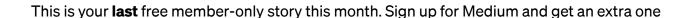


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HANDS-ON TUTORIALS

NMF — A visual explainer and Python **Implementation**



(Anupama Garla Mar 18 · 14 min read *

Gain an intuition for the unsupervised learning algorithm that allows data scientists to extract topics from texts, photos, and more, and build those handy recommendation systems. NMF explanation is followed by a Python Implementation on a toy example of topic modelling on Presidential Inauguration Speeches.

Origins of NMF

"Is perception of the whole based on perception of its parts?"

Researchers Lee and Seung go on to lay out the mathematical basis of NMF in their 1999 paper in Nature — "Here we demonstrate an algorithm for non-negative matrix factorization that is able to learn parts of faces and semantic features of text."

he beauty of data science is its ability to translate rather philosophical theory into mathematical algorithms that test the usefulness of such theory. NMF answers the question — to what extent a whole is a sum of its parts? And how do we use these parts? Companies typically use these parts to find patterns and associations between



them differently. Additionally, the document-topic matrix can be used to plot each document in space and provide a system to give recommendations based on similarities and differences.

Let's start looking at NMF in the context of natural language processing where it is often used for topic modeling.

Topic Modeling: How do we extract topics from a large corpus of documents?

We convert a corpus of documents into numbers to answer questions like:

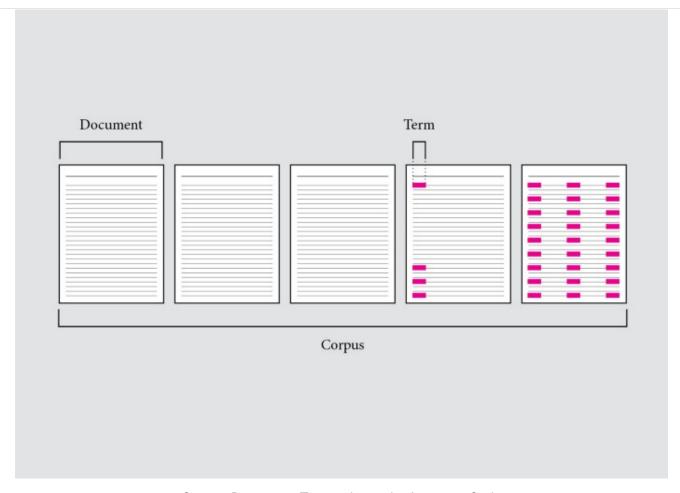
- What are the prevailing topics in this corpus?
- To what extent is each topic important in each document?
- How well do these extracted topics describe the original document?
- How similar is one document to another?

There are many more questions that can be answered with NMF and natural language processing, but these are the core questions. First, let's understand the terminology data scientists and a lot of our literature like to use.

Terminology

We use **corpus** to refer to a group of similar media. For NMF, this could be a group of texts like articles, images like aerial photos or portraits, audio like songs, or youtube videos — anything that can be conceptualized as the addition of parts (rather than the addition and subtraction of parts). We use **document** to refer to one text, photo, song, or video. A **term** is a word.

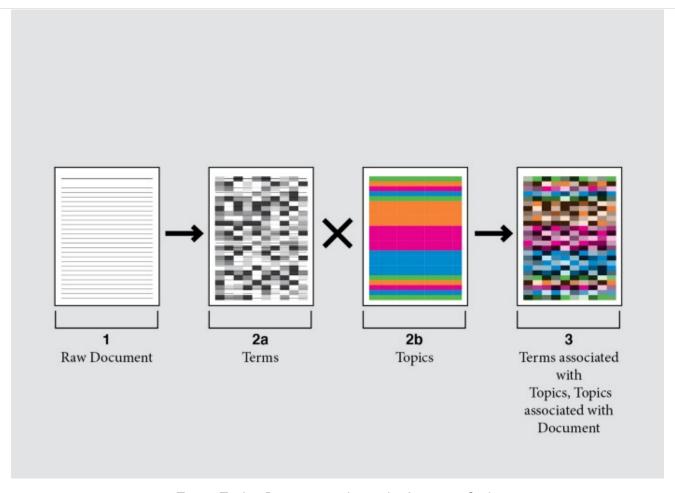




Corpus, Document, Term — Image by Anupama Garla

NMF is a form of **Topic Modelling** — the art of extracting meaningful themes that recur through a corpus of documents. A corpus is composed of a set of topics embedded in its documents. A **document** is composed of a hierarchy of **topics**. A **topic** is composed of a hierarchy of **terms**.





