

# **Supplemental Lecture: Trade, Foreign Direct Investment, and Development**

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BU and NBER

STEG Virtual Course

# Definitions

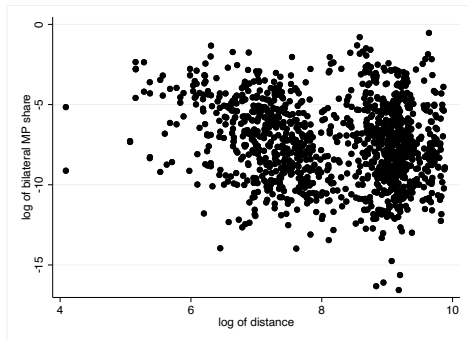
- Multinational Enterprise (MNE)
  - A firm with operations in more than one country, with 10% or more ownership
  - Parent and affiliate firms
- Foreign Direct Investment (FDI)
  - A (financial) flow in the Balance of Payment of countries
  - Equity stake of 10% or more
- Multinational Production (MP)
  - The activity of parents and affiliates (e.g., sales, employment)
  - MP by country  $i$  in  $I =$  sales of affiliates belonging to parents in  $i$  operating in  $I$

# Outline

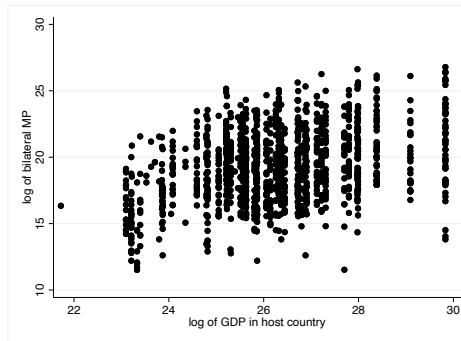
- Some facts
- Models of trade and MP
  - Melitz/Chaney: Helpman, Melitz & Yeaple (04)
  - EK: Ramondo & Rodríguez-Clare (13)
  - Krugman/Melitz/Chaney/EK: Arkolakis, Ramondo, Rodríguez-Clare & Yeaple (18)
  - Subsequent literature
  - Not today: MNE boundaries and contracts (Ántras's work)
- Empirical evidence on spillovers: state-of-the-art
  - Greenstone, Hornbeck, & Moretti (10)
  - Setzler & Tintelnot (21); Alfaro-Ureña, Manelici, & Vasquez (19, 20); Van Patten (20)

# Fact I: Bilateral MP, Market Size, and Bilateral Distance

Distance: OLS coef = -0.38 (0.065)



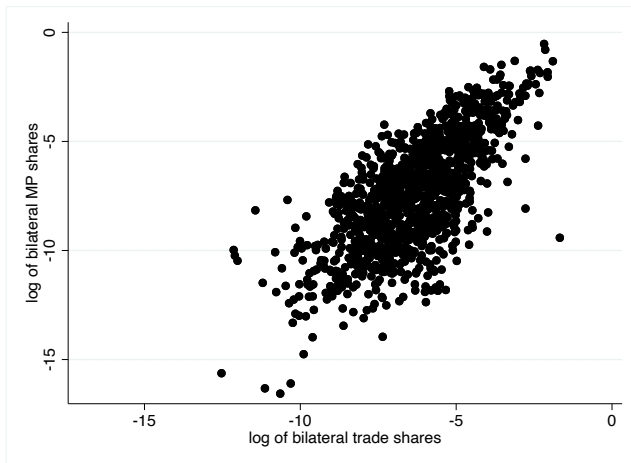
Size: OLS coef = 0.64 (0.047)



Source: Ramondo, Rodríguez-Clare, & Tintelnot (15).

Bilateral MP share = MP by  $i$  in  $l$  as a share of  $l$ 's gross output. Non-financial sectors.

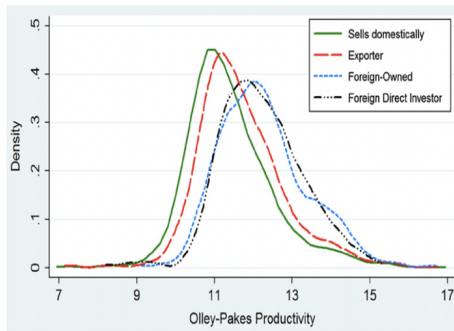
## Fact II: Trade and MP



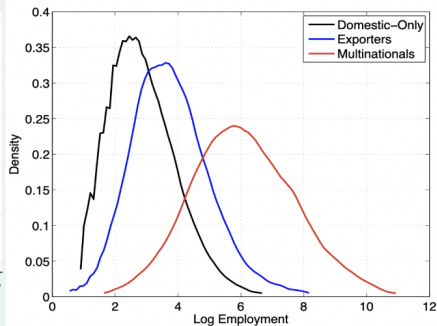
Source: Ramondo, Rodríguez-Clare, & Tintelnot (15). Correlation is 0.72.

# Fact III: MNE Advantage

Spain. 2007.



United States. 2007.

