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Roll #: BAI09056

IIMB - BAI09 - Assignment 3

Out[2]:

Toggle on/off Code

Q1 - 1

The following problem has been obtained by solving the set of following LP formulation:

Maximize Objective: 50 x_dh + 45 x_fn + 10 x_kbh + 60 x_kh

Decision variables:

- x_fn: quantity of FN
- x_dh: quantity of DH
- x_kh: quantity of KH
- x_kbh: quantity of KBH

Subject To

- Demand_1: x_fn <= 250
- Demand_2: x_dh <= 120
- Demand_3: x_kh <= 90
- Demand_4: x_kbh <= 550
- Non Zero Constraint 1: x fn >= 0
- Non_Zero_Constraint_2: x_dh >= 0
- Non_Zero_Constraint_3: x_kh >= 0
- Non_Zero_Constraint_4: x_kbh >= 0
- Supply_1: $0.2 \times dh + 0.3 \times fn + 0.3 \times kbh + 0.4 \times kh \le 500$
- Supply_2: $0.5 \times dh + 0.4 \times fn + 0.8 \times kbh + 0.8 \times kh \le 450$
- Supply_3: $0.3 x_dh + 0.4 x_fn + 0.1 x_kbh + 0.1 x_kh <= 75$
- Supply_4: $0.3 \times dh + 0.2 \times fn + 0.5 \times kbh + 0.6 \times kh \le 300$
- Supply_5: $0.5 \times dh + 0.5 \times fn + 0.8 \times kbh + 0.4 \times kh \le 200$
- The optimal values for the Problem are as follows.

fn :: 75.0 :: dh :: 120.0 :: kh :: 90.0 :: kbh :: 0.0 :: Objective 14775.0

# %load HNMix. GLPK 4.65 - SE		ANALYSIS REPOR	Т					Page	1
Problem: Objective: Ob	jective = 1	14775 (MAXimum)						
No. Row nam	e St	Activity	Slack Marginal	Lower bound Upper bound	Activity range	Obj coef range	Obj value at break point		
1 Demand_	1 BS	75.00000	175.00000	-Inf 250.00000	50.37037 165.00000	-5.00000 21.66667	14400.00000 16400.00000		
2 Demand_ Non Zero Const		120.00000		-Inf		-16.25000	12825.00000		
Non_Zero_Const	_		16.25000	120.00000	220.00000	+Inf	16400.00000		
3 Demand_ Non_Zero_Const		90.00000		-Inf		-48.75000	10387.50000		
Non_zero_const	raint_3		48.75000	90.00000	331.81818	+Inf	26563.63636	Supply_5	
4 Demand_	4 BS		550.00000	-Inf 550.00000	98.51852	-Inf 1.25000	14775.00000 14775.00000		
5 Non_Zer	o_Constraiı BS	nt_1 75.00000	-75.00000		50.37037	-5.00000	14400.00000	v khh	
	03	73.00000	-73.00000	+Inf	165.00000	21.66667	16400.00000		
6 Non_Zer	o_Constraiı BS	nt_2 120.00000	-120.00000	+Inf	120.00000	-16.25000 +Inf	12825.00000 +Inf		
7 Non_Zer	o_Constraiı BS	nt_3 90.00000	-90.00000	+Inf	90.00000	-48.75000 +Inf	10387.50000 +Inf		
8 Non_Zer	o_Constrai	-				T., C	14775 00000		
	BS	•		+Inf	98.51852	-Inf 1.25000	14775.00000 14775.00000		
9 Supply_	1 BS	82.50000	417.50000	-Inf	53.25000	-150.00000	2400.00000	Demand_3	

				500.00000	104.66667	5.55556	15233.33333	x_kbh	
10 Supply_2	BS	162.00000	288.00000	-Inf 450.00000	99.00000 230.96296	-69.64286 1.78571	3492.85714 15064.28571		
GLPK 4.65 - SENSIT	IVITY	ANALYSIS REPORT						Page	2
Problem: Objective: Objecti	ive =	14775 (MAXimum)							
No. Row name	St	Activity	Slack Marginal	Lower bound Upper bound	Activity range	Obj coef range	Obj value at break point		
11 Supply_3	NU NU	75.00000		-Inf	45.00000	-112.50000	11400.00000		
Non_Zero_Constraint	L_1		112.50000	75.00000	128.20000	+Inf	20760.00000	Supply_5	
12 Supply_4	BS	105.00000	195.00000	-Inf 300.00000	55.50000 149.33333	-88.63636 2.77778	5468.18182 15066.66667		
13 Supply_5	BS	133.50000	66.50000	-Inf 200.00000	96.00000 336.00000	-90.00000 1.85185	2760.00000 15022.22222		
GLPK 4.65 - SENSIT	IVITY	ANALYSIS REPORT						Page	3
Problem: Objective: Objecti	ive =	14775 (MAXimum)							
No. Column name	St	Activity	Obj coef Marginal	Lower bound Upper bound	Activity range	Obj coef range	Obj value at break point	variable	
1 x_dh	BS	120.00000	50.00000	+Inf	120.00000	33.75000 +Inf			
2 x_fn	BS	75.00000	45.00000	+Inf	50.37037 165.00000	40.00000 66.66667	14400.00000 16400.00000		
3 x_kbh	NL • 4		10.00000			-Inf	14775.00000		
Non_Zero_Constraint	L_4		-1.25000	+Inf	98.51852	11.25000	14651.85185	Supply_5	
4 x_kh	BS	90.00000	60.00000	+Inf	90.00000	11.25000 +Inf	10387.50000 +Inf	Demand_3	
End of report									