Terms, Topics, Document — Image by Anupama Garla

NMF uses the logic of the 'the distributional hypothesis' discussed in detail in the Swedish linguist, Magnus Sahlgren's paper, <u>The Distributional Hypothesis</u>.

Sahlgren offers one often cited explanation,

'This hypothesis is often stated in terms like "words which are similar in meaning occur in similar contexts" (Rubenstein & Goodenough, 1965)'

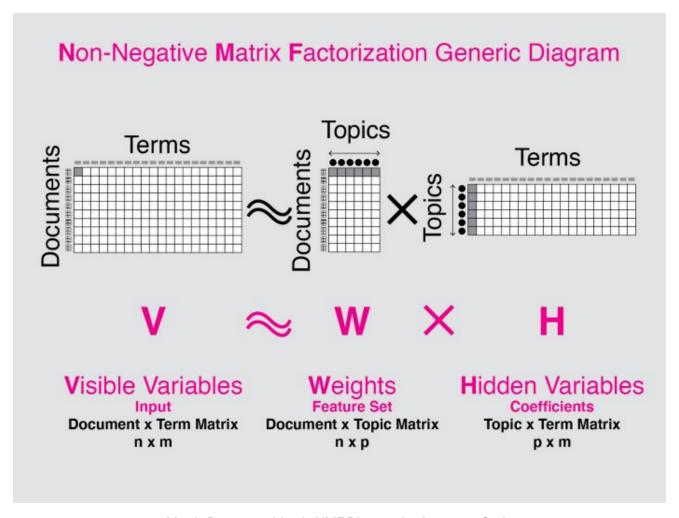
and continues — 'The general idea behind the distributional hypothesis seems clear enough: there is a correlation between distributional similarity and meaning similarity, which allows us to utilize the former in order to estimate the latter.'

For us, this means that documents can be treated as a bag of words. Similar documents have similar word frequency distributions — and similar topics. Two words that occur together are likely similar — belonging to a single topic. This algorithm ignores *syntactic*

rer 2 mis mi:

NMF

NMF stands for Latent Semantic Analysis with the 'Non-negative Matrix-Factorization' method used to decompose the document-term matrix into two smaller matrices — the document-topic matrix (U) and the topic-term matrix (W) — each populated with unnormalized probabilities.



Matrix Decomposition in NMF Diagram by Anupama Garla

The values in V can be approximated through matrix multiplication of W and H. For instance the grey box in V can be found through matrix multiplication of the first row of W by the first column of H, also greyed in. The first row of V can be approximated through matrix multiplication of the first row of W with the entire matrix of H.

V is for Visible

In the *V matrix*, each row represents a *Document* that is composed of a *frequency of*



excerpt of a V Matrix of Presidential Inauguration Speech Text:

