

P-P PHYSICS AT LHC

Hard scattering. Underlying event. Pile Up
Lecture 2

DIPARTIMENTO DI FISICA



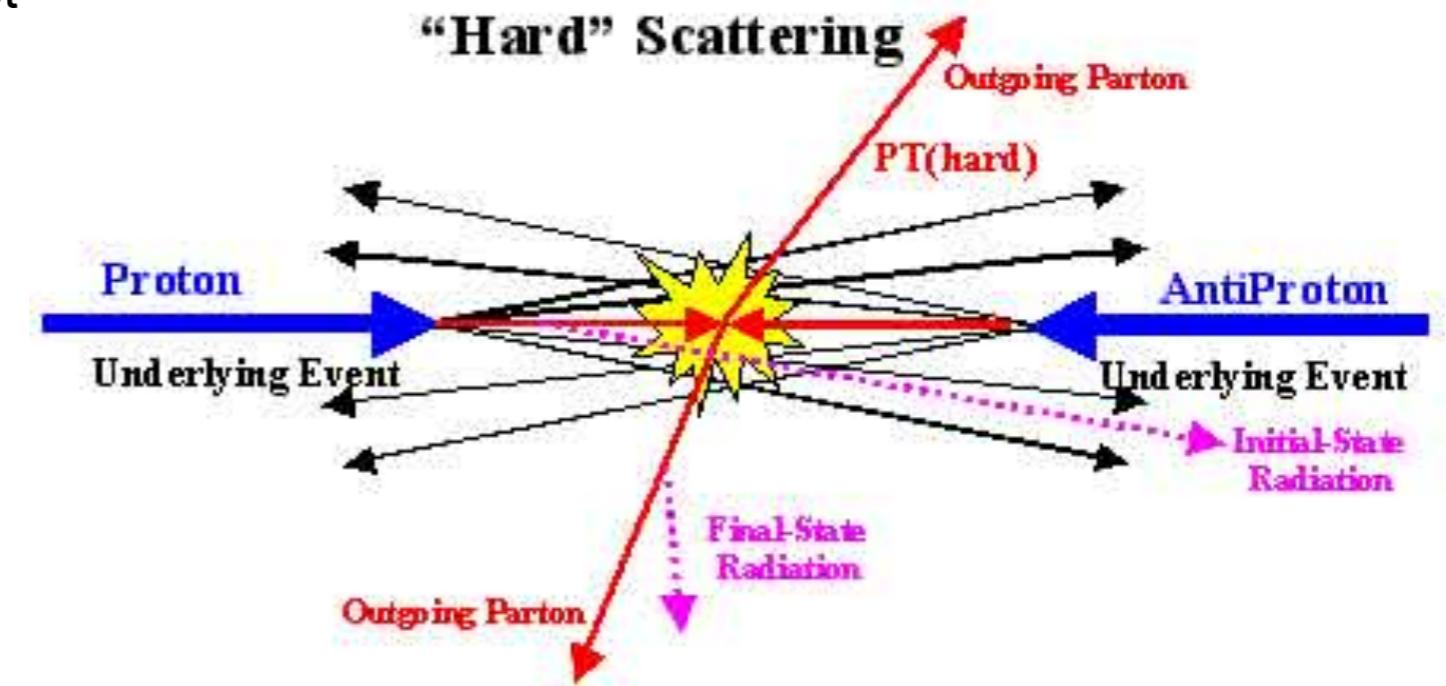
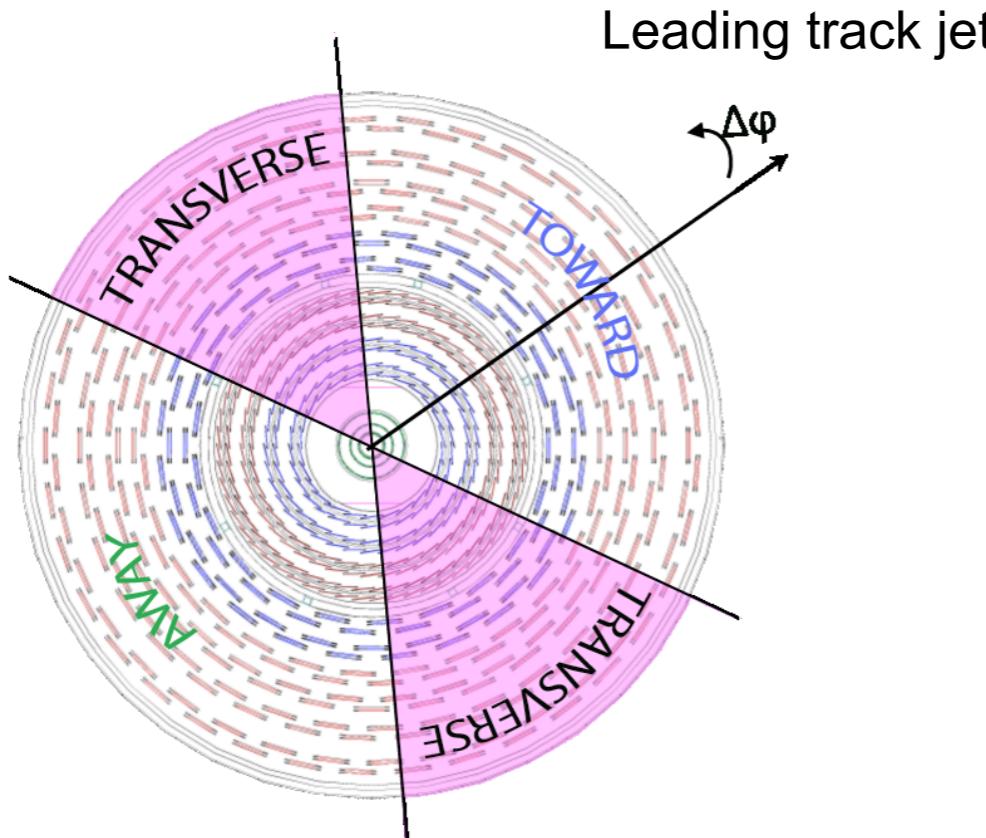
SAPIENZA
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Fisica delle Particelle Elementari, Anno Accademico 2015-16

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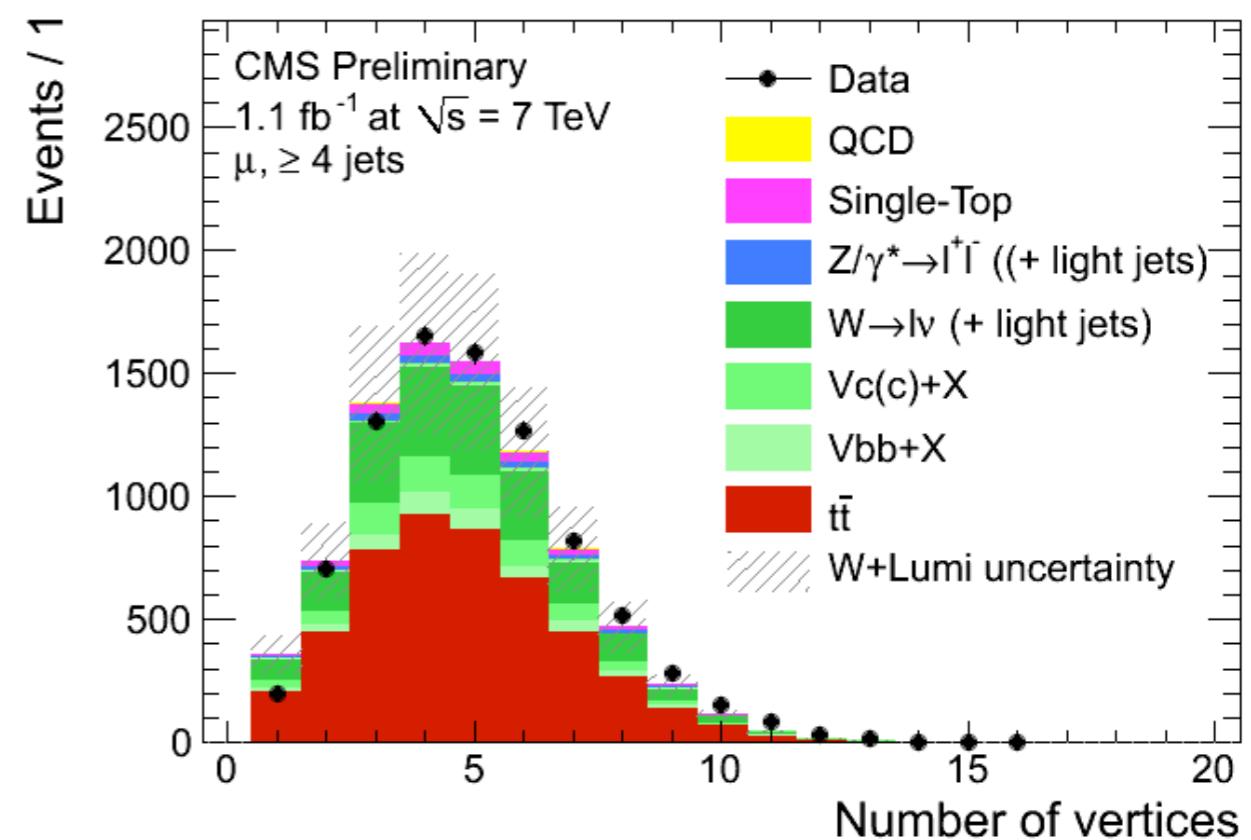
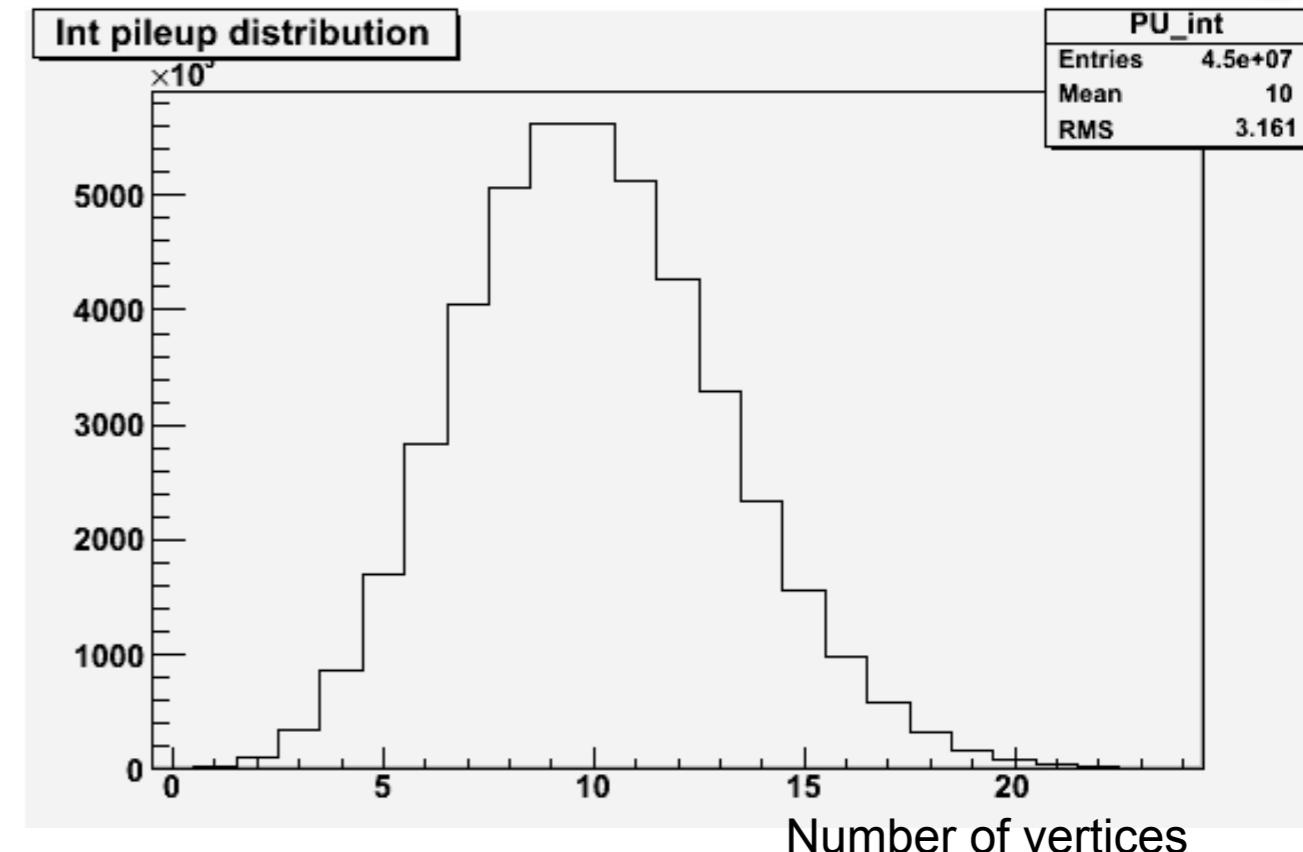
UNDERLYING EVENT



