

### **B.TECH SECOND YEAR**

ACADEMIC YEAR: 2022-2023



## **COURSE NAME: ENGINEERING MATHEMATICS-III**

COURSE CODE : MA 2101

LECTURE SERIES NO:

CREDITS : 3

MODE OF DELIVERY: ONLINE (POWER POINT PRESENTATION)

FACULTY: DR. BHOOPENDRA PACHAURI

EMAIL-ID : Bhoopendra.pachauri@jaipur.manipal.edu

PROPOSED DATE OF DELIVERY:



#### VISION

Global Leadership in Higher Education and Human Development

#### MISSION

- Be the most preferred University for innovative and interdisciplinary learning
- Foster academic, research and professional excellence in all domains
- Transform young minds into competent professionals with good human values

#### VALUES

Integrity, Transparency, Quality,



# SESSION OUTCOME

"KNOWLEDGE OF DIFFERENT TYPES OF GRAPHS"



### **ASSIGNMENT**

#### OUIZ

MID TERM EXAMINATION -I & II

**END TERM EXAMINATION** 

# **ASSESSMENT CRITERIA'S**

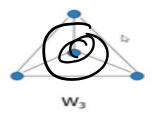


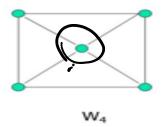


## Simple graphs — special cases

Wheels: W<sub>n</sub>, obtained by adding additional vertex to Cn and connecting all vertices to this new vertex by new edges.

Representation Example: W3, W4

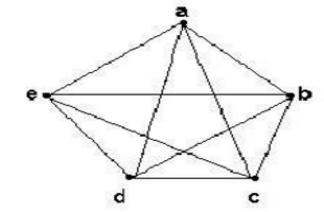






# Complete graph K<sub>n</sub>

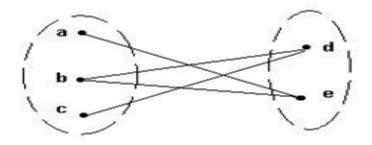
- Let n ≥ 3
- The complete graph K<sub>n</sub>is
  the graph with n vertices
  and every pair of
  vertices is joined by an
  edge.
- The figure represents K<sub>5</sub>





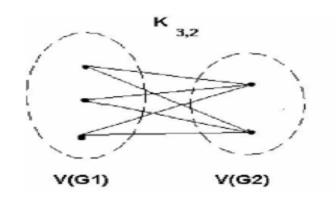
## Bipartite graphs

- A bipartite graph G is
  a graph such that
  V(G) = V(G₁) ∪ V(G₂)
  |V(G₁)| = m, |V(G₂)| = n
   V(G₁) ∩V(G₂) = Ø
  - No edges exist between any two vertices in the same subset V(G<sub>k</sub>), k = 1,2





# Complete bipartite graph K<sub>m,n</sub>



A bipartite graph is the complete bipartite graph K<sub>mn</sub>if every vertex in V(G<sub>1</sub>) is joined to a vertex in V(G<sub>2</sub>) and conversely,

$$|V(G_1)| = m$$
  
 $|V(G_2)| = n$ 



# REMARK

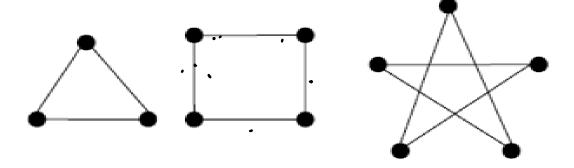
## Maximum Number Of Edges-

- 1. Any bipartite graph consisting of "n" vertices can have at most  $1/4 n^2$  edges.
- 2. Minimum possible number of edges in a bipartite graph on "n" vertices= $1/4 n^2$



### Regular graph

A graph, in which all vertices are of **equal degree**, is called a **regular graph**. If the degree of each vertex is *r*, then the graph is called a regular **graph of degree** *r*.





## Exercises

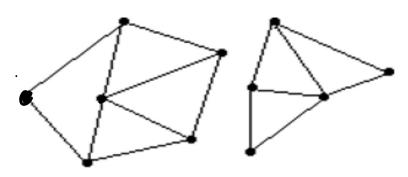
- N1: Show that each  $K_{m,n}$  is bipartite.
- N2: Show that each Q<sub>n</sub> is bipartite.
- N3(\*): Show that a graph is bipartite if and only if it has no odd cycles.
- N4: Which generalized Petersen graphs G(n,k) are bipartite?



# Connected graphs

A graph is connected if every pair of vertices can be connected by a path.

Each connected subgraph of a non-connected graph G is called a component of G



2 connected components