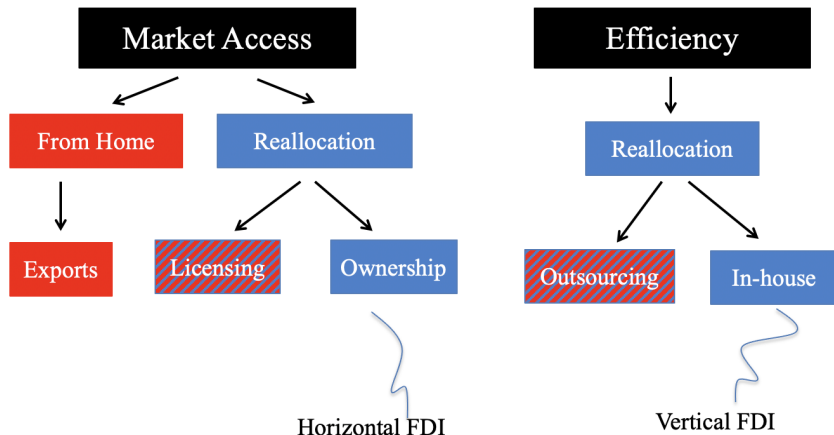


Source: Ántras and Yeaple (14) for Spain. Flaen (15) for the United States.

# Affiliate Activities: Taxonomy

- Horizontal Activities
  - Sales to the host market
  - The median US affiliate sells 66% to host market (Ramondo et al., 15)
- Export-Platform Activities
  - Sales outside the host market
  - The median US affiliate sells 34% outside host market (Ramondo et al., 15)
- Vertical Activities
  - Sales to parent company and other related parties
  - The median US affiliate sells zero to the parent (Ramondo et al., 15)

# Why Do Firms Engage in International Activities?





# The Proximity-Concentration Tradeoff

- How to serve a foreign market?
  - Export from domestic plant vs set up foreign affiliate
  - Exports and FDI are *substitute* ways of serving a foreign market
- Tradeoff
  - MP: High sunk and fixed of creating a new plant, but proximity to consumer
  - Exports: Concentrate production in one location, but far-away from consumer

# The Proximity-Concentration Tradeoff

- How to serve a foreign market?
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  - MP: High sunk and fixed of creating a new plant, but proximity to consumer
  - Exports: Concentrate production in one location, but far-away from consumer
- Evidence: Robust at the aggregate level; mixed at the firm level
  - $X_{ij}$ : Exports from  $i$ .  $S_{ij}$ : sales of foreign affiliates of MNEs from  $i$ . Industry  $j$ .

$$\log \frac{X_{ij}}{X_{ij} + S_{ij}} = \underbrace{\alpha_1}_{(-)} \log \text{trade costs}_{ij} + \underbrace{\alpha_2}_{(+)} \log \text{plant scale}_j + \beta_1 Z_i + \beta_2 Y_j + u_{ij}$$

# Multinational Production into Melitz-Chaney Model

- Proximity-concentration tradeoff at the firm and aggregate level
- Firms can transfer their productivity abroad (knowledge capital, Markusen 84)
  - Bloom, Sadun & Van Reenen (07); Giroud (13); Bilir & Morales (20)
- Firms are heterogeneous in productivity → Most productive firms choose MP
- Firms' response to the PC tradeoff is different across firms
  - Ratio of MP to export sales increases with firm heterogeneity

# Helpman, Melitz, and Yeaple (04): Set up

- N countries. Only labor.
- Continuum of varieties. CES preferences with  $\sigma > 1$ .
- Firm productivity drawn from Pareto distribution

$$\mathbb{P}(\Phi \leq \varphi) = 1 - \varphi^{-\kappa} \quad \text{with} \quad \varphi \geq 1 \quad \text{and} \quad \kappa + 1 - \sigma > 0$$

- Monopolistic competition

$$p(\varphi) = \frac{\sigma}{\sigma - 1} \frac{W_i}{\varphi}$$

- Variable trade costs from country  $i$  to  $j$ :  $\tau_{ij} \geq 1$  with  $\tau_{ii} = 1$
- Fixed export costs for country  $j$ :  $f_j^x > 0$ . Fixed MP costs for country  $j$ :  $f_j^m > 0$ .
- Additionally: fixed domestic cost  $f_i^d > 0$  and entry cost  $f_i^e > 0$

# Profits and Zero-Profit Conditions

- CES profits

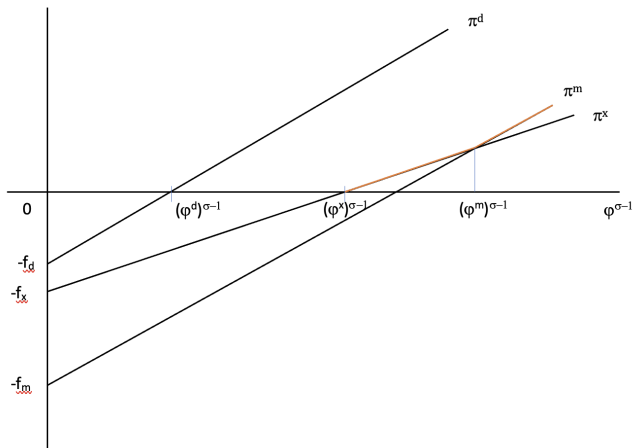
- From sales to domestic market:  $\pi_i^d(\varphi) = (W_i/\varphi)^{1-\sigma} B_i - W_i f_i^d$
- From exports to market  $j$ :  $\pi_{ij}^x(\varphi) = (\tau_{ij} W_i/\varphi)^{1-\sigma} B_j - W_j f_j^x$
- From MP sales to market  $j$ :  $\pi_{ij}^m(\varphi) = (W_j/\varphi)^{1-\sigma} B_j - W_j f_j^m$