- Jet reconstruction with only charged tracks
- Use leading jet (jet with highest pt in the event) to define forward direction
- Study activity in 4 different regions

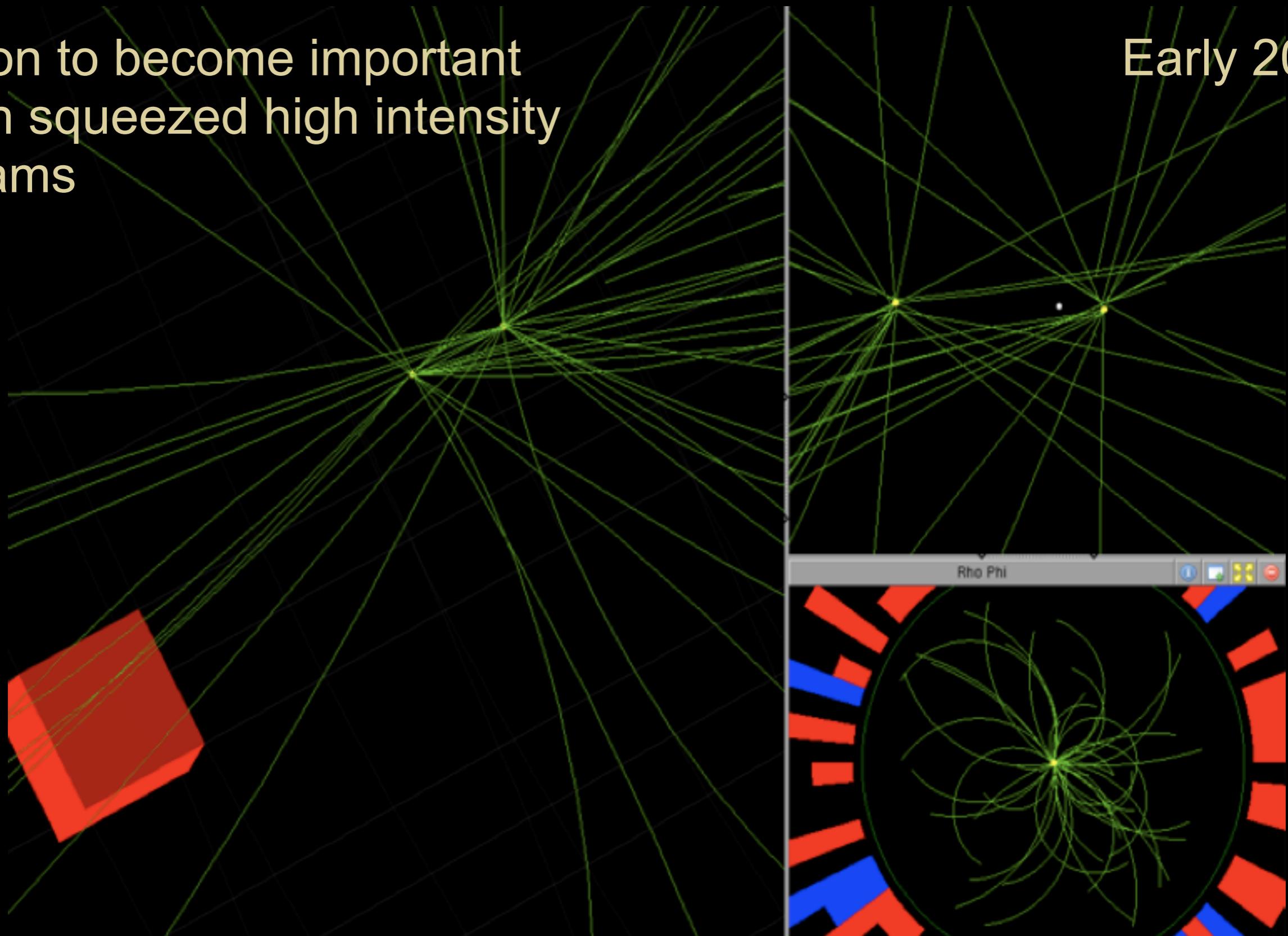
PILE-UP

- High probability of more than 1 proton-pair interaction with
 - ▶ smaller beam section
 - ▶ higher number of protons per bunch
- Typically one interesting hard-scattering of interest
 - the “event” causing the trigger
- Additional collisions in same bunch crossing increase average energy density in detectors
 - higher occupancy
 - distortion or mis-measurement of energy in calorimeters
 - Potential inefficiency in track reconstruction in very busy events
- Much larger event processing time