	constitution	union	peace	freedom	principle	man	spirit	party	congress	justice	year	day	policy	president	service
Name															
Theodore Roosevelt	0.00	0.00	0.10	0.00	0.00	0.00	0.12	0.00	0.00	0.07	0.00	0.10	0.00	0.00	0.00
William Howard Taft	0.02	0.00	0.03	0.01	0.02	0.02	0.00	0.02	0.13	0.02	0.04	0.01	0.12	0.01	0.00
Woodrow Wilson	0.00	0.00	0.00	0.00	0.03	0.05	0.03	0.14	0.00	0.17	0.07	0.09	0.03	0.06	0.03
Warren G. Harding	0.00	0.02	0.09	0.07	0.00	0.03	0.05	0.01	0.02	0.06	0.00	0.00	0.05	0.00	0.08
Calvin Coolidge	0.07	0.00	0.15	0.09	0.08	0.05	0.00	0.17	0.03	0.09	0.04	0.01	0.10	0.02	0.03
Herbert Hoover	0.02	0.00	0.16	0.07	0.00	0.03	0.02	0.08	0.04	0.15	0.03	0.04	0.04	0.00	0.09
Franklin D. Roosevelt	0.02	0.00	0.00	0.00	0.00	0.00	0.06	0.00	0.10	0.00	0.02	0.08	0.06	0.00	0.00
Harry S. Truman	0.00	0.00	0.20	0.21	0.05	0.07	0.00	0.00	0.00	0.09	0.03	0.00	0.02	0.02	0.00
Dwight D. Eisenhower	0.02	0.00	0.19	0.18	0.10	0.11	0.02	0.00	0.00	0.00	0.00	0.05	0.02	0.00	0.03
John F. Kennedy	0.00	0.00	0.10	0.12	0.00	0.12	0.00	0.03	0.00	0.03	0.05	0.05	0.00	0.12	0.03
Lyndon Baines Johnson	0.00	0.24	0.00	0.05	0.00	0.25	0.02	0.00	0.00	0.13	0.06	0.08	0.00	0.00	0.00
Richard Milhous Nixon	0.02	0.00	0.22	0.02	0.00	0.21	0.12	0.00	0.00	0.02	0.11	0.04	0.00	0.07	0.00
Jimmy Carter	0.00	0.00	0.03	0.13	0.06	0.03	0.19	0.00	0.00	0.03	0.06	0.03	0.03	0.10	0.00
Ronald Reagan	0.02	0.00	0.03	0.15	0.02	0.11	0.00	0.02	0.02	0.02	0.05	0.10	0.00	0.10	0.00
George Bush	0.00	0.02	0.05	0.09	0.02	0.10	0.00	0.02	0.07	0.03	0.03	0.15	0.00	0.12	0.00
Bill Clinton	0.00	0.00	0.00	0.05	0.00	0.00	0.02	0.00	0.06	0.00	0.00	0.00	0.00	0.05	0.10
George W. Bush	0.00	0.02	0.02	0.08	0.06	0.00	0.06	0.00	0.00	0.06	0.04	0.04	0.00	0.07	0.06
Barack Obama	0.00	0.00	0.07	0.06	0.02	0.06	0.10	0.00	0.00	0.00	0.05	0.09	0.00	0.02	0.06
Donald J. Trump	0.00	0.00	0.00	0.03	0.00	0.00	0.03	0.05	0.00	0.02	0.05	0.09	0.00	0.14	0.00

Excerpt of V Matrix (Using TF-IDF Vectorizer) by Anupama Garla

W is for weights

In the *W matrix*, each row represents a *Document* that is composed of unnormalized probabilities of *Topics*. Each column represents a *semantic feature* that recurs throughout the corpus. For image processing, the *features* would be specific prototypical characteristics like 'mustache'. Here is an excerpt of a *W Matrix* of Presidential Inauguration Speech Text:

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	Union + Constitution	Man + Freedom	Business + Policy	Principles + Improvement	Family + Jobs
Name					
George Washington	0.00	0.00	0.00	0.55	0.01
John Adams	0.03	0.00	0.02	0.53	0.03
Thomas Jefferson	0.05	0.19	0.00	0.37	0.00
James Madison	0.00	0.00	0.00	0.61	0.00
James Monroe	0.21	0.00	0.01	0.35	0.00
John Quincy Adams	0.31	0.10	0.00	0.18	0.00
Andrew Jackson	0.00	0.00	0.00	0.58	0.00
Martin Van Buren	0.15	0.01	0.02	0.38	0.02
William Henry Harrison	0.34	0.00	0.00	0.22	0.04
James Knox Polk	0.47	0.01	0.00	0.01	0.00
Zachary Taylor	0.15	0.00	0.02	0.32	0.01
Franklin Pierce	0.19	0.13	0.04	0.27	0.01
James Buchanan	0.47	0.00	0.00	0.00	0.00

Excerpt of W Matrix (1) by Anupama Garla

Abraham Lincoln	0.44	0.00	0.00	0.00	0.00
click to scroll output; double cli	0.14	0.00	0.22	0.00	0.00
Rutherford B. Hayes	0.21	0.00	0.24	0.09	0.00
James A. Garfield	0.35	0.04	0.08	0.00	0.03
Grover Cleveland	0.08	0.01	0.34	0.11	0.00
Benjamin Harrison	0.17	0.00	0.37	0.00	0.01
William McKinley	0.07	0.00	0.54	0.00	0.00
Theodore Roosevelt	0.00	0.06	0.15	0.07	0.20
William Howard Taft	0.05	0.00	0.52	0.00	0.00
Woodrow Wilson	0.00	0.00	0.25	0.00	0.30
Warren G. Harding	0.00	0.11	0.46	0.00	0.02
Calvin Coolidge	0.00	0.09	0.51	0.06	0.00
Herbert Hoover	0.00	0.06	0.56	0.00	0.02
Franklin D. Roosevelt	0.00	0.03	0.38	0.00	0.07