- Zero-profit conditions and cutoff productivities

- Domestic:  $(W_i/\varphi_i^d)^{1-\sigma} B_i = W_i f_i^d$  for all  $i$
- Export:  $(W_i \tau_{ij}/\varphi_{ij}^x)^{1-\sigma} B_j = W_j f_j^x$  for all  $i \neq j$
- MP:  $\left[1 - \left(\frac{W_i}{W_j} \tau_{ij}\right)^{1-\sigma}\right] (W_j/\varphi_{ij}^m)^{1-\sigma} B_j = W_j f_j^m - W_j f_j^x$  for all  $i \neq j$

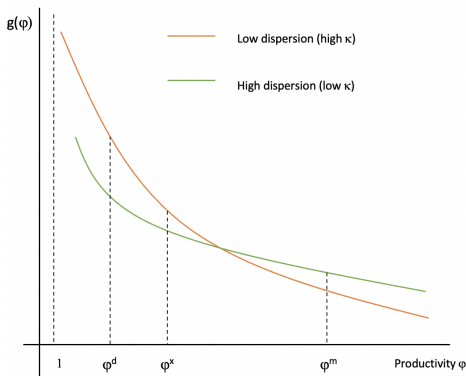
# Profits Under Symmetry

**Key assumptions:**  $f^d < \tau^{\sigma-1} f^x < f^m$ . Only horizontal flows, no export-platforms.



# Heterogeneity and the Proximity-Concentration Tradeoff

$$\frac{\text{Export sales}}{\text{MP sales}} = \tau^{1-\sigma} \left[ \frac{V(\varphi^x)}{V(\varphi^m)} - 1 \right] = \tau^{1-\sigma} \left[ \left( \frac{f^m - f^x}{f^x} \frac{1}{\tau^{\sigma-1} - 1} \right)^{\kappa+1-\sigma} - 1 \right]$$



$$V(\varphi^m) \equiv \int_{\infty}^{\varphi^m} \varphi^{\sigma-1} dG(\varphi) \quad \text{and} \quad V(\varphi^x) \equiv \int_{\varphi^m}^{\varphi^x} \varphi^{\sigma-1}$$

# Multinational Production into EK Model

- Quantitative general equilibrium EK model for trade and MP
  - Trade and MP are alternative ways to serve a market
  - Foreign affiliates import intermediates
  - A does MP in B and exports to C (“bridge” MP, BMP)
- Calibrate model to match bilateral trade and MP data
- Quantify gains from openness, trade, and MP
  - Other counterfactual exercises



# EK Trade

- $N$  countries of size  $L_n$
- Continuum of tradable goods,  $v \in [0, 1]$ , CES aggregator with  $\sigma > 1$
- Productivity  $z_l(v)$  is independent Fréchet over  $v$  and across countries  $l$

$$\mathbb{P}[Z_l(v) \leq z] = \exp[-T_l z^{-\theta}]$$

- Iceberg trade costs  $\tau_{ln} \geq 1$ , with  $\tau_{ll} = 1$ . Unit cost in  $n$  of good  $v$  produced in  $l$

$$p_{ln}(v) = \tau_{ln} \frac{W_l}{z_l(v)}$$

- Lowest cost producer of good  $v$  in country  $n$  (head-to-head competition)

$$p_n(v) = \min_l p_{ln}(v)$$

# Multinational Production (MP)

- Good  $v$  can be produced in country  $l$  with technologies from  $i$  and sold in  $n$

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- Unit cost of good  $v$  produced in  $l$  with technology from  $i$  for  $n$

$$p_{iln}(v) = \tau_{ln} \frac{c_{il}}{z_{il}(v)}$$

- $c_{il}$  = unit cost of the input bundle for MP by  $i$  in  $l$
- $z_{il}(v)$  = productivity of producing good  $v$  in  $l$  with technologies from  $i$

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- Lowest cost producer of good  $v$  in country  $n$  (head-to-head competition)

$$p_n(v) = \min_{i,l} p_{iln}(v)$$

# Multinational Input Bundle: Sourcing

- Unit cost of the input bundle for MP by  $i$  in  $I$

$$c_{il} = \left[ \sum_{k \neq I} a_{kl} (W_k \tau_{kl})^{1-\xi} + a_{II} (W_I \gamma_{il})^{1-\xi} \right]^{\frac{1}{1-\xi}} \quad \text{with} \quad \sum_k a_{kl} = 1$$

- Home sourcing

$$c_{il} = \left[ a (W_i \tau_{il})^{1-\xi} + (1-a) (W_I \gamma_{il})^{1-\xi} \right]^{\frac{1}{1-\xi}}$$