Q1 - 2

• From the **SENSITIVITY ANALYSIS REPORT** report above we can clearly see that amount of KBH to be produced to maximize profit under current profit rates is **Zero (0)**

The **Reduced Cost / Marginal Cost for Objective Coefficient** for KBH is -1.25 implying the profit will reduce by 1.25 units if AH are to produce one unit of KBH. It is a Non-Basic variable with coefficient equal to Zero

Q1 - 3

• From the SENSITIVITY ANALYSIS REPORT report above we can clearly see that Supply_1 Constraint (Availability of Maida = 500 Kg) is not a binding constraint. There is already 417 Kg of extra (SLACK) Maida available with the supplier. Hence he should not be procuring the extra Maida from his friend.

We are assuming his friend will provide Maida at Market price and not free of cost

Q1 - 4

Assuming this question is for KH

• AH is producing 90Kg of KH @ Profit of 60/unit. Hence he can accept the order of 20Kg from the Halva Shop

Assuming this question is for additional 20 Kg of KH (above 90Kg)

• As per the sesitivity report we see that upper bound for KH production is 90, i.e. if they are to produce additional 20 Kg, then we need to change the Constraints and re-solve the LP. Current Optimal Solution will not remain same

Assuming this question is for KBH

• From the Sensitivity Report we can see that, Reduced Cost / Marginal Cost for Objective Coefficient for KBH is -1.25. In order for him to accept any orders for KBH the minimum value of Profit from KBH should be 11.25/unit. Hence he should increase the Profit on KBH by 1.25/unit, if he is to accept this order

Q1 - 5

• From the Sensitivity Report we can see that the Profit on DH can be reduced by max of 16.25/unit for the current solution to remain optimal. Hence providing a discount of 10 INR/unit of DH does not change the optimal production plan

Q1 - 6

- ASSUMPTIONS for the following solution
 - We are increasing the profit amounts by 20% implying the Profit of KBH will increase from 10 to 12

```
Increased Profit for DH = 54.0
Increased Profit for FN = 60.0
Increased Profit for KH = 72.0
Increased Profit for KBH = 12.0
```

- Since the simultaneous increase in the coefficients of the Non-Basic Variables (non Zero) are withing the permissible ranges (as seen from the Sensitivity Report) and the sum of percentage increase is less than 100%, hence as per the 100% Rule there is **no change in the optimal Solution**
- · We are still assuming that KBH is not being produced

Current Profit due to change in Profit Values = 17730

Q1 - 7

- As per the sensitivity Report the Constraint Supply_3 is binding and has the highest Marginal Cost (112.5). This constraint corresponds to the Supply Constraints
 for Fruits and Nuts.
- What this implies:
 - Increasing availability of Fruits and Nuts from 75 Kg by one unit increases profit by 112.5 INR
 - The above is valid only in the amount of Fruits and Nuts are increases from current available level of 75 till 128. Beyond this range if availability is increased then the current shadow price will not hold true

Q1 - 8

- From the Sensitivity Report we can see that the Profit on DH can be reduced to 33.75/unit for the current solution to remain optimal.
- From the Sensitivity Report we can see that the Profit on KH can be reduced to 11.25/unit for the current solution to remain optimal.
- As per the problem statement the reduction in DH is 8/Unit and reduction in KH is 24/Unit
- We will compute the % change and use the 100% Rules to check if the changes are below 100% or not. Since both are Non-Basic Variables hence if the allowed change is less than 100% hence from using the 100% Rule for change in Objective coefficients we know the Optimal Solution will remain unchanged

```
% change in DH in the allowed direction = 0.49230769230769234
% change in KH in the allowed direction = 0.49230769230769234
```

Sum of the % changes in the allowed directions is < 100%, hence there is no change in the Optimal Solution

Q2 - a

Decision Variables: 15 Binary Variables for each compartment and each Fule Type. This will indicate which type of Fuel should be carried in which container.

e.g. ys1 = 1, will indicate Fuel S is being carried in Container 1 We use Python (PULP and GLPK Solver to solve the solution). Hence the DV will be as follows:

compartments = ['1', '2', '3', '4', '5']

- ys = LpVariable.dicts("Ys_", compartments, 0, None, cat = LpBinary) # 5 Variables for Fuel S
- yr = LpVariable.dicts("Yr_", compartments, 0, None, cat = LpBinary) # 5 Variables for Fuel R
- yu = LpVariable.dicts("Yu_", compartments, 0, None, cat = LpBinary) # 5 Variables for Fuel U

15 Binary Variables for quantity of fuel carried in each compartment. If corresponding binary indicator is 1, this will have non zero value.

e.g. ys1 = 1, s1 = 2800

In Python we will define these variables as follows:

- S = pulp.LpVariable.dict('S_%s', compartments, lowBound = 0)
- R = pulp.LpVariable.dict('R_%s', compartments, lowBound = 0)
- U = pulp.LpVariable.dict('U_%s', compartments, lowBound = 0)