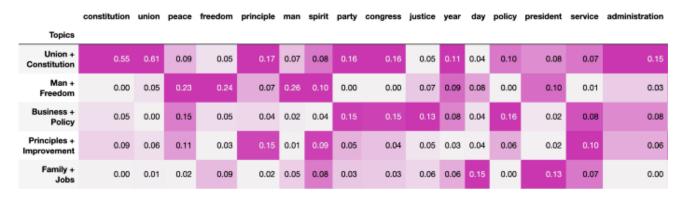
Excerpt of W Matrix (2) by Anupama Garla



Excerpt of W Matrix (3) by Anupama Garla

H is for hidden

In the *H matrix, each row represents a Topic* or *semantic feature* that is composed of *term frequencies*. *Each column represents a visible variable*. Two terms that occur frequently together form a topic, and each term gives more contextual meaning for the term it is grouped together with. If a term occurs frequently in two topics, then those topics are likely related. Here is an excerpt of an H *Matrix* of Presidential Inauguration Speech Text:



Excerpt of H Matrix by Anupama Garla



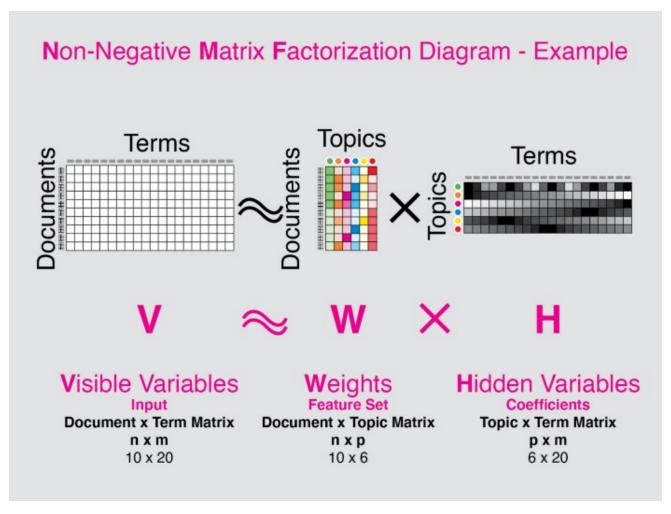
Excerpt of H Matrix (2) by Anupama Garla



The W and H matrix can be used to approximately reconstruct V through matrix multiplication.

The Art of Topic Modeling

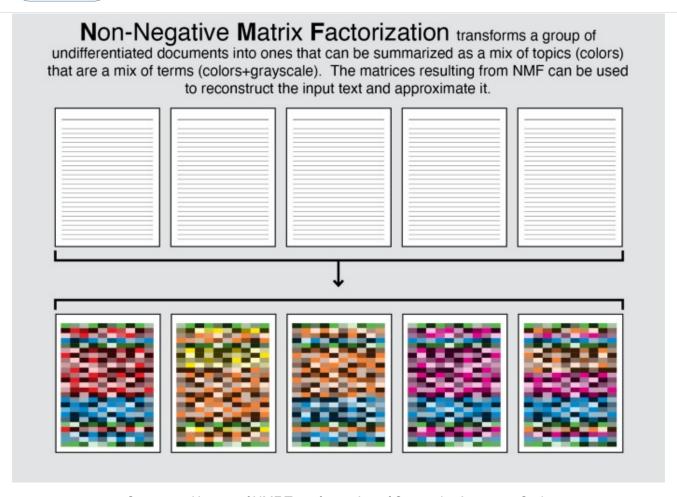
The output of NMF changes each time you run it, and the topics are not resolved — the data scientist must infer the topic from the highest word frequencies per topic, using the H matrix. This is where the art of choosing the correct number of topics comes into play. Too many, and you have topic repeats or topics composed of sparsely related words. Too few, and you have not very meaningful topics.



