

# Lab Report

## Week 9/10

```
function out = fcos(t)
    out = cos(pi*t);
```

```
>> quad('fcos',0,5)
```

```
ans =
```

```
2.2204e-16
```

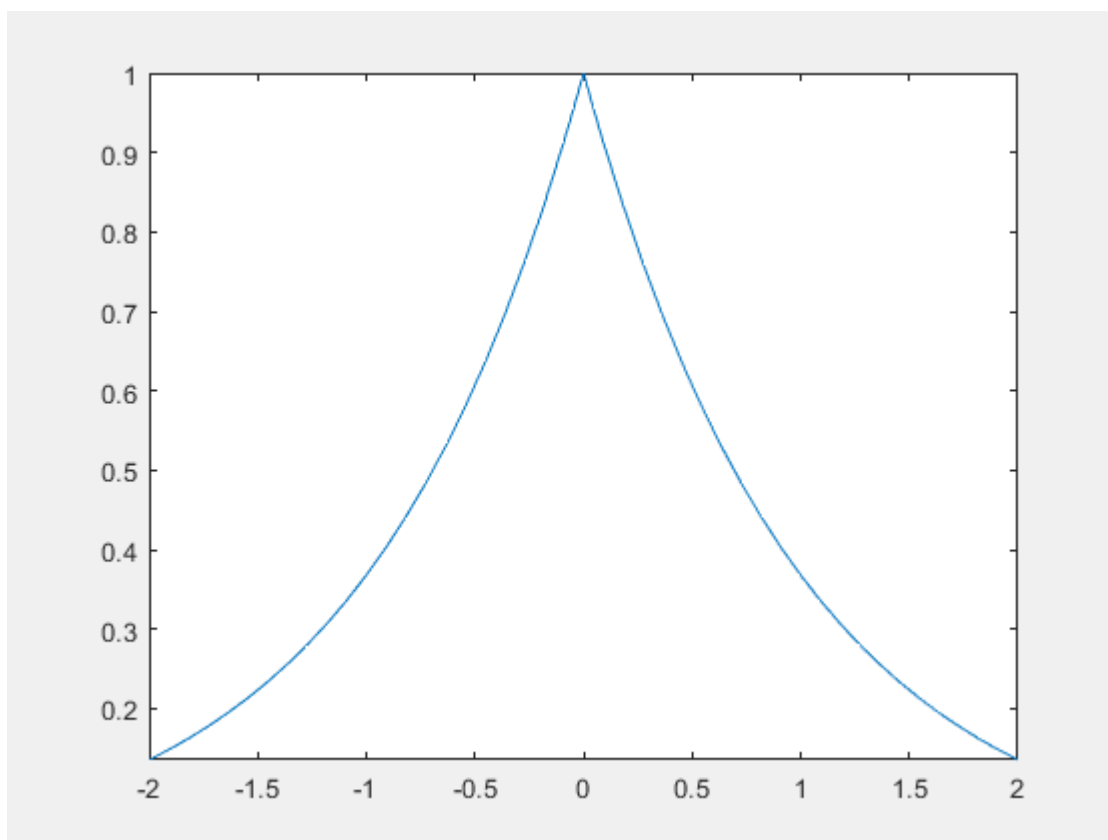
```
function out = fexp(t)
    out = exp(-abs(t));
```

```
>> quad('fexp',-2,2)
```

```
ans =
```

```
1.7293
```

```
>> fplot(@fexp,[-2,2])
```



```
>> feval('fcos',0:0.25:2)
```

