

Lecture (3)

Block Ciphers

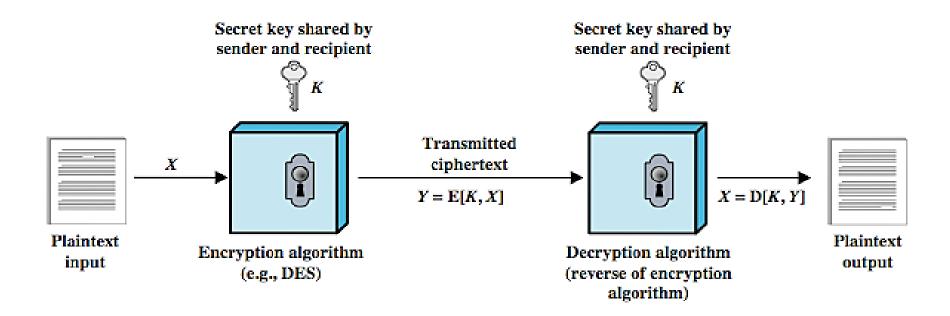
Cryptographic Tools



- □ Cryptographic algorithms important element in security services
- ☐ Review various types of elements
 - symmetric encryption
 - public-key (asymmetric) encryption
 - digital signatures and key management
 - secure hash functions
- Example is to encrypt stored data

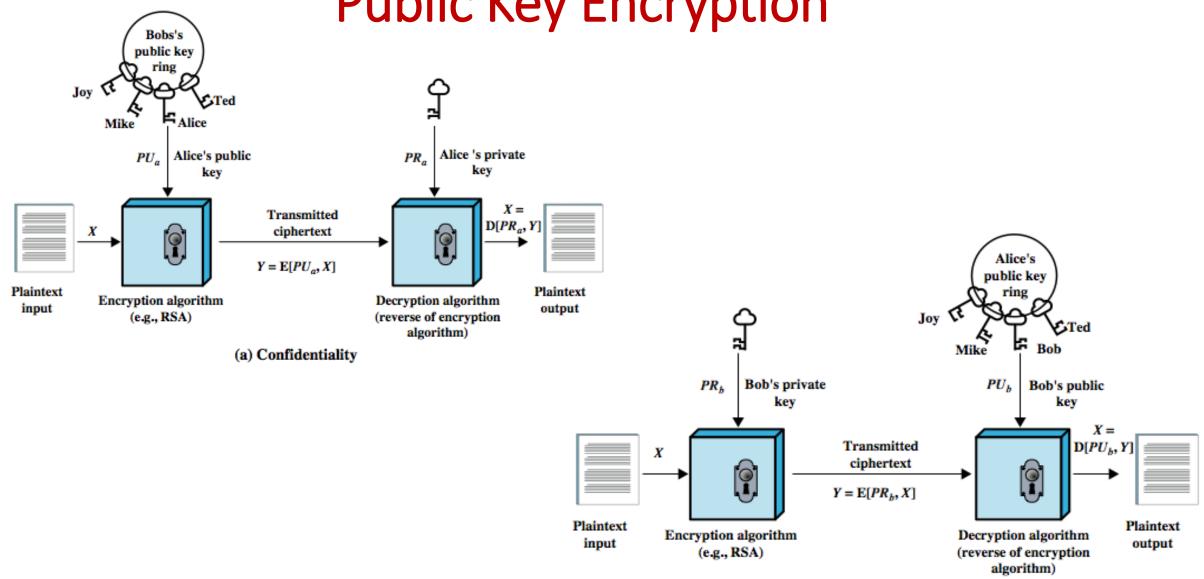
- ☐ Characterize cryptographic system by:
 - ☐ Type of encryption operations used
 - substitution / transposition / product
 - □ Number of keys used
 - single-key or private / two-key or public
 - ☐ Way in which plaintext is processed
 - block / stream

Symmetric Encryption



- Conventional / private-key / single-key
- Sender and recipient share a common key
- All classical encryption algorithms are private-key
- > Was only type prior to invention of public-key in 1970's, and by far most widely used