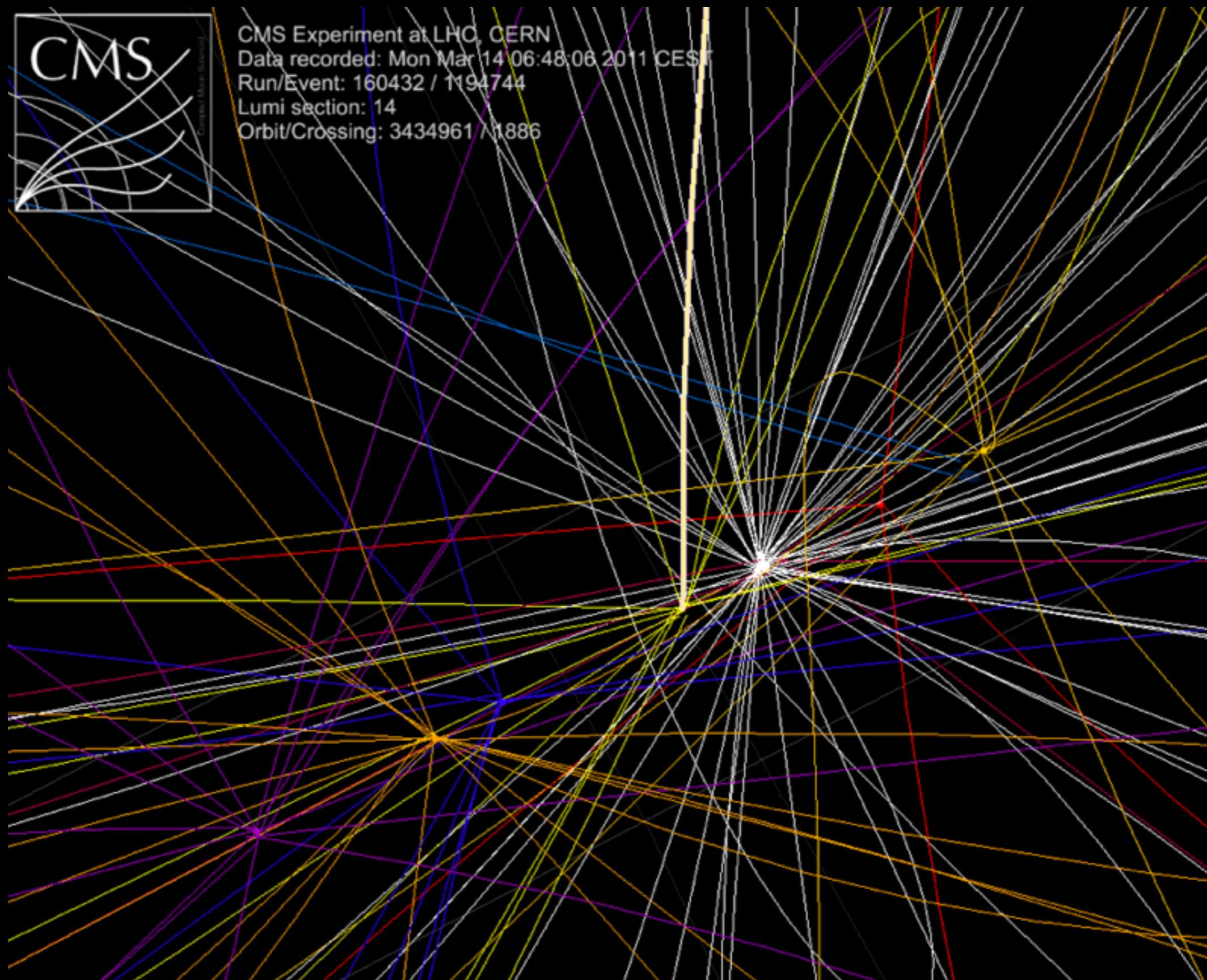


PILE-UP AT LOW LUMINOSITY

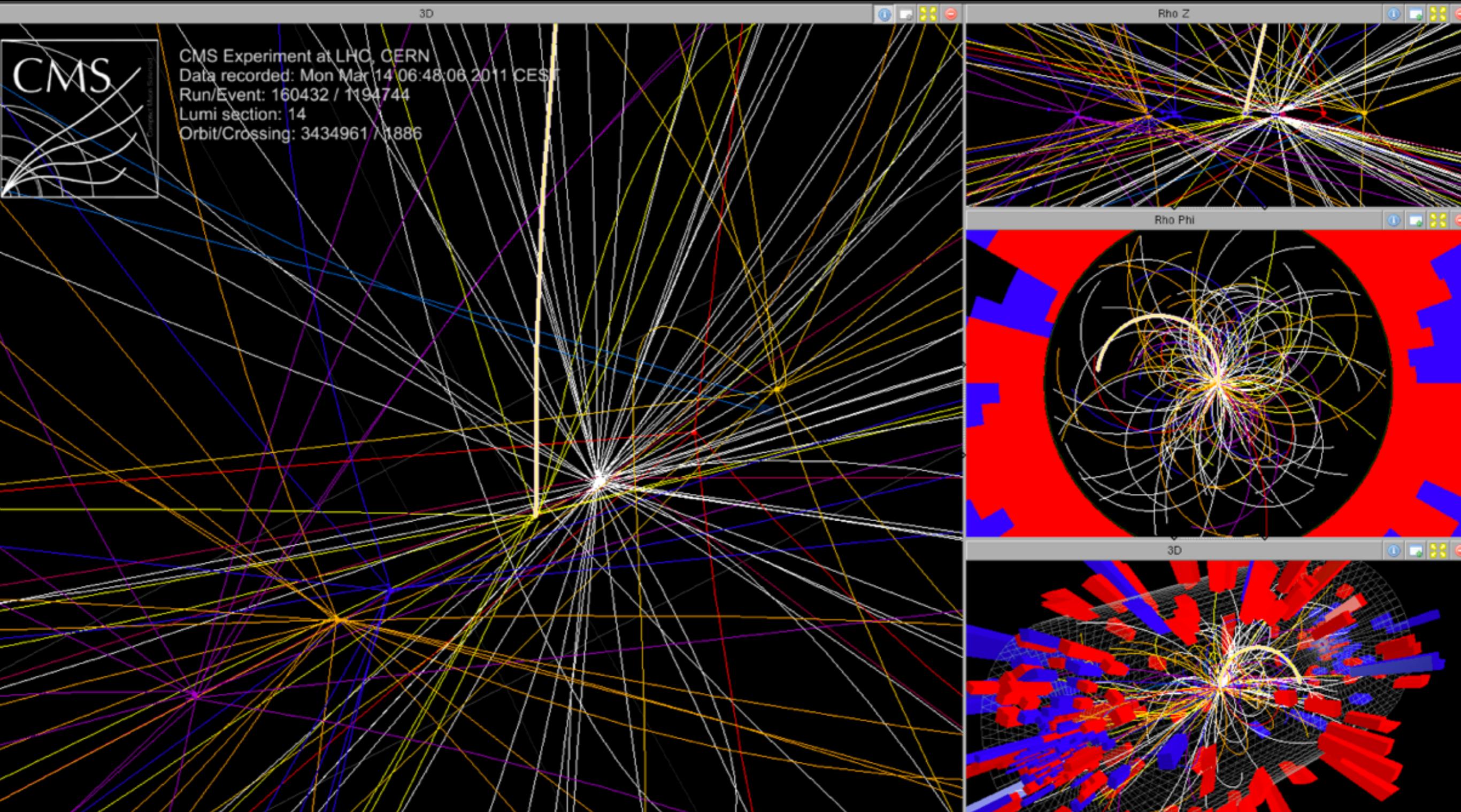
Soon to become important
with squeezed high intensity
beams



