

Springfield Answers

Marking Scheme 2023 2NA Paper 1 EOY Exam

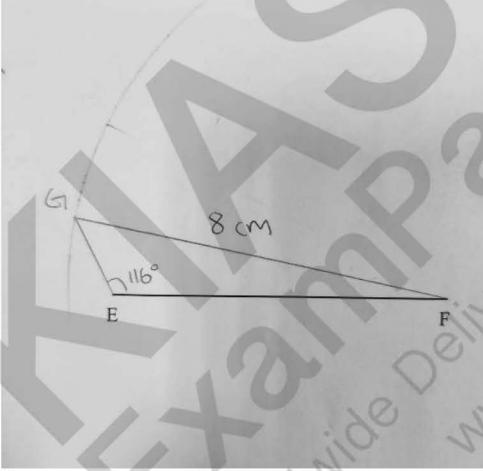
| No. | Answer | Marks | Remarks | AOs |
|-----|-----------------------------------|----------|--|-----|
| 1a | 3, -4 | B1 | | AO1 |
| 1b | $\sqrt{3}$ | B1 | | AO1 |
| 2a | $2y - 14x - 8 = 2(y - 7x - 4)$ | B1 | | AO1 |
| 2b | $x^2 - 7x - 8 = (x - 8)(x + 1)$ | M1 A1 | Award 1 mark for correct use of multiplication frame. Award full 2 marks if full working is not | AO1 |
| 3a | $-3x < -20$ $x > \frac{20}{3}$ | B1 | o.e. | AO1 |
| 3b | 7 | B1 | | AO2 |

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|----|--|----------------|---|-----|
| 4 | $\begin{aligned} 2x + 5y &= 8 & (1) \\ x + 3y &= 6 & (2) \end{aligned}$ <p>$2 \times (2):$</p> $2x + 6y = 12 \quad (3)$ <p>$(3) - (1):$</p> $(2x + 6y) - (2x + 5y) = 12 - 8$ $2x + 6y - 2x - 5y = 4$ $y = 4$ <p>Sub $y = 4$ into (2):</p> $x + 3(4) = 6$ $x = -6$ <p>$x = -6, y = 4$</p> <p><i>OR</i></p> $\begin{aligned} 2x + 5y &= 8 & (1) \\ x + 3y &= 6 & (2) \end{aligned}$ <p>From (2):</p> $x = 6 - 3y \quad (3)$ <p>Sub (3) into (1):</p> $2(6 - 3y) + 5y = 8$ $12 - 6y + 5y = 8$ $y = 4$ <p>Sub $y = 4$ into (3):</p> $x = 6 - 3(4)$ $x = -6$ <p>$x = -6, y = 4$</p> | M1 M1 A1 | Award M1 for correct subtraction of one eqn from another. Award M1 for substituting y or x into eqn. | AO1 |
| 5a | $A(-2, 3)$ $B(2, 0)$ | B1 B1 | | AO1 |

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|----|---|----------------------------------|---|-----|
| 5b | $\text{Gradient} = \frac{3-0}{-2-2}$ $= -\frac{3}{4}$ | M1 A1 | Award M1 for correct substitution Accept rise over run method. Award full 2 marks if working not shown. | AO1 |
| 6a | $p = kx$, where is k a constant. When $x = 8, p = 12$ $12 = 8k$ $k = 1.5$ $p = 1.5x$ | M1 A1 | Award if student finds k correctly. | AO1 |
| 6b | $p = 1.5 \times 25$ $p = 37.5$ | B1 | | AO2 |
| 7a | 1 cm : 0.25 km 2 km : 8 cm Length on map is 8 cm. OR 1 : 25000 Length on map = 2 km \div 25000 $= 0.00008$ km $= 8$ cm | M1 A1 [M1] [A1] | | AO2 |