Public Key Encryption



(b) Authentication

Requirements

- > Two requirements for secure use of symmetric encryption:
 - a strong encryption algorithm
 - a secret key known only to sender / receiver
- Mathematically have:

$$Y = E_{\kappa}(X)$$

 $X = D_{\kappa}(Y)$

- Assume encryption algorithm is known
- Implies a secure channel to distribute key

Attacking Symmetric Encryption

Cryptanalysis

- rely on the nature of the algorithm
- plus some knowledge of plaintext characteristics
- even some sample plaintext-ciphertext pairs
- exploits characteristics of algorithm to deduce specific plaintext or key

☐ Brute-force attack

 try all possible keys on some ciphertext until get an intelligible translation into plaintext

Cryptanalysis Attacks

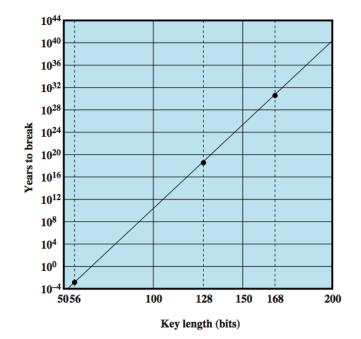
- Ciphertext only
 - only know algorithm & ciphertext, is statistical, know or can identify plaintext
- Known plaintext
 - know/suspect plaintext & ciphertext
- Chosen plaintext
 - select plaintext and obtain ciphertext
- Chosen ciphertext
 - select ciphertext and obtain plaintext (subsumes chosen plaintext)
- Related-key attack
 - Observe the operation of the encryption algorithm under different keys

Encryption Schemes

- An encryption scheme is **unconditionally secure** if the ciphertext generated by the scheme does not contain enough information to determine uniquely the corresponding plaintext, no matter how much ciphertext is available
- ☐ An encryption scheme is said to be **computationally secure** if:
 - The cost of breaking the cipher exceeds the value of the encrypted information
 - The time required to break the cipher exceeds the useful lifetime of the information

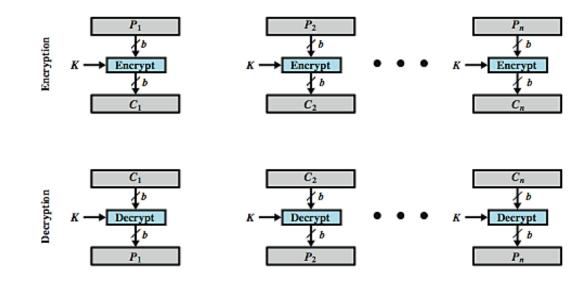
Exhaustive Key Search

Key Size (bits)	Number of Alternative Keys		equired at 1 ryption/µs	Time Required at 10 ⁶ Decryptions/μs
32	$2^{32} = 4.3 \times 10^9$	$2^{31} \mu s =$	= 35.8 minutes	2.15 milliseconds
56	$2^{56} = 7.2 \times 10^{16}$	2 ⁵⁵ μs =	= 1142 years	10.01 hours
128	$2^{128} = 3.4 \times 10^{38}$	$2^{127} \mu \text{s} =$	= 5.4 × 10 ²⁴ years	5.4 × 10 ¹⁸ years
168	$2^{168} = 3.7 \times 10^{50}$	2 ¹⁶⁷ μs =	= 5.9 × 10 ³⁶ years	5.9 × 10 ³⁰ years
26 characters (permutation)	26! = 4 × 10 ²⁶	$2 \times 10^{26} \mu \text{s} =$	= 6.4 × 10 ¹² years	6.4 × 10 ⁶ years

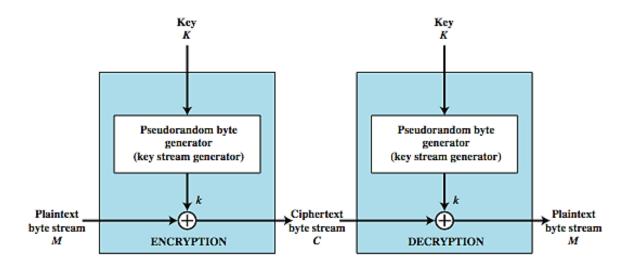


Block vs Stream Ciphers

- Block ciphers process
 messages in blocks, each of which is then en/decrypted
- Like a substitution on very big characters
 - 64-bits or more
- Stream ciphers process messages a bit or byte at a time when en/decrypting