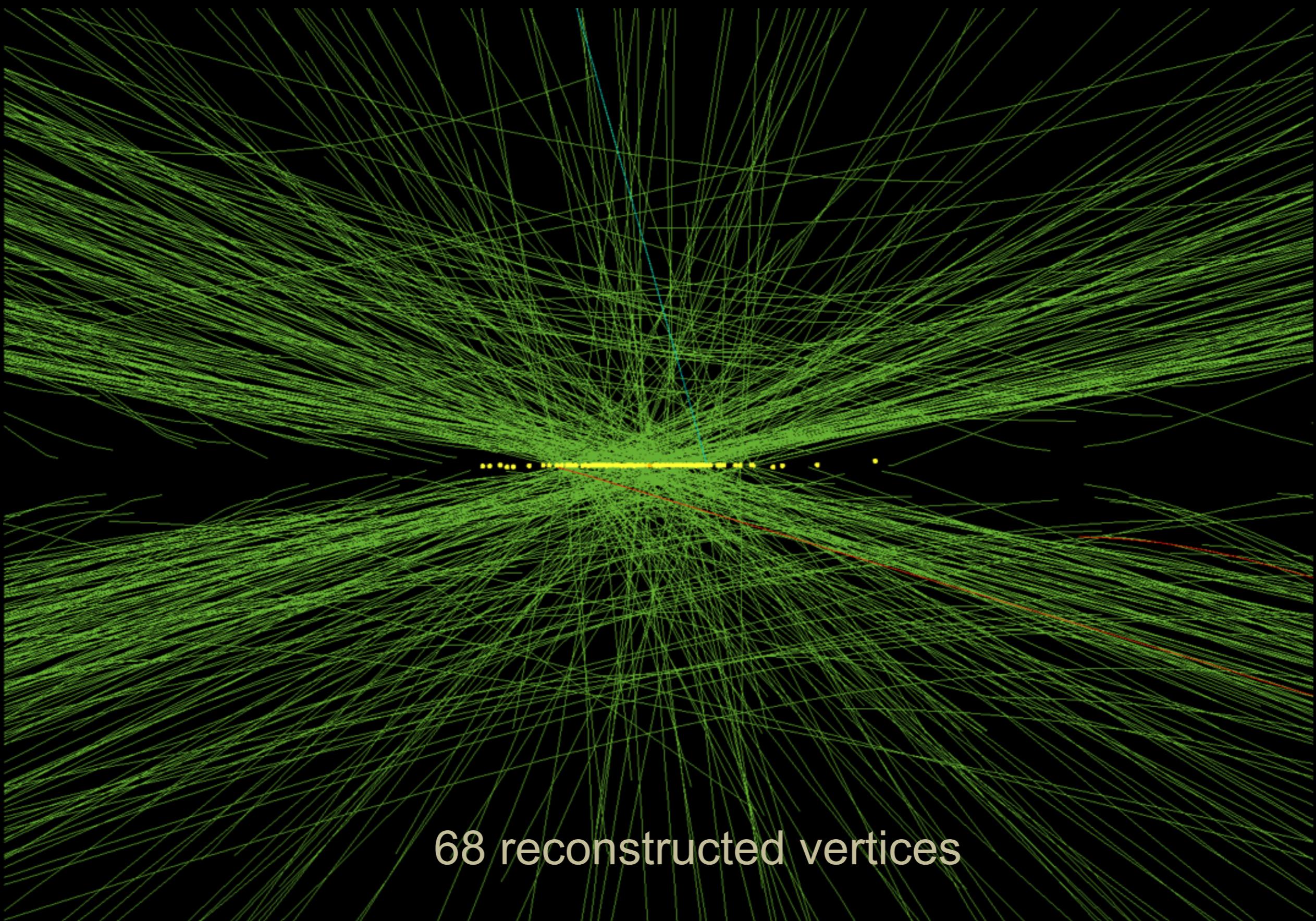
PILE-UP EARLY 2011

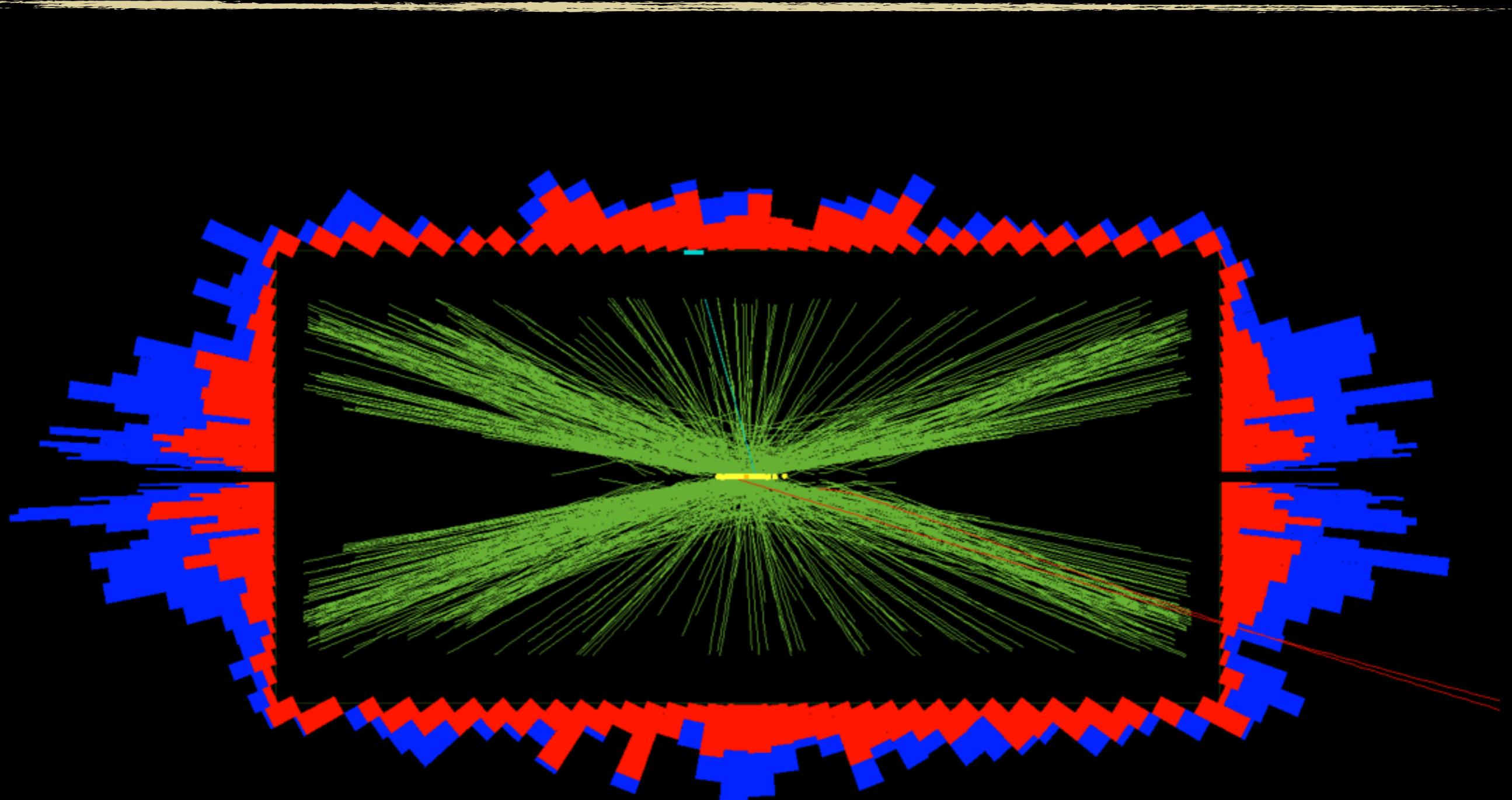


PILE-UP EARLY 2011

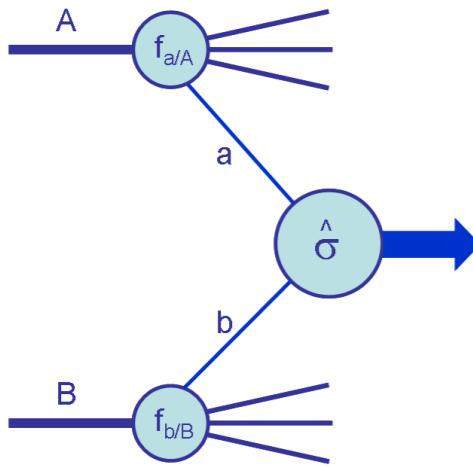


HIGH PILE-UP EVENT IN 2012





HADRONIC CROSS SECTION



$$\sigma_{AB} = \int dx_a dx_b f_{a/A}(x_a) f_{b/B}(x_b) \hat{\sigma}_{ab \rightarrow X}$$

- Successful data/prediction comparison until corrections due to virtual and real gluons computed
 - Large diverging logarithms
- Corrections depend on momentum scale Q^2 of the process
 - e.g. intermediate mass M^2 or p_T^2 of leptons in final state
 - Logarithmic violation of scaling (as already seen in structure functions)

$$\sigma_{AB} = \int dx_a dx_b f_{a/A}(x_a, Q^2) f_{b/B}(x_b, Q^2) \hat{\sigma}_{ab \rightarrow X} \quad Q^2 = \mu_F^2$$

- Factorization scale: energy scale at which perturbative (short range) and non-perturbative (long range) effects can be separated

COMPUTING CROSS SECTION

- In addition to PDF corrections must take into account also corrections to hard process cross section

$$\sigma_{AB} = \int dx_a dx_b f_{a/A}(x_a, \mu_F^2) f_{b/B}(x_b, \mu_F^2) \times [\hat{\sigma}_0 + \alpha_S(\mu_R^2) \hat{\sigma}_1 + \dots]_{ab \rightarrow X}$$

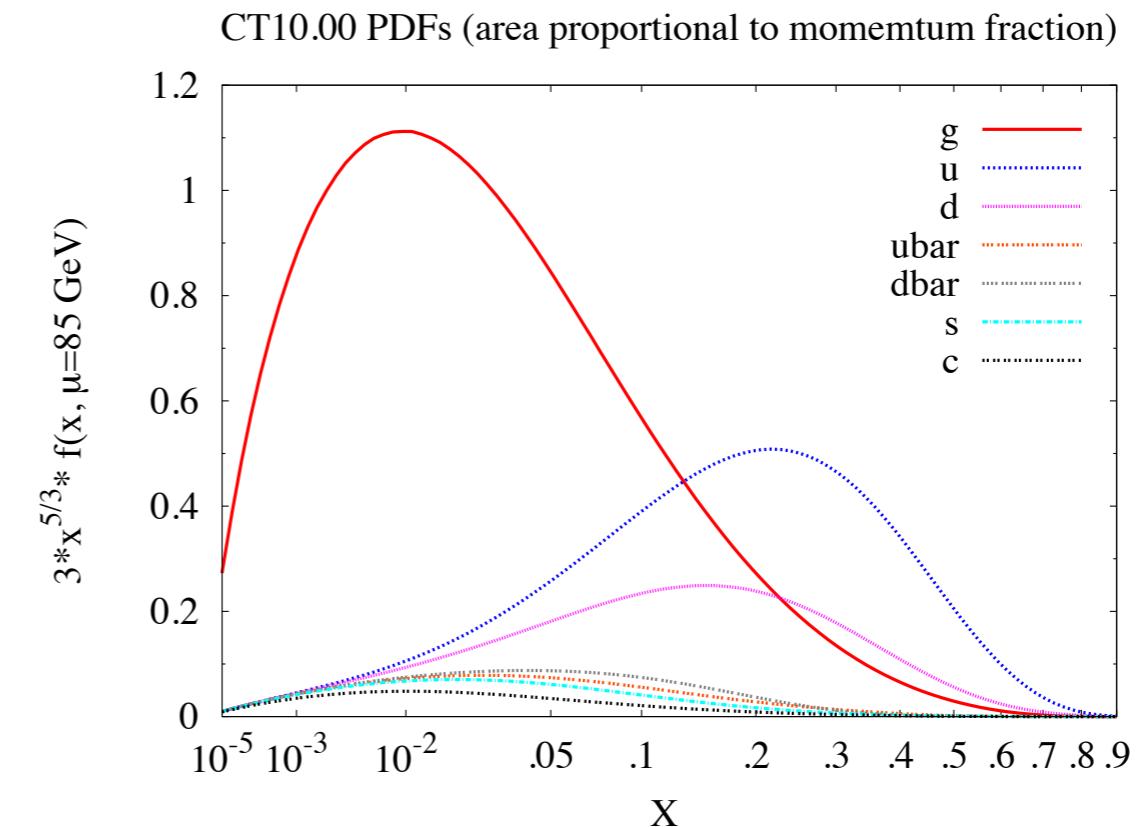
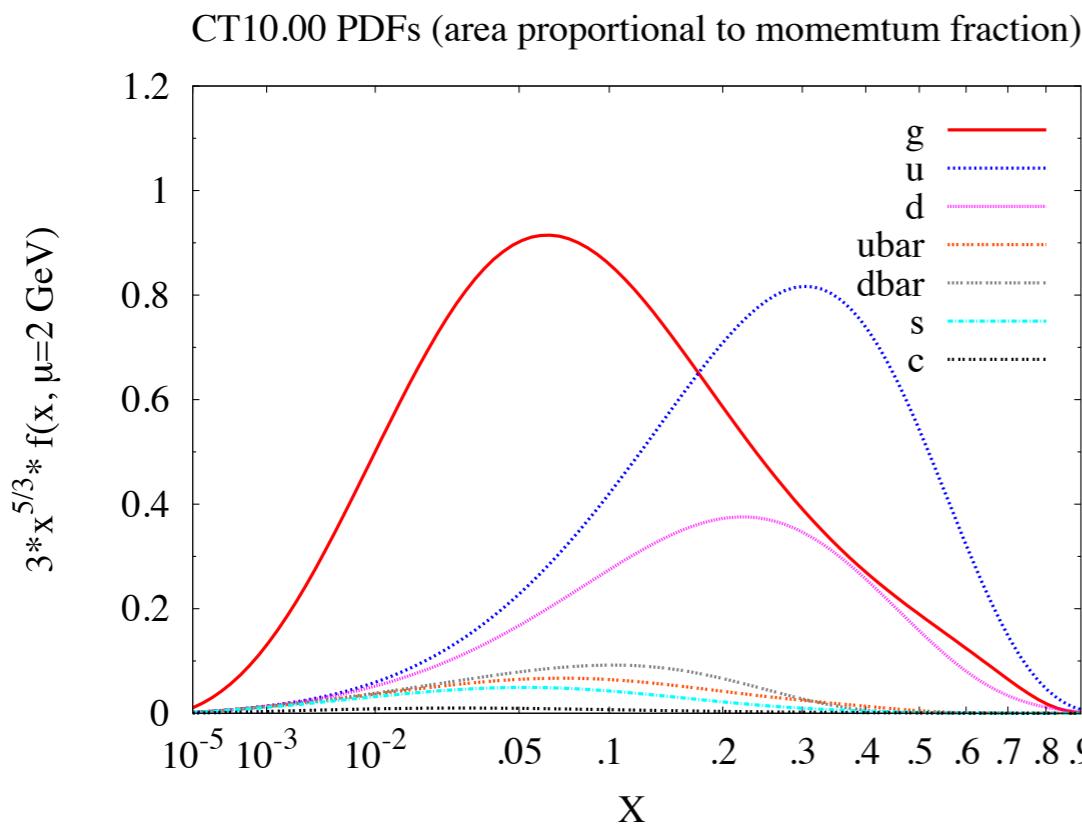
- Corrections specific to individual hard processes and cannot be generalized
 - Introduces dependency on QCD renormalization scale μ_R via α_S
- Typically one uses $\mu_R = \mu_F$
 - Value used depends on the process being studied: often m_Z , m_W , p_T^2 of products in final state (jets or leptons) can be appropriate
- Cross sections and PDFs must be computed at same perturbation order for large logarithms to cancel each other

$$\sigma_{AB} = \sum_{a,b=q,g} [\hat{\sigma}_{ab}^{\text{LO}} + \alpha_S(Q^2) \hat{\sigma}_{ab}^{\text{NLO}} + \dots] \otimes f_{a/A}(x_a, Q^2) \otimes f_{b/B}(x_b, Q^2)$$

NLO

EVOLUTION OF PARTON DENSITY FUNCTIONS

- The dependency of PDFs from x is determined from fit to data
 - global fit to fixed target, ep, and collider data
- Dependency of PDFs from momentum scale cannot be computed analytically from first principles
- Single experiments explore different and very specific values of
- In principle one would need to measure each PDF at each scale Q^2 !
 - Not practical nor allows to benefit from existing knowledge



gluon momentum fraction grows at higher scales

DOKSHITZER–GRIBOV–LIPATOV–ALTARELLI–PARISI EQUATIONS

- Integro-differential equations to compute PDFs at a desired scale Q^2 given measurements at a different scale