ans =

Columns 1 through 5

1.0000 0.7071 0.0000 -0.7071 -1.0000

Columns 6 through 9

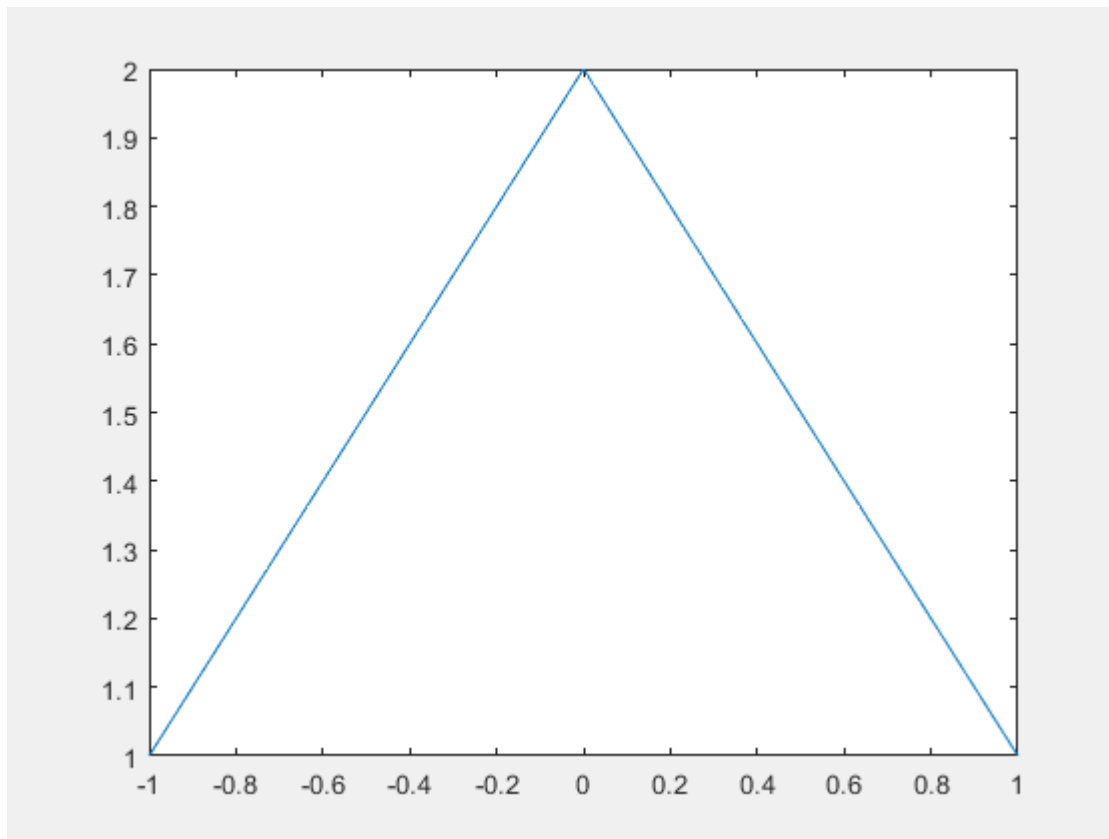
-0.7071 -0.0000 0.7071 1.0000

```
>> quad(inline('cos(pi*t)'),0,5)
```