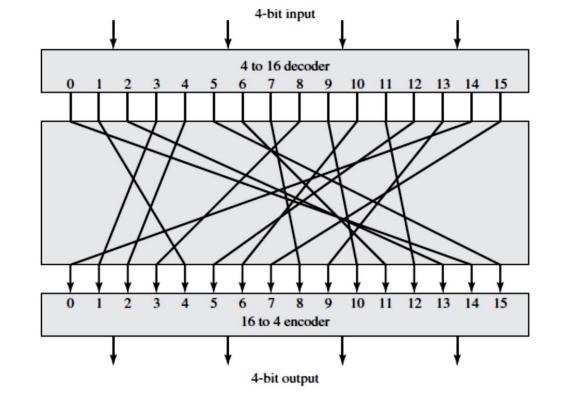


(a) Block cipher encryption (electronic codebook mode)



The Ideal Block Cipher

- The ideal block cipher provides oneto-one reversible mapping between n plaintext bits and n ciphertext bits
- □ There are 2ⁿ! possible reversible mappings
- □ They key length is $n \times 2^n$
- Ex: for n = 64, they key size is $64 \times 2^{64} = 2^{70}$
- Not practical!!



Plaintext	Ciphertext
0000	1110
0001	0100
0010	1101
0011	0001
0100	0010
0101	1111
0110	1011
0111	1000
1000	0011
1001	1010
1010	0110
1011	1100
1100	0101
1101	1001
1110	0000
1111	0111

Ciphertext	Plaintext
0000	1110
0001	0011
0010	0100
0011	1000
0100	0001
0101	1100
0110	1010
0111	1111
1000	0111
1001	1101
1010	1001
1011	0110
1100	1011
1101	0010
1110	0000
1111	0101

Shannon Substitution-Permutation Ciphers

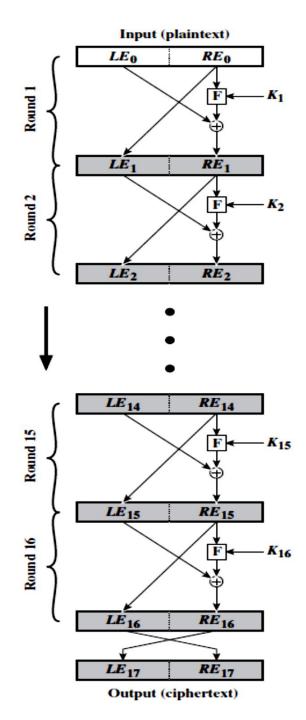
- We need to approximate the ideal block cipher using functions that are used repetitively
- Claude Shannon introduced idea of substitution-permutation (S-P) networks in 1949 paper
- Form basis of modern block ciphers
- □ S-P nets are based on the two primitive cryptographic operations seen before:
 - substitution (S-box)
 - permutation (P-box)
- Provide confusion & diffusion of message & key

Confusion and Diffusion

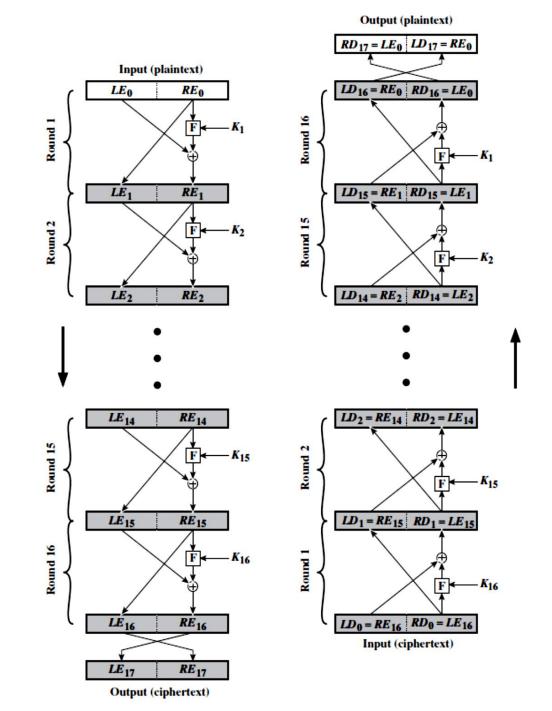
- Cipher needs to completely obscure statistical properties of original message
- A one-time pad does this
- More practically Shannon suggested combining S & P elements to obtain:
- Diffusion dissipates statistical structure of plaintext over bulk of ciphertext
- Confusion makes relationship between ciphertext and key as complex as possible

