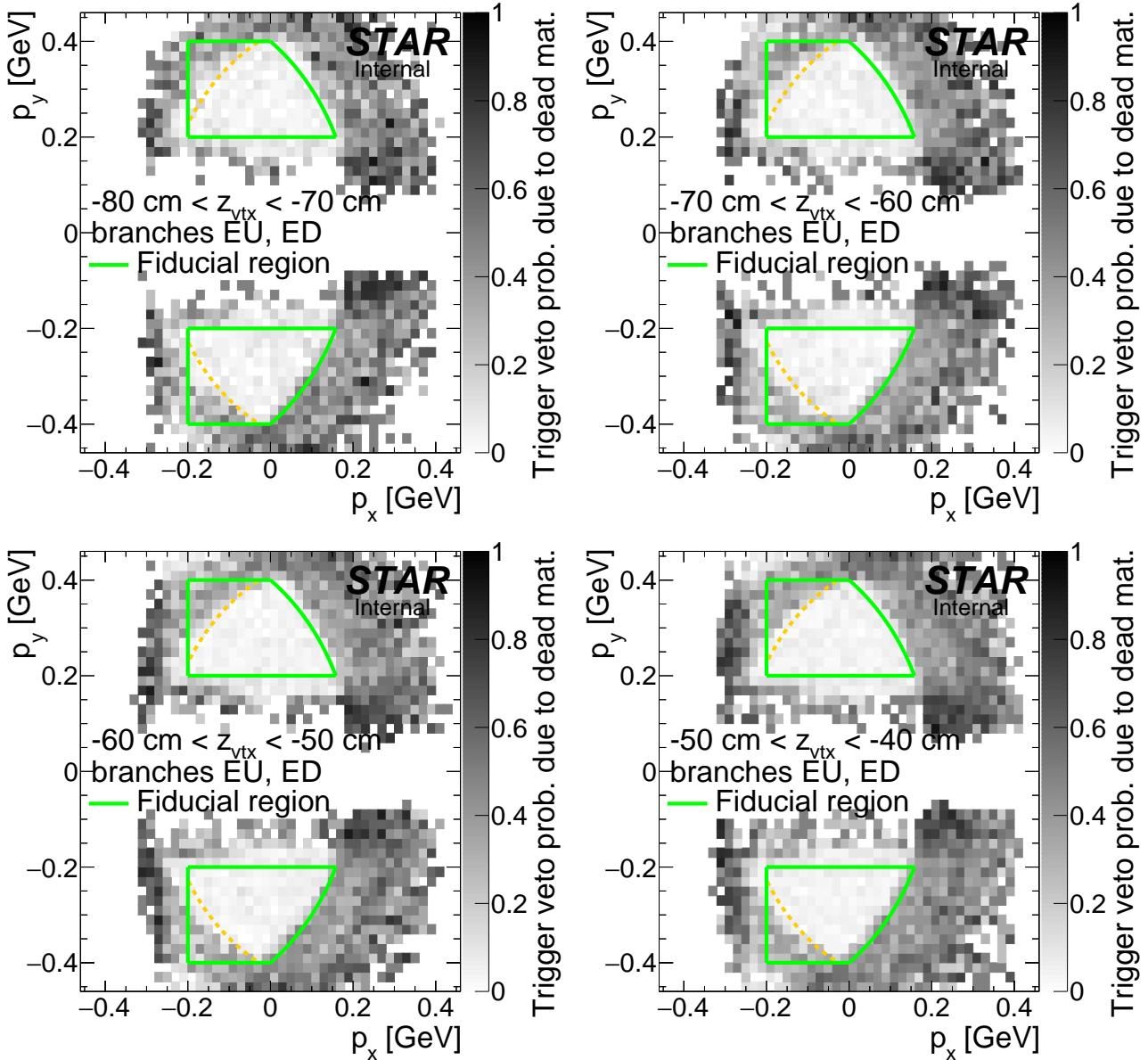


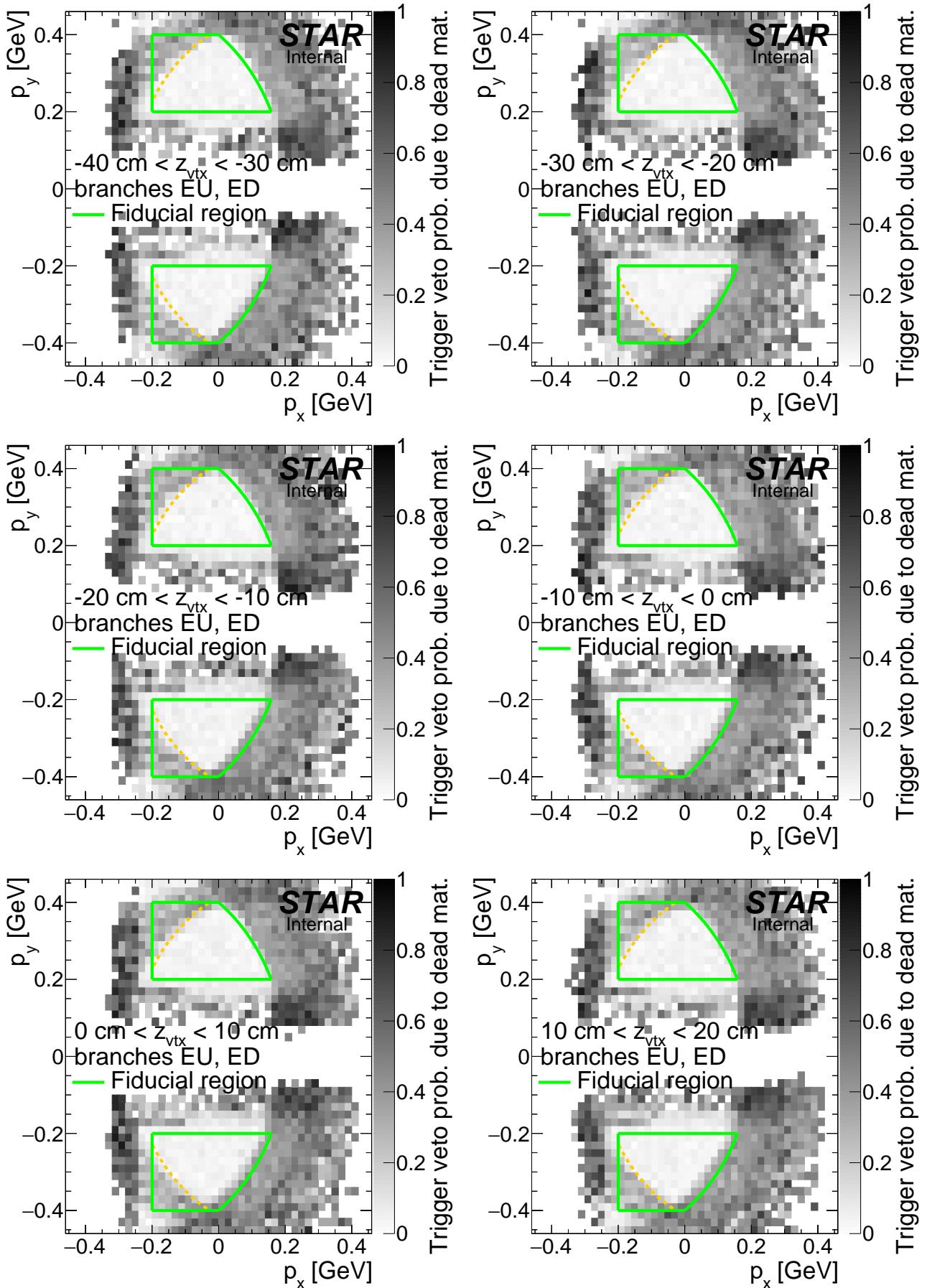




F.2 RP trigger veto probability related to dead material

