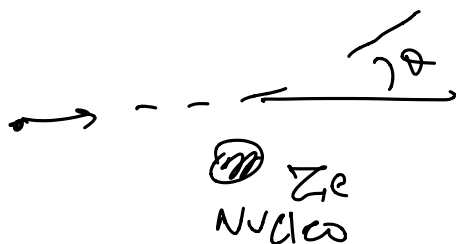


$$f(\theta | \vec{p}, m, Ze)$$



$$\frac{d\sigma}{d\Omega}$$

Settore d'inter
diff. di
Rutherford.

$$d\Omega = \sin\theta d\theta d\varphi = 2\pi \sin\theta d\theta$$

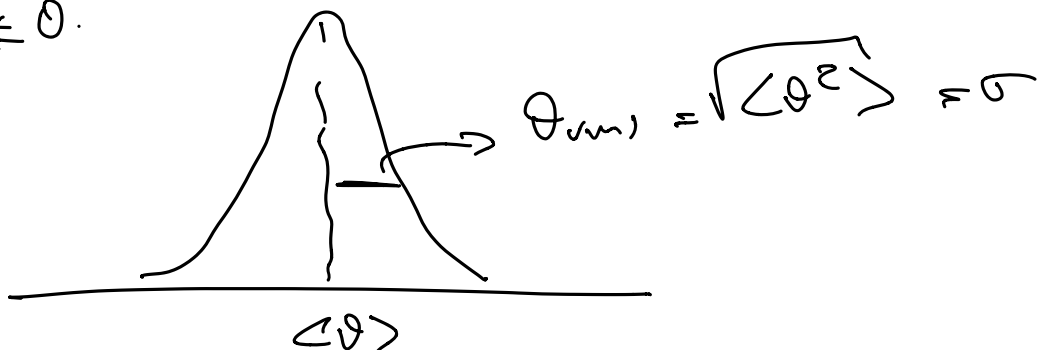
$$\frac{d\sigma}{d\Omega} \propto \frac{1}{\sin^4 \frac{\theta}{2}}$$

$$\langle \theta^n \rangle = \frac{\int \theta^n \frac{d\sigma}{d\Omega} d\Omega}{\int \frac{d\sigma}{d\Omega} d\Omega} \propto \frac{\int \theta^n \frac{1}{\sin^4 \frac{\theta}{2}} \sin\theta d\theta}{\int \frac{1}{\sin^4 \frac{\theta}{2}} \sin\theta d\theta}$$

$$\langle \theta \rangle = 0$$

$$\langle \theta^2 \rangle \neq 0.$$

$$f(\theta | \dots) \propto \frac{1}{\sqrt{2\pi} \sigma_{rms}} e^{-\frac{\theta^2}{2\sigma_{rms}^2}}$$

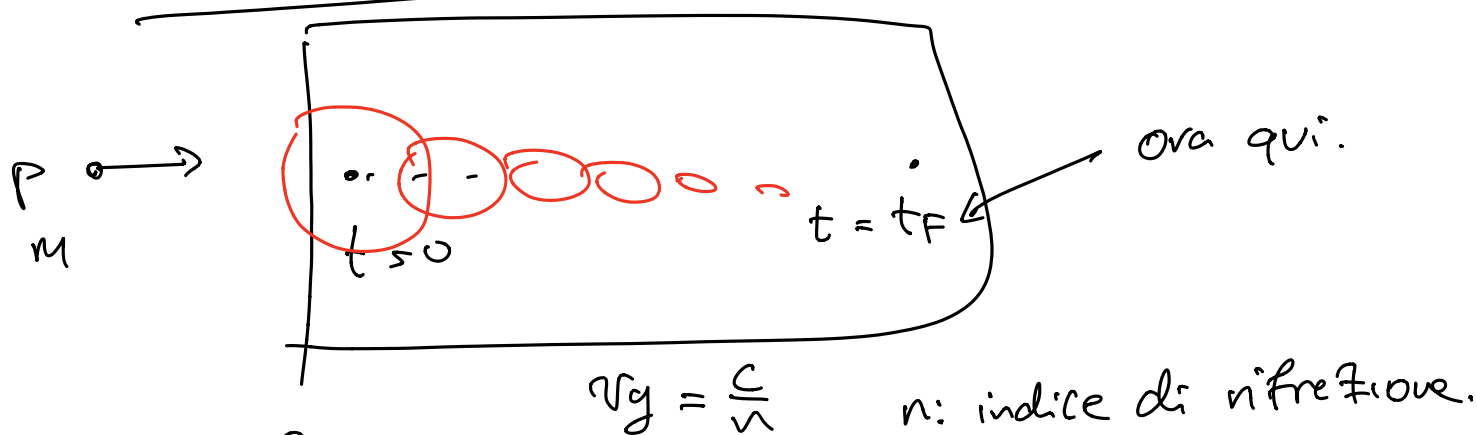


$$\sqrt{CO^2} = 21 \text{ MeV} \frac{Z_{\text{proj.}}}{\beta P} \sqrt{\frac{x}{x_0}} \quad x: \text{spessore attravers. nel materiale.}$$