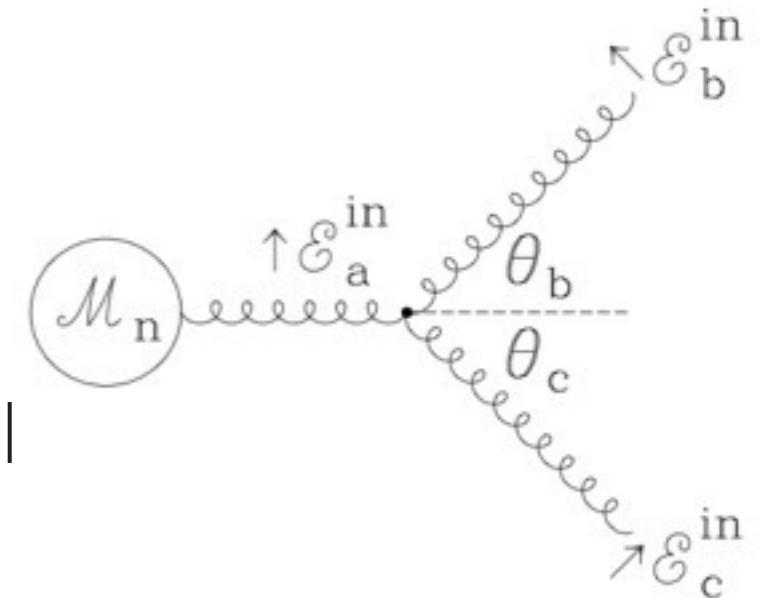
$$\frac{\partial q_i(x, \mu^2)}{\partial \log \mu^2} = \frac{\alpha_S}{2\pi} \int_x^1 \frac{dy}{y} \left\{ P_{q_i q_j}(y, \alpha_S) q_j\left(\frac{x}{y}, \mu^2\right) + P_{q_i g}(y, \alpha_S) g\left(\frac{x}{y}, \mu^2\right) \right\}$$

$$\frac{\partial g(x, \mu^2)}{\partial \log \mu^2} = \frac{\alpha_S}{2\pi} \int_x^1 \frac{dy}{y} \left\{ P_{g q_j}(y, \alpha_S) q_j\left(\frac{x}{y}, \mu^2\right) + P_{g g}(y, \alpha_S) g\left(\frac{x}{y}, \mu^2\right) \right\}$$

$$P_{ab}(x, \alpha_S) = P_{ab}^{(0)}(x) + \frac{\alpha_S}{2\pi} P_{ab}^{(1)}(x) + \dots \quad a, b = g, q, \bar{q}$$

- Fundamental for having PDFs for LHC processes based on previous experiments

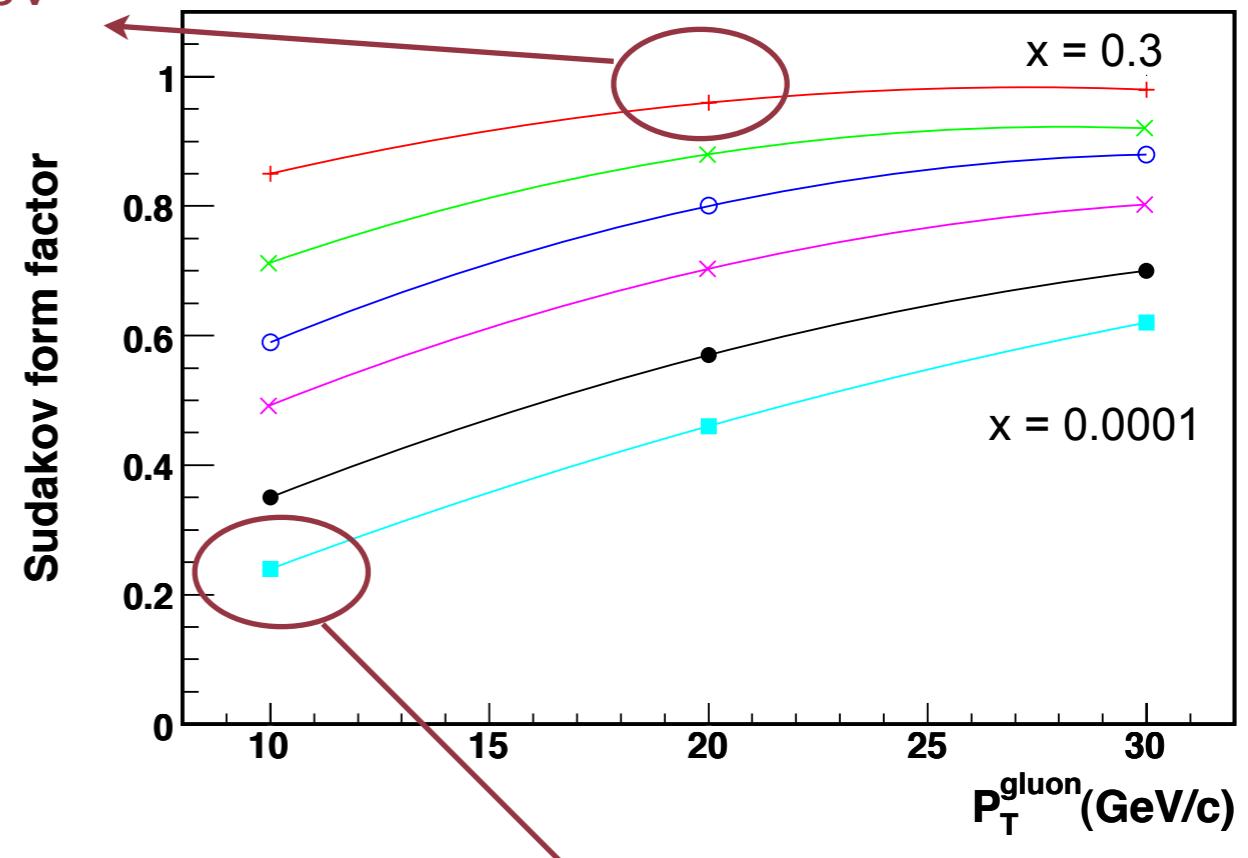
- Splitting functions $P_{ab}(x)$: probability of partons emitting additional quarks or gluons in collinear | – depends again on both x and momentum scale



SUDAKOV FORM FACTORS

- Probability of parton evolution for softer scale without emission of partons
- Gluons are dominant at LHC hence gluon splitting is most important
- Probability of a initial-state gluon at momentum scale of 100 GeV **NOT emitting** a gluon of given p_T
- Depends on
 - parton type
 - hard process scale
 - intial parton x
- Non-emission probability lower for
 - lower p_T for emitted gluon
 - ▶ more gluons can be emitted for given energy
 - lower momentum initial parton has larger emission phase space

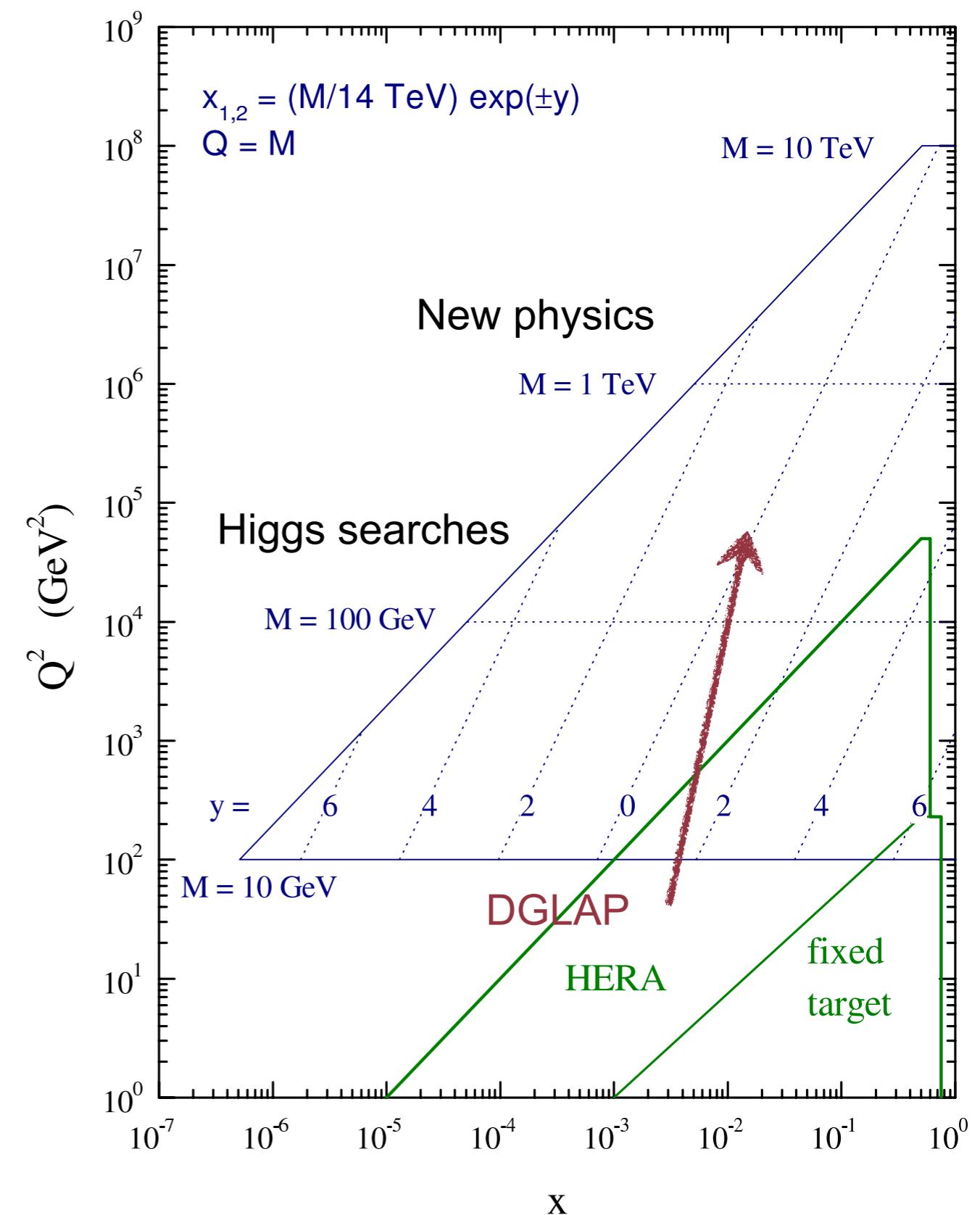
10% probability of emitting
a gluon with p_T of 20 GeV