Figure F.3: Probability of ET&IT trigger veto due to forward proton interaction with dead material on the east side. Results were obtained from forward proton MC simulation embedded into zero-bias data. Each plot corresponds to z -vertex range given in the plot.





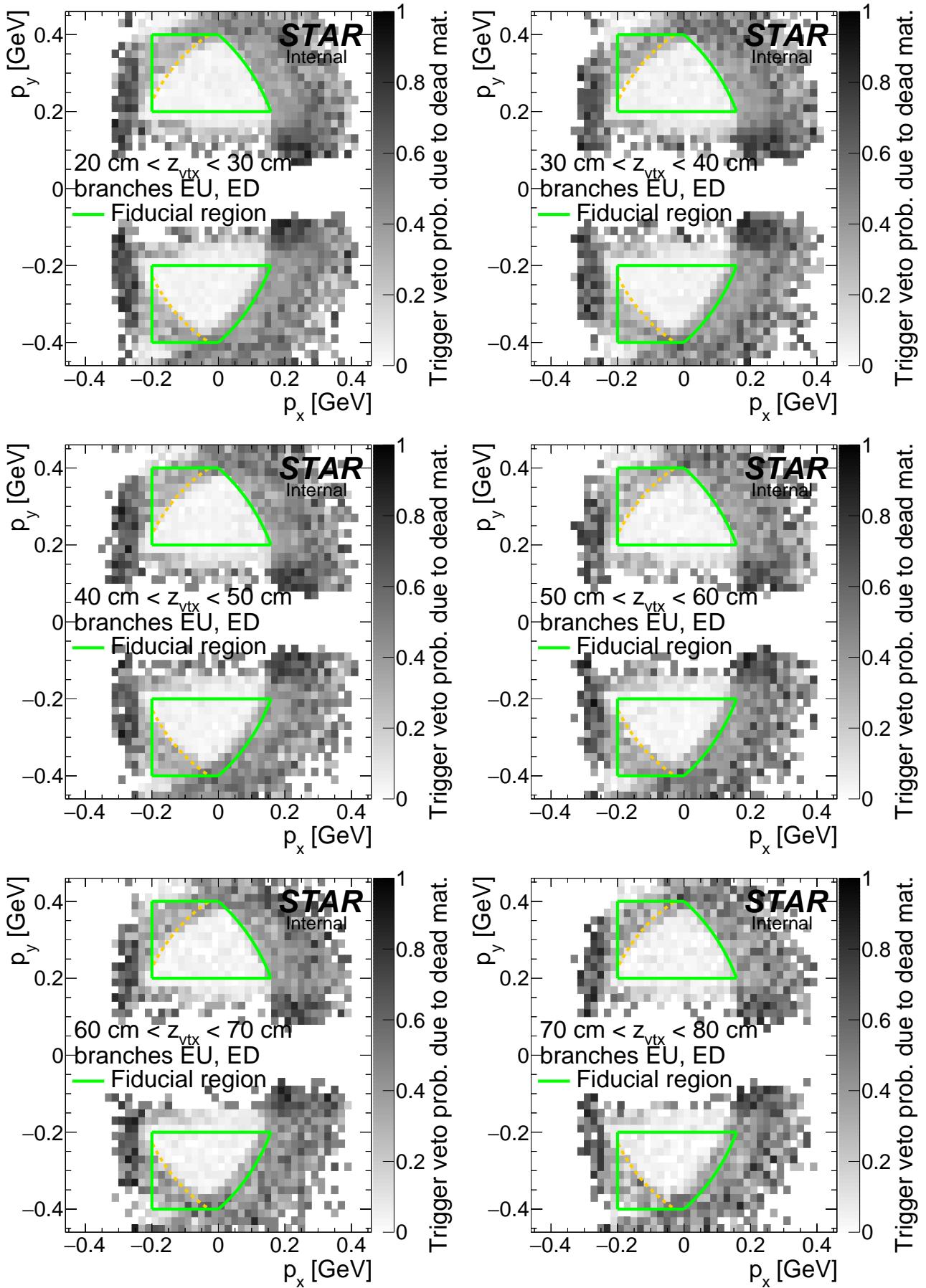
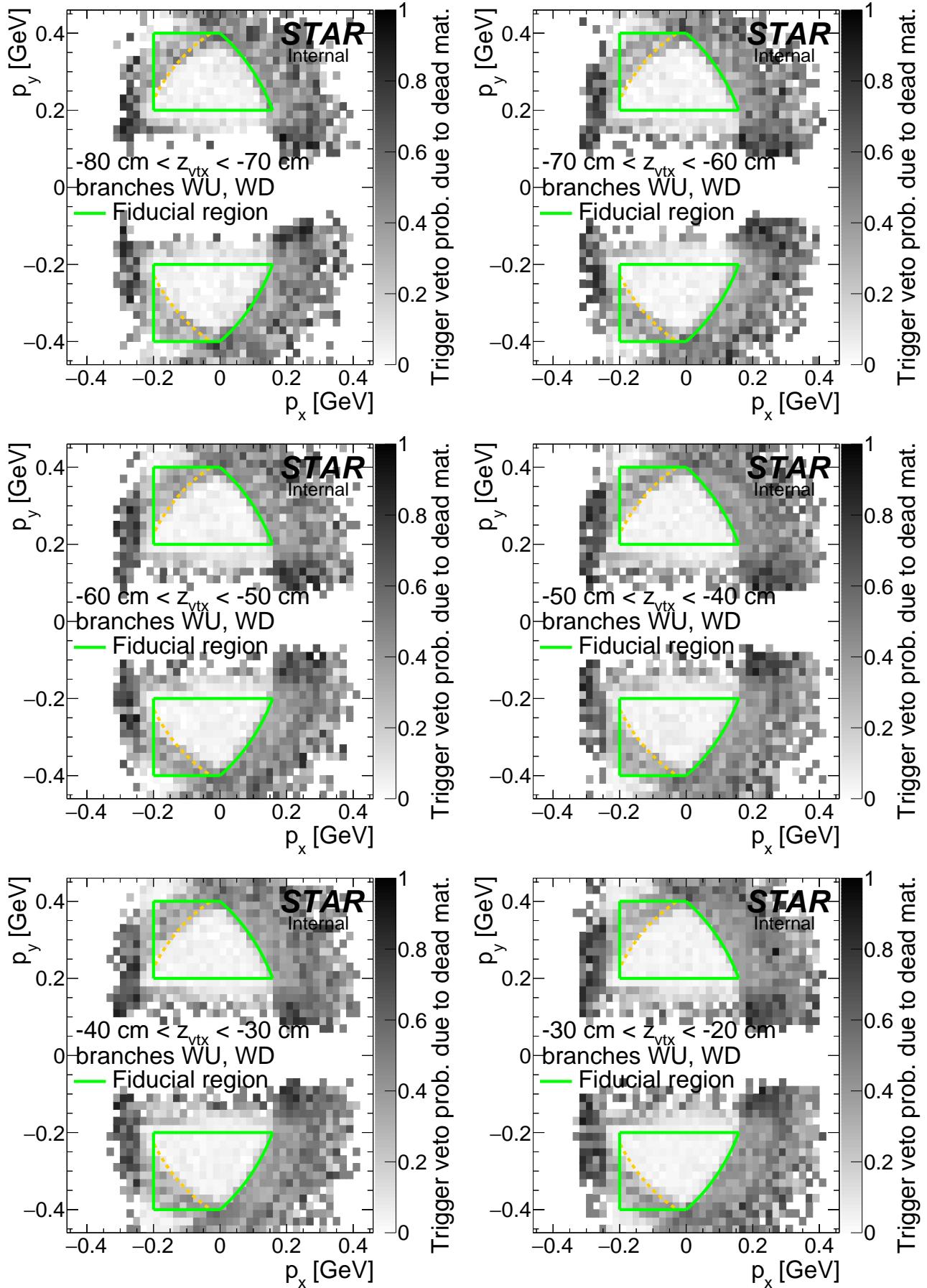