Constraints

 Demand_Constraint_for_R_Fuel: R_1 + R_2 + R_3 + R_4 + R_5 <= 4000 • Demand Constraint for S Fuel: S 1 + S 2 + S 3 + S 4 + S 5 <= 2900 Demand_Constraint_for_U_Fuel: U_1 + U_2 + U_3 + U_4 + U_5 <= 4900 Integer_Constraint_for_One_Type_of_Fuel_in_Container_1: Yr__1 + Ys__1 + Yu__1 <= 1 Integer_Constraint_for_One_Type_of_Fuel_in_Container_2: Yr__2 + Ys__2 + Yu__2 <= 1 • Integer_Constraint_for_One_Type_of_Fuel_in_Container 3: Yr 3 + Ys 3 + Yu 3 <= 1 • Integer Constraint for One Type of Fuel in Container 4: Yr 4 + Ys 4 + Yu 4 <= 1 Integer_Constraint_for_One_Type_of_Fuel_in_Container_5: Yr__5 + Ys__5 + Yu__5 <= 1 Maximum_Capacity_of_R_Fuel_if_Container_1_has_R: R_1 - 2700 Yr__1 <= 0 Maximum_Capacity_of_R_Fuel_if_Container_2_has_R: R_2 - 2800 Yr__2 <= 0 Maximum_Capacity_of_R_Fuel_if_Container_3_has_R: R_3 - 1100 Yr__3 <= 0 • Maximum_Capacity_of_R_Fuel_if_Container_4_has_R: R_4 - 1800 Yr 4 <= 0 Maximum_Capacity_of_R_Fuel_if_Container_5_has_R: R_5 - 3400 Yr__5 <= 0 Maximum_Capacity_of_S_Fuel_if_Container_1_has_S: S_1 - 2700 Ys_1 <= 0 Maximum_Capacity_of_S_Fuel_if_Container_2_has_S: S_2 - 2800 Ys__2 <= 0 Maximum_Capacity_of_S_Fuel_if_Container_3_has_S: S_3 - 1100 Ys__3 <= 0 Maximum_Capacity_of_S_Fuel_if_Container_4_has_S: S_4 - 1800 Ys__4 <= 0 Maximum_Capacity_of_S_Fuel_if_Container_5_has_S: S_5 - 3400 Ys_5 <= 0 Maximum_Capacity_of_U_Fuel_if_Container_1_has_U: U_1 - 2700 Yu_1 <= 0 Maximum_Capacity_of_U_Fuel_if_Container_2_has_U: U_2 - 2800 Yu__2 <= 0 Maximum_Capacity_of_U_Fuel_if_Container_3_has_U: U_3 - 1100 Yu__3 <= 0 Maximum_Capacity_of_U_Fuel_if_Container_4_has_U: U_4 - 1800 Yu__4 <= 0 Maximum_Capacity_of_U_Fuel_if_Container_5_has_U: U_5 - 3400 Yu_5 <= 0 Maximum_Shortfall_(500)Constraintfor_R_Fuel: R_1 + R_2 + R_3 + R_4 + R_5 >= 3500 Maximum_Shortfall_(500)Constraintfor_S_Fuel: S_1 + S_2 + S_3 + S_4 + S_5 >= 2400 Maximum_Shortfall_(500)Constraintfor_U_Fuel: U_1 + U_2 + U_3 + U_4 + U_5 >= 4400 • Binaries Yr 1 Yr 2 Yr 3 Yr 4 Yr 5 Ys 1 Ys 2 Ys 3 Ys 4 Ys 5 Yu 1 Yu 2 Yu 3 Yu 4 Yu 5 • Non Zero: S1, S2, S3, S4, S5, R1, R2, R3, R4, R5, U1, U2, U3, U4, U5 >= 0

2 - c

Objective

Minimize Objective: -8 R_1 - 8 R_2 - 8 R_3 - 8 R_4 - 8 R_5 - 10 S_1 - 10 S_2 - 10 S_3 - 10 S_4 - 10 S_5 - 6 U_1 - 6 U_2 - 6 U_3 - 6 U_4 - 6 U_5

- 1. 8 = Penalty on not fulfilling R typer Fuel / Litre
- 2. 10 = Penalty on not fulfilling S typer Fuel / Litre
- 3. 6 = Penalty on not fulfilling U typer Fuel / Litre
- $4. \ \ Decision \ \ Variables: Fuel of \ Type \ S/R/U \ in \ Container \ 1/2/3/4/5: S1, S2, S3, S4, S5, R1, R2, R3, R4, R5, U1, U2, U3, U4, U5 >= 0$

2 - d

In order to incorporate the new Penalty Structure, I will modify the objective and the constarints in the following manner:

New Decision Variables:

- D1_0 = Non Zero value means S1 deficit is more than 250 by D1_0 amount. D1_0 will zero if Total deficit is less 250. e.g. If D1_0 = 10, defict = 250+10 = 260
- D1_1 = Non Zero value means S1 deficit is less than 250 by D1_1 amount. D1_1 will zero if Total deficit is more 250. e.g. If D1_1 = 10, defict = 250-10 = 240
- D2_0 = Same logic for quantity > 250 for R
- D2_1 = Same logic for quantity < 250 for R
- D3_0 = Same logic for quantity > 250 for U
- D3_1 = Same logic for quantity < 250 for U

