

$$a_t = Ux_t + Wh_{t-1} + b$$

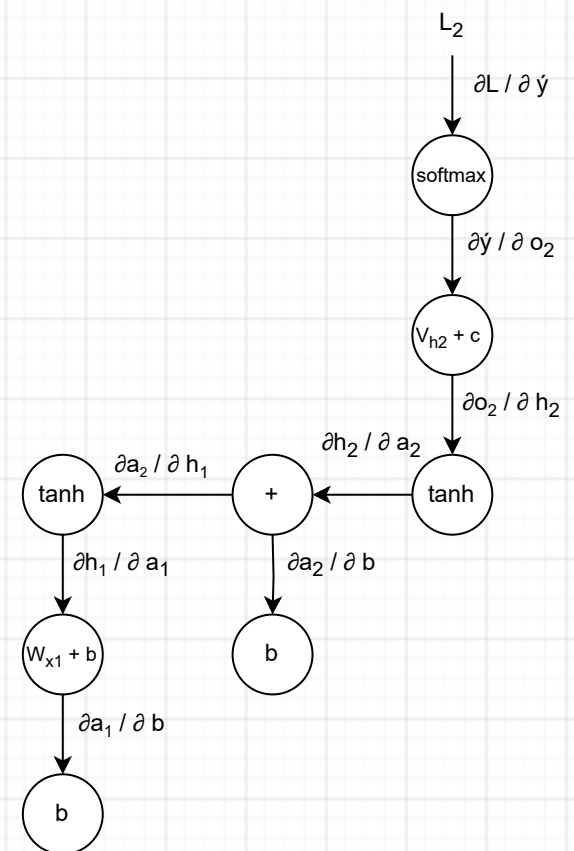
$$h_t = \tanh(a_t)$$

$$o_t = Vh_t + c$$

$$\hat{y}_t = \text{Softmax}(o_t)$$

$$L_t = \text{CE}(\hat{y}_t, y_t)$$

$$f(x) = \tanh(x) \rightarrow f'(x) = 1 - \tanh^2(x)$$



$$\frac{\partial L}{\partial b} = \left( \frac{\partial L}{\partial \hat{y}} \right) * \left( \frac{\partial \hat{y}}{\partial o_2} \right) * \left( \frac{\partial o_2}{\partial h_2} \right) * \left( \frac{\partial h_2}{\partial a_2} \right) * \left( \frac{\partial a_2}{\partial b} \right) + \left( \frac{\partial a_2}{\partial h_1} \right) * \left( \frac{\partial h_1}{\partial a_1} \right) * \left( \frac{\partial a_1}{\partial b} \right) =$$

$$= (\hat{y}_2 - y_2) * V * (1 - \tanh^2(a_2)) * (1 + W(1 - \tanh^2(a_1)))$$