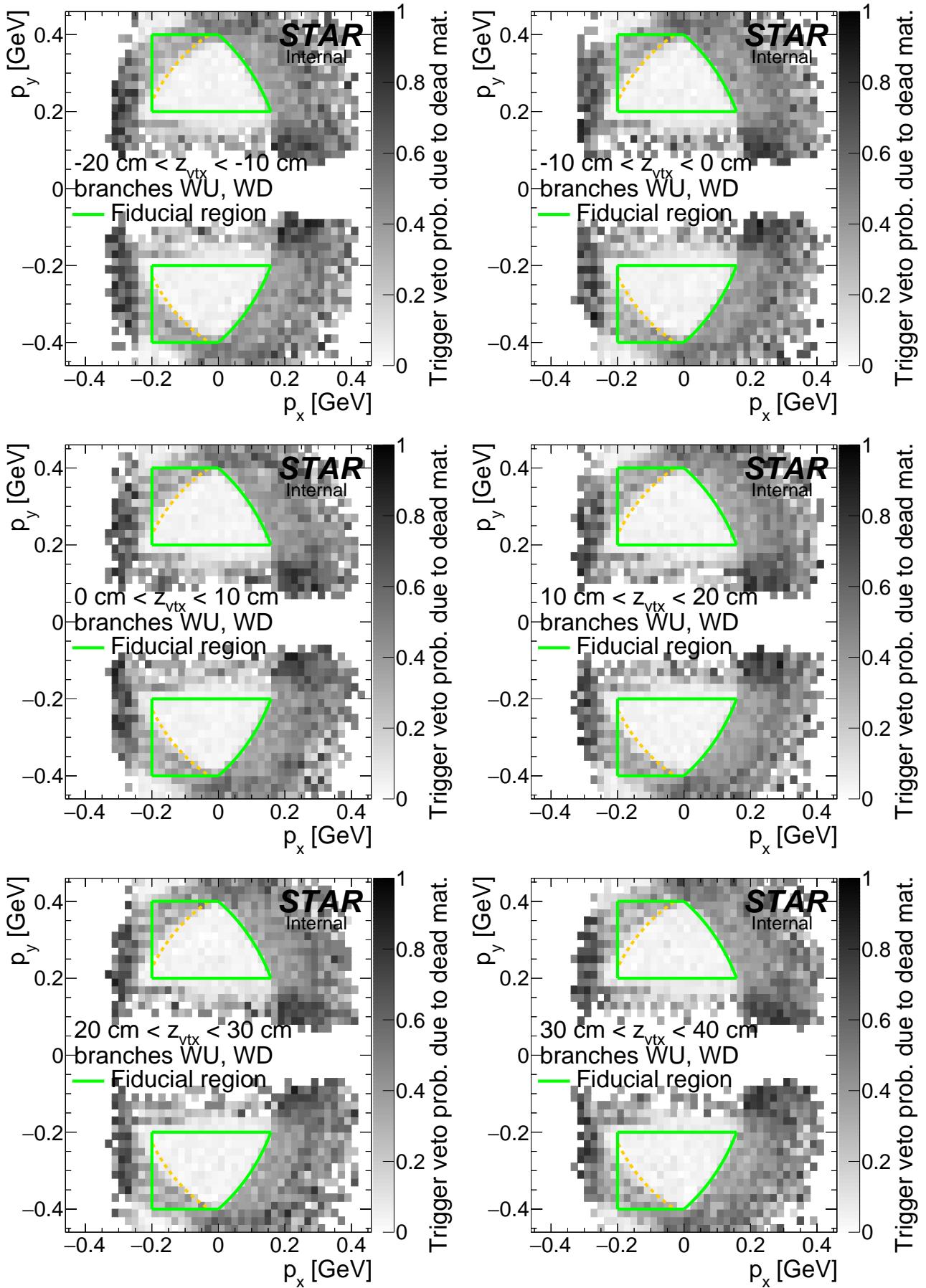
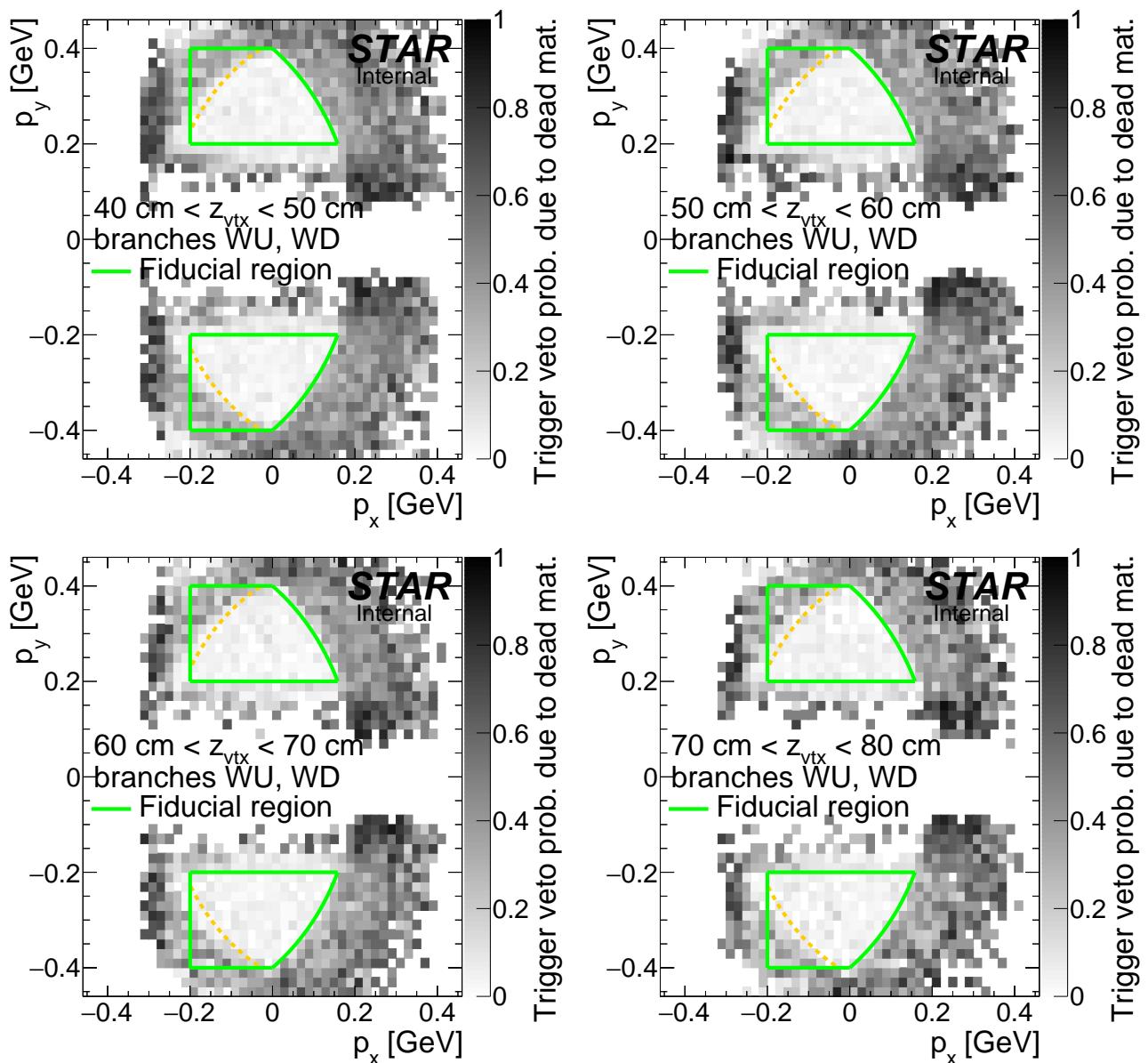


Figure F.4: Probability of ET&IT trigger veto due to forward proton interaction with dead material on the west side. Results were obtained from forward proton MC simulation embedded into zero-bias data. Each plot corresponds to z -vertex range given in the plot.