Feistel Cipher

- Horst Feistel devised the Feistel cipher
 - based on concept of invertible product cipher
- Partitions input block into two halves
 - process through multiple rounds which
 - perform a substitution on left data half
 - based on round function of right half & subkey
 - then have permutation swapping halves
- implements Shannon's S-P net concept
- Design elements of Feistel cipher include:
 - block size
 - key size
 - number of rounds
 - subkey generation algorithm
 - round function
 - fast software en/decryption
 - ease of analysis



Feistel Cipher Decryption



Advanced Encryption Standard (AES)

Requirements

- private key symmetric block cipher
- ☐ 128-bit data, 128/192/256-bit keys
- ☐ stronger & faster than Triple-DES
- ☐ active life of 20-30 years (+ archival use)
- provide full specification & design details
- □ NIST have released all submissions &
 - unclassified analyses

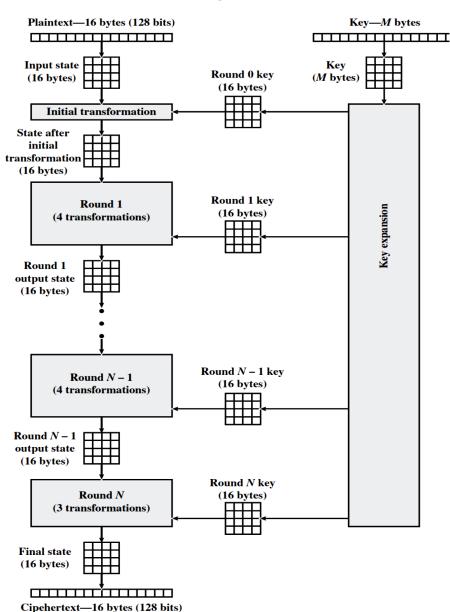
Evaluation Criteria

- > initial criteria:
 - ☐ security effort for practical cryptanalysis
 - ☐ cost in terms of computational efficiency algorithm
 - & implementation characteristics
- > final criteria:
 - ☐ general security
 - ☐ ease of software & hardware implementation
 - ☐ implementation attacks
 - ☐ flexibility (in en/decrypt, keying, other factors)

Advanced Encryption Standard (AES) - Rijndael

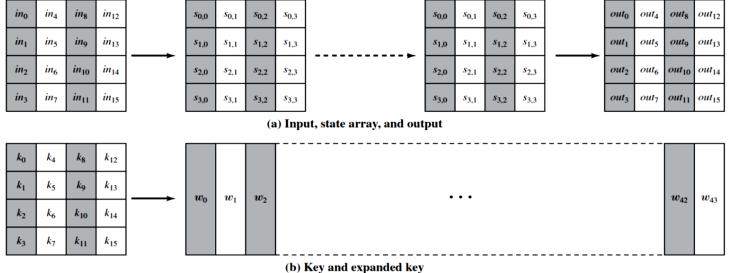
- designed by Rijmen-Daemen in Belgium
- → has 128/192/256 bit keys, 128 bit data
- an iterative rather than Feistel cipher
 - processes data as block of 4 columns of 4 bytes
 - operates on entire data block in every round
- designed to be:
 - resistant against known attacks
 - speed and code compactness on many CPUs
 - design simplicity