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|-----|---|--------------------------------------|--|-----|
| 7b | $1 \text{ cm}^2 : 0.0625 \text{ km}^2$ $14 \text{ cm}^2 : 0.875 \text{ km}^2$ Actual area on map is 0.875 km^2 . OR Area scale: $1 : 625000000$ Actual area $= 14 \times 625000000$ $= 8750000000 \text{ cm}^2$ $= 0.875 \text{ km}^2$ | M1 A1 [M1] [A1] | | AO2 |
| 8a | $\text{Mean} = \frac{9+12+13+13+14+14+16}{7}$ $= 13$ | M1 A1 | | AO1 |
| 8b | 13 | B1 | | AO1 |
| 8c | Let the age of new student be x . $13.5 = \frac{9+12+13+13+14+14+16+x}{8}$ $108 = 91 + x$ $x = 17$ | M1 A1 | | AO2 |
| 9 | $OA = \sqrt{10^2 - 6^2}$ $= 8$ $OB = \sqrt{8^2 - 6^2}$ $= \sqrt{28}$ $AOB = \sqrt{28} + 8$ $= 13.3 \text{ (3 s.f.)}$ | M1 A1 | Award M1 for correct application of Pythagoras' theorem. | AO2 |
| 10a | $\frac{2}{5}x - 5 = \frac{3}{2}x$ $\frac{11}{10}x = -5$ $x = -\frac{50}{11}$ | M1 A1 o.e. | | AO1 |

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|-----|---|------------------------------|-----|
| 10b | $\frac{3(y-2)}{2} = \frac{y+4}{5}$ $\frac{3y-6}{2} = \frac{y+4}{5}$ $\frac{15y-30}{10} = \frac{2y+8}{10}$ $15y-30 = 2y+8$ $13y = 38$ $y = \frac{38}{13}$ <p><i>OR</i></p> $\frac{3(y-2)}{2} = \frac{y+4}{5}$ $\frac{15(y-2)}{2} = y+4$ $15(y-2) = 2(y+4)$ $15y-30 = 2y+8$ $y = \frac{38}{13}$ | M1 M1 A1 o.e. | AO1 |
| 11a | No. of yellow markers = $40 - \frac{3}{8}(40) - \frac{2}{5}(40)$ $= 40 - 15 - 16$ $= 9$ | [M1] [M1] [A1] o.e. | AO2 |
| 11b | 0 | B1 | AO1 |
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|------|---|--------------|---|-----|
| 12a | $\hat{A}BC = 180^\circ - 30^\circ - 30^\circ$ $= 120^\circ$ $\text{Ext. angle} = 180^\circ - 120^\circ$ $= 60^\circ$ <p style="text-align: center;"><i>OR</i></p> $\text{Ext. angle} = 30^\circ + 30^\circ \text{ (ext. angle of triangle)}$ $= 60^\circ$ | M1 A1 | [M1] [A1] | AO2 |
| 12b | $\text{no. of sides} = \frac{360}{60}$ $= 6$ | M1 A1 | Award M1 only if student applies correct formula with incorrect 12a | AO1 |
| 13a |  <p>Refer to diagram shown. B1 – correct length of GF with arc B1 – correct angle GEF</p> | | Deduct 1m if student does not draw correct shape with labels. | AO1 |
| 13b | $1.7 \pm 0.1 \text{ cm}$ | B1 | | AO1 |
| 13c | $11^\circ \pm 1^\circ$ | B1 | | AO1 |
| 14ai | $\hat{B}CD = 36^\circ \text{ (opp } \angle \text{ of rhombus)}$ | A1 | Overall minus 1m if wrong | AO2 |

