

① Find GCD and LCM of 12 and 18:

GCD Calculation: Use Euclidean Algorithm

$$\text{GCD}(a, b) = \text{GCD}(b, a \bmod b)$$

$$\text{GCD}(\text{large \#}, \text{small \#})$$

$$\text{GCD}(18, 12) = \text{GCD}(12, 18 \bmod 12) = \text{GCD}(12, 6)$$

$$\text{GCD}(12, 6) = \text{GCD}(6, 12 \bmod 6) = \text{GCD}(6, 0) = 6$$

$$\boxed{\text{GCD}(12, 18) = 6}$$

LCM Calculation: Use LCM formula that uses GCD:

$$\text{LCM}(a, b) = (a \times b) / \text{GCD}(a, b)$$

$$\text{LCM}(12, 18) = (12 \times 18) / \text{GCD}(12, 18)$$

$$= 216 / 6$$

$$\boxed{\text{LCM}(12, 18) = 36}$$

Result:

$$\boxed{\text{GCD} = 6 \quad \text{LCM} = 36}$$

② Find GCF and LCM of 8 and 12

GCD:

$$\text{GCD}(a, b) = \text{GCD}(b, a \bmod b) \text{ until } a \bmod b = 0$$

$$\text{GCD}(\text{larger \#}, \text{smaller \#}) - \text{commutative}$$

$$\text{GCD}(12, 8) = \text{GCD}(8, 12 \bmod 8) = \text{GCD}(8, 4)$$

$$\text{GCD}(8, 4) = \text{GCD}(4, 8 \bmod 4) = \text{GCD}(4, 0) = 4$$

$$\text{GCD}(8, 12) = 4$$

LCM:

$$\text{LCM}(a, b) = (a \times b) / \text{GCD}(a, b)$$

$$\text{LCM}(8, 12) = (8 \times 12) / \text{GCD}(8, 12)$$

$$= 96 / 4$$

$$\text{LCM}(8, 12) = 24$$

$$\boxed{\text{GCD} = 4 \quad \text{LCM} = 24}$$

③ Find GCD and LCM of 14, 21, and 28

Step 1: Compute GCD for 2 numbers (14 and 21):

$$\bullet \text{GCD}(21, 14) = \text{GCD}(14, 21 \bmod 14) = \text{GCD}(14, 7)$$

$$\text{GCD}(14, 7) = \text{GCD}(7, 14 \bmod 7) = \text{GCD}(7, 0)$$

$$\text{GCD}(14, 21) = 7$$

Step 2: Compute GCD for the result of the first GCD calculation and the third number (7, 28) to get final GCD:

$$\bullet \text{GCD}(28, 7) = \text{GCD}(7, 28 \bmod 7) = \text{GCD}(7, 0) = 7$$

$$\boxed{\text{GCD}(14, 21, 28) = 7}$$

Step 3: Compute LCM for two numbers (14 and 21):

$$\bullet \text{LCM}(14, 21) = (14 \times 21) / \text{GCD}(14, 21)$$

$$= 294 / 7$$

$$\text{LCM}(14, 21) = 42$$

Step 4: Compute GCD and LCM with result from Step 3 and the third number (42, 28)

$$\bullet \text{GCD}(42, 28).$$

$$42 \bmod 28 = 14 \rightarrow 28 \bmod 14 = 0$$

$$\text{GCD}(42, 28) = 14$$

$$\bullet \text{LCM}(42, 28):$$

$$\text{LCM}(42, 28) = (42 \times 28) / \text{GCD}(42, 28)$$

$$= 1176 / 14$$

$$\boxed{\text{LCM}(42, 28) = 84}$$

$$\boxed{\text{GCD} = 7 \quad \text{LCM} = 84}$$