New Objective

• Minimize Objective: 10* (250 - d1[1]) + 11 * d1[0]+ 8* (250 - d2[1]) + 8.8 * d2[0] + 6* (250 - d3[1]) + 6.6 * d3[0]

Logic:

- If quantity > 250: # assume 260 for S1
- D1_1 = 10, D1_0 = 0, Penalty = 10 * (250-D1_0) + 11 * D1_1

Logic:

- If quantity < 250: # assume 240 for S1
- D1_1 = 0, D1_0 = 10, Penalty = 10 * (250-D1_0) + 11 * D1_1

Subject To

- New Constraints
 - C1: S1 + S_2 + S_3 + S_4 + S_5 + 250 + d1_0 d1_1 <= 2900
 - C2: R1 + R_2 + R_3 + R_4 + R_5 + 250 + d2_0 d2_1 <= 4000
 - C3: U1 + U_2 + U_3 + U_4 + U_5 + 250 + d3_0 d3_1 <= 4900

Earlier Constraints

- Demand_Constraint_for_R_Fuel: R_1 + R_2 + R_3 + R_4 + R_5 == 4000
- Demand_Constraint_for_S_Fuel: S_1 + S_2 + S_3 + S_4 + S_5 == 2900
- Demand_Constraint_for_U_Fuel: U_1 + U_2 + U_3 + U_4 + U_5 == 4900
- Integer_Constraint_for_One_Type_of_Fuel_in_Container_1: Yr__1 + Ys__1 + Yu__1 <= 1
- Integer_Constraint_for_One_Type_of_Fuel_in_Container_2: Yr__2 + Ys__2 + Yu__2 <= 1
- Integer_Constraint_for_One_Type_of_Fuel_in_Container_3: Yr__3 + Ys__3 + Yu__3 <= 1
- Integer_Constraint_for_One_Type_of_Fuel_in_Container_4: Yr__4 + Ys__4 + Yu__4 <= 1
- Integer_Constraint_for_One_Type_of_Fuel_in_Container_5: $Yr_5 + Ys_5 + Yu_5 \le 1$

```
Maximum_Capacity_of_R_Fuel_if_Container_1_has_R: R_1 - 2700 Yr__1 <= 0</li>
Maximum_Capacity_of_R_Fuel_if_Container_2_has_R: R_2 - 2800 Yr__2 <= 0</li>
Maximum_Capacity_of_R_Fuel_if_Container_3_has_R: R_3 - 1100 Yr__3 <= 0</li>
• Maximum_Capacity_of_R_Fuel_if_Container_4_has_R: R_4 - 1800 Yr__4 <= 0
• Maximum_Capacity_of_R_Fuel_if_Container_5_has_R: R_5 - 3400 Yr_5 <= 0
Maximum_Capacity_of_S_Fuel_if_Container_1_has_S: S_1 - 2700 Ys_1 <= 0</li>

    Maximum_Capacity_of_S_Fuel_if_Container_2_has_S: S_2 - 2800 Ys__2 <= 0</li>

Maximum_Capacity_of_S_Fuel_if_Container_3_has_S: S_3 - 1100 Ys__3 <= 0</li>
• Maximum_Capacity_of_S_Fuel_if_Container_4_has_S: S_4 - 1800 Ys__4 <= 0
Maximum_Capacity_of_S_Fuel_if_Container_5_has_S: S_5 - 3400 Ys__5 <= 0</li>
Maximum_Capacity_of_U_Fuel_if_Container_1_has_U: U_1 - 2700 Yu_1 <= 0</li>

    Maximum_Capacity_of_U_Fuel_if_Container_2_has_U: U_2 - 2800 Yu__2 <= 0</li>

Maximum_Capacity_of_U_Fuel_if_Container_3_has_U: U_3 - 1100 Yu__3 <= 0</li>

    Maximum_Capacity_of_U_Fuel_if_Container_4_has_U: U_4 - 1800 Yu__4 <= 0</li>

Maximum_Capacity_of_U_Fuel_if_Container_5_has_U: U_5 - 3400 Yu_5 <= 0</li>

    Maximum_Shortfall_(500)Constraintfor_R_Fuel: R_1 + R_2 + R_3 + R_4 + R_5 >= 3500

    Maximum_Shortfall_(500)Constraintfor_S_Fuel: S_1 + S_2 + S_3 + S_4 + S_5 >= 2400

    Maximum_Shortfall_(500)Constraintfor_U_Fuel: U_1 + U_2 + U_3 + U_4 + U_5 >= 4400

    Binaries: Yr_1 Yr_2 Yr_3 Yr_4 Yr_5 Ys_1 Ys_2 Ys_3 Ys_4 Ys_5 Yu_1 Yu_2 Yu_3 Yu_4 Yu_5 End
```

Q2 - e

New Objective:

