

# Introduction to Matlab

## Lesson 01 — Preliminaries and Matlab Syntax

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# Preliminaries

# Preliminaries

## The Course

- Introduction to Matlab Programming
- Check the [syllabus](#)

## Me

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- Office hours: Any time. Send me an email and we can arrange a meeting.

## You

- A quick roundtable of names, interests, and coding background.

# What will we cover?

1. Matlab preliminaries.
  - First interactions. Script vs Command Window.
  - Creating Variables. Basic Operations. Arrays and Matrices.
  - Control Flow. Plots. Functions.
2. Importing and manipulating data. Polynomial fit and evaluation. Nonlinear least squares.
3. Basics of root finding, numerical differentiation and integration.
4. Basics of numerical optimization.

# Syllabus Highlights

## What you have to do

1. Two problem sets
2. In class solutions
3. Final exam (take-home)

## Materials (for the first two lectures, check the syllabus)

- Peter H. Gruber — Script Solving Economics and Finance Problems with MATLAB
- QuantEcon Cheatsheet — for Matlab, Python, and Julia.
- QuantEcon Lectures. For Python and Julia but many ideas port to Matlab easily.

## First Time Opening Matlab

# First Time Opening Matlab

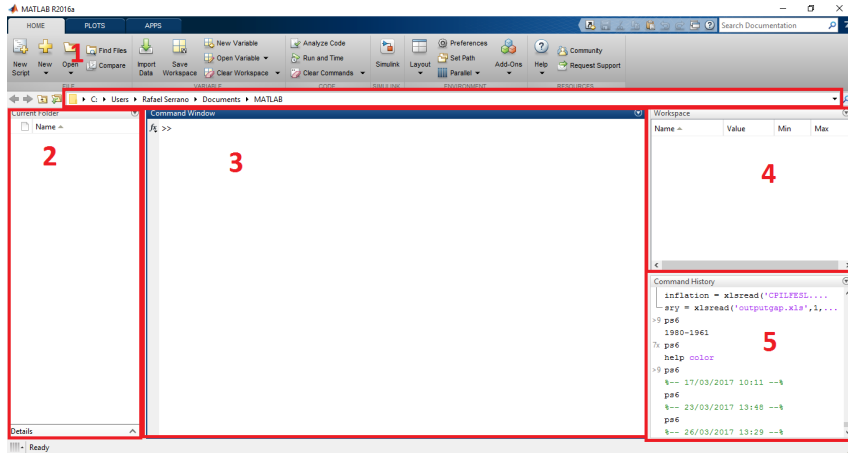


Figure 1: Matlab's Interface

## Scripts vs Command Window



# Scripts vs Commands

- The *command window* allows us to evaluate commands we type.
- *Scripts* are *recipes* that can be saved. Useful for:
  - Reproducing a set of codes *exactly* in the same order
  - Automating tasks
  - Correcting mistakes in long tasks
- A script is evaluated sequentially line by line.

# Scripts vs Commands

- To start a new script:
  - Home -> New Script
  - Type `edit` in the command window
- Write comments with the symbol `%`
- Everything after a `%` will not be processed by Matlab
- A block of comments is defined within `%{ %}`

# Script Example

```
1 clear all
2 close all
3 clc
4
5 % This is a comment
6
7 %{
8     This is a block of comments. Everything within the two
9     symbols is not processed by Matlab. Useful to define
10    headers or helps for user defined functions.
11 %}
```

## Creating Variables

# Creating Variables

- We can assign *values* to a variable.
- Matlab has several types of objects (arrays, struct arrays, cell arrays...)
- To name a variable the first character **needs to be a letter**.
- Matlab is case sensitive  $x \neq X$

# Creating Variables

## Forbidden names:

- $i$  and  $j$  indicate complex numbers.
- `pi` is assigned to  $\pi$ .
- `ans` is assigned to the last value that has not been assigned to anything.
- `Inf` or `-Inf` are  $\pm\infty$ .
- `NaN` represents “*Not a Number*” (typically missing data).
- `eps` is the *machine epsilon* (we will comment a bit on this below).

# Creating Variables

```
1 clear
2 clc
3
4 %=====
5 % == Creating Variables == %
6 %=====
7
8 % Assignment and basic operations
9 x = 5
10 x*2
11 x-7
12 x+7
13
14 % Creating variable from another
15 y = x^2; % Semicolon ; suppresses output
16 disp(y)
```

# Matlab as a Calculator

- To perform basic arithmetic operations Matlab uses five symbols.
- These operators are defined for both *matrices and scalars*.