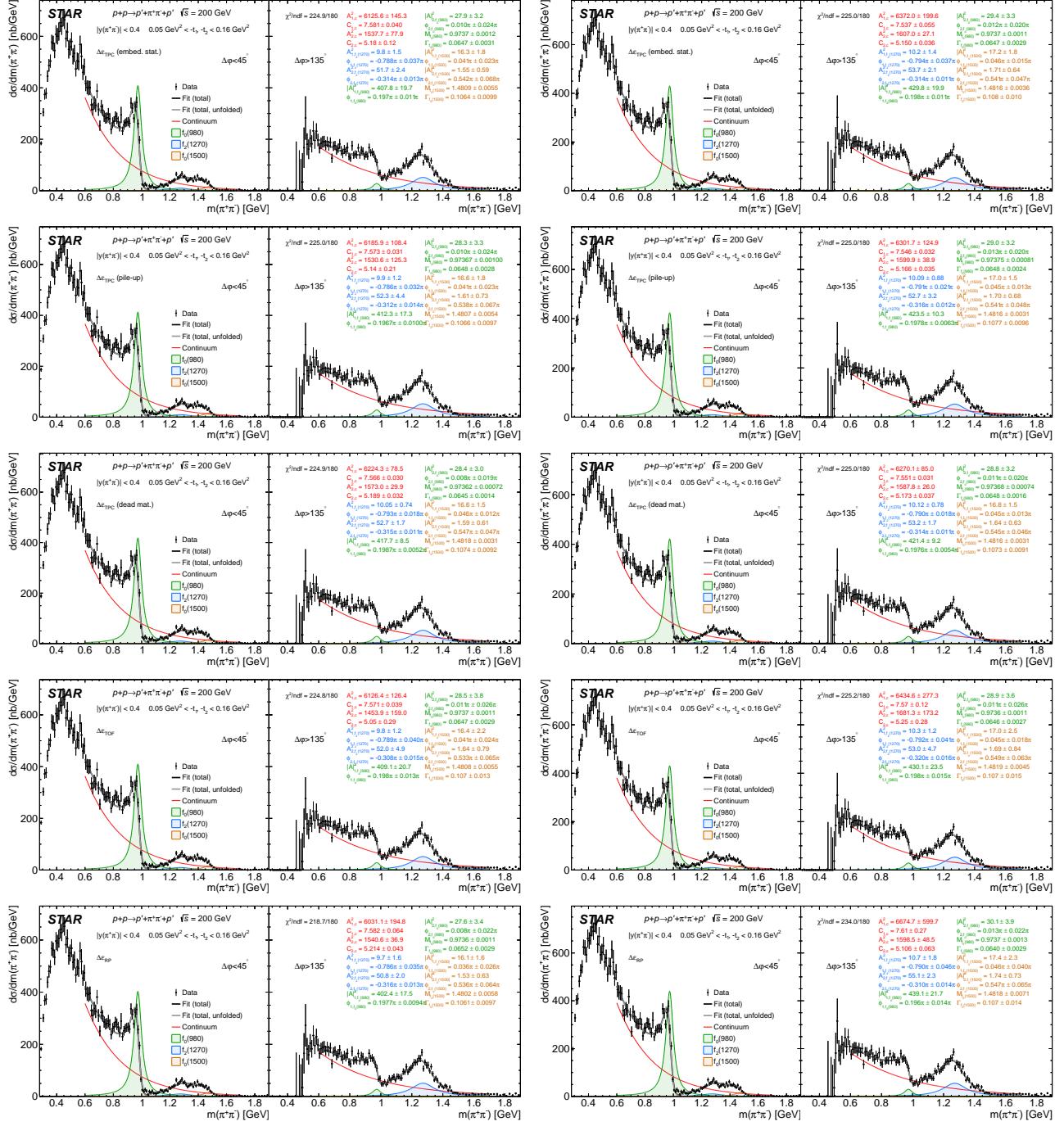


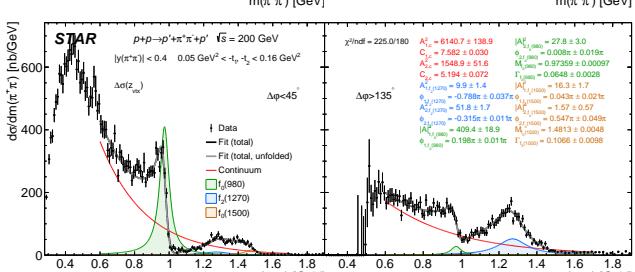
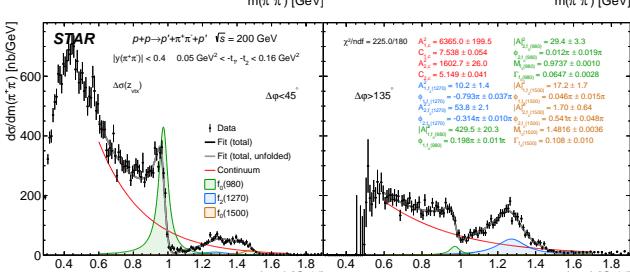
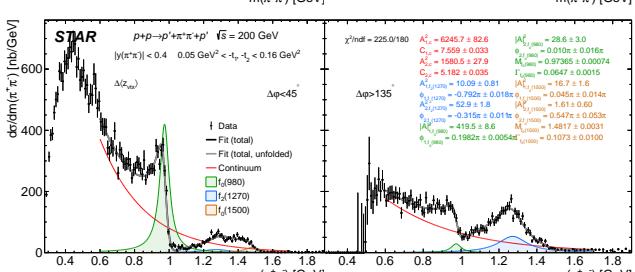
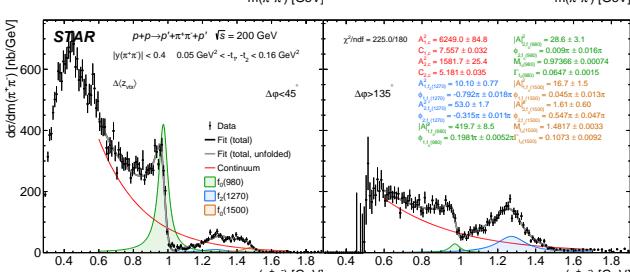
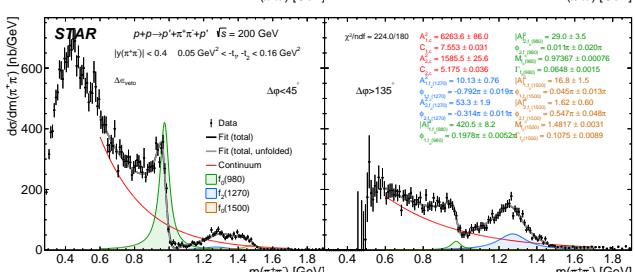