Minimize Objective: -10*(250 - d1[1]) + 11*(250 + d1[0]) - 10*250*(1 - y1[0]) - 11*250*(y1[0]) + 8*(250 - d2[1]) + 8.8*(250 + d2[0]) - 8*250*(1 - y1[1]) - 8.8* 250*(y1[1]) + 6*(250 - d3[1]) + 6.6*(250 + d3[0]) - 6*250*(1 - y1[2]) - 6.6*250*(y1[2])

Logic:

```
• If S deficit = 240,
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• d1_1 = 10, Y[1] = 1, hence Loss = 10 *240 + 11 * 250 - 0 - 11 * 250 ...

• If S deficit = 260,

d1_0 = 10, Y[1] = 0, hence Loss = 10 *250 + 11 * 260 - 10 * 250 - 8 ...

The constraints to factor the above in added below:

Subject To

New Constraints

```
• C10: - 250 Y1__2 + d31 <= 0

• C11: d30 + d3_1 <= 250

• C12: 250 Y1__2 + d30 <= 250

• C4: - 250 Y1__0 + d11 <= 0

• C5: d10 + d1_1 <= 250

• C6: 250 Y1__0 + d10 <= 250

• C7: - 250 Y1__1 + d21 <= 0

• C8: d20 + d2_1 <= 250

• C9: 250 Y1__1 + d20 <= 250
```

Older COnstraints

```
• C1: S1 + S_2 + S_3 + S_4 + S_5 + 250 + d1_0 - d1_1 <= 2900
• C2: R1 + R_2 + R_3 + R_4 + R_5 + 250 + d2_0 - d2_1 <= 4000
• C3: U1 + U_2 + U_3 + U_4 + U_5 + 250 + d3_0 - d3_1 <= 4900

    Demand_Constraint_for_R_Fuel: R_1 + R_2 + R_3 + R_4 + R_5 <= 4000</li>

Demand_Constraint_for_S_Fuel: S_1 + S_2 + S_3 + S_4 + S_5 <= 2900</li>

    Demand_Constraint_for_U_Fuel: U_1 + U_2 + U_3 + U_4 + U_5 <= 4900</li>

    Integer_Constraint_for_One_Type_of_Fuel_in_Container_1: Yr__1 + Ys__1 + Yu__1 <= 1</li>

• Integer_Constraint_for_One_Type_of_Fuel_in_Container_2: Yr__2 + Ys__2 + Yu__2 <= 1
• Integer Constraint for One Type of Fuel in Container 3: Yr 3 + Ys 3 + Yu 3 <= 1

    Integer_Constraint_for_One_Type_of_Fuel_in_Container_4: Yr__4 + Ys__4 + Yu__4 <= 1</li>

    Integer_Constraint_for_One_Type_of_Fuel_in_Container_5: Yr _ 5 + Ys _ 5 + Yu _ 5 <= 1</li>

Maximum_Capacity_of_R_Fuel_if_Container_1_has_R: R_1 - 2700 Yr__1 <= 0</li>
• Maximum_Capacity_of_R_Fuel_if_Container_2_has_R: R_2 - 2800 Yr__2 <= 0
Maximum_Capacity_of_R_Fuel_if_Container_3_has_R: R_3 - 1100 Yr__3 <= 0</li>
• Maximum_Capacity_of_R_Fuel_if_Container_4_has_R: R_4 - 1800 Yr__4 <= 0
• Maximum_Capacity_of_R_Fuel_if_Container_5_has_R: R_5 - 3400 Yr__5 <= 0
Maximum_Capacity_of_S_Fuel_if_Container_1_has_S: S_1 - 2700 Ys_1 <= 0</li>
• Maximum_Capacity_of_S_Fuel_if_Container_2_has_S: S_2 - 2800 Ys_2 <= 0
Maximum_Capacity_of_S_Fuel_if_Container_3_has_S: S_3 - 1100 Ys__3 <= 0</li>

    Maximum_Capacity_of_S_Fuel_if_Container_4_has_S: S_4 - 1800 Ys__4 <= 0</li>

Maximum_Capacity_of_S_Fuel_if_Container_5_has_S: S_5 - 3400 Ys__5 <= 0</li>
Maximum_Capacity_of_U_Fuel_if_Container_1_has_U: U_1 - 2700 Yu__1 <= 0</li>
Maximum_Capacity_of_U_Fuel_if_Container_2_has_U: U_2 - 2800 Yu__2 <= 0</li>
• Maximum_Capacity_of_U_Fuel_if_Container_3_has_U: U_3 - 1100 Yu__3 <= 0

    Maximum_Capacity_of_U_Fuel_if_Container_4_has_U: U_4 - 1800 Yu__4 <= 0</li>

Maximum_Capacity_of_U_Fuel_if_Container_5_has_U: U_5 - 3400 Yu__5 <= 0</li>

    Maximum_Shortfall_(500)Constraintfor_R_Fuel: R_1 + R_2 + R_3 + R_4 + R_5 >= 3500

• Maximum_Shortfall_(500) Constraintfor_S_Fuel: S_1 + S_2 + S_3 + S_4 + S_5 >= 2400