Matrix Decomposition in NMF Diagram Example by Anupama Garla

In the example above, the Topics (p) are set to 6. Each column of the W matrix represents a probability that the topic is in the document. Each row of the W matrix represents a distribution of topic frequencies in each Document. Each row of the H matrix represent the distribution of term frequencies in each topic, and can be seen as the degree to which each term is activated in each topic.





Conceptual Image of NMF Transformation of Corpus by Anupama Garla

NMF Math

Like most machine learning algorithms, NMF operates by starting with a guess of values for W and H, and iteratively minimizing the loss function. Typically it is implemented by updating one matrix (either W or H) for each iteration, and continuing to minimize the error function, ||V - WH|| = 0, while W and H values remain non-negative, until W and H are stable. There are different loss functions used to update the matrices based on the specific programming package you use, but the one proposed in the original Lee and Seung paper is the *multiplicative update rule*. Honestly the math is fairly complex, and it would take me some study to wrap my head around it and explain it in a no-fuss style. I'm going to call it out-of-scope of this article. :-).

NMF caveats

NMF requires that all documents are fairly similar — for instance if you are comparing faces, you would look at faces from a similar angle. If you are comparing texts, you would look at texts of similar lengths. For more complex documents/images, you would



NMF and TF-IDF

The advantage of NMF, as opposed to TF-IDF is that NMF breaks down the V matrix into *two smaller matrices*, W and H. The data scientist can set the number of Topics (p) to determine how small these matrices get. Data scientists often use the TF-IDF derived Document-Term Matrix as the Input Matrix, V, because it yields better results.

NMF vs. other matrix decomposition methods

NMF differs from other matrix decomposition methods like PCA and VQ in that it only uses non-negative numbers. This allows for each *Topic* or *feature* to be *interpretable*. Additionally, W and H can be represented by sparse matrices where only the values > 0 are encoded, making for *a smaller dataset*.

Python Implementation

This is generally the order of operations:

- 1. Import Relevant Libraries to Jupyter Notebook / Install Libraries in your Environment
- 2. Select Data and Import
- 3. Isolate Data to Topic Model
- 4. Clean Data
- 5. Create Function to Pre-process Data*
- 6. Create Document Term Matrix 'V'
- 7. Create Function to Display Topics*
- 8. Run NMF on Document Term Matrix 'V'
- 9. Iterate until you find useful Topics

1. Import the Python Libraries you will need.

For **dataframe manipulation** and exporting you will need:

^{*}Star indicates optional steps



```
import pandas as pd
```

From scikit learn for **modeling** you will need:

- TfidfVectorizer
- NMF
- text

```
from sklearn.feature_extraction.text import TfidfVectorizer
from sklearn.decomposition import NMF
from sklearn.feature extraction import text
```

From nltk for **text processing** you may need:

- stopwords
- word_tokenize
- pos_tag

```
from nltk.corpus import stopwords
from nltk import word_tokenize, pos_tag
from nltk.stem import WordNetLemmatizer
```

For **text cleaning** you may need:

- re (regular expressions)
- string

```
import re
import string
```



Next, select your corpus of documents. I am using American President's Inauguration Speeches, available as a <u>Kaggle Dataset</u>. I did get an error when I tried to import the speeches without the engine clause but I just googled my error and took this 'engine' suggestion which worked for me.

```
# expand pandas df column display width to enable easy inspection
pd.set_option('max_colwidth', 150)

# read in csv to dataframe
df = pd.read_csv('inaug_speeches.csv', engine='python')

# visually inspect dataframe
df.head()
```

	Unnamed: 0	Name	Inaugural Address	Date	text
0	4	George Washington	First Inaugural Address	Thursday, April 30, 1789	Fellow-Citizens of the Senate and of the House of Representatives: ◆♦AMONG the vicissitudes incident to life no event could have fille
1	5	George Washington	Second Inaugural Address	Monday, March 4, 1793	Fellow Citizens: ��I AM again called upon by the voice of my country to execute the functions of its Chief Magistrate. When the occas
2	6	John Adams	Inaugural Address	Saturday, March 4, 1797	WHEN it was first perceived, in early times, that no middle course for America remained between unlimited submission to a foreign le
3	7	Thomas Jefferson	First Inaugural Address	Wednesday, March 4, 1801	Friends and Fellow-Citizens: ��CALLED upon to undertake the duties of the first executive office of our country, I avail myself of th
4	8	Thomas Jefferson	Second Inaugural Address	Monday, March 4, 1805	PROCEEDING, fellow-citizens, to that qualification which the Constitution requires before my entrance on the charge again conferred