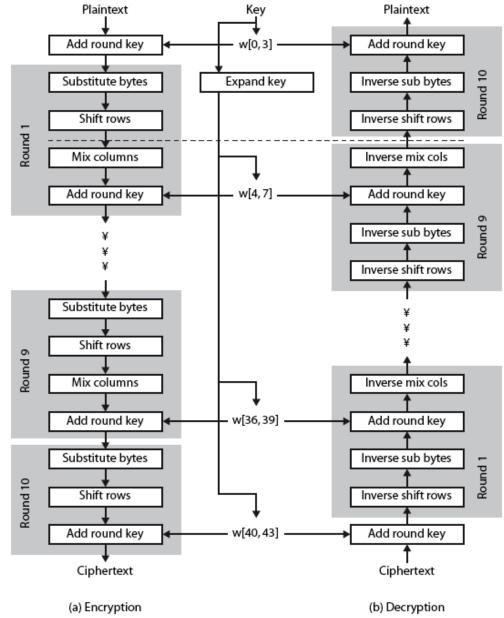
Key size (words/bytes/bits)	4/16/128	6/24/192	8/32/256
Plaintext block size (words/bytes/bits)	4/16/128	4/16/128	4/16/128
Number of rounds	10	12	14
Round key size (words/bytes/bits)	4/16/128	4/16/128	4/16/128
Expanded key size (words/bytes)	44/176	52/208	60/240



Advanced Encryption Standard (AES) - Rijndael

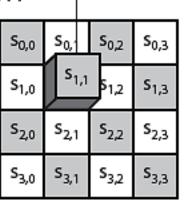
- □ data block of 4 columns of 4 bytes is state
- □ key is expanded to array of words
- → has 9/11/13 rounds in which state undergoes:
 - byte substitution (1 S-box used on every byte)
 - shift rows (permute bytes between groups/columns)
 - mix columns (subs using matrix multiple of groups)
 - add round key (XOR state with key material)
 - view as alternating XOR key & scramble data bytes
- □ initial XOR key material & incomplete last round
- with fast XOR & table lookup implementation

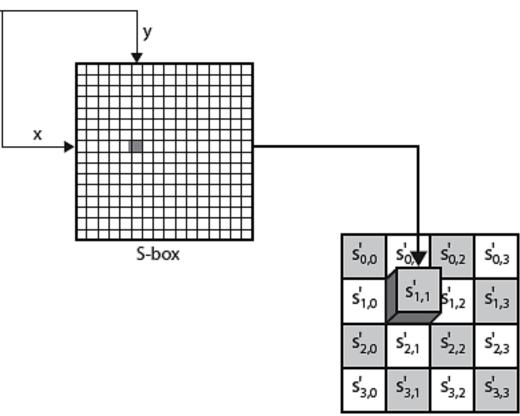




Byte Substitution

- □ a simple substitution of each byte
- □ uses one table of 16x16 bytes containing a permutation of all 256 8-bit values
- each byte of state is replaced by byte indexed by row (left 4-bits) & column (right 4-bits)
 - eg. byte {95} is replaced by byte in row 9 column 5
 - which has value {2A}
- □ S-box constructed using defined transformation of values
- designed to be resistant to all known attacks





									,	r							
		θ	1	2	3	4	5	6	7	8	9	A	В	C	D	E	F
	0	63	7C	77	7B	F2	6B	6F	C5	30	01	67	2B	FE	D7	AB	76
	1	CA	82	C9	7D	FA	59	47	F0	AD	D4	A2	AF	9C	A4	72	C0
	2	В7	FD	93	26	36	3F	F7	CC	34	A5	E5	F1	71	D8	31	15
	3	04	C7	23	C3	18	96	05	9A	07	12	80	E2	EB	27	B2	75
	4	09	83	2C	1A	1B	6E	5A	A 0	52	3B	D6	В3	29	E3	2F	84
	5	53	D1	00	ED	20	FC	B1	5B	6A	CB	BE	39	4A	4C	58	CF
	6	D0	EF	AA	FB	43	4D	33	85	45	F9	02	7F	50	3C	9F	A8
x	7	51	A3	40	8F	92	9D	38	F5	BC	B6	DA	21	10	FF	F3	D2
	8	CD	0C	13	EC	5F	97	44	17	C4	A7	7E	3D	64	5D	19	73
	9	60	81	4F	DC	22	2A	90	88	46	EE	B8	14	DE	5E	0B	DB
	Α	E0	32	3A	0A	49	06	24	5C	C2	D3	AC	62	91	95	E4	79
	В	E7	C8	37	6D	8D	D5	4E	A9	6C	56	F4	EA	65	7A	AE	08
	C	BA	78	25	2E	1C	A6	B4	C6	E8	DD	74	1F	4B	BD	8B	8A
	D	70	3E	B5	66	48	03	F6	0E	61	35	57	B9	86	Cl	1D	9E
	E	E1	F8	98	11	69	D9	8E	94	9B	1E	87	E9	CE	55	28	DF
	F	8C	A1	89	0D	BF	E6	42	68	41	99	2D	0F	B0	54	BB	16

