

**CSCE 500 Spring 2014**  
**Homework #2 (Due on 2/20/2014)**

1. For the following questions, assume that an array implementation of heap.
  - a. If you are adding one element at a time onto a heap that maintains min heap property, find the tight bound taken to add  $N$  elements to the min-heap.
  - b. Suppose these  $N$  elements are already in an array, not in any particular order. Find the tight bound to maintain the min-heap property for this array of  $N$  elements.
  - c. Assuming that the content of an array in problem b. is shown as 10,12,7,1,5,9,20,6,15. Show the content of the array after maintaining the min-heap property.
  - d. Obtain the time complexity of combining two min heaps of length  $N$ .
  
2. Solve for the recurrence relation of the following using the master theorem
  - a.  $T(n) = 2T(n/2) + n^3$
  - b.  $T(n) = 16 T(n/4) + n^2$
  - c.  $T(n) = 7 T(n/2) + n^2$
  - d.  $T(n) = 2T(n/4) + n^{0.5}$
  - e.  $T(n) = 3T(n/2) = n \log n$