Raw DataFrame Image by Anupama Garla

3. Isolate Data to Topic Model

I'm going to make a dataframe of the President's names and speeches, and isolate to the first term inauguration speech, because some President's did not have a second term. This makes for a corpus of documents with similar lengths.

```
# Select Rows that are first term inaugural addresses
df = df.drop_duplicates(subset=['Name'], keep='first')

# Clean Up Index
df = df.reset_index()

# Select only President's Names and their Speeches
df = df[['Name', 'text']]

# Set Index to President's Names
df = df.set index('Name')
```



text

Reorge Washington
Thomas Jefferson
Friends and Fellow-Citizens: CALLED upon to undertake the duties of the first executive office of our country, I avail myself of th...

James Madison
James Monroe
Andrew Jackson
Fellow-Citizens: ABOUT to undertake the arduous duties that I have been appointed to perform by the choice of a free people, I avai...

Isolated Text DataFrame Image by Anupama Garla

4. Clean Data

I want to make all of the text in the speeches as comparable as possible so I will create a cleaning function that removes punctuation, capitalization, numbers, and strange characters. I use regular expressions for this, which offers a lot of ways to 'substitute' text. There are tons of regular expression cheat sheets, like this <u>one</u>. I 'apply' this function to my speech column.

```
def clean_text_round1(text):
    '''Make text lowercase, remove text in square brackets,
    remove punctuation, remove read errors,
    and remove words containing numbers.'''

    text = text.lower()
    text = re.sub('\[.*?\]', ' ', text)
    text = re.sub('\[.*?\]', ' ', text)
    text = re.sub('\[.*x\]', ' ', text)
    text = re.sub('\[.*x\]', ' ', text)
    return text

round1 = lambda x: clean_text_round1(x)

# Clean Speech Text
df["text"] = df["text"].apply(round1)

# Visually Inspect
df.head()
```



Cleaned Text DataFrame Image by Anupama Garla

5. Create Function to Pre-process Data*

Here we will *lemmatize* all the words in the speeches so that different forms of a particular word will be reduced to a base form, for instance noun plurals become singular and all verb tenses become present. This simplifies the text so that repeated instances of slight variations of a word are interpreted as one word. One can stem or lemmatize, more info here. The other thing we are doing here is isolating the speech text to a particular part of speech — nouns. You can experiment with different parts of speech isolation but I have found most success with nouns in this particular dataset. More info on how to select parts of speech with 'pos' (part of speech) tagging here. This is a step you can skip if you want to setup a basic pipeline first and then you can add it in when you iterate to find what works best with your dataset.

```
# Noun extract and lemmatize function
def nouns (text):
    '''Given a string of text, tokenize the text
    and pull out only the nouns.'''
    # create mask to isolate words that are nouns
    is noun = lambda pos: pos[:2] == 'NN'
    # store function to split string of words
    # into a list of words (tokens)
    tokenized = word tokenize(text)
    # store function to lemmatize each word
   wordnet lemmatizer = WordNetLemmatizer()
    # use list comprehension to lemmatize all words
    # and create a list of all nouns
    all nouns = [wordnet lemmatizer.lemmatize(word) \
    for (word, pos) in pos tag(tokenized) if is noun(pos)]
    #return string of joined list of nouns
```



```
data_nouns = pd.DataFrame(df.text.apply(nouns))
# Visually Inspect
data_nouns.head()
```