ans =

2.2204e-16

```
>> fplot(inline('2 - abs(t)'),[-1,1])
```



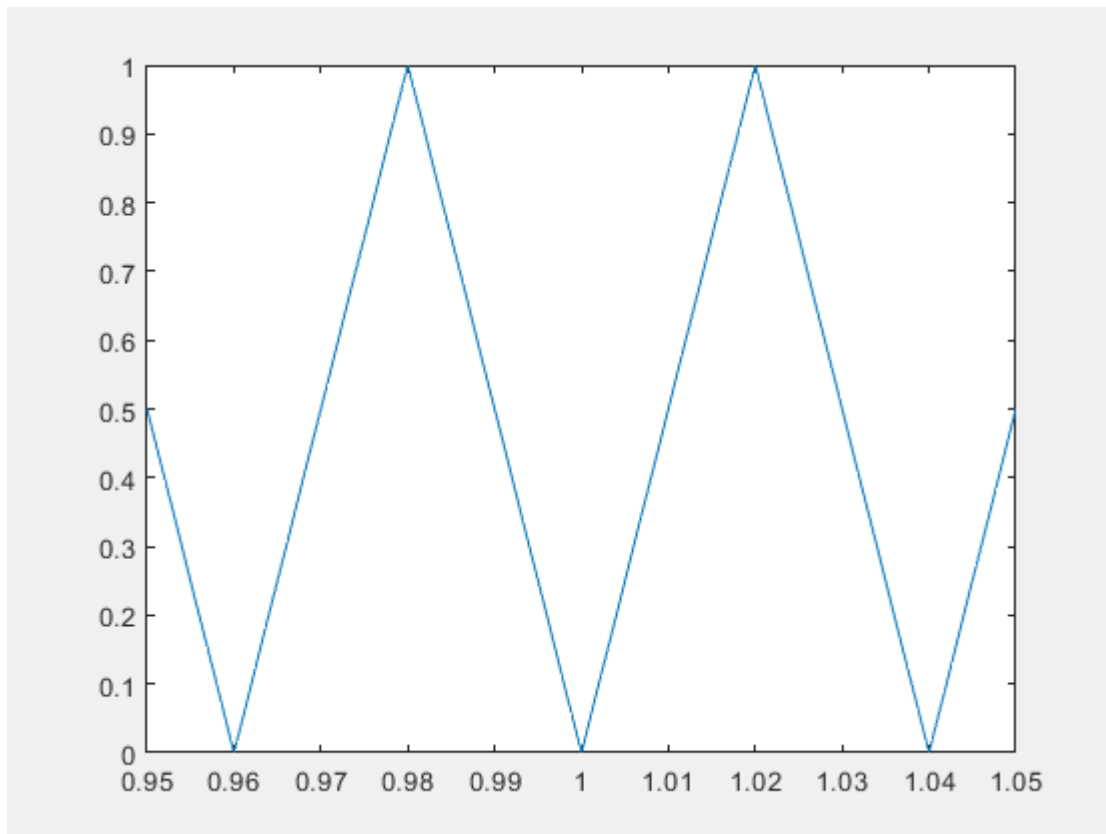
```
>> quad(inline('2 - abs(t)'),-1,1)
```

ans =

3

```
function out = triwave(tt)
    tt = mod(tt,0.04);
    out = (50*tt).*((tt >=0) - (tt >= 0.02)) + (2 - 50*tt).*((tt >= 0.02) - (tt >= 0.04));
```

```
>> fplot(@triwave,[0.96,1.05])
```



```
>>
fplot(inline('A*cos(pi*alfa*t.*t)','t','A','alfa'),[0,1],200,[],[],100,13)
Error using fplot (line 149)
Invalid parameter ' '.
```

```
>> quad(inline('A*cos(pi*alfa*t.*t)','t','A','alfa'),0,1,[],[],100,13)
```

```
ans =
```

```
9.8208
```