    Maximum_Shortfall_(500)Constraintfor_U_Fuel: U_1 + U_2 + U_3 + U_4 + U_5 >= 4400

• Binaries: Yr_1 Yr_2 Yr_3 Yr_4 Yr_5 Ys_1 Ys_2 Ys_3 Ys_4 Ys_5 Yu_1 Yu_2 Yu_3 Yu_4 Yu_5 y1_0 y1_1 y2_0 y2_1 y3_0 y3_1 End
```

O3 - 1

- Optimal Production PLan
 - Alloy 1 0
 - Alloy 2 1500
 - Alloy 3 500
 - Alloy 4 1000

These can be derived from the Constraints Section of the Sensitivity Report

Objective Function Value = 495000

Q3 - 2 - Check / Object will definitely increase

As per the sesitivity Report Maximum Allowable increase in Metal 3 is 100 GM. Hence if 200 GM of metal is imported then this exceeds allowable increase for the Optimal Solution. This will change the current Optimal Solution, unfortunately the sensitivity report does not tell how it will change.

From Solving the dual solution we see that the Shadow Price for Y3 is 555 (Please see ans to 3-4, details are provided). Hence even if we procure 100 Gm of Metal 3, cost incurred is 20000, while for the 100 GM we know a additional revnue of 55500 can be made.

If we have to procude all 200GM they can procure even if they decide not to use the additional 100 GM as it will change the optimal solution.

Hence we can procure the amount.

Objective increases by 35000 to 530000

Q3 - 3

- From the sensitivity report we can see that the Demand for Alloy 3 can be increased by 750 units without changing the Optimal Solution. So if the demand increases by 200, it will not change the optimal solution.
- If we solve the Dual Formulation, the Dual Price for Y6 (Corresponding Variable for the Demand Constraint for Alloy 3) is 59 (See 3-4 for Details below). Hence they will add 5 * 200 = 11,800. Overall Objective = 506800
- However, we know the profit per unit of Alloy 3 is 281. Ideally as per my understanding the Dual Price should have been same as the Profit (Objective Value), may be the numbers have been changed from the actual formulation. I will consider the increase in objective to be equal to the increase due to profit from selling the additional 200 units of Alloy 3. Hence the Objective will increase by 281 * 200 = 56200,

Final Objective = 551200

Q3-4

• The corresponding Dual formulations are:

0.2y1 + 0.4y2 + 0.4y3 + y4 + 0 + 0 + 0 >= 186

0.2y1 + 0.6y2 + 0.2y3 + 0 + y5 + 0 + 0 >= 111

0.3y1 + 0.3y2 + 0.4y3 + 0 + 0 + y6 + 0 >= 281

0.5y1 + 0.5y2 + 0 + 0 + 0 + 0 + y7 >= 188

• Constraints 3, 6, 7 are binding in Primal, hence the corresponding Dual Variables are non-Zero. Hence y3, y6 and y7 are non zero.

Solving above equations we get: y3 = 555 y6 = 59 y7 = 188

Substituting the value of Y3 in equation 1 we get the Surplus = 36. This is the Reduced Cost for x1. hence the profit needs to be increased by 36 (Profit = 222) for Sedon to accept the order

Q3-5

• As we can clearly see that the increase in the profit values for all are well outside the range of the permissible values as per the sensitivity report. The Solution will no longer remain optimal with these revised objective values. We need to resolve to find new Optimal Solution with these Profits

03 - 6

- From sensitivity report we see that maximum Allowed decrease of Alloy 2 is 500 (Actual Value = 1000), which does not alter the optimal solution.
- The government restriction which reduces sales of alloy 2 value to 1000, hence does not impact the optimal Solution

Q3-7

- Maximum Permissible change (increase) for Alloy 3 = 500. Actual change = 500. Hence percentage increase is 100%
- Maximum Permissible change (decrease) for Alloy 2 = 500. Actual change = 500. Hence percentage increase is 100%

Since the simultatneous change is more than 100%, hence this violates the 100% Rule for change. The solution may no longer remain optimal. We need to resolve the problem before making any conclusions.

Q3-8

Alloy 5 is introduced

The new sets of Primal equations are:

• Objective:

