

- **Stirling's Formula:**

$$n! = \sqrt{2\pi n} \left(\frac{n}{e}\right)^n \left(1 + \frac{1}{12n} + O\left(\frac{1}{n^2}\right)\right)$$

- Let $n \geq k \geq 0$

$$\binom{n}{k} \leq \left(\frac{ne}{k}\right)^k$$

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- For all $t \in \mathbb{R}$, $e^t \geq 1 + t$ with equality holding at $t = 0$.

- For all $t, n \in \mathbb{R}$, such that $n \geq 1$ and $|t| \leq n$,

$$e^t \left(1 - \frac{t^2}{n}\right) \leq \left(1 + \frac{t}{n}\right)^n \leq e^t$$

Note that this even holds for negative values of t .

- For all $n \in \mathbb{N}$, we define the n th Harmonic number H_n , as follows:

$$H_n = 1 + \frac{1}{2} + \cdots + \frac{1}{n}$$

For all $n \in \mathbb{N}$, the n th Harmonic number H_n is:

$$H_n = \ln n + \Theta(1)$$

- **Chernoff's Bound:** For any $\delta > 0$,

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$$\mathbf{P}(\mathbf{X} \leq (1 - \delta)\mu) \leq e^{-\mu\delta^2/2}$$

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$$\mathbf{P}(\mathbf{X} \geq (1 + \delta)\mu) \leq \left(\frac{e^\delta}{(1 + \delta)^{(1 + \delta)}}\right)^\mu$$

Alternate and more usable forms:

If $\delta \geq 2e - 1$ then

$$\mathbf{P}(\mathbf{X} \geq (1 + \delta)\mu) \leq 2^{-(1 + \delta)\mu}$$

If $0 < \delta < 2e - 1$, then

$$\mathbf{P}(\mathbf{X} \geq (1 + \delta)\mu) \leq e^{-\mu\delta^2/4}$$