									,	v							
		0	1	2	3	4	5	6	7	8	9	A	В	С	D	E	F
	0	52	09	6A	D5	30	36	A5	38	BF	40	A3	9E	81	F3	D7	FB
	1	7C	E3	39	82	9B	2F	FF	87	34	8E	43	44	C4	DE	E9	CB
	2	54	7B	94	32	A6	C2	23	3D	EE	4C	95	0 B	42	FA	C3	4E
	3	08	2E	A1	66	28	D9	24	B2	76	5B	A2	49	6D	8B	D1	25
	4	72	F8	F6	64	86	68	98	16	D4	A4	5C	CC	5D	65	B6	92
	5	6C	70	48	50	FD	ED	B9	DA	5E	15	46	57	A7	8D	9D	84
	6	90	D8	AB	00	8C	BC	D3	0 A	F7	E4	58	05	B8	В3	45	06
x	7	D0	2C	1E	8F	CA	3F	0F	02	C1	AF	BD	03	01	13	8A	6B
	8	3A	91	11	41	4F	67	DC	EA	97	F2	CF	CE	F0	B4	E6	73
	9	96	AC	74	22	E7	AD	35	85	E2	F9	37	E8	1C	75	DF	6E
	A	47	F1	1A	71	1D	29	C5	89	6F	B7	62	0E	AA	18	BE	1B
	В	FC	56	3E	4B	C6	D2	79	20	9A	DB	C0	FE	78	CD	5A	F4
	C	1F	DD	A8	33	88	07	C7	31	B1	12	10	59	27	80	EC	5F
	D	60	51	7F	A9	19	B5	4A	0D	2D	E5	7A	9F	93	C9	9C	EF
	E	A 0	E0	3B	4D	AE	2A	F5	B0	C8	EB	BB	3C	83	53	99	61
	F	17	2B	04	7E	BA	77	D6	26	E1	69	14	63	55	21	0C	7D

EA	04	65	85
83	45	5D	96
5C	33	98	B 0
F0	2D	AD	C5

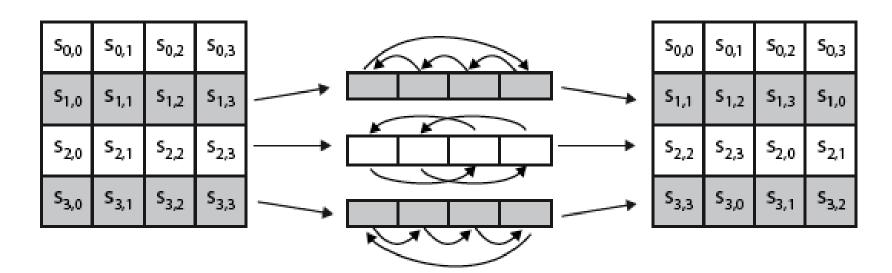
87	F2	4D	97
EC	6E	4C	90
4A	C3	46	E7
8C	D8	95	A6

Byte Substitution - Rationale

- □ Resistant to cryptanalytic attacks
- □ Low correlation between input bits and output bits
- □ No fixed points [s box(a) = a] and no opposite fixed points $[s box(a) = \bar{a}]$, where \bar{a} is the bitwise complement of a
- □ Must be invertible Is box[s box(a)] = a, but the S-box is not self-inverse s box(a) = Is box(a). Ex: [s box(95)] = a