80% probability of emitting
a gluon with p_T of 10 GeV

LHC PARTON KINEMATICS

- For $y = 0$ need $x_1 \sim x_2$:
 - partons have similar x
 - small longitudinal boost
 - parton center of mass almost at rest
- New heavy particles need relatively large values of x
- Producing particles at large rapidity ($y \sim 2$ or more) implies very different x for incoming partons
- Heavy vector bosons Z' and W' excluded for < 2 TeV
- Higgs searches: 100-200 GeV



K-FACTOR

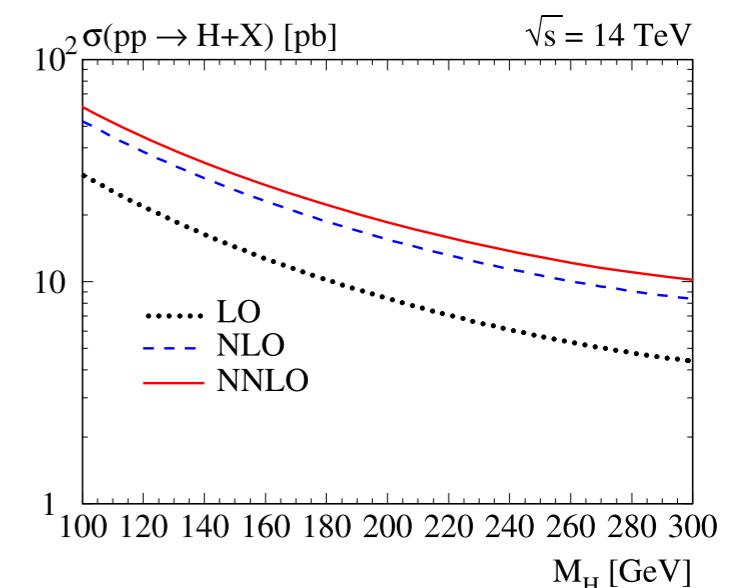
- Express strength of Next-to-Leading-Order corrections compared to Leading Order (LO)

$$\mathcal{K} = \frac{\sigma_{NLO}(PDF\ NLO)}{\sigma_{LO}(PDF\ LO)}$$

$$\mathcal{K}' = \frac{\sigma_{NLO}(PDF\ LO)}{\sigma_{LO}(PDF\ LO)}$$

- typically use PDF at same order as the cross section

Process	Typical scales		Tevatron K-factor			LHC K-factor		
	μ_0	μ_1	$\mathcal{K}(\mu_0)$	$\mathcal{K}(\mu_1)$	$\mathcal{K}'(\mu_0)$	$\mathcal{K}(\mu_0)$	$\mathcal{K}(\mu_1)$	$\mathcal{K}'(\mu_0)$
W	m_W	$2m_W$	1.33	1.31	1.21	1.15	1.05	1.15
$W + 1$ jet	m_W	$\langle p_T^{\text{jet}} \rangle$	1.42	1.20	1.43	1.21	1.32	1.42
$W + 2$ jets	m_W	$\langle p_T^{\text{jet}} \rangle$	1.16	0.91	1.29	0.89	0.88	1.10
$t\bar{t}$	m_t	$2m_t$	1.08	1.31	1.24	1.40	1.59	1.48
$b\bar{b}$	m_b	$2m_b$	1.20	1.21	2.10	0.98	0.84	2.51
Higgs via WBF	m_H	$\langle p_T^{\text{jet}} \rangle$	1.07	0.97	1.07	1.23	1.34	1.09



- Caveat: commonly used as just one number but can strongly depend on phase space
 - kinematic cuts can change significantly the K factor
 - can be affected by large uncertainties for specific hard processes and/or selection requirements of individual analyzes
- Usually used in experiments to re-weight simulated events
 - Common source of systematic uncertainty in cross section measurement

PARTON LUMINOSITY

COMPARING DATA AT DIFFERENT
CENTER OF MASS ENERGY

CROSS SECTION FOR FIXED PARTON CMS ENERGY

$$\sigma_{AB} = \int dx_a dx_b f_{a/A}(x_a, Q^2) f_{b/B}(x_b, Q^2) \hat{\sigma}_{ab \rightarrow X}$$

- Calculation sums over all values of x for each parton but they are not independent if we look at processes with given
 - s is fixed for given operating point: 8 TeV @ LHC, 1.96 TeV @ Tevatron

$$\hat{s} = x_1 x_2 s \quad \tau = x_1 x_2 = \frac{\hat{s}}{s}$$

- if we fix value of \hat{s} then only one of the two x_i can vary $\delta(x_1 x_2 s - \hat{s})$

$$\sigma_{AB} = \int dx_a dx_b f_{a/A}(x_a, Q^2) f_{b/B}(x_b, Q^2) \hat{\sigma}_{ab \rightarrow X}$$

$$dx \frac{d\tau}{x} f_{a/A}(x, Q^2) f_{b/B}(\tau/x, Q^2) \quad \tau = \frac{\hat{s}}{s} \rightarrow 1$$

PARTON LUMINOSITY

$$\frac{\tau}{\hat{s}} \frac{d\mathcal{L}_{ij}}{d\tau} \equiv \frac{\tau/\hat{s}}{1 + \delta_{ij}} \int_{\tau}^1 dx [f_i^{(a)}(x) f_j^{(b)}(\tau/x) + f_j^{(a)}(x) f_i^{(b)}(\tau/x)]/x$$

$$\sigma(s) = \sum_{\{ij\}} \int_{\tau_0}^1 \frac{d\tau}{\tau} \cdot \frac{\tau}{\hat{s}} \frac{d\mathcal{L}_{ij}}{d\tau} \cdot [\hat{s} \hat{\sigma}_{ij \rightarrow \alpha}(\hat{s})]$$

Can be roughly estimated
by coupling constants

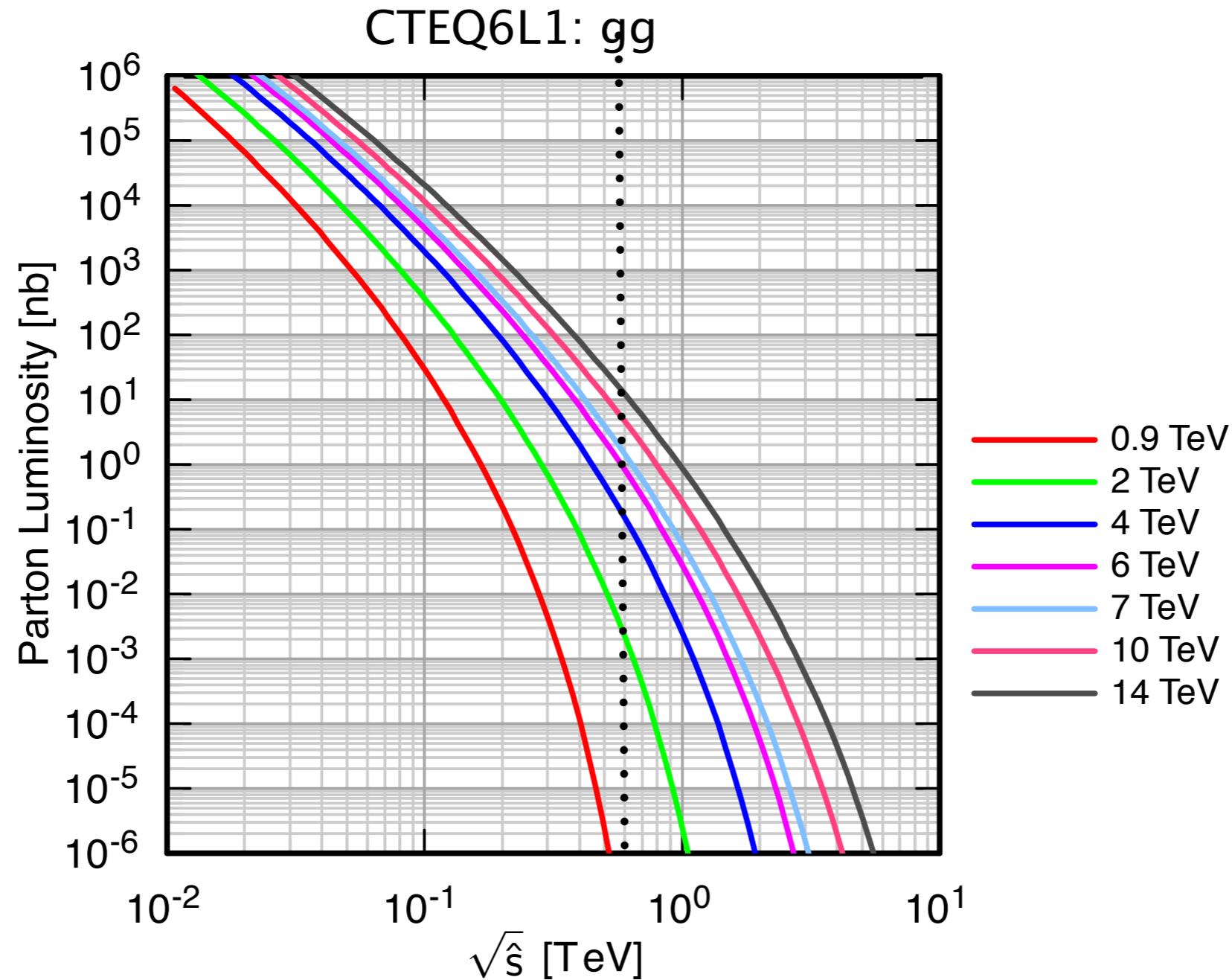
- quantity with dimensions of a cross section commonly referred to a “parton luminosity”
 - very bad and confusing choice but by now largely used in literature
 - In practice a weight factor in front of parton level hard process cross section
 - Determines which hard process is dominating in total cross section for given

$$\tau = x_1 x_2 = \frac{\hat{s}}{s}$$

WHY DO WE CARE ABOUT PARTON LUMINOSITY?

