

## Sheet 2

### series (part two)

Discuss the convergence and divergence of the following series:

$$1) \sum_{n=2}^{\infty} \frac{1}{\sqrt{n}-1}$$

$$2) \sum_{n=1}^{\infty} \frac{5n^3-3n}{n^2(n-2)(n^2+5)}$$

$$3) \sum_{n=1}^{\infty} \frac{1}{n3^n}$$

$$4) \sum_{n=2}^{\infty} \frac{1}{\ln n}$$

$$5) \sum_{n=1}^{\infty} \frac{\sqrt{n}+1}{\sqrt{n^2}+3}$$

$$6) \sum_{n=1}^{\infty} \frac{1-n}{n2^n}$$

$$7) \sum_{n=1}^{\infty} \frac{2^n}{3+4^n}$$

$$8) \sum_{n=1}^{\infty} \frac{2^n+3^n}{3^n+4^n}$$

$$9) \sum_{n=1}^{\infty} \frac{n+2^n}{n^2 2^n}$$

$$10) \sum_{n=1}^{\infty} \frac{n+1}{n^2+3n} \left(\frac{1}{5^n}\right)$$

$$11) \sum_{n=3}^{\infty} \frac{1}{\ln(\ln n)}$$

$$12) \sum_{n=1}^{\infty} \frac{\sin^2 n}{2^n}$$

$$13) \sum_{n=1}^{\infty} \frac{1+\cos n}{n^2}$$

$$14) \sum_{n=1}^{\infty} \frac{\cos^2 n}{\frac{3}{n^2}}$$

$$15) \sum_{n=1}^{\infty} \sin \frac{1}{n}$$

$$16) \sum_{n=1}^{\infty} \tan \frac{1}{n}$$

$$17) \sum_{n=1}^{\infty} \frac{2n}{3n-1}$$

$$18) \sum_{n=2}^{\infty} \frac{\ln(n+1)}{n+1}$$

$$19) \sum_{n=2}^{\infty} \frac{1}{\sqrt{n}(\ln n)}$$

$$20) \sum_{n=1}^{\infty} \frac{\sqrt[n]{n}}{n^2}$$

$$21) \sum_{n=1}^{\infty} \frac{n}{(\ln n)^2}$$

$$22) \sum_{n=1}^{\infty} \frac{(\ln n)^2}{n}$$

$$23) \sum_{n=1}^{\infty} \frac{(\ln n)^2}{n^3}$$

$$24) \sum_{n=1}^{\infty} \frac{n}{e^n}$$