



Inspiring Excellence

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**Subject** : Automata And Computability  
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**Section** : 18

(ii) (a)

A  
→ 0A  
→ 1B  
→ 0AB  
→ 1C  
→ 1C1  
→ 10C1  
→ 100C1  
→ 1001C1  
→ 10011

Q1

A  
↓  
0B  
↓  
01B

↓  
010A

↓  
0101C

↓  
01011C1.

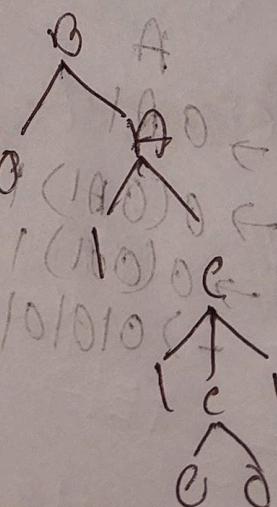
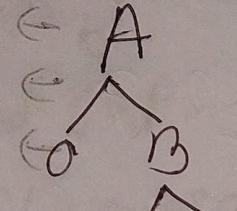
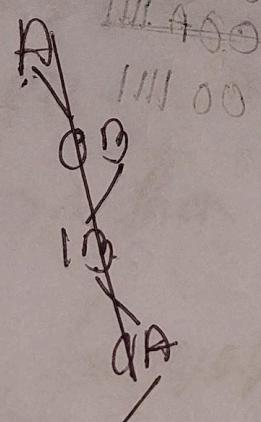
↓  
01010001

(d)

A (2) 10  
↓  
1A0C  
↓  
1A00C  
↓  
1100C

↓  
1000C1

57



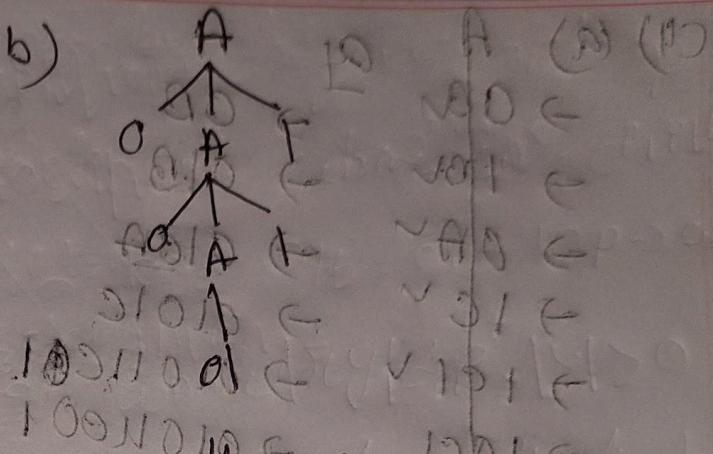
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(continued on the next page)

(1)

5(a) A  
 $\rightarrow 0A1$   
 $\rightarrow 00A11$   
 $\rightarrow 00111$

b)



c)

A (B) (D)

AB ←

AC ←

AD ←

BC ←

BD ←

CD ←

ABC ←

ACD ←

BCD ←

ABD ←

BCD ←

ACD ←

ABD ←

ABCD ←

c) another - 1

A  
 $\rightarrow 0AU$   
 $\rightarrow 00AU1$   
 $\rightarrow 001U1$

another - 2

A  
 $\rightarrow AU$   
 $\rightarrow 0AU11$   
 $\rightarrow \cancel{0AU11}$   
 $\rightarrow 001U1$

d)

A  
 $\rightarrow 0A1$   
 $\rightarrow 0(0A1)1$   
 $\rightarrow 0(001)1$   
 $\rightarrow 010101$

(has only one parenthesis)

~~Elanthen~~

S → O A / / C  
A → I S / E  
C → O S / E

Q Let  $L$  be regular &  $p$  is the pumping length.  
 $s = a^p b^p$  so  $i = p+1$ ,  $j = p$  and  
 $i > j$  where  $s \in L$

Now  $s = xyz$  where  $|xy| \leq p$ .  
So  $y$  consists only of  $a$ .  
Now let  $y = a^k$ ,  $k > 0$ .  
So,  $xy^2 = a^{p+k} b^p$  to hold  
 $y' = p+1 - k$  and  $y^2 = p$ .  
if  $k \geq 1$ , then  $y' \geq p$  so  $c \leq j - [p + k]$

So the language is not regular.

b) Let  $L$  be a regular language and  $p$  be the pumping length where  $w = 0^p 1^p 0^p$

~~OS~~  $a^p b^p c^p$  and  $a+b \geq p \Rightarrow a \geq p$

Split  $w = xyz$  where  $|xy| \leq p$ ,  $|y| > 0$

so  $y$  consists only of  $a$ s from the first

block of  $a$ s. Now, let  $y = 0^k$  [  $k > 0$  ]

Pumping  $i = 2$  gives  $xy^2 = 0^{p+k} 1^p 0^p$

Now  $a = p+k$ ,  $b = p$ ,  $c = 0^p$  so  $a+b < 2p+k$

But  $a+b = 2p$  so  $a+b \neq c+d$

so the language is not regular.

2(a) Let  $p$  will be the pumping length

&  $s = 0^n$  where  $n \geq p$

Now split  $s = xy^z$  such that  $|xy| \leq p$ .

$|y| > 0$ . ~~since~~ Since  $|xy| \leq p$ ,  $y$  contains

only 0s. So  $y = 0^k$  where  $k = |y| > 0$ .

Pumping  $xy^mz = 0^{(p+1)+k}$

But  $(p+1)+k$  is not a factorial

So  $xy^mz \notin L$  violating part

of pumping lemma result