```
186x1 + 111x2 + 281x3 + 188x4 + 220x5
• Constraints:
0.2x1 + 0.2x2 + 0.3x3 + 0.5x4 + 0.5x5 \le 2000
0.4x1 + 0.6x2 + 0.3x3 + 0.5x4 + 0.4x5 \le 3000
0.2x1 + 0.2x2 + 0.4x3 + 0x4 + 0.1x5 \le 500
x1 \le 1000
x2 \le 2000
x3 \le 500
x4 \le 1000
x5 \le 1500
Let us assume that x5 = 0, then the formulation remains optimal if the following dual constraint is feasible and non-binding:
0.5y1 + 0.4y2 + 0.1y3 + 0 + 0 + 0 + 0 + 0 = 220
We know: y1, y2 = 0
y3 = 555,
```

hence $55.5 \ge 220$, which is infeasible. Hence x5 = 0, and with new alloy the old solution is no longer optimal

Q4

Decision Variables

- hiredEmpl_i, i = 1,2,3,4. Employees to be hired for Months September, October, January, February (Integers)
- transfrEmpl_i, i= 1..6, Employees to be trasferred from other location all 6 months (Integers)
- Binary Variables: isReqHire_1 (Hiring in March), isReqHire_2 (Hiring in December)
- analyst_1 = 79, as of First Day of September

Minimize Objective: 36000 analyst_1 + 34800 hiredEmpl_1 + 29100 hiredEmpl_2 + 12000 hiredEmpl_3 + 6000 hiredEmpl_4 + 20000 isReqHire_1 + 20000 isReqHire_2 + 8000 transfrEmpl_1 + 8000 transfrEmpl_2 + 8000 transfrEmpl_3 + 8000 transfrEmpl_4 + 8000 transfrEmpl_6

Subject To

- Demand_Dec: analyst_1 + 0.95 hiredEmpl_1 + 0.95 hiredEmpl_2 + 0.8 transfrEmpl_4 >= 65
- Demand_Feb: analyst_1 + 0.95 hiredEmpl_1 + 0.95 hiredEmpl_2 + hiredEmpl_3 + hiredEmpl_4 + 0.8 transfrEmpl_6 >= 90
- Demand_Jan: analyst_1 + 0.95 hiredEmpl_1 + 0.95 hiredEmpl_2 + hiredEmpl_3 + 0.8 transfrEmpl_5 >= 80
- Demand_Nov: analyst_1 + 0.95 hiredEmpl_1 + hiredEmpl_2 + 0.8 transfrEmpl_3 >= 90
- Demand_Oct: analyst_1 + hiredEmpl_1 + hiredEmpl_2 + 0.8 transfrEmpl_2 >= 105
- Demand_Sept: analyst_1 + hiredEmpl_1 + 0.8 transfrEmpl_1 >= 110
- Initial_Number_of_confirmed_Analyst_as_of_Sept01: analyst_1 = 79
- Transferred_Employee_20%Constraint: 1.2 analyst1 + 1.16 hiredEmpl_1 + 0.97 hiredEmpl_2 + 0.4 hiredEmpl_3 + 0.2 hiredEmpl_4 transfrEmpl_1 transfrEmpl_2 transfrEmpl_3 transfrEmpl_5 transfrEmpl_6 >= 0
- Hired Employees per month C1: hiredEmpl1 50 isReqHire_1 <= 0
- C2: hiredEmpl2 50 isReqHire_1 <= 0
- C3: hiredEmpl3 50 isReqHire_2 <= 0
- C4: hiredEmpl4 50 isReqHire_2 <= 0
- 0 <= hiredEmpl_1
- 0 <= hiredEmpl_2
- 0 <= hiredEmpl_3
- 0 <= hiredEmpl_4
- 0 <= transfrEmpl_10 <= transfrEmpl_2
- 0 <= transfrEmpl_3
- 0 <= transfrEmpl_4
- 0 <= transfrEmpl_5
- 0 <= transfrEmpl_6

End

```
Transferred Employee by Month 1 :: 25 ::
Transferred Employee by Month 2 :: 19 ::
Transferred Employee by Month 3 :: 1 ::
Transferred Employee by Month 4 :: 0 ::
Transferred Employee by Month 5 :: 0 ::
Transferred Employee by Month 6 :: 1 ::
Is Hiring required Period 1 :: 1 ::
Is Hiring required Period 2 :: 0 ::
Nu mber of Hired Employees by Month1 :: 11 ::
Nu mber of Hired Employees by Month2 :: 0 ::
Nu mber of Hired Employees by Month3 :: 0 ::
Nu mber of Hired Employees by Month4 :: 0 ::
Number of Analyst on Month 1 (September) 1 :: 79.0 ::
Objective 3614800.0
```

Q5

- Problem is not solving if we have to match monthly demand. For Month 5 Demand == 2000, this cannot be achieved (Max that can be achieved is 1600 for month 5)
- LP will solve if monthly constraints does not have to be met. Hence we will design a solution to meet overall demand of 7000 Stones

Decision variables (DV)

- Q1_Stone_i, i = 1..6
- Q2_Stone_i, i = 1..6
- carryFwd_i, i = 1..6 Carry for each period (Extra Stones)
- unMetDemand_i, i = 1..6 Unmet Demand for each period (Less stones Stones to be met in subsequent years)

Minimize Objective: 1000 carryFwd_0 + 1000 carryFwd_1 + 1000 carryFwd_2 + 1000 carryFwd_3 + 1000 carryFwd_4 + 1000 carryFwd_5 + 1000 carryFwd_6 + 215000 q1Stones_1 + 215000 q1Stones_2 + 215000 q1Stones_3 + 207500 q1Stones_4 + 207500 q1Stones_5 + 207500 q1Stones_6 + 240000 q2Stones_1 + 240000 q2Stones_2 + 240000 q2Stones_3 + 232500 q2Stones_4 + 232500 q2Stones_5 + 232500 q2Stones_6

Subject To

- All DV >0
- Stopped_Production_1: q2Stones_4 = 0
- Stopped_Production_2: q2Stones_5 = 0
- Overall Demand_Constraints_6: q1Stones_1 + q1Stones_2 + q1Stones_3 + q1Stones_4 + q1Stones_5 + q1Stones_6 + q2Stones_1 + q2Stones_2 + q2Stones_3
 - + q2Stones_4 + q2Stones_5 + q2Stones_6 >= 7000
- Production_Constraints_Q1_1: q1Stones_1 <= 800
- Production_Constraints_Q1_2: q1Stones_2 <= 800
- Production_Constraints_Q1_3: q1Stones_3 <= 800
- Production_Constraints_Q1_4: q1Stones_4 <= 800
- Production_Constraints_Q1_5: q1Stones_5 <= 800
- Production_Constraints_Q1_6: q1Stones_6 <= 800
- Production_Constraints_Q2_1: q2Stones_1 <= 1400
- Production_Constraints_Q2_2: q2Stones_2 <= 1400
- Production_Constraints_Q2_3: q2Stones_3 <= 1400
- Production_Constraints_Q2_4: q2Stones_4 <= 1400
- Production_Constraints_Q2_5: q2Stones_5 <= 1400
- Production_Constraints_Q2_6: q2Stones_6 <= 1400
- Stone_Storage_Limit_1: carryFwd_1 <= 1200
- Stone_Storage_Limit_2: carryFwd_2 <= 1200
- Stone Storage Limit 3: carryFwd 3 <= 1200
- Stone_Storage_Limit_4: carryFwd_4 <= 1200
- Stone_Storage_Limit_5: carryFwd_5 <= 1200
- Stone_Storage_Limit_6: carryFwd_6 <= 1200
- Demand_C1: carryFwd_1 + q1Stones_1 + q2Stones_1 + unMetDemand_1 <= 700
- Demand_C2: carryFwd_1 carryFwd_2 + q1Stones_2 + q2Stones_2 unMetDemand_1 + unMetDemand_2 <= 700
- Demand_C3: carryFwd_2 carryFwd_3 + q1Stones_3 + q2Stones_3 unMetDemand_2 + unMetDemand_3 <= 1000
- Demand_C4: carryFwd_3 carryFwd_4 + q1Stones_4 + q2Stones_4 unMetDemand_3 + unMetDemand_4 <= 1200
- Demand_C5: carryFwd_4 carryFwd_5 + q1Stones_5 + q2Stones_5 unMetDemand_4 + unMetDemand_5 <= 2000
- Demand C6: carryFwd 5 carryFwd 6 + g1Stones 6 + g2Stones 6 unMetDemand 5 + unMetDemand 6 <= 1400

End