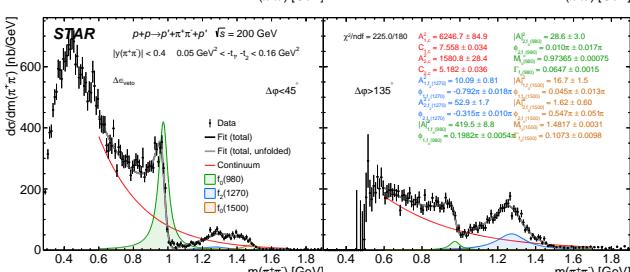
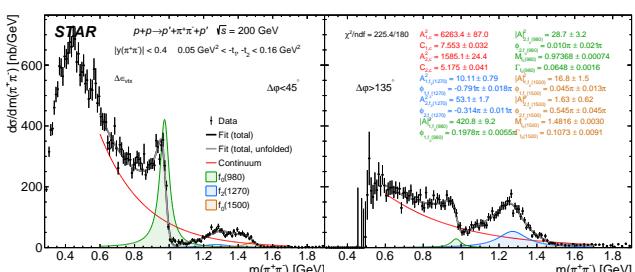
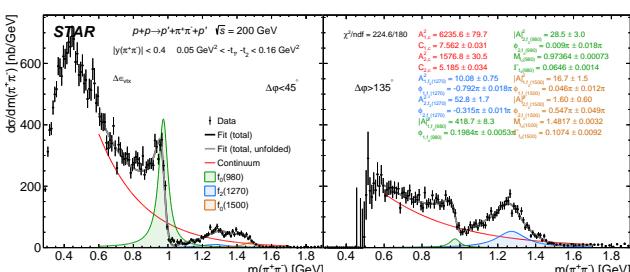
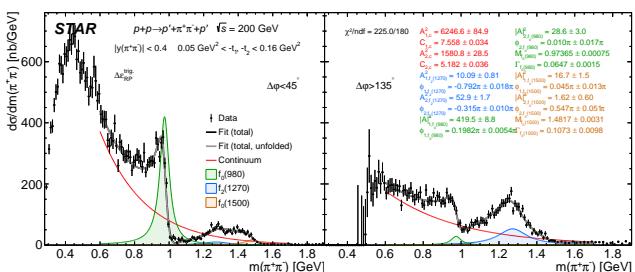
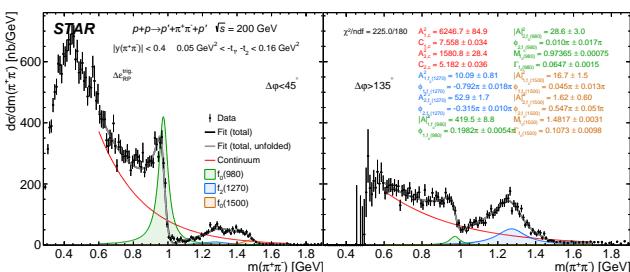
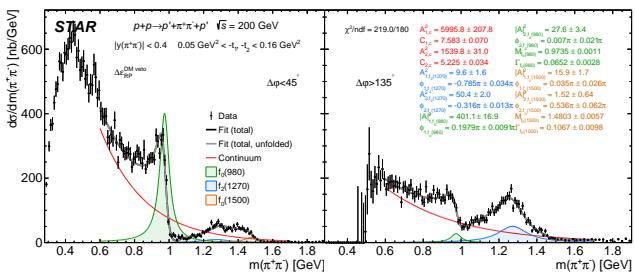
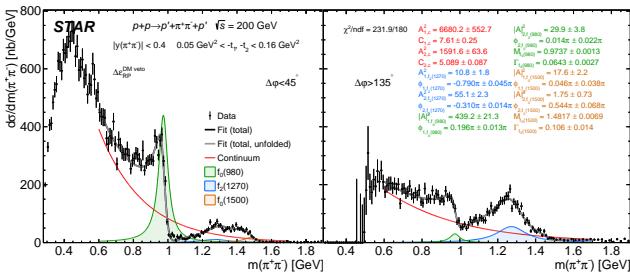