- No sourcing

$$c_{il} = W_I \gamma_{il} \quad \rightarrow \quad p_{iln}(v) = \tau_{ln} \gamma_{il} \frac{W_I}{z_{il}(v)}$$

- 'MP cost' by  $i$  in  $I$ :  $\gamma_{il} \geq 1$  with  $\gamma_{II} = 1$

# Distributional Assumption (for Aggregation)

- Productivity is *symmetric multivariate Fréchet* across  $l$ , for each  $i$

$$\mathbb{P}[Z_{i1}(v) \leq z_1, \dots, Z_{iN}(v) \leq z_N] = \exp \left[ - \left( \sum_{l=1}^N (T_{il} z_l^{-\theta})^{\frac{1}{1-\rho}} \right)^{1-\rho} \right]$$

- $\rho = 0$  corresponds to independent draws
  - $\rho \rightarrow 1$  corresponds to perfectly correlated draws
- Productivity is i.i.d. over  $v$  and across  $i$

# MV Max-Stable Fréchet and Correlation Function

$$\mathbb{P}[Z_1(v) \leq z_1, \dots, Z_N(v) \leq z_N] = \exp \left[ -G \left( T_1 z_1^{-\theta}, \dots, T_N z_N^{-\theta} \right) \right]$$

- Key property:  $G$  is homogeneous of degree 1  $\implies$  max-stability

$$\mathbb{P} \left[ \max_l Z_l(v) \leq z \right] = \exp \left[ -G \left( T_1, \dots, T_N \right) z^{-\theta} \right]$$

- The conditional and unconditional probability of the max coincide
- Key implication: probabilities equal expenditure shares
- Other properties: unboundedness; differentiability. Normalization.
- Special cases: independence (additive  $G$ ); symmetry (CES  $G$ )
- MV max-stable Fréchet is equivalent to Generalized Extreme Value (GEV) expenditure

$$\frac{X_{ln}}{X_n} = \frac{T_{ln} W_l^{-\theta} G_l(T_{1n} W_1^{-\theta}, \dots, T_{Nn} W_N^{-\theta})}{G(T_{1n} W_1^{-\theta}, \dots, T_{Nn} W_N^{-\theta})} \quad \text{where} \quad G_l(x_1, \dots, x_N) \equiv \frac{\partial G(x_1, \dots, x_N)}{\partial x_l}$$

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# Correlation Through Multinational Production

- Correlation function is cross-nested CES (CNCES)

$$\mathbb{P}(Z_{i1n}(v) \leq z_1, \dots, Z_{iNn}(v) \leq z_N) = \exp \left[ - \sum_i \left( \sum_l (T_{iln} z_l^{-\theta})^{\frac{1}{1-\rho_i}} \right)^{1-\rho_i} \right]$$

- Relax assumptions
  - Different correlation for each home country  $i$
  - More general MP and trade cost — not necessarily iceberg
  - Unit cost of producing good  $v$  in  $l$  with technologies from  $i$  to deliver to  $n$

$$\frac{W_l}{Z_{iln}(v)} \quad \text{instead of} \quad \gamma_{il} \tau_{ln} \frac{W_l}{Z_{il}(v)}$$

- Keep assumptions
  - Productivity is i.i.d. over  $v$  and across  $i$
- See Lind and Ramondo (20)

# Expenditure Shares

- Expenditure in  $n$  of goods produced in  $l$  with technologies from  $i$

$$\frac{X_{iln}}{X_n} = \underbrace{\left( \frac{P_{iln}}{P_{in}} \right)^{-\frac{\theta}{1-\rho_i}}}_{\text{within-}i \text{ expenditure}} \times \underbrace{\left( \frac{P_{in}}{P_n} \right)^{-\theta}}_{\text{between-}i \text{ expenditure}}$$

$$P_{iln}^{-\theta} \equiv T_{iln} W_l^{-\theta} \quad P_{in}^{-\frac{\theta}{1-\rho_i}} \equiv \sum_l P_{iln}^{-\frac{\theta}{1-\rho_i}} \quad P_n^{-\theta} \equiv \sum_i P_{in}^{-\theta}$$

- Special case (RRC,13):  $P_{iln}^{-\theta} \equiv T_{il}(\gamma_{il}\tau_{ln}W_l)^{-\theta}$  and  $\rho_i = \rho$

- Bilateral trade:  $X_{ln} = \sum_i X_{iln}$
- Bilateral MP:  $X_{il} = \sum_n X_{iln}$
- Total expenditure:  $X_n = \sum_i \sum_l X_{iln}$

# Gains from Trade: Sufficient-Statistic Approach

- Gains from trade for GEV class

$$GT_n \equiv \frac{W_n/P_n}{W_n^A/P_n^A} = \left( \frac{X_{nn}/X_n}{G_{nn}} \right)^{-\frac{1}{\theta}} \quad \text{where} \quad G_{nn} \equiv \frac{\partial G(P_{1n}^{-\theta}, \dots, P_{Nn}^{-\theta})}{\partial P_{1n}^{-\theta}}$$