Shift Rows

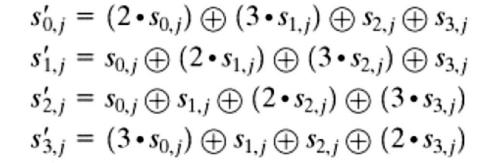
- a circular byte shift
 - 1st row is unchanged
 - 2nd row does 1 byte circular shift to left
 - 3rd row does 2 byte circular shift to left
 - 4th row does 3 byte circular shift to left
- decrypt inverts using shifts to right
- since state is processed by columns, this step permutes bytes between the columns



Mix Columns

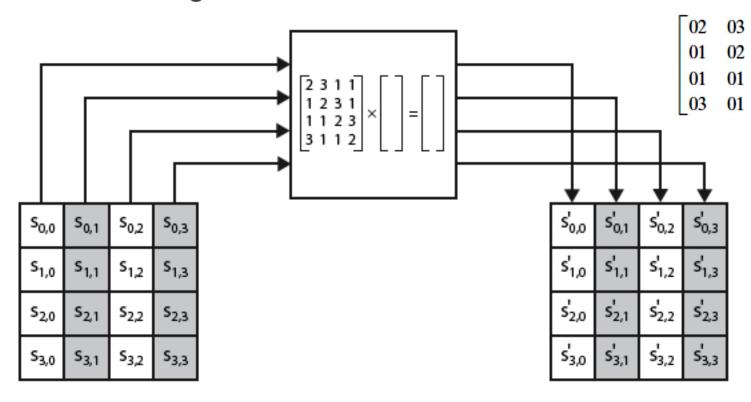
- each column is processed separately
- each byte is replaced by a value dependent on all 4 bytes in the column
- effectively a matrix multiplication
- ☐ The coefficients of the matrix ensure a good mixing among the bytes of each column by maximizing the distances between the code words.
- The mix column transformation combined with the shift row transformation ensures that after a few rounds all output bits depend on all input bits.

$$\begin{bmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{bmatrix} \begin{bmatrix} s_{0,0} & s_{0,1} & s_{0,2} & s_{0,3} \\ s_{1,0} & s_{1,1} & s_{1,2} & s_{1,3} \\ s_{2,0} & s_{2,1} & s_{2,2} & s_{2,3} \\ s_{3,0} & s_{3,1} & s_{3,2} & s_{3,3} \end{bmatrix} = \begin{bmatrix} s_{0,0} & s_{0,1} & s_{0,2} & s_{0,3} \\ s_{1,0} & s_{1,1} & s_{1,2} & s_{1,3} \\ s_{2,0} & s_{2,1} & s_{2,2} & s_{2,3} \\ s_{3,0} & s_{3,1} & s_{3,2} & s_{3,3} \end{bmatrix}$$



Mix Columns

- can express each col as 4 equations
 - to derive each new byte in col
- decryption requires use of inverse matrix
 - with larger coefficients, hence a little harder



$$s'_{0,j} = (2 \cdot s_{0,j}) \oplus (3 \cdot s_{1,j}) \oplus s_{2,j} \oplus s_{3,j}$$

$$s'_{1,j} = s_{0,j} \oplus (2 \cdot s_{1,j}) \oplus (3 \cdot s_{2,j}) \oplus s_{3,j}$$

$$s'_{2,j} = s_{0,j} \oplus s_{1,j} \oplus (2 \cdot s_{2,j}) \oplus (3 \cdot s_{3,j})$$

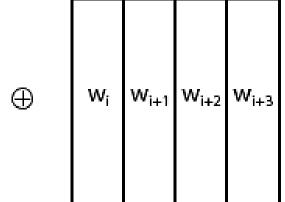
$$s'_{3,j} = (3 \cdot s_{0,j}) \oplus s_{1,j} \oplus s_{2,j} \oplus (2 \cdot s_{3,j})$$

01 $| s_{1,0} s_{1,1} s_{1,2} s_{1,3} |$

Add Round Key

- ☐ XOR state with 128-bits of the round key
- again processed by column (though effectively a series of byte operations)
- inverse for decryption identical
 - since XOR own inverse, with reversed keys
- designed to be as simple as possible
 - a form of Vernam cipher on expanded key
 - requires other stages for complexity / security