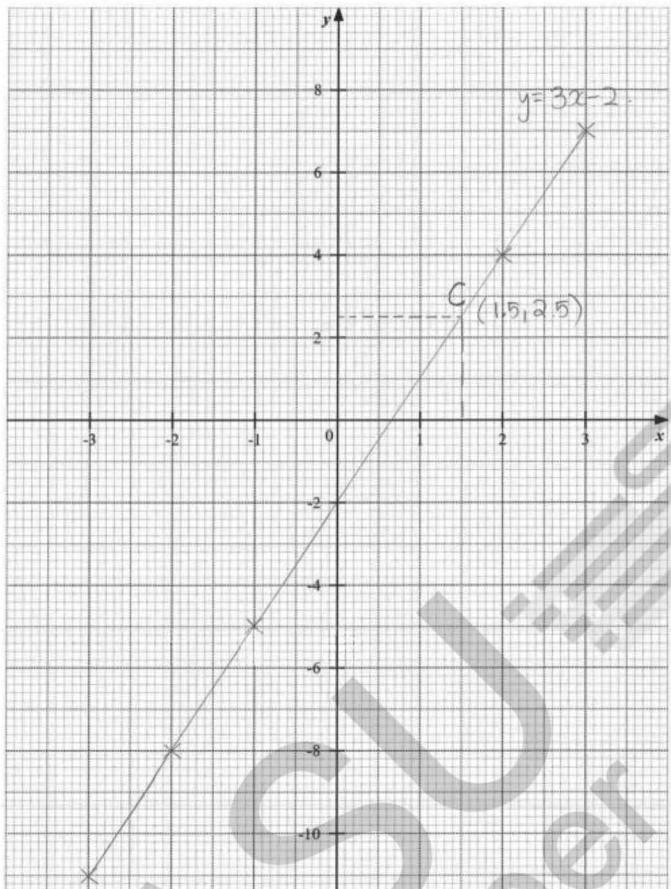
| | | | reasoning given. | |
|-------|---|------------------------------|-------------------------------------|-----|
| 14aii | $D\hat{B}C = (180^\circ - 36^\circ) \div 2$ (base \angle of isos. triangle) $= 72^\circ$ <i>OR</i> $A\hat{B}C = 180^\circ - 36^\circ$ (int. \angle AD // BC) $= 144^\circ$ $D\hat{B}C = 144^\circ \div 2$ (rhombus diagonals bisect int. angles) $= 72^\circ$ | M1 A1 [M1] [A1] | | AO2 |
| 14b | Yes. Opposite sides of a rhombus are parallel. <i>OR</i> Both opposite angles are equal. | A1 M1 | Award only if reasoning is correct. | AO3 |

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| No. | Answer | Marks | Remarks | AOs |
|-----|--|----------------|---------|-----|
| 1a | $\frac{4mn^2}{9} \div \frac{14m^2}{3}$ $= \frac{4mn^2}{9} \times \frac{3}{14m^2}$ $= \frac{2n^2}{21m}$ | M1 A1 | | AO1 |
| 1b | $2(x+3) - 3(x+4)$ $= 2x + 6 - 3x - 12$ $= -x - 6$ | M1 A1 | o.e. | AO1 |
| 2 | $\frac{3q^2 - 12q}{q^2 - 16}$ $= \frac{3q(q-4)}{q^2 - 16}$ $= \frac{3q(q-4)}{(q-4)(q+4)}$ $= \frac{3q}{q+4}$ | M1 M1 A1 | | AO1 |
| 3a | $x = 56$ | B1 | | AO1 |
| 3b | $\frac{AD}{PS} = \frac{CD}{RS}$ $\frac{12}{18} = \frac{3}{y}$ $y = 4.5$ | M1 A1 | | AO2 |
| 4a | Sub $h = 9$, $b = 7$: $9 \times 7 = 63$ $k = 63$ $hb = 63$ | M1 A1 | | AO1 |
| 4b | k is the area of the rectangle. | B1 | | AO3 |
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| 5a | $9^2 + 12^2 = 225 = 15^2$ <p>Since $AN^2 + BN^2 = AB^2$, triangle ABN is a right angled triangle.</p> | M1 A1 | Also accept "converse of Pythagoras' theorem" | AO3 | | | | | | | | | | | | |
|-------|---|-----------------|---|------|---|-------|----|-------|----|-------|----|-------|---|----|--|-----|
| 5b | $71.5 = 0.5(9)(BC)$ $BC = 15.9 \text{ (3 s.f.)}$ | M1 A1 | | AO1 | | | | | | | | | | | | |
| 6a | $5x$ | B1 | | AO2 | | | | | | | | | | | | |
| 6b | $3(x+4)$ | B1 | o.e. | AO2 | | | | | | | | | | | | |
| 6c | $5x+9=3x+12$ $x=1.5$ <p>Hence, Umairah paid:</p> $3(1.5)+12$ $=\$16.50$ | M1 M1 A1 | Award 1m for correct eqn | AO2 | | | | | | | | | | | | |
| 7ai | $p = 40 - 5 - 6 - 12 - 13$ $= 4$ | B1 | Award 1m if working is shown | AO2 | | | | | | | | | | | | |
| 7aii | <table border="1"> <caption>Data from Histogram</caption> <thead> <tr> <th>Marks</th> <th>Frequency</th> </tr> </thead> <tbody> <tr><td>0-10</td><td>5</td></tr> <tr><td>10-20</td><td>12</td></tr> <tr><td>20-30</td><td>13</td></tr> <tr><td>30-40</td><td>15</td></tr> <tr><td>40-50</td><td>4</td></tr> </tbody> </table> | Marks | Frequency | 0-10 | 5 | 10-20 | 12 | 20-30 | 13 | 30-40 | 15 | 40-50 | 4 | B1 | | AO2 |
| Marks | Frequency | | | | | | | | | | | | | | | |
| 0-10 | 5 | | | | | | | | | | | | | | | |
| 10-20 | 12 | | | | | | | | | | | | | | | |
| 20-30 | 13 | | | | | | | | | | | | | | | |
| 30-40 | 15 | | | | | | | | | | | | | | | |
| 40-50 | 4 | | | | | | | | | | | | | | | |
| 7b | <p>Estimate = $\frac{5(5) + 6(15) + 12(25) + 13(35) + 4(45)}{40} = 26.25 \text{ marks}$</p> | M1, M1 A1 | Award M1 for mid values used Award M1 for correct formula used | AO2 | | | | | | | | | | | | |