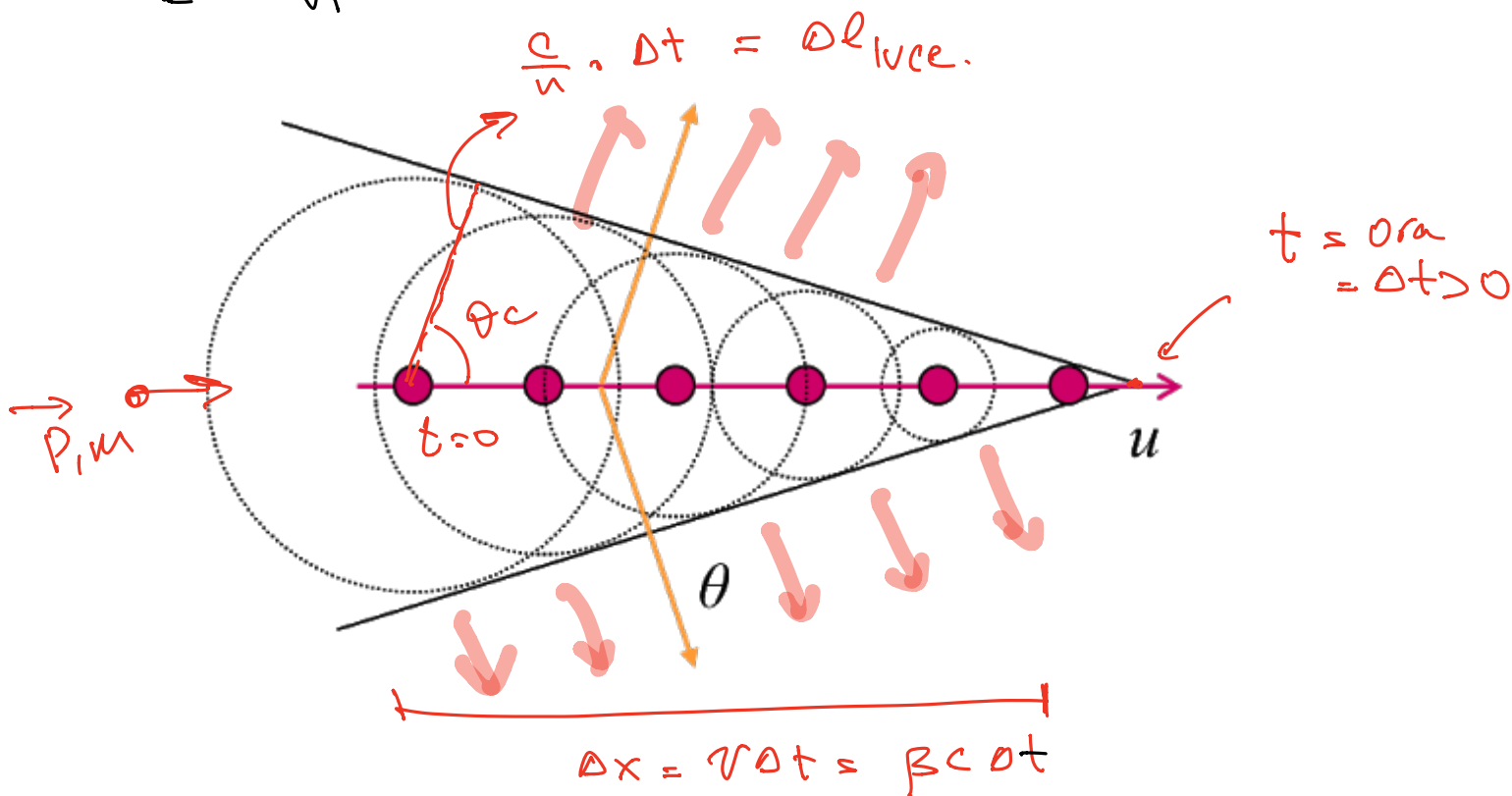
$$x_0 \propto \rho \frac{NA}{A} Z^2 \ln(183 Z^{-1/3}) \quad x_0: \text{lunghezza di radiazione Carott. del mezzo non del proiettile.}$$

Interazione particelle coniche nel mezzo.