- Hard process cross section calculation independent from particle accelerator or center of mass
 - except for kinematic phase space factors and requirements
- Final states can be in common for Tevatron and LHC although different types of hadron collisions and different parton level diagrams
- Parton luminosity allows to compare cross sections at different energies and between proton-proton vs proton-antiproton
- For a signal process if sources of background are known we can use parton luminosity to estimate S/B at different center-of-mass energies
 - Currently being used to estimate LHC performance and comparison with Tevatron if running at 13 TeV in 2015

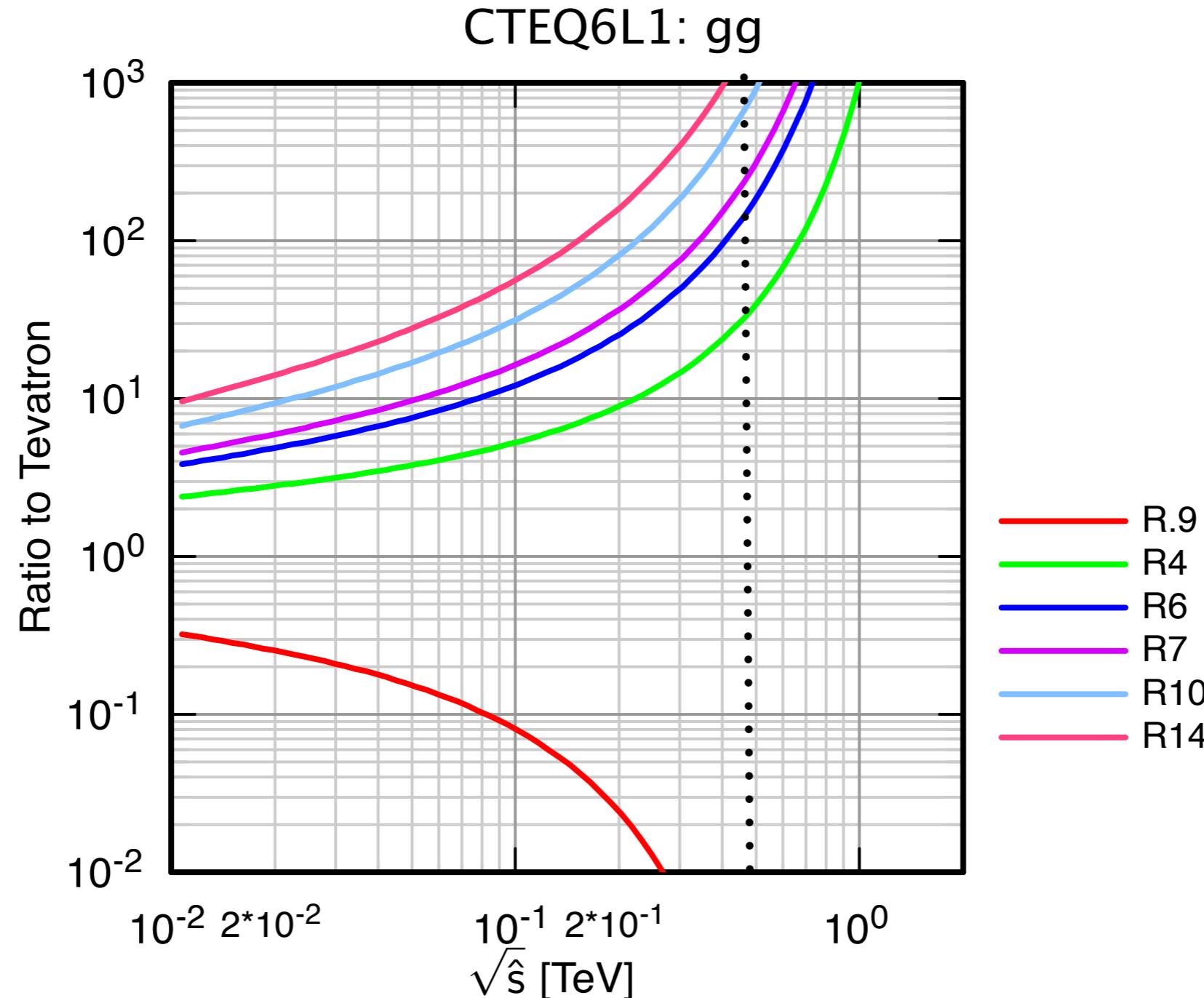
GLUON-GLUON FUSION



- Loss of an order of magnitude running at 7 TeV instead of 14 TeV!
- Significant for new physics searches
- reduction in cross section implies longer data taking period to accumulate same number of events needed for discovery or exclusion

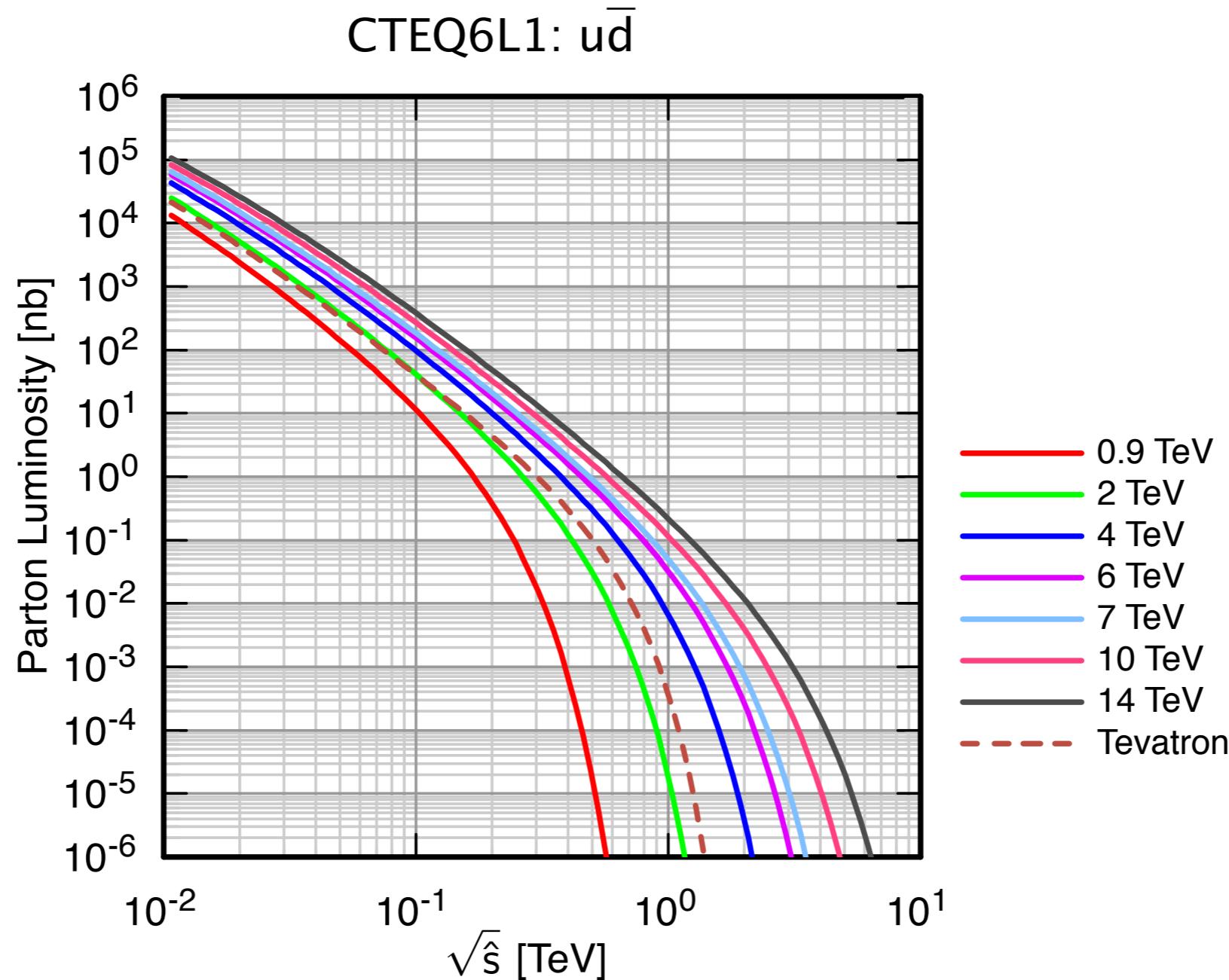
$$N = \mathcal{L}_{inst} \times \sigma \times \Delta t = \mathcal{L}_{int} \times \sigma$$

GLUON-GLUON: LHC vs. TEVATRON



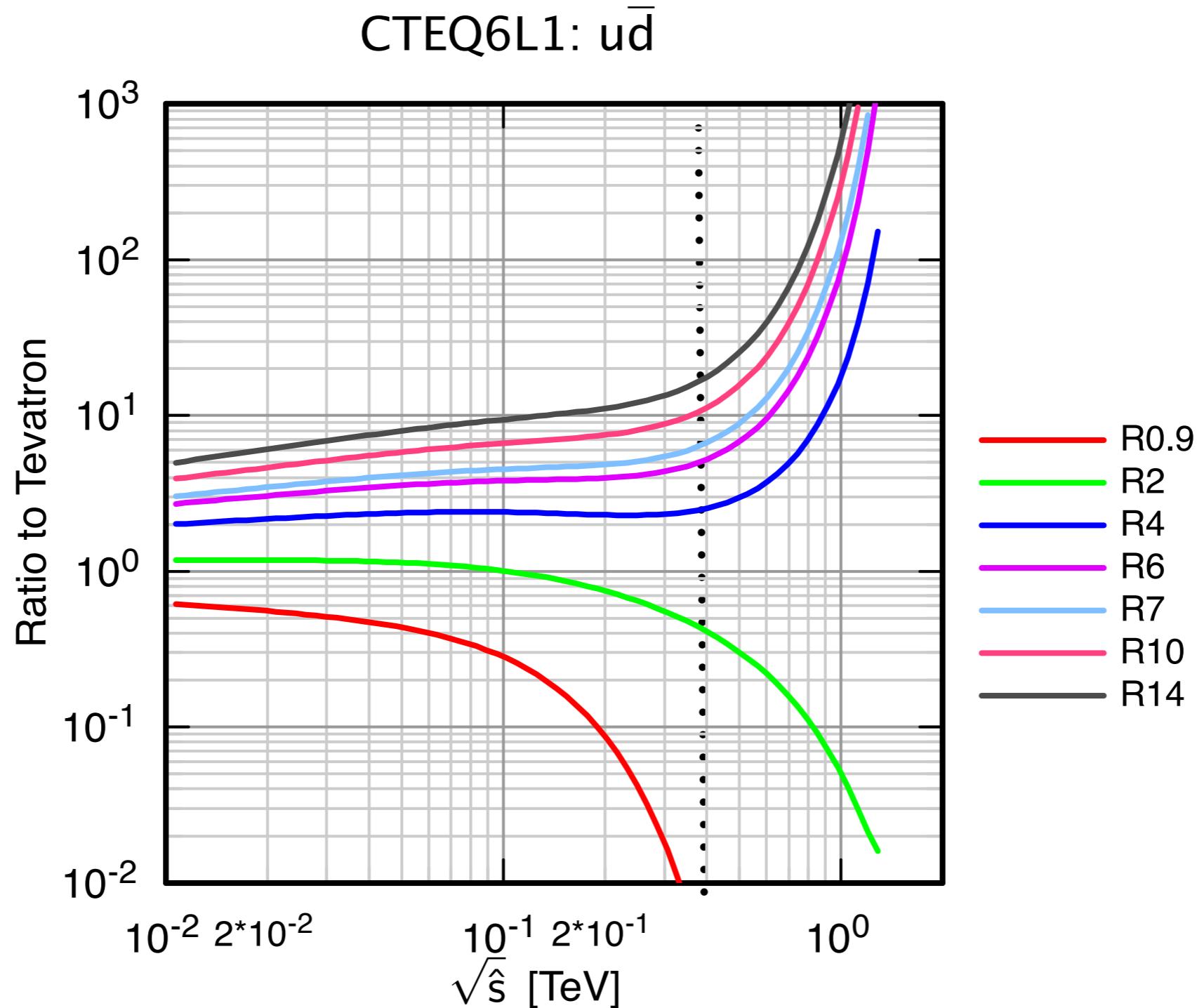
- x100 gain in gluon-gluon fusion processes at 7 TeV compared to Tevatron for $\sqrt{\hat{s}} \sim 0.5 \text{ TeV}$
 - Competitive results from LHC with much less data
 - gg processes play critical role in Higgs discovery at LHC!
- $$\mathcal{L}_{int}^{LHC} \times \sigma_{LHC} = \mathcal{L}_{int}^{tevat.} \times \sigma_{tevat.}$$