- Gains from trade are lower than under independence
- Under independence,  $G(x_1, \dots, x_N) = \sum_I x_I$  and  $G_{nn} = 1 \rightarrow \text{CES-ACR}$

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- Gains from trade for CNCES subclass

$$GT_n = \left( \frac{\sum_i X_{inn}}{X_n} \right)^{-\frac{1}{\theta}} \left[ \sum_i \left( \frac{X_{inn}}{\sum_{i'} X_{i'nn}} \right) \left( \frac{X_{inn}}{\sum_l X_{iln}} \right)^{-\rho_i} \right]^{-\frac{1}{\theta}}$$

# Gains from Trade, MP, and Openness

- Gains from trade\* (isolation to trade) and Gains from MP\* (isolation to MP)

$$GT_n^* = \left( \frac{X_{nnn}}{\sum_l X_{nl n}} \right)^{-\frac{1}{\theta}} \quad GMP_n^* = \left( \frac{X_{nnn}}{\sum_i X_{inn}} \right)^{-\frac{1}{\theta}}$$

- Gains from trade (only MP to trade and MP)

$$GT_n = \left( \frac{\sum_i X_{inn}}{X_n} \right)^{-\frac{1}{\theta}} \left[ \sum_i \left( \frac{X_{inn}}{\sum_{i'} X_{i' nn}} \right) \left( \frac{X_{inn}}{\sum_l X_{il n}} \right)^{-\rho_i} \right]^{-\frac{1}{\theta}}$$

- Gains from MP (only trade to trade and MP)

$$GMP_n = \frac{GT_n}{GT_n^*} GMP_n^*$$

- Gains from openness (isolation to trade and MP)

$$GO_n = \left( \frac{X_{nnn}}{X_n} \right)^{-\frac{1-\rho_n}{\theta}} \left( \frac{\sum_l X_{nl n}}{X_n} \right)^{-\frac{\rho_n}{\theta}}$$

# Trade and MP: Complements or Substitutes?

- Definitions
  - Trade is MP-complement when  $GT_n > GT_n^*$
  - Trade is MP-substitute when  $GT_n < GT_n^*$
  - Trade is MP-independent when  $GT_n = GT_n^*$
- For intuition, calculate gains in a symmetric world (with home imports)
  - For  $a = 0$ :  $\rho = 0$ : Trade is MP-independent
  - For  $a = 0$ :  $0 < \rho < 1$ : Trade is MP-substitute
  - For  $a > 0$ :  $\rho = 0$ : Trade is MP-complement
  - For  $\xi \rightarrow 1$  ( $\xi \rightarrow \infty$ ): Trade is MP-complement (MP-substitute)

# Full Quantitative Model

- Tradable intermediate goods  $v \in [0, 1]$ , CES aggregator with price index  $P_n^g$ 
  - unit cost of MP by  $i$  in  $n$  is  $c_{in}$  (imports from home)
- Non-tradable final goods  $u \in [0, 1]$ , CES aggregator with price index  $P_n^f$ 
  - unit cost of MP by  $i$  in  $n$  is  $c_n^f \gamma_{in}^f$  (no imports from Home), with  $\gamma_{in}^f = \mu \gamma_{il}^g$
- Input-output loop

$$c_n^g = BW_n^\beta (P_n^g)^{1-\beta} \quad \text{and} \quad c_n^f = AW_n^\alpha (P_n^g)^{1-\alpha}$$



# Calibration Procedure

- Bilateral trade and MP costs

Alt. 1 Trade and MP costs are functions of, e.g., distance. Target observed bil. trade and MP

Alt. 2 Set trade and MP costs to exactly match observed bil trade and MP

Alt. 3 Given MP & trade shares, unique set of  $X_{iln}$ . Assume symmetric costs and compute

$$\left( \sqrt{\frac{X_{inn}X_{ill}}{X_{iln}X_{inl}}} \right)^{\frac{1-\theta}{\rho}} = \tau_{ln}\tau_{nl} \quad \left( \sqrt{\frac{X_{iin}X_{iin}}{X_{iln}X_{lin}}} \right)^{\frac{1-\theta}{\rho}} = \gamma_{li}\gamma_{il}$$

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- For  $\theta$ , target 'unrestricted' gravity OLS coefficient  $\beta^u \neq \theta$

$$\ln X_{ln} = I_l + I_n + \beta^u \ln \tau_{ln} + u_{ln}$$

- For  $\rho$ , target 'restricted' gravity (to origin  $i$ ) OLS coefficient  $\beta^r = -\frac{\theta}{1-\rho}$

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$$\ln X_{iln} = I_{il} + I_{in} + \beta^r \ln \tau_{ln}$$

- Set  $T_i = \phi_i L_i$  where  $\phi_i$  is R&D employment share and  $L_i$  equipped labor in the data
- For CES weights in MP input bundle ( $a$ 's), target affiliates' intermediate (intra-firm) imports
- Remaining parameters from the literature (important: MP input-bundle CES elasticity  $\xi$ )

# Krugman-Melitz-Chaney Meets EK: Motivation

- Goods increasingly produced far from where ideas are created
  - Key: the rise of multinational production (MP)
- Some countries specialize in innovation; others specialize in production
  - Countries specialized in production worry about low innovation rates
  - Countries specialized in innovation worry about loss of production jobs

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  - Countries specialized in innovation worry about loss of production jobs
- Quantitative general equilibrium model with innovation and production
  - Specialization reflects comparative advantage & home market effects
  - Expansion of production may trigger deterioration of ToT (Venables, 87)
  - Countries may lose from openness

# Krugman-Melitz-Chaney Meets EK: Ingredients

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  - Iceberg trade  $\tau_{ln}$  and MP costs  $\gamma_{il}$ . Fixed export costs,  $W_n F_n$
- Continuum of varieties  $v \in [0, 1]$ . CES preferences with  $\sigma > 1$ . Monopolistic competition.