Table 1: Basic Arithmetic Operators

Operator	Meaning
+	Addition
-	Subtraction
*	Multiplication
/	Division
^	Exponentiation



# Matlab as a Calculator

## Exercise 1

*Use Matlab as a calculator and try to solve the following operations using the functions needed. Solve them for  $x = 0$  and  $x = \frac{\pi}{4}$*

$$\frac{(\ln(1+x^2))^2 - \sqrt{1+\sqrt[3]{x^2}}}{1+\sin^2 x} ; \ln \left| \frac{x-\pi}{x+\pi} \right| + \sqrt{\frac{e^x}{1+xe^x}}$$

# Matlab as a Calculator

Solving for  $x = 0$ . Check commands:

- log, sqrt, sin, abs, pi

```
1 % === Ex. 1: Solve Complex Operations === %  
2 x = 0;  
3  
4 op1 = ((log(1+x^2))^2 - sqrt(1+x^(2/3)))/(1+sin(x)^2);  
5 op2 = log(abs((x-pi)/(x+pi))) + sqrt(exp(x)/(1+x*exp(x)));
```

# Arrays — Vectors and Matrices

- Matrices and arrays are the fundamental representation of data in Matlab.
- An **array** is just a systematic arrangement of objects. A vector is a one-dimensional array, while a matrix is a two-dimensional array.
- **Row vectors** (the default in Matlab) are created as

```
1 %=====
2                               % === Vectors === %
3 %=====
4
5 rowV = [1 2 3 4 5];          % Spaces separate elements
6 rowV2 = [6,7,8,9,10];        % Commas work as spaces
```

# Arrays — Vectors and Matrices

- **Column vectors** are created with the semicolon operator ;

```
1 colV = [1; 2; 3; 4; 5];
```

- Sequences as row vectors

```
1 % A sequence from 0 to 10 in steps of 2
2 seq1 = 0:2:10;
3 % 1000 equally spaced elements in [0,10]
4 seq2 = linspace(0,10,1000);
```

- **Check your workspace!**

## Arrays — Vectors and Matrices

- **Matrices** can be created element by element or by *concatenating vectors*.
- A semicolon ; after a number indicates a new row.

```
1 A = [1 2 3; 4 5 6; 7 8 9];  
2 B = [4 5 6; 7 9 2; 1 5 32];  
3 ConcatenatedMatrix = [rowV;rowV2];
```

- Produces:

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} \quad B = \begin{bmatrix} 4 & 5 & 6 \\ 7 & 9 & 2 \\ 1 & 5 & 32 \end{bmatrix} \quad \text{ConcatenatedMatrix} = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 \\ 6 & 7 & 8 & 9 & 10 \end{bmatrix}$$

# Arrays — Vectors and Matrices

## Array Indexing

- In matrix  $A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$  the element  $a_{2,3} = 6$  is the element in row 2 and column 3.
- In Matlab we can access element  $a_{j,k}$  as  $A(j,k)$  to access 6 in matrix  $A$  before:

```
1 A(2,3) % Element in row 2 and column 3 of matrix A
```

- For vectors, we can index by the position only.

```
1 colV(1) % First element in colV vector
```

# Arrays — Vectors and Matrices

## Array Indexing

- For matrices in general, we can access whole columns or rows.

```
1 A(2,:) % Index the 2nd row and all columns
```

- In general, we can index matrices as

Table 2: Basic Indexing

Index	Result
$A(i, j)$	$a_{i,j}$
$A(i, :)$	Row $i$
$A(:, j)$	Column $j$

## Arrays — Operations

- We can use the same operators described in Table 1 **BUT** mind the laws of matrix algebra.
- Matrix products  $A*B$

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} \quad B = \begin{bmatrix} 4 & 5 & 6 \\ 7 & 9 & 2 \\ 1 & 5 & 32 \end{bmatrix} \quad AB = \begin{bmatrix} 21 & 38 & 106 \\ 57 & 95 & 226 \\ 93 & 152 & 346 \end{bmatrix}$$

- To transpose a matrix  $A$ :

```
1 % To transpose a matrix use transpose() or '  
2 A '  
3 transpose(A)
```



# Arrays — Operations

## Element-wise Operations

- Element-wise product of  $A$  and  $B$  is computed by  $a_{i,j} \times b_{i,j}$

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} \quad B = \begin{bmatrix} 4 & 5 & 6 \\ 7 & 9 & 2 \\ 1 & 5 & 32 \end{bmatrix} \quad A \odot B = \begin{bmatrix} 4 & 10 & 18 \\ 28 & 45 & 12 \\ 7 & 40 & 288 \end{bmatrix}$$