QUARK-ANTI-QUARK PROCESS



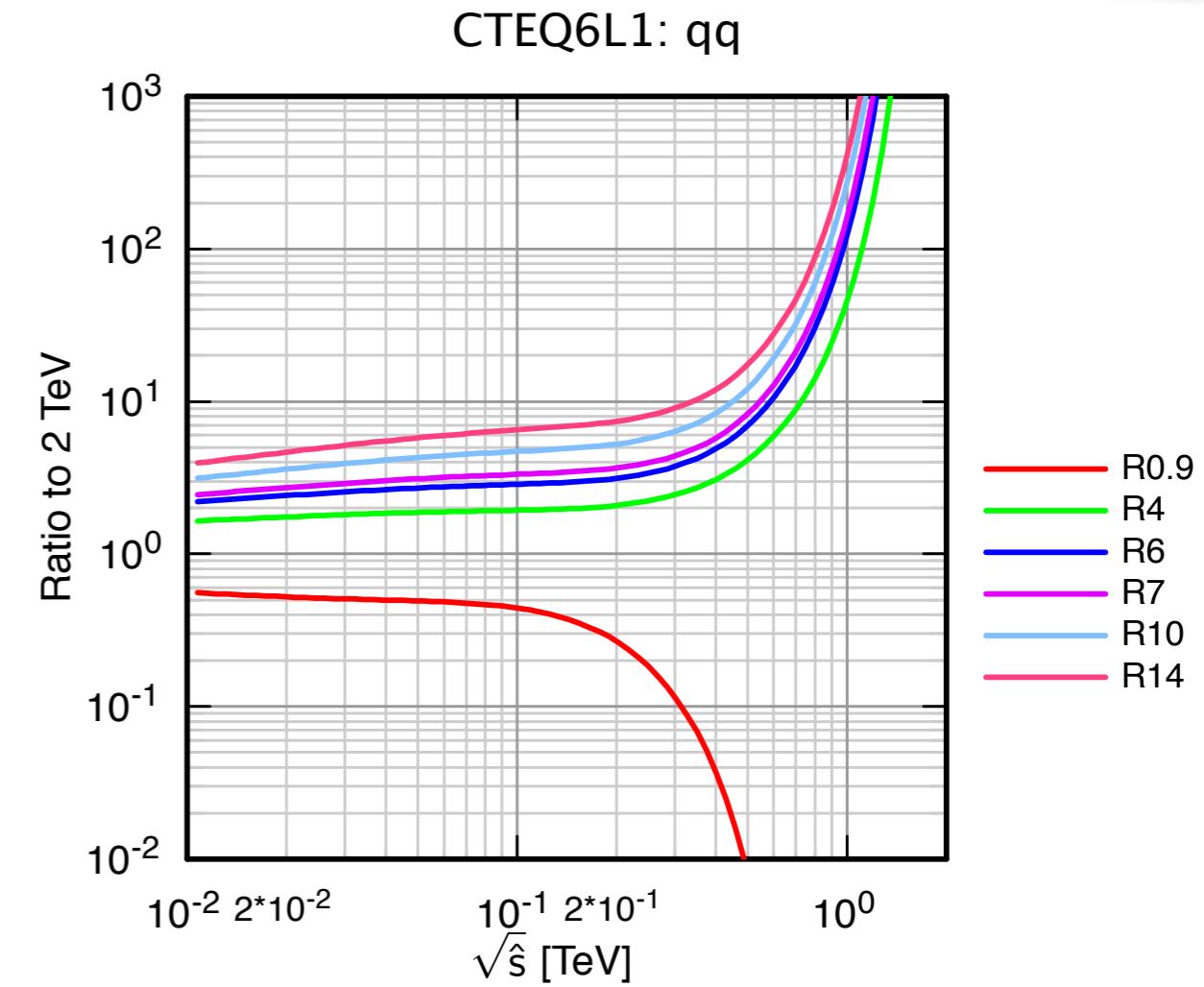
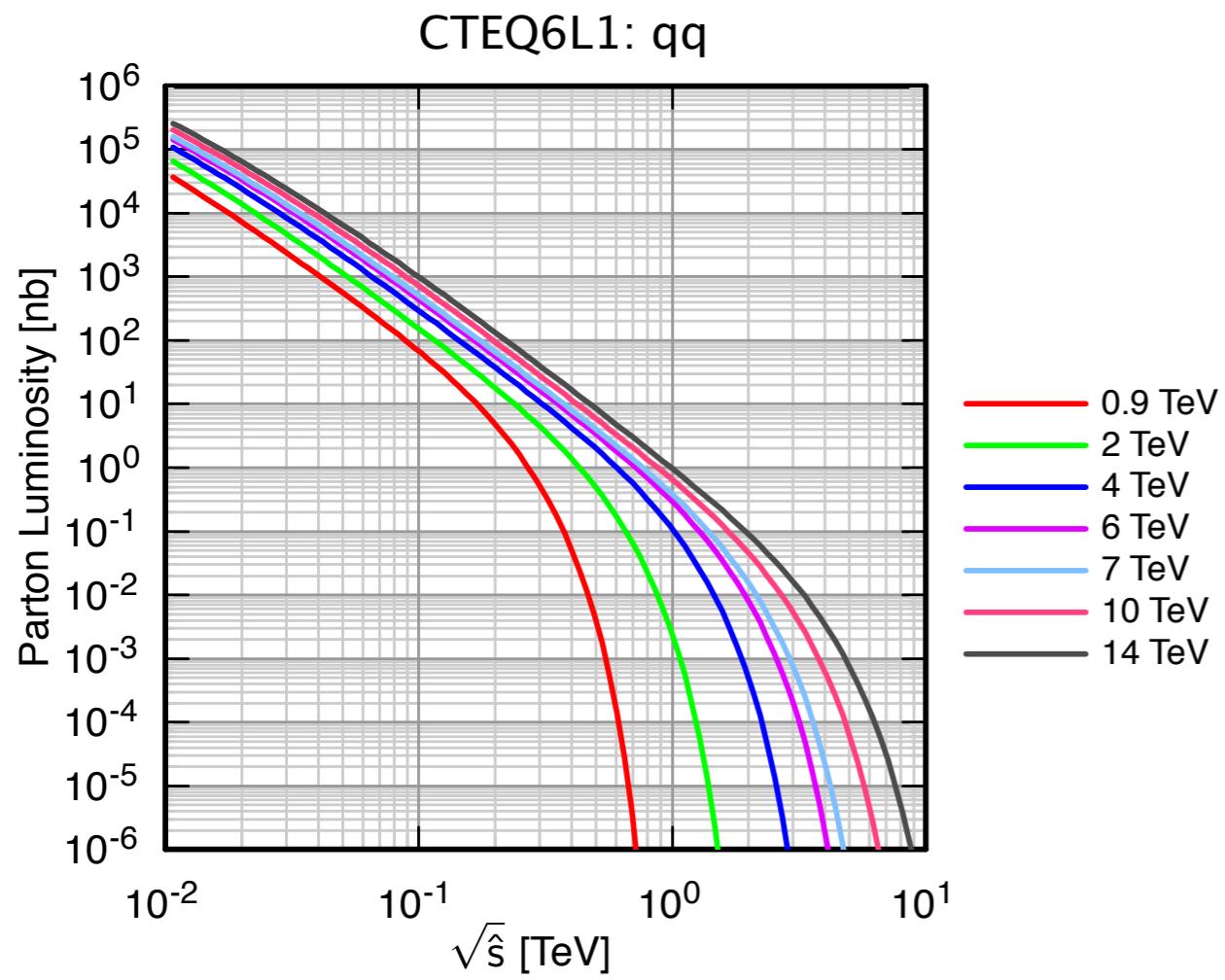
- Major difference between Tevatron and LHC
 - only sea anti-quarks at LHC
- Smaller gain for higher center of mass energy at LHC

QUARK-ANTIQUARK: LHC vs. Tevatron



- Moderate gain of LHC on Tevatron but much less compared to gluon-gluon
 - Competition with Tevatron more challenging and open in 2011 for final states dominated by this hard process

QUARK-QUARK PROCESS



- Moderate but not huge gain at LHC even at 14 TeV
- gluon-gluon fusion is critical for higgs and new physics discovery at LHC

REFERENCES

- Hard Interactions of Quarks and Gluons: a Primer for LHC Physics
 - <http://arxiv.org/abs/hep-ph/0611148>
- Lectures on LHC Physics
 - <http://arxiv.org/abs/0910.4182v2>
- Charged-particle multiplicities in pp interactions at $\text{sqrt}(s) = 900 \text{ GeV}$ measured