

epsilon:

$$\begin{aligned}
 z &= a * \sin(2\pi ft) \\
 \dot{z} &= 2\pi fa * \cos(2\pi ft) \\
 \ddot{z} &= -4\pi^2 f^2 a * \sin(2\pi ft) = -4\pi^2 f^2 z \\
 a_y &= -\ddot{z} = 4\pi^2 f^2 z \\
 a_x &= \alpha \\
 \vec{a} &= [\alpha, 4\pi^2 f^2 z] \\
 \epsilon_1 &= \frac{\vec{l}}{2} * m * \vec{a} / \frac{1}{3} ml^2 = \frac{3}{2l} a \cdot (-\cos \phi, \sin \phi) \\
 \epsilon_2 &= \frac{l}{2} * \frac{l}{2} * \omega * \mu / \frac{1}{3} ml^2 = \frac{3}{4m} \omega \mu \\
 \epsilon &= \epsilon_1 - \epsilon_2 = \frac{3}{2l} a \cdot (-\cos \phi, \sin \phi) - \frac{3}{4m} \omega \mu
 \end{aligned}$$

simulate:

$$\begin{aligned}
 i(0) &= 0 \\
 t(0) &= 0 \\
 \phi(0) &= \phi_0 \\
 x(0) &= x_0 \\
 \omega(0) &= \omega_0 \\
 v(0) &= v_0 \\
 z(0) &= 0 \\
 \\
 i[i+1] &= i[i] + 1 \\
 t[i+1] &= t[i] + \frac{1}{f_{prob}} \\
 z[i+1] &= a * \sin(2\pi f(t+1)) \\
 \alpha[i+1] &= \alpha(\phi[i], \omega[i], z[i]) \\
 \epsilon[i+1] &= \epsilon(\phi[i], \omega[i], \alpha[i], z[i]) \\
 \omega[i+1] &= \omega[i] + \frac{\epsilon[i] + \epsilon[i+1]}{2} * \frac{1}{f_{prob}} \\
 v[i+1] &= v[i] + \frac{\alpha[i] + \alpha[i+1]}{2} * \frac{1}{f_{prob}} \\
 \phi[i+1] &= \phi[i] + \frac{\omega[i] + \omega[i+1]}{2} * \frac{1}{f_{prob}} \\
 x[i+1] &= x[i] + \frac{v[i] + v[i+1]}{2} * \frac{1}{f_{prob}}
 \end{aligned}$$