- In Matlab, we use

```
1 % Element-wise multiplication of A and B
2 A.*B
3
4 % Be careful with element wise multiplication. Check what
   would happen if:
5 rowV.*rowV2'
```

# Arrays — Matrix Operations

Table 3: Matrix Arithmetic Operations

Operator	Meaning
+	Addition
-	Subtraction
*	Multiplication
.*	Element-wise product
\	Left division ( $A \setminus B = A^{-1}B$ ). Equivalent to <code>mldivide()</code>
/	Right division ( $A/B = AB^{-1}$ ). Equivalent to <code>mrdivide()</code>
./	Element-wise division
^	Exponentiation
.^	Element-wise exponentiation
<code>inv()</code>	Inverse of matrix

# Arrays — Matrix Operations

## Exercise 2

*Solve the following system of linear equations using `inv()` and `\`.*

$$3x + 2y - z = 1$$

$$2x - 2y + 4z = -2$$

$$-x + \frac{1}{2}y - z = 0$$

## Arrays — Matrix Operations

To solve systems of equations, it is recommended to use `\` instead of `inv()`. If you're interested you can [check this](#) or try [this example](#).

```
1 % === Ex.2 Solve the system === %  
2 b = [1; - 2; 0];  
3 A = [3 2 -1; 2 -2 4; -1 0.5 -1];  
4 x = inv(A)*b;      % Slower and inaccurate  
5 x_oth = A\b;       % This method is preferred  
6 x_oth2 = mldivide(A,b); % Same as the previous one  
7 disp([x,x_oth,x_oth2])
```

## Relational and Logical Operators and Loops

# Relational and Logical Operators

## Relational Operators

- Check if  $a \neq b$
- Check whether  $a \lesseqgtr b$

## Logical Operators

- Check whether one or more conditions are satisfied
- Access elements that are **NOT** equal to  $a$ .

# Relational and Logical Operators

- Relational and logical operators return either *true* or *false* values.
- In Matlab, *true* is coded with 1 and *false* with 0.
- But **these are not numbers!!**
- The result is a *logical array*.

# Relational and Logical Operators

```
1 A > 5
2 A == 5
3 A <= 5
```

Table 4: Relational Operators

Operator	Meaning
==	Exactly equal to
~=	NOT equal to
<	Lower than
<=	Lower or equal than
>	Lower than
>=	Lower or equal than



# Relational and Logical Operators

```
1 A > 5 | A < 9
2 ~(A > 3 & A < 6)
```

Table 5: Logical Operators

Operator	Meaning
&	Element-wise AND
&&	AND for scalars
	Element-wise OR
	OR for scalars
~	NOT
any()	True if any element of a vector is <i>true</i>
all()	True if all elements of a vector are <i>true</i>

# If-Else Statements

- Typically, relational and logical operators are used as conditions.
- If** something happens, do something. **Else** do another thing.
- If-Else statements start with `if` and are closed with `end`. General syntax:

```
1 b = 3;  
2 if b < 0  
3     disp('b is negative')  
4 else  
5     disp('b is non-negative')  
6 end
```

# If-Else-Else Statements

- If we want to include two possible conditions, we use `elseif`

```
1 b = 4;  
2 if mod(b,2) == 0 % Check if even  
3     disp('b is even')  
4 elseif mod(b,5) == 0 % Check if divisible by 5  
5     disp('b is divisible by 5')  
6 else  
7     disp('b is not even nor divisible by 5')  
8 end
```

# For and While Loops

- Sometimes we need to repeat the same operation several times.
- When we know how many times exactly, we should use `for` loops.
- If we do not know how many times, but we know a criterion, then we should use `while`

# For and While Loops

Suppose we want to simulate an  $AR(1)$  process for 100 periods such as

$$y_{t+1} = \rho y_t + \varepsilon_t$$

where  $\rho = 0.85$ ,  $y_0 = 0$ , and  $\varepsilon_t \underset{iid}{\sim} \mathcal{N}(0, 1)$

```
1 T = 100;  
2 rho = 0.85;  
3 y = zeros(100,1);  
4 for t=2:T  
5     y(t,1) = rho*y(t-1,1) + randn;  
6 end
```

**Check command** randn !!

# For and While Loops

Suppose we want to add one to a number for as long as it remains below a threshold. We can use `while` loops!

```
1 a = 0;  
2 while a < 25  
3     a = a + 1;  
4 end
```

