

$$\det(A) = -2, \det(B) = 4, \det(C) = 3$$

$$\textcircled{1} \underline{\det(A^2 B^T)} = \textcircled{16}$$

$$\begin{aligned} \det(A^2) \det(B^T) &= \\ [\det(A)]^2 [\det(B)] &= \\ (-2)^2 \times 4 &= \\ 4 \times 4 &= 16 \end{aligned}$$

$$\bullet \det(A^k) = [\det(A)]^k$$

$$\bullet \det(B^T) = \det(B)$$

$$\textcircled{2} \underline{\det(A^2 + B^2)} = \textcircled{N/A}$$

There is no general formula expressing $\det(X+Y)$ in terms of $\det(X)$ and $\det(Y)$ alone.

Without additional information about the relationship between A and B , $\det(A^2 + B^2)$ can not be determined from determinants alone.

$$\textcircled{3} \underline{\det(CB^{-1})} = \textcircled{\frac{3}{4}}$$

$$\begin{aligned} \det(C) \det(B^{-1}) &= \\ \det(C) [\det(B)]^{-1} &= \\ 3 \times \frac{1}{4} &= \frac{3}{4} \end{aligned}$$

$$\bullet \det(B^{-1}) = \frac{1}{\det(B)}$$