Effetto Cerenkov (1934)



$$\beta = \frac{p}{E} = \frac{p}{\sqrt{p^2 c^2 + m^2 c^4}}$$



$$\frac{d\mathbf{x}}{dt} = \beta c \hat{\mathbf{x}} \cdot \cos \theta_c.$$

$$\cos \theta_c = \frac{1}{\beta n} \quad \text{angolo di Cerenkov } \theta_c$$

$$\cos \theta_c \leq 1 \Rightarrow \frac{1}{\beta n} \leq 1 \Rightarrow \beta \geq \frac{1}{n} = \beta_{th.}$$

Effetto a soglia.



$$\beta \geq \frac{1}{n} = \beta_{th.} = \frac{P_{th.}}{E_{th.}} = \frac{P_{th.}}{\sqrt{P_{th.}^2 + m^2}}$$

$$\beta = \frac{P}{E} = \frac{P}{\sqrt{P^2 + m^2}} \geq \frac{1}{n}.$$

$$n^2 = \frac{P_{th.}^2 + m^2}{P_{th.}^2} = 1 + \frac{m^2}{(P_{th.})^2}.$$

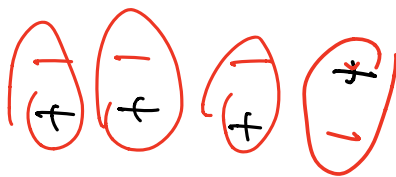
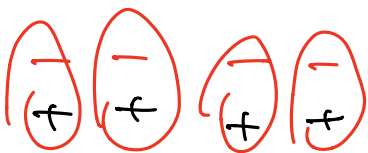
$$n^2 - 1 = \frac{m^2}{P_{th.}^2} \Rightarrow P_{th.} = \frac{m}{\sqrt{n^2 - 1}}$$

$$P > \frac{m}{\sqrt{n^2 - 1}} \quad \text{emissione luce Cerenkov.}$$

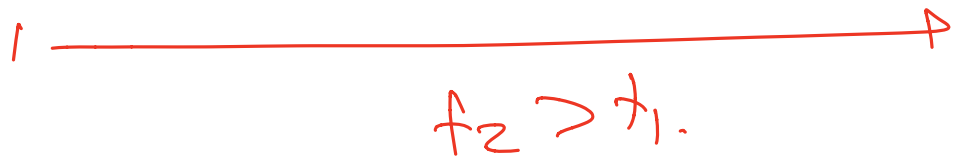
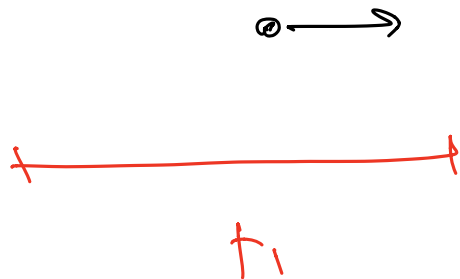
$P_{lum} \rightarrow$



$$\beta > \frac{1}{n_1} \text{ ed } \beta < \frac{1}{n_2} \Rightarrow \frac{1}{n_1} < \beta < \frac{1}{n_2}$$



\rightarrow



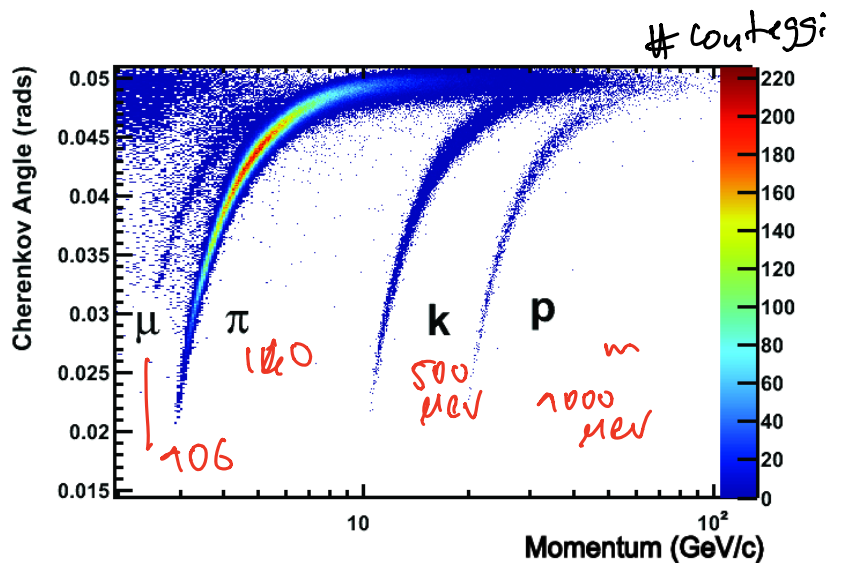
$$\cos \theta_c = \frac{1}{\beta n}$$

$$= \frac{1}{n} \frac{E}{p} = \frac{1}{n} \sqrt{1 + \left(\frac{m}{p}\right)^2}$$