# An Example with Grades

## Exercise 3

*Suppose we have a list of grades of students. Create a loop that goes through all the notes and checks whether that student has passed the subject or not. To get the list, generate a random list of 200 grades uniformly distributed between 0 and 10 (check `rand` command), and to assign if a student has passed or not, generate a vector called `passed` that equals one if the student has obtained a grade larger or equal than 5, and 0 otherwise.*

## An Example with Grades

```
1 % === Ex. 5 List of students === %  
2 nstudents = 200;  
3 grades = 10.*rand(nstudents,1);  
4 pass = ones(nstudents,1);  
5  
6 for student = 1:nstudents  
7     if grades(student,1) >= 5  
8         pass(student,1) = 1;  
9     else  
10         pass(student,1) = 0;  
11     end  
12 end
```



## An Example with Grades — A More Efficient Approach

The previous example was perfectly correct, but we could improve performance by *vectorizing* the operations.

```
1 pass_vect = zeros(nstudents,1);  
2 pass_vect(grades >= 5) = 1;  
3  
4 % To test they are equal  
5 isequal(pass, pass_vect)
```

Vectorizing is **extremely important**. In this simple example, the vectorized function takes  $\approx 18\%$  of the time it takes for the loop.

## Simple Plots

# Simple Plots

- Matlab has a powerful command to generate figures `plot`.
- To plot the  $AR(1)$  process we simulated before, is as easy as

```
1 figure
2 plot(1:T,y)
```

- Command `figure` opens a clear figure window.
- `plot` takes as first argument the  $x$ -axis vector (the time periods) and the value of  $y_t$  as second argument.

## A More Involved Example

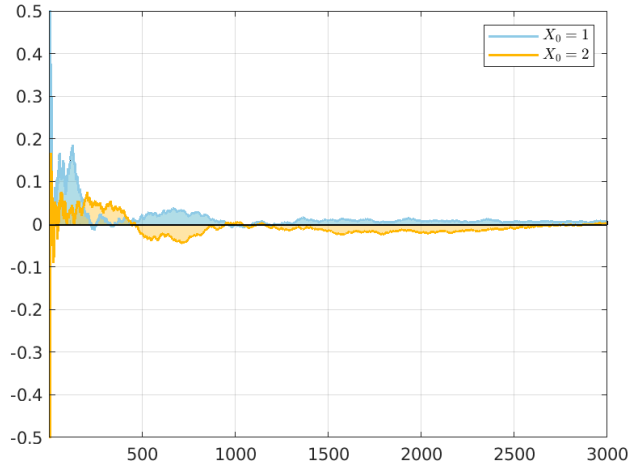


Figure 2: A Model of Unemployment Dynamics

# Functions

# User Defined Functions

- Commands are functions that take inputs and yield a result.
- In Matlab we can create our own functions just like in the mathematical sense.
- If  $f(x) = 3x + 1$  then we can plug any  $x$  and the result is  $3x + 1$ . This function in Matlab would be

```
1 function [fx] = simple_function(x)
2     fx = 3*x + 1;
3 end
```

# User Defined Functions

- The general structure of a function is

```
1 function [out1,out2,...,outN] = name(in1,in2,...,inN)
2     % Document the function. Author, inputs, outputs...
3     Operations
4     out1 = %operations to get out1;
5     ...
6     outN = %operations to get outN;
7 end
```

- Save the function as an `.m` file in the working directory (or add to path).
- The name of the file **must be** the name you assigned.

# User Defined Functions

## Exercise 4

Create a function called `my_wave` that gives as output the plot of a sinusoidal wave. The function should take as arguments the parameters that will give the amplitude, the frequency, and the upper and lower bounds in which it will be plotted. By default, plot 1000 points. Plot the sinusoidal wave with amplitude and frequency one for comparison. A sinusoidal wave  $W$  with amplitude  $A$  and frequency  $f$  is computed as

$$W = A \sin(2\pi f x)$$



# User Defined Functions

A general function to compute a sine wave

```
1 function [wave] = my_wave(A,freq,lb,ub)
2     points = 1000;
3     x = linspace(lb,ub,points);
4     wave = A.*sin(2.*pi.*freq.*x);
5
6     figure
7     plot(x,wave,'--','LineWidth',1.3)
8     hold on
9     grid on
10    plot(x,sin(x),'-','LineWidth',1.3)
11    legend({'$A\sin(\omega x)$','$\sin(x)$'},'Interpreter',''
12           'latex','Location','best')
13    xlabel('$x$', 'Interpreter','latex')
14    title(['Sinusoidal wave with amplitude ', num2str(A), ' and
15          frequency ', num2str(freq)])
16 end
```