Nouns DataFrame Image by Anupama Garla

6. Create Document Term Matrix 'V'

Here I added some stopwords to the stopword list so we don't get words like 'America' in the topics as that is not super meaningful in this context. I also use TF-IDF Vectorizer rather than a simple Count Vectorizer in order to give greater value to more unique terms. You can learn more about TF-IDF here.

```
# Add additional stop words since we are recreating the document-term
stop noun = ["america", 'today', 'thing']
stop words noun agg = text.ENGLISH STOP WORDS.union(stop noun)
# Create a document-term matrix with only nouns
# Store TF-IDF Vectorizer
tv noun = TfidfVectorizer(stop words=stop words noun agg, ngram range
= (1,1), \max df = .8, \min df = .01)
# Fit and Transform speech noun text to a TF-IDF Doc-Term Matrix
data tv noun = tv noun.fit transform(data nouns.text)
# Create data-frame of Doc-Term Matrix with nouns as column names
data dtm noun = pd.DataFrame(data tv noun.toarray(),
columns=tv noun.get feature names())
# Set President's Names as Index
data dtm noun.index = df.index
# Visually inspect Document Term Matrix
data dtm noun.head()
```



TF-IDF Document Term Matrix DataFrame Image by Anupama Garla

7. Create Function to Display Topics*

To evaluate how useful the topics created by NMF are, we need to know what they are. Here I create a function to display the top words activated for each topic.

8. Run NMF on Document Term Matrix 'V'

Perhaps the easiest step is running NMF on the document term matrix once you have one.

```
nmf_model = NMF(2)
# Learn an NMF model for given Document Term Matrix 'V'
# Extract the document-topic matrix 'W'
```





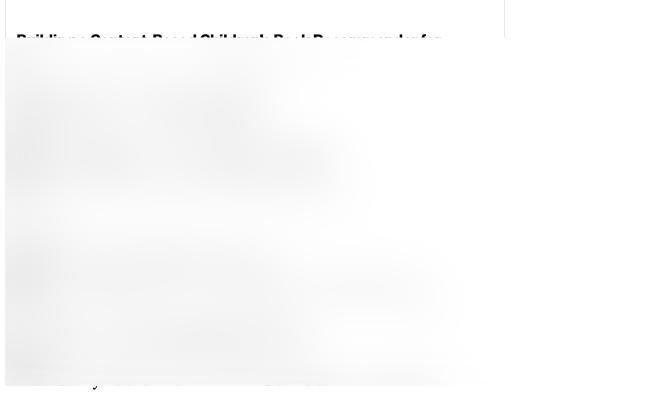
display topics (nmf model, tv noun.get feature names(), 5)

2 Topics displayed with strongest terms — Image by Anupama Garla

Further Reading 8, Iterate until you find useful Topics

This is where the art comes in. As a basic dummy model, I usually run the text through a count vectorizer and then NMF to get an idea of what we are looking TF-IDF: A visual explainer and Python implementation on the text through a threshold of the county of the same of the county of the county

On Creating a Recommendation System from NMF generated Topics



8 Topics displayed with strongest terms — Image by Anupama Garla

• LDA: Latent Dirichlet Algorithm — probability based and decomposes the corpus **Conclusions** trices. This is a generative model where you can use these smaller



However, here we can see 8 inauguration themes which could be described as — laws, peace SVD: Latent Semantic Analysis with Singular Value Decomposition — a way of leadership, spending, justice, revenue, ideals, decision-making. This is just the beginning of decomposing the document-term matrix into three smaller matrices that can be project that would investigate inauguration speeches. Some questions we can ask of these reformatted into two matrices containing both *negative and positive* unnormalized results are:

probabilities which prevents a direct interpretation of the decomposed matrices.

- Which President focussed on which topics?
 NMF: Latent Semantic Analysis with Non-Negative Matrix Factorization a way of
- decomposing the document term matrix into two smaller matrices that contain only positive values which allows *direct interpretation* of each matrix as unnormalized
- Is there in telegraphic description of the second Democratic and Republican Presidents in terms of topic focus? Is there a clear progression of topics through time?

NMF Original Paper

The opportunities are many and the process is iterative, depending on what questions you so Evans weight being resting restings and price for the suppression and present the suppression and the part of the suppression and expected as we are all living through similar challenges at this moment. Wonder what topic modeling on adjectives would yield... Lee, D., Seung, H. Learning the parts of objects by non-negative matrix factorization.

Nature 401, 788–791 (1999). https://doi.org/10.1038/44565

NMF scikit learn Documentation

It's also best to get acquainted with the toggles on your NMF algorithm in scikit learn. Dig in here once you start iterating.

Topic Supervised NMF

This method is a supervised spin on NMF and allows more user control over the topics. I haven't dug into it yet, but would love to know if anyone has!

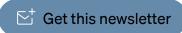
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