# Model inference from protein time-course in Hematopoietic Stem Cells (HSC)

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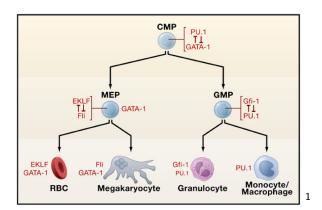
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#### Introduction

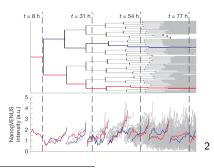
 Dynamics of hematopoetic stem cell maturation cell from Common Myeloid Progenitor (CMP) to Megakaryocyte-Erythroid Progenitor (MEP) and Granulocyte-Macrophage Progenitor (GMP)



<sup>&</sup>lt;sup>1</sup>Graf & Enver, 2009, *Nature* 

## Introduction (cont'd)

- ► Assumed corss-inhibition dynamics between Pu.1 and Gata1 in cell maturation fate:
  - Dynamics is assumed to be a bistable toggle-switch system
  - ▶ Lineage decision is a stochastics process resulting in uneven yield of MEP and GMP (70% : 30%)
- Analysis on single-cell time-lapsed data to infer parameters of this dynamics



<sup>&</sup>lt;sup>2</sup>Feigelman, 2016, Ph.D. Thesis



#### **Problems**

- Stochaticity in single cell resolution is more punctuated
- ► Tree structure of the data add ore complexity: inheritance of information during inference process is not trivial

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- ► Final inferred parameters are expected value *E* of the distribution

## Particle Filtering (6)

A particle K is defined as a triple of trajectory X, parameter set  $\theta$  and assumed model M,

$$K := (X, \theta, M) \tag{1}$$

- Par
- prior, posterior bzw Bayesian update rule

## Particle Filtering (7)

## Particle Filtering: algorithm

- 1. Initialization of parameters  $\theta$ .
- 2. Input of data  $\mathcal{D}$ .
- 3. Particle filtering routine:
  - 3.1 Generation of initial particles for step i

$$Ki := (K_{i1}, K_{i2}, \dots, K_{im})$$
 (2)

- 3.2 Simulation run of each particle  $K_{ij}$
- 3.3 Weighting of each particle. The weight is a function of the probability of observing the data given the simulation result.

$$w_i^k = P(D_i|X_i^k) = \mathcal{N}(\mathcal{D}_i|X_i^k)$$
 (3)

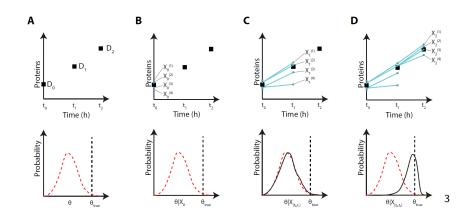
3.4 Parameter update for every K,

$$\theta^k \propto P(\theta|X_{[to,ti]}^k) \tag{4}$$

4. Model comparison.



# Particle Filtering: visualization





<sup>&</sup>lt;sup>3</sup>Feigelman, 2016, Ph.D. Thesis