## Lab Assessable Exercises

```
>> quad(@FSC, 0, 1/100)

ans =

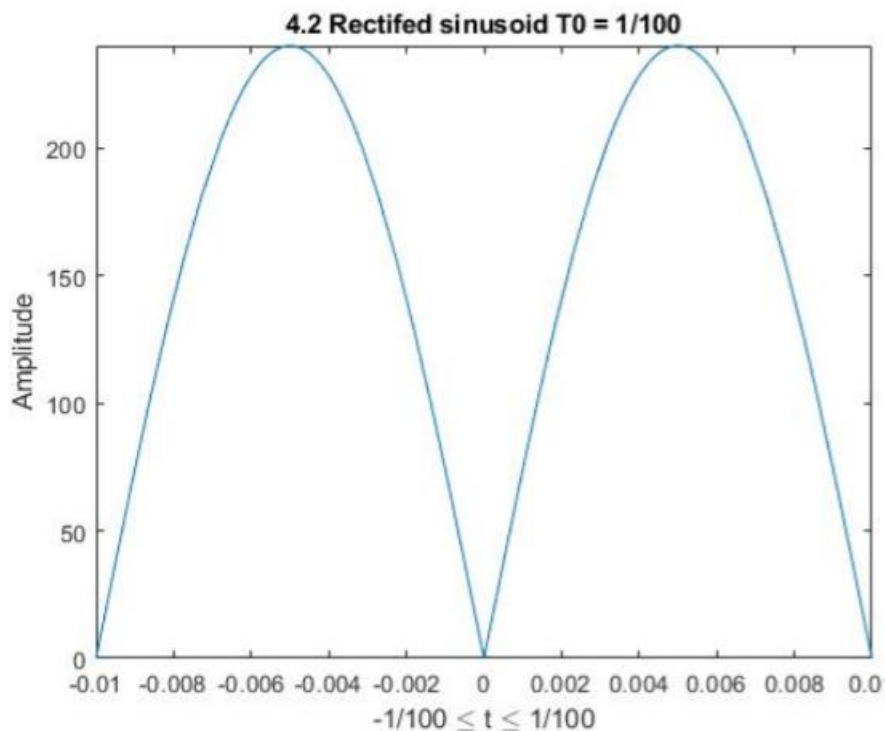
1.5279
```

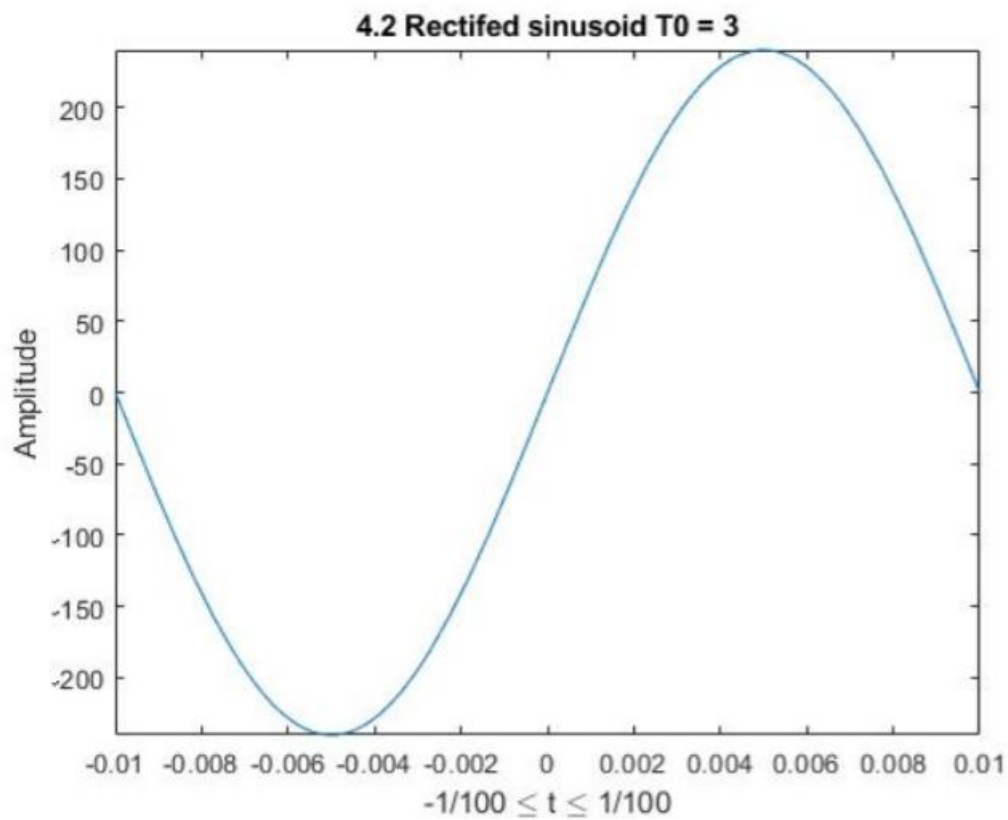
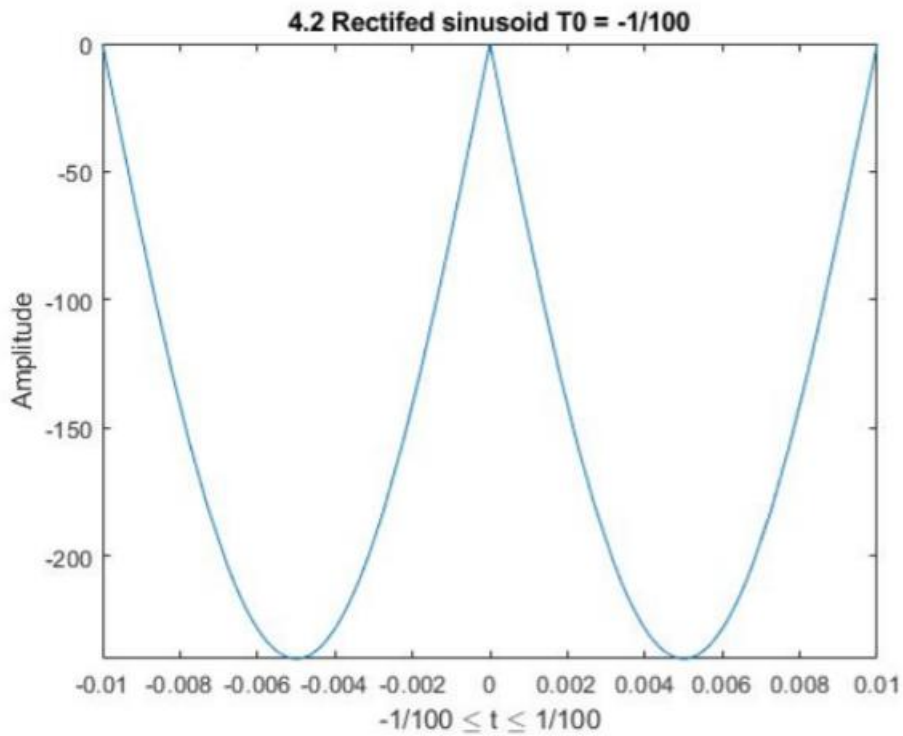
```
function out = FSC(t)
    out = 240*sin(100*pi*t);
```

```
function [xx,tt] = synthApprox(fK, xK, fs, duration, ts)
    xK=xK(:); fK=fK(:);
    tt=ts:(duration/fs):ts+duration;
    xx=real( (xK.')*exp((j*(2*pi*fK))*tt) );
```

```
function xx = syn_fourier(tt, aK, fK)
%SYN_FOURIER Function to synthesize a sum of complex
%              exponentials over the time range given by tt
%
%  usage:
%      xx = syn_fourier(tt, ak, fk)
%      tt = vector of times, for the time axis
%      ak = vector of complex Fourier coefficients
%      fk = vector of frequencies
%           (usually contains both negative and positive freqs)
%      xx = vector of synthesized waveform values
%
%  Note: fk and ak must be the same length.
%        ak(1) corresponds to frequency fk(1),
%        ak(2) corresponds to frequency fk(2), etc.
%
%  Note: the output might have a tiny imaginary part even if it
%        is supposed to be purely real.  If so, take the real part.
%
xx = exp( tt(:)*(2i*pi*fK(:)') ) * aK(:);
if( max(abs(imag(xx)))<1e-6 ), xx = real(xx); end