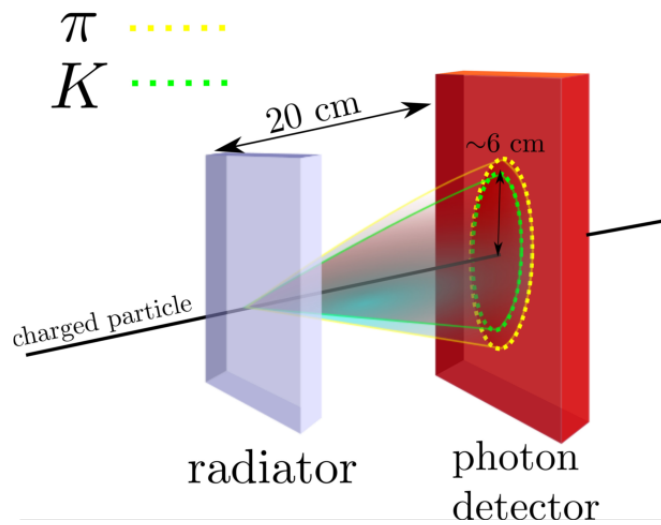
$$\theta_c = \arccos \left[\frac{1}{n} \sqrt{1 + \left(\frac{m}{p}\right)^2} \right]$$

$$p > p_{th} = \frac{m}{\sqrt{n^2 - 1}}$$

Se misuro $(p, \theta_c) \Rightarrow$ stime massa.
 \Rightarrow identificazione particella.



misuro p con spettrometro.



quante energie emesse con luce Cherenkov?
 Z : proiettile.
 dall'EM.

$$\frac{d^2N}{dx dE} = \frac{\alpha Z^2}{4\pi} \sin^2 \theta_C$$

di fotoni emessi per unità di spessore
 unità di energia.

luce blu: 400 nm. = $4 \times 10^2 \times 10^6$ fm

luce rosso: 700 nm. = $7 \times 10^2 \times 10^6$ fm

$$E = h\nu = h \frac{c}{\lambda} = Z\beta \frac{hc}{\lambda} = Z\beta \frac{200 \text{ MeV} \times \text{fm}}{\lambda}$$

$$\text{Blu: } E = Z\beta \times \frac{200 \text{ MeV fm}}{4 \times 10^8 \text{ fm}} = 3 \times \frac{10^8}{10^8} \text{ eV.}$$

$$= 3 \text{ eV.}$$

$$\text{rosso: } E = 1.7 \text{ eV}$$

$$E = \hbar \omega = \frac{\hbar c}{\lambda}$$

$$dE = \hbar c \frac{1}{\lambda^2} d\lambda$$

$$\frac{d^2 N}{dx d\lambda} = \frac{d^2 N}{dx dE} \frac{dE}{d\lambda} \propto \frac{\alpha Z^2}{\hbar c} \frac{1}{\lambda^2} \sin^2 \theta_c.$$

$\lambda_{\max} \approx 1000 \text{ nm}$

$$\frac{dN}{dx} \propto \int_{\lambda_{\min} = 410} \frac{1}{\lambda^2} d\lambda$$

$$\frac{dN}{dx} \approx 450 Z^2 \sin^2 \theta_c \text{ fotoni/cm.}$$

$$\sin^2 \theta \approx 1. \quad Z^2 \approx 1.$$

$$\Rightarrow \text{circa } 450 \text{ fotoni/cm.}$$

$$\langle E \rangle \approx Z eV.$$

$$\Rightarrow \text{circa } \frac{dE}{dx} \approx 900 \text{ eV/cm.}$$

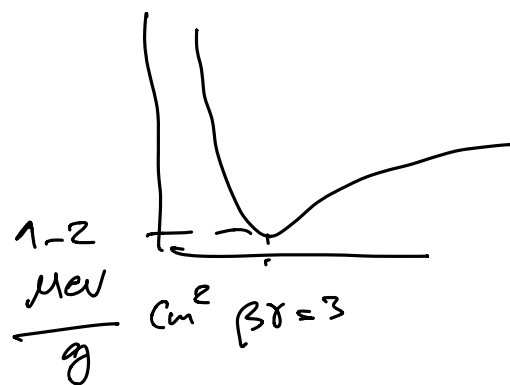
energia emessa per Cerenkov.

$$\frac{1}{\rho} \frac{dE}{dx} \Big|_{\text{min.}} \approx 1-2 \frac{\text{MeV}}{\text{cm}}$$

Nell'acqua:

$$\frac{dE}{dx} \Big|_{\text{Cerenkov}} \approx 1 \frac{\text{KeV}}{\text{cm.}}$$

$$\frac{dE}{dx} \Big|_{\text{ion.}} \approx 1 \frac{\text{MeV}}{\text{cm.}} \Rightarrow$$



Perdite per Cerenkov trascurabile