# The Multivariate Pareto Distribution

$$\mathbb{P}(z_1, \dots, z_N) = 1 - \left( \sum_{l=1}^N [T_{il} z_l^{-\theta}]^{\frac{1}{1-\rho}} \right)^{1-\rho}$$

$$\text{where } z_l \geq \tilde{T}_i^{1/\theta} \quad \text{and} \quad \tilde{T}_i \equiv \left[ \sum_l T_{il}^{1/(1-\rho)} \right]^{1-\rho}$$

- $\theta > \sigma - 1$  regulates heterogeneity over varieties (firms)
- $\rho \in [0, 1)$  regulates heterogeneity across locations
- $T_{il} = T_i^e T_l^p$ : Country  $i$  has CA in innovation if  $T_i^e / T_i^p$  is relatively high

# Firm's Problem and Aggregation

- Unit cost for firm  $z$  from country  $i$  serving  $n$  from  $l$ :

$$C_{iln} = \frac{\gamma_{il} W_l \tau_{ln}}{z_l}$$

- Firm  $i$  chooses cheapest production location for each  $n$ :

$$l = \arg \min_v C_{ivn}$$

- Firm  $i$  chooses to serve market  $n$  if

$$\pi_n(C_{iln}) - w_n F_n \geq 0 \implies C_{iln} \leq c_n^*$$

- MVP gives us closed-form for  $\mathbb{P}(\arg \min_k C_{ikn} | \min_k C_{ikn} \leq c_n^*)$  and (aggregate) flows
- Firm level: proximity-CA tradeoff. Aggregate level: proximity-concentration tradeoff

# Innovation Shares, Specialization, and Trade Imbalances

- Innovation share

$$r_i \equiv \frac{W_i L_i^e}{X_i} = \eta + \frac{\sigma - 1}{\sigma} \frac{X_i - Y_i}{X_i}$$

- $Y_i$ : total production in  $i$ .  $X_i$ : total expenditure of  $i$
- $\eta$ : sales' share of profits (net of marketing costs)
- $r_i = \eta$  in autarky (or MP-autarky)

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  - $r_i = \eta$  in autarky (or MP-autarky)
- A trade deficit ( $X_i > Y_i$ ) implies specialization in innovation ( $r_i > \eta$ )
  - Import goods to repatriate profits from MP. Innovation hub
- A trade surplus ( $X_i < Y_i$ ) implies specialization in production ( $r_i < \eta$ )
  - Export goods to send profits from MP abroad. Production hub.

# The Gains from Openness

$$GO_n = \underbrace{\left( \frac{\sum_l X_{nl n}}{X_n} \right)^{-\frac{\rho}{\theta}} \left( \frac{X_{nnn}}{\sum_l X_{nl n}} \right)^{-\frac{1-\rho}{\theta}}}_{\text{Direct Effect}} \times \underbrace{\left( 1 + \theta \frac{X_n - Y_n}{Y_n} \right)^{1/\theta}}_{\text{Indirect Effect}}$$

- Indirect effect (due to innovation) can induce losses:  $GO_n < 1$ 
  - Countries that lose innovation experience ToT deterioration
- Additional results
  - Countries can lose from more openness to trade or MP
  - Both production and innovation workers can lose from more liberalization

# Useful Isomorphisms (Online Appendix in ARRY)

1. MV Pareto productivity  $\equiv$  Firm-specific Pareto productivity  $\times$   
Firm-location-specific independent Fréchet productivity:  $\varphi z_l$

$$\varphi z_l : \quad \mathbb{P}(\Phi \leq \varphi) = 1 - \varphi^{-\kappa} \quad \text{and} \quad \mathbb{P}(Z_l \leq z_l) = \exp(-T_{il} z_l^{-\theta})$$

2. Krugman-meets-EK model of MP & trade  $\equiv$  Two-sector trade model
  - Krugman free-entry monopolistic sector. EK head-to-head competition sector
3. Product innovation  $\equiv$  Process innovation
  - (Uncertain) Investment to lowering unit costs of production
4. For  $\rho = 0$ : ARRY model  $\equiv$  model with plant-level location-specific fixed costs



# Quantitative GE Models of Trade and MP

- Irarrazabal, Moxnes, & Oromolla (13) — HMY with intra-firm trade
- Garetto (13) — MP sourcing
- Tintelnot (17) — plant-level fixed costs
- Alvarez (19) — many sectors
- Head & Mayer (19) — HQ gravity
- Eaton & Kortum (19) — trade in services
- Sun (20) — MP with non-neutral technologies
- Fan (21) — Offshore R&D
- Wang (21) — bounds approach