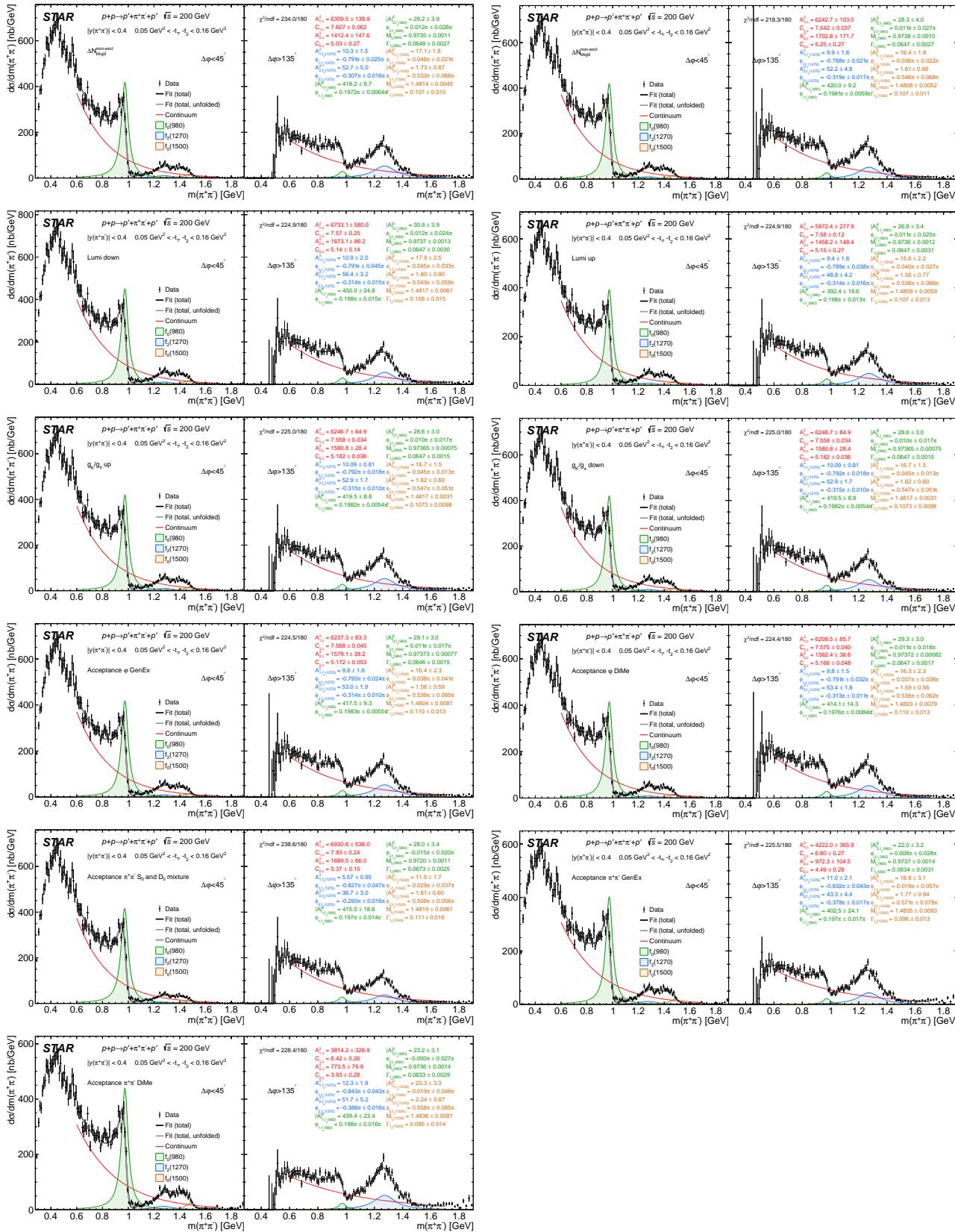


G. Fits to extrapolated $d\sigma/dm(\pi^+\pi^-)$

Figure G.1: Fits to $d\sigma/dm(\pi^+\pi^-)$ modified by systematic and model variations.







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