size(tt)
xx = xx';
```

```
function out = FSC(t)      >> quad(inline('240*sin(100*pi*t)'), T1, T2)
out = 240*sin(100*pi*t);
```





```
fplot(@fscMOD, [-1/100 1/100]); title('4.2 Rectified sinusoid  $T_0 = 1/100$ '); xlabel('-1/100 \leq t \leq 1/100'); ylabel('Amplitude');
fplot(@fscMOD, [-1/100 1/100]); title('4.2 Rectified sinusoid  $T_0 = 3$ '); xlabel('-1/100 \leq t \leq 1/100'); ylabel('Amplitude');
fplot(@fscMOD, [-1/100 1/100]); title('4.2 Rectified sinusoid  $T_0 = -1/100$ '); xlabel('-1/100 \leq t \leq 1/100'); ylabel('Amplitude');
```

```
>> quad(@fscMOD, -1/100, 1/100)
```

```
ans =
```

```
-3.0558
```

```
function out = integrandXte(t,k)
    out = aK(t).*exp(-1i*2*pi*k*t/4);
```

```
function out = ak(t)
    t_t = mod(t,4);
    out = 3*((t_t>=0)-(t_t>=1)) - 2*((t_t>=1) - (t_t>=4));
```

```
T = 1/120;
ft = pi/T;
N = 8;
k_k = -N:N;
for k=1:length(k_k)
    wk = 2*pi*k_k(k)/T;
    integrand = inline('sin(ft*t).*exp(-j*wk*t)','t','ft','wk');
    X(k) = (1/T)*integral(integrand,0,T,[],[],ft,wk);
    Kf = k_k(k)+(k_k(k)==0);
    a(k) = T*((j*Kf*pi+1)*exp(j*Kf*pi) - 1)/(4*pi*pi*Kf*Kf);
    if k_k(k)==0, a(k)=2;end
end
tt = linspace(-T,T,1001)';
xx = real( exp(j*2*pi*tt*k_k/T)*(X.') );
```