# Spillovers: State-of-the-Art

'Incumbent firms increase TFP when more productive firm locates nearby'

- Traditionally, regression of domestic-firm outcome on 'nearby' MP presence
  - Many papers (80s', 90s'), mixed results
- More recently, refinements to include channels for spillovers
  - e.g. Backward linkages: Javorcik (04) and literature thereafter
- Now, very detailed data allow for much better identification
  - Firm-to-firm; employer-employee; natural experiments

# Large Plant Openings: Greenstone et al. (10)

- Effects of new large plants on incumbent plants across US counties
- Use information from SITE Selection magazine
  - Report counties chosen by new million-dollar plants ....
  - ... And counties that almost got chosen
- Identification strategy
  - Compare incumbent plants in winning vs almost-winning counties
  - Ex-ante: counties are similar; incumbent plants are similar
- Results
  - Incumbent plants increase TFP by 8% after a large plant locates nearby
  - Entry of new plants increases, as do local wages
  - Incumbent firms that are economically less "distant" gain most
- Abebe et al. (2018): Effects of FDI spillovers on domestic plants in Ethiopia
  - Foreign-plant openings are allocated to regions by the government

# Employer-Employee Data: Setzler and Tintelnot (21)

- Corporate tax fillings merged with W-2 for the US (1999-2017)
- Effects of MNEs in the US
  - Direct effect: Identify MNE wage premium
  - Indirect effect: Identify MNE effects on domestic firms (e.g., wages)
- Identification strategy
  - Use movers from domestic to foreign firms and two-way fixed effect
  - IV based on the spatial clustering of foreign firms by origin
- Results
  - The average foreign firm wage premium is 7% — higher for skilled workers
  - One more job created by a foreign MNE generates in the same labor market:
    - approx. 0.5 jobs and 139,000\$ in value added in a domestic firms;
    - avg annual aggregate wage gain for incumbent workers of approx. 13,400\$
  - Tradeoff: the cost of mega-deals

# The Case of Costa Rica

1. The effect of MNEs on workers (Alonso-Ureña, Manelici, and Vasquez, 19)
  - Employer-employee + firm-to-firm data for Costa Rica
  - Identify wage premium for MNEs (9%) and effects on domestic firms (1%)
    - o "Movers" design and two-way fixed effects
  - Dig deeper on the mechanisms: better outside options; input-output linkages
2. The effect of MNEs on suppliers (Alonso-Ureña, Manelici, and Vasquez, 20)
  - Firm-to-firm data for Costa Rica
  - Event-study strategy to identify effects of starting supplying an MNE
    - o Also: "winner vs loser" policy event; placebo strategies; survey to managers
  - Results reveal strong and persistent gains in performance by domestic firms
3. The effects of monopsony power on development (Van Patten, 20)
  - Exploit a quasi-random assignment of land to the United Fruit Co.

# What's Next?

- MNE dynamics
- Taxation and MNEs
- Cross-border Mergers & Acquisitions
- Automation and MNEs
- Global value chains in production and R&D

# Appendix

## Property of Pareto Used for Estimation in HMY(04)

$$\mathbb{P}[Z \geq z] = \left(\frac{z}{\underline{z}}\right)^{-\gamma} \rightarrow \log(\mathbb{P}[Z \geq z]) = \gamma \log \underline{z} - \gamma \log z$$

- The log of the mass of the upper tail above  $z$  is linear in  $\log z$ 
  - e.g. if the number of employees in a randomly selected firm,  $Z$ , is Pareto distributed, the share of firms in the population with more than  $z$  (log) employees is linear in the (log) number of employees
- Regression of log firm size ranking on firm size identifies the shape parameter
- In this case:  $\gamma = \kappa + 1 - \epsilon$



## Symmetry: Set Up

- $L_n = L$ ,  $T_n = T$ ;  $\tau_{ln} = \tau > 1$ ,  $\gamma_{il} = \gamma > 1$ , for all  $l \neq n$ .
  - Wages, costs, prices are equal across countries.  $W = 1$ .
  - Unit cost of the multinational input bundle

$$m = \left[ (1-a)\gamma^{1-\xi} + a\tau^{1-\xi} \right]^{\frac{1}{1-\xi}}$$

- Unit cost of the multinational input bundle when  $\tau \rightarrow \infty$

$$\tilde{m} = (1-a)^{\frac{1}{1-\xi}} \gamma$$

# Symmetry: Real Wages

- Isolation

$$T^{\frac{1}{\theta}}$$

- Only trade

$$[1 + (N - 1)\tau^{-\theta}]^{\frac{1}{\theta}} T^{\frac{1}{\theta}}$$

- Only MP

$$[1 + (N - 1)\tilde{m}^{-\theta}]^{\frac{1}{\theta}} T^{\frac{1}{\theta}}$$

- Trade and MP

$$[\Delta_0 + (N - 1)\Delta_1]^{\frac{1}{\theta}} T^{\frac{1}{\theta}}$$

$$\Delta_0 \equiv \left(1 + (N - 1)(m\tau)^{-\frac{\theta}{1-\rho}}\right)^{1-\rho} \quad \Delta_1 \equiv \left(\tau^{-\frac{\theta}{1-\rho}} + m^{-\frac{\theta}{1-\rho}} + (N - 2)(m\tau)^{-\frac{\theta}{1-\rho}}\right)^{1-\rho}$$