S _{0,0}	S _{0,1}	S _{0,2}	S _{0,3}
s _{1,0}	S _{1,1}	s _{1,2}	S _{1,3}
S _{2,0}	S _{2,1}	S _{2,2}	S _{2,3}
S _{3,0}	S _{3,1}	S _{3,2}	S _{3,3}



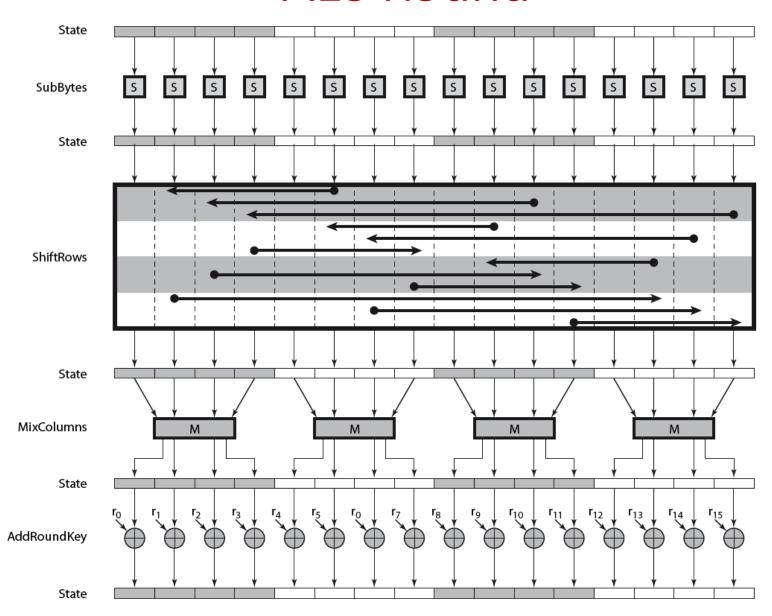
 S'_{0,0}
 S'_{0,1}
 S'_{0,2}
 S'_{0,3}

 S'_{1,0}
 S'_{1,1}
 S'_{1,2}
 S'_{1,3}

 S'_{2,0}
 S'_{2,1}
 S'_{2,2}
 S'_{2,3}

 S'_{3,0}
 S'_{3,1}
 S'_{3,2}
 S'_{3,3}

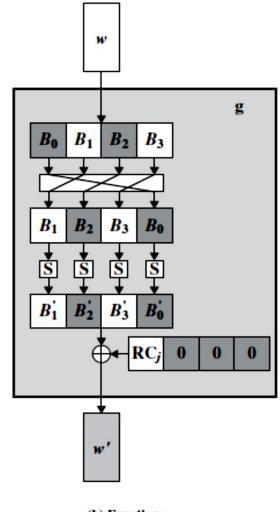
AES Round



AES Key Expansion

- takes 128-bit (16-byte) key and expands into array of 44/52/60 32-bit words
- start by copying key into first 4 words

the va	en la lue: in 3	oop s in of 4 ord	cre pre case in 4	eatir viou es ju has	ng w us & st X rota	vorc k 4 p OR t te +	ls tholac these	nat o es le e tog	back gethe	end on c r c round	w ₀ w ₁ w ₂ w ₃ (w ₄ w ₅ w ₆ w ₇
j	1	2	3	4	5	6	7	8	9	10	
RC[j]	01	02	04	08	10	20	40	80	1B	36	W44 W45 W46 W47



(b) Function g

k₅ k₉

 $k_6 | k_{10} | k_{14}$

Key Expansion Rationale

- designed to resist known attacks
- □ design criteria included
 - knowing part key insufficient to find many more
 - invertible transformation
 - fast on wide range of CPU's
 - use round constants to break symmetry
 - diffuse key bits into round keys
 - enough non-linearity to hinder analysis
 - simplicity of description

AES Decryption

- □ AES decryption is not identical to encryption since steps done in reverse
- □ but can define an equivalent inverse cipher with steps as for encryption
 - but using inverses of each step
 - with a different key schedule
- works since result is unchanged when
 - swap byte substitution & shift rows
 - swap mix columns & add (tweaked) round key