```
Carry Forward :: Period :: 0 :: 0.0 ::
Carry Forward :: Period :: 1 :: 100.0 :: Carry Forward :: Period :: 2 :: 200.0 ::
Carry Forward :: Period :: 3 :: 800.0 :: Carry Forward :: Period :: 4 :: 400.0 ::
Carry Forward :: Period :: 5 :: 0.0 ::
Carry Forward :: Period :: 6 :: 0.0 ::
Quarry1 :: Period :: 1 :: 800.0 ::
Quarry1 :: Period :: 2 :: 800.0 ::
Quarry1 :: Period :: 3 :: 800.0 ::
Quarry1 :: Period :: 4 :: 800.0 ::
Quarry1 :: Period :: 5 :: 800.0 ::
Quarry1 :: Period :: 6 :: 800.0 ::
Quarry2 :: Period :: 1 :: 0.0 ::
Quarry2 :: Period :: 2 :: 0.0 ::
Quarry2 :: Period :: 3 :: 800.0 ::
Quarry2 :: Period :: 4 :: 0.0 ::
Quarry2 :: Period :: 5 :: 0.0 ::
Quarry2 :: Period :: 6 :: 1400.0 ::
Unmet Demand :: Period :: 1 :: 0.0 :: Unmet Demand :: Period :: 2 :: 0.0 :: Unmet Demand :: Period :: 3 :: 0.0 ::
Unmet Demand :: Period :: 4 :: 0.0 ::
Unmet Demand :: Period :: 5 :: 800.0 ::
Unmet Demand :: Period
Objective 1533000000.0
```

Q - 6

Decision Variables:

- xi, i=1..5. Mins for each type of advertisement
- $d1_0$: if this takes positive value, then GRP Overall (Goal 1) >=100
- d1_1: if this takes positive value, then GRP Overall (Goal 1)<=100 $\,$
- d2_0: if this takes positive value, then GRP Sport (Goal 2)>=20
- d2_1: if this takes positive value, then GRP Sport (Goal 2)<=20 $\,$
- d3_0: if this takes positive value, then GRP Eng Chnl (Goal 2)>=5
- d3_1: if this takes positive value, then GRP Eng Chnl (Goal 2)<=5

Minimize Objective: d1_1 + d2_1 + d3_0

- Goal1_C1: d1_0 + d1_1 + 4.2 x1 + 3.5 x2 + 2.8 x3 + 2.5 x4 + 0.2 x5 >= 100
- Goal2_C2: d2_0 + d2_1 + 4.2 x1 + 3.5 x2 >= 20
- Goal3_C3: d3_0 d3_1 0.2 x5 >= -5
- Budget_C4: 120000 x1 + 85000 x2 + 70000 x3 + 60000 x4 + 25000 x5 <= 2000000
- All Variables >= 0

End

Cricket :: 0 ::
Oth Sport :: 8 ::
Hindi Serial :: 0 ::
Hindi Movie :: 22 ::
English News :: 0 ::
D1 0 :: 0.0
D1 1 :: 17.0
D2 0 :: 0.0
D2 1 :: 0.0
D3 0 :: 0.0
D3 1 :: 0.0
Objective 17.0::