## Symmetry: Gains

$$GT = \left[ \frac{\Delta_0 + (N-1)\Delta_1}{1 + (N-1)\tilde{m}^{-\theta}} \right]^{\frac{1}{\theta}}$$

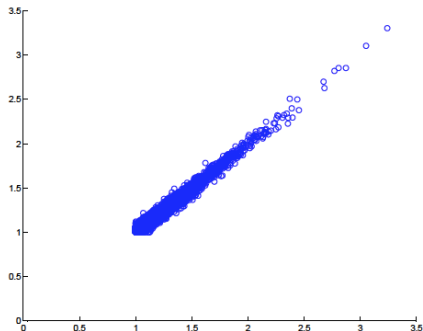
$$GMP = \left[ \frac{\Delta_0 + (N-1)\Delta_1}{1 + (N-1)\tau^{-\theta}} \right]^{\frac{1}{\theta}}$$

$$GO = [\Delta_0 + (N-1)\Delta_1]^{\frac{1}{\theta}}$$

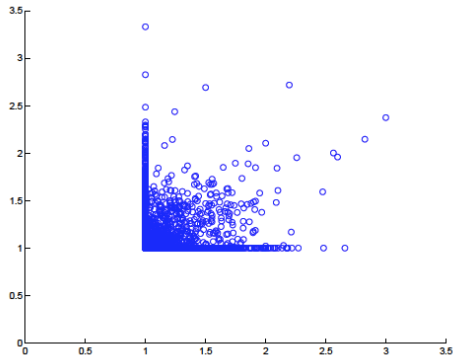
$$\Delta_0 \equiv \left( 1 + (N-1)(m\tau)^{-\frac{\theta}{1-\rho}} \right)^{1-\rho} \quad \Delta_1 \equiv \left( \tau^{-\frac{\theta}{1-\rho}} + m^{-\frac{\theta}{1-\rho}} + (N-2)(m\tau)^{-\frac{\theta}{1-\rho}} \right)^{1-\rho}$$

# Multivariate Pareto Distribution: Two-Country Simulation

High  $\rho$



Low  $\rho$



Note:  $N = 2$ ,  $T_{il} = T_{ij}$

# ARRY: Taking the Model to the Data

**Sample: 26 OECD countries, including China & Brazil**

- Match key trade elasticities (detailed data on MP activity)
- Match bilateral trade and MP patterns
- Match country's GDP, productive labor, and innovation share

# ARRAY: Estimation of Model Elasticities

- **'Unrestricted'** gravity regression does not recover  $\theta$  but  $\beta^u$

$$\ln X_{ln} = I_l + I_n + \beta^u \ln \tau_{ln}$$

- Same regression **'restricted'** to origin  $i$  can be used to recover  $-\frac{\theta}{1-\rho}$ :

$$\ln X_{iln} = \underbrace{\ln T_l^p (\gamma_{il} W_l)^{-\theta/(1-\rho)}}_{I_{il}} + \underbrace{\ln T_i^e \lambda_{in}^E (\Psi_{in})^{-1/(1-\rho)}}_{I_{in}} - \frac{\theta}{1-\rho} \ln \tau_{ln}$$

- We use BEA data for  $X_{iln}$  for  $i = US$  and selected  $l, n$  pairs

- Model implies  $\beta^u \approx -\theta > -\frac{\theta}{1-\rho}$

# ARRY: Calibration of Trade and MP costs, and Technology

- **Step 1:** Given MP & trade shares, the model implies a unique set of  $X_{iln}$ 
  - Trade and MP shares are constructed with data from WIOD & UNCTAD
  - Calculate *symmetric* trade and MP costs using a generalized HR index
  - Remark: the procedure is "over-identified"

$$\left( \sqrt{\frac{X_{inn}X_{ill}}{X_{iln}X_{inl}}} \right)^{(1-\theta)/\rho} = \tau_{ln}\tau_{nl}, \quad \left( \sqrt{\frac{X_{iin}X_{iIn}}{X_{iln}X_{iIn}}} \right)^{(1-\theta)/\rho} = \gamma_{li}\gamma_{il}$$

- **Step 2:** Set  $T_l^p = L_l^{1-\rho}$ 
  - $L_l$  is equipped labor (K-RC, 05)  $\times$  the employment share in mfg (UNIDO)
- **Step 3:**  $T_i^e$  matches  $r_i$  constructed from data on (implied) trade imbalances

# ARRY Results: CA vs HMEs

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## **Specialization due to Comparative Advantages**

Benelux	Innovation
Canada	Production
Denmark	Innovation
Sweden	Innovation
Ireland	Production
China	Production

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## **Specialization due to Home Market Effects**

Germany	Innovation
Mexico	Production
United States	Innovation

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