

CSEN 1003 Compiler, Spring Term 2020
Practice Assignment 10

Exercise 10-1

Determine the types and relative addresses for the identifiers in the following sequence of declarations:

```
float x;
record ( float x; float y; ) p;
record ( int tag; float x; float y; ) q;
```

Solution:

Identifier	Relative Address	Type
x	0	<i>float</i>
p.x	8	<i>float</i>
p.y	16	<i>float</i>
p	8	<i>record</i> ([$\langle x, 0, float \rangle$; $\langle y, 8, float \rangle$])
q.tag	24	<i>integer</i>
q.x	28	<i>float</i>
q.y	36	<i>float</i>
q	24	<i>record</i> ([$\langle tag, 0, integer \rangle$; $\langle x, 4, float \rangle$; $\langle y, 12, float \rangle$])

Exercise 10-2

Assuming that function *widen* in lecture 9 slide 25 can handle any of the types in the hierarchy (a) in lecture 9 slide 23, translate the expressions below. Assume that c and d are characters, s and t are short integers, i and j are integers, and x is a float.

- a) $x = s + c.$
- b) $i = s + c.$
- c) $x = (s + c) * (t + d).$

Solution:

We assume the type of the right-side expression of an assignment to be coerced into the type of the left-side identifier.

a) `x = s + c`

Solution.

```
t1 = (int) s
t2 = (int) c
t3 = t1 + t2
t4 = (float) t3
x = t4
```

b) `i = s + c`

Solution.

```
t1 = (int) s
t2 = (int) c
t3 = t1 + t2
i = t3
```

c) `x = (s + c) * (t + d)`

Solution.

```
t1 = (int) s
t2 = (int) c
t3 = t1 + t2
t4 = (int) t
t5 = (int) d
t6 = t4 + t5
t7 = t3 * t6
t8 = (float) t7
x = t8
```

Exercise 10-3

Consider the following polymorphic function:

```
fun reverse(x) =
  if length(x)==1 then x
  else append(head(x), reverse(tail(x)))
```

What is the type of `reverse`? Show the type inferences and the unifications computed by the type inference algorithm in Lecture 9 Slide 30.

Solution:

Expression	Type	Unification
reverse	$\alpha_1 \rightarrow \beta_1$	
x	α_1	
if	$bool \times \alpha_2 \times \alpha_2 \rightarrow \alpha_2$	
length	$list(\alpha_3) \rightarrow int$	
length(x)	int	$\alpha_1 = list(\alpha_3)$
==	$\alpha_4 \times \alpha_4 \rightarrow bool$	
length(x) == 1	$bool$	$\alpha_4 = int$
x	$list(\alpha_3)$	$\alpha_2 = list(\alpha_3)$
append	$\alpha_5 \times list(\alpha_5) \rightarrow list(\alpha_5)$	
append(head(x), reverse (tail(x)))	$\alpha_2 = list(\alpha_3)$	$\alpha_5 = \alpha_3$
head	$list(\alpha_6) \rightarrow \alpha_6$	
head(x)	$\alpha_5 = \alpha_3$	$\alpha_6 = \alpha_5 = \alpha_3$
reverse(tail(x))	β_1	$\beta_1 = list(\alpha_5) = list(\alpha_3)$
tail	$list(\alpha_7) \rightarrow list(\alpha_7)$	
tail(x)	$list(\alpha_3)$	$\alpha_7 = \alpha_3$

Therefore, **reverse** has the type $list(\alpha_3) \rightarrow list(\alpha_3)$.