## Week 11/12

```
>> b = [1,3,1];
>> a = [1,5,2,7,3];
>> [r,p,k] = residue(b,a);
>> r
```

```
r =
```

```
-0.0856 + 0.0000i
 0.0496 - 0.2369i
 0.0496 + 0.2369i
-0.0135 + 0.0000i
```

```
>> p
```

```
p =
```

```
-4.8587 + 0.0000i
 0.1441 + 1.1902i
 0.1441 - 1.1902i
-0.4295 + 0.0000i
```

```
>> k
```

k =

[]

```
>> num = [1,0,4];
>> den = [1,4,7,15,31,75];
>> H1 = tf(num,den);
>> H1
```

H1 =

$$\frac{s^2 + 4}{s^5 + 4 s^4 + 7 s^3 + 15 s^2 + 31 s + 75}$$

Continuous-time transfer function.

```
>> z = [-4];
>> p = [-3,-10];
>> k = 20;
>> H2 = zpk(z,p,k);
>> H2
```

H2 =

$$\frac{20 (s+4)}{(s+3) (s+10)}$$

Continuous-time zero/pole/gain model.

```
>> s = tf('s')
```

s =

s

Continuous-time transfer function.

```
>> H3 = s*(s + 3)/(s^2 + 2*s + 8)
```

H3 =

$$\frac{s^2 + 3 s}{s^2 + 2 s + 8}$$

Continuous-time transfer function.

```
>> tf(H2)
```

ans =

$$\frac{20 s + 80}{s^2 + 13 s + 30}$$

Continuous-time transfer function.

```
>> zpk(H1)
```

ans =

$$\frac{(s^2 + 4)}{(s+3.081)(s^2 + 2.901s + 5.45)(s^2 - 1.982s + 4.467)}$$

Continuous-time zero/pole/gain model.

```
>> [num,den] = tfdata(H2,'v');
```

```
>> num
```

num =

```
0    20    80
```

```
>> den
```

den =

```
1    13    30
```

```
>> [z,p,k] = zpkdata(H1,'v');
```

```
>> z
```

z =

```
0.0000 + 2.0000i
0.0000 - 2.0000i
```

```
>> p
```

p =

```
-3.0807 + 0.0000i
-1.4505 + 1.8291i
-1.4505 - 1.8291i
0.9909 + 1.8669i
0.9909 - 1.8669i
```

```
>> k
```