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|-----|---|----------------------------|------------------------------------|-----|
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| 8a | Sum of interior angles = $(13 - 2) \times 180^\circ$ = 1980° | M1 A1 | | AO1 |
| 8b | $1980 - 72 = 1908$ $x = \frac{1908}{12}$ = 159 | M1 A1 | | AO2 |
| 9a | Maximum no. of cans = $2 \times 3 \times 1$ = 6 | B1 | Award if student shows both steps. | AO2 |
| 9b | No. of large boxes needed = $216 \div 18$ = 12 Total cost for 12 large boxes = $12(\$1.20) + \5 = \$19.40 No. of medium boxes needed = $216 \div 6$ = 36 Total cost for 36 medium boxes = $36(\$0.50)$ = \$18 He should use the medium boxes as they are cheaper. | M1 M1 M1 M1 A1 | | AO3 |
| 10a | $a = -8$ | B1 | | AO1 |
| 10b | Refer to graph attached. Plotting at least 2 points correctly. Straight line that passes through all plotted points. | B1 B1 | | AO1 |
| 10c | Refer to graph attached. Point C labelled correctly at (1.5, 2.5). | B1 | | AO1 |
| 10d | (0, -2) | B1 | | AO1 |



Graph for Q10.

Section B (2 choose 1)

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|--------|--|----------|--|-----|
| | | | | |
| 11ai | 21 students | B1 | | AO1 |
| 11aii | 57 marks | B1 | | AO1 |
| 11aiii | 44 marks | B1 | | AO1 |
| 11bi | $\text{Probability} = \frac{14}{21}$ $= \frac{2}{3}$ | B1 | | AO1 |
| 11bii | $\text{Percentage} = \frac{11}{21} \times 100$ $= 52.4\% \text{ (3 s.f.)}$ | M1 A1 | | AO2 |
| 11d | 4 | B2 | | AO2 |
| 12a | ABGD: Trapezium BEFG: Kite | B2 | | AO1 |

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|-----|---|--------------------------------------|---|-----|
| 12b | $H\hat{C} = C\hat{B}J$ (diagonals bisect kite) $= 27^\circ$ $B\hat{G}E = 180^\circ - 27^\circ - 90^\circ$ (\angle sum of triangle) $= 63^\circ$ | M1 M1 A1 | Award if student subtracts $^{\circ}90$ | AO2 |
| 12c | $A\hat{B}J = 90^\circ + 27^\circ$ $= 117^\circ$ | B1 | | AO1 |
| 12d | $C\hat{J}B = 360^\circ - 77^\circ - 90^\circ - 117^\circ$ (\angle sum of quad.) $= 76^\circ$ <i>OR</i> $H\hat{D}G = 90^\circ - 77^\circ$ $= 13^\circ$ $C\hat{J}B = 13^\circ + 63^\circ$ (ext. \angle of triangle) $= 76^\circ$ | M1 A1 [M1] [A1] | | AO2 |