k =

```
1
```

```
>> num = [2,0,5];
```

```
>> den = [1,3,2];
```

```
>> [r,p,k] = residue(num,den)
```

r =

```
-13
7
```



p =

-2  
-1

k =

2

```
>> num = [2,7,4];  
>> den = [conv(conv([1,1],[1,2]),[1,2])];  
>> [r,p,k] = residue(num,den);  
>> r
```

r =

3.0000  
2.0000  
-1.0000

```
>> p
```

p =

-2.0000  
-2.0000  
-1.0000

```
>> k
```

k =

[]

```
>> num = [8,21,19];  
>> den = [conv([0,1,2],[1,1,7])];  
>> [r,p,k] = residue(num,den)
```

r =

3.5000 - 0.4811i  
3.5000 + 0.4811i  
1.0000 + 0.0000i

p =

-0.5000 + 2.5981i  
-0.5000 - 2.5981i  
-2.0000 + 0.0000i

k =

```
[]

>> [angle,mag] = cart2pol(real(r),imag(r))

angle =

    -0.1366
     0.1366
         0

mag =

    3.5329
    3.5329
    1.0000

>> f = str2sym('sin(a*t) + cos(b*t)');
>> F = laplace(f)

F =

a/(a^2 + s^2) + s/(b^2 + s^2)

>> F = str2sym('(a*s^2)/(s^2 + b^2)');
>> f = ilaplace(F)

f =

a*dirac(t) - a*b*sin(b*t)
```

### Lab Assessable Exercises

```
>> a = [1 2 -3]; b = [1 8 12];
>> [r p k] = residue(b,a)

r =

    0.7500
    5.2500

p =

   -3.0000
    1.0000

k =
```

```
>> a = [1]; b = [1 1 1];
>> [r p k] = residue(b,a)
```

r =

[]

p =

[]

k =

1 1 1

```
>> a = [1 10]; b = [1 11 10];
>> [r p k] = residue(b,a)
```

r =

0

p =

-10

k =

1 1

```
>> a = [1]; b = [1 3.236 5.235924 5.235924 3.236 1];
>> [r p k] = residue(b,a)
```

r =

[]

p =

[]

k =

1.0000 3.2360 5.2359 5.2359 3.2360 1.0000

```
>> syms t
>> f = exp(t);
>> laplace(f)
```

ans =

$1/(s - 1)$

```
>> syms t
>> f = exp(2*t)*cos(200*pi*t)
```

f =

$\exp(2*t) \cdot \cos(200*\pi*t)$

```
>> laplace(f)
```

ans =

$(s - 2)/((s - 2)^2 + 40000*\pi^2)$

```
>> syms t
>> f = ramp(t); laplace(f)
```

ans =

$1/(2*s^2) + \text{laplace}(t*\text{sign}(t), t, s)/2$

```
>> syms t
>> f = t*exp(t);laplace(f)
```

ans =

$1/(s - 1)^2$

```
>> f = (24)/(s*(s+8))
```

```
f =
```

```
24/(s*(s + 8))
```

```
>> ilaplace(f)
```

```
ans =
```

```
3 - 3*exp(-8*t)
```

```
f =
```

```
20/(s^2 + 4*s + 3)
```

```
>> ilaplace(f)
```

```
ans =
```

```
10*exp(-t) - 10*exp(-3*t)
```

```
>> syms s
```

```
>> f = (5)/(s^2+6*s+73)
```

```
f =
```

```
5/(s^2 + 6*s + 73)
```

```
>> ilaplace(f)
```

```
ans =
```

```
(5*sin(8*t)*exp(-3*t))/8
```

```
>> syms s
```

```
>> f = (10)/(s*(s^2+6*s+73))
```

```
f =
```

```
10/(s*(s^2 + 6*s + 73))
```

```
>> ilaplace(f)
```

```
ans =
```

```
10/73 - (10*exp(-3*t)*(cos(8*t) + (3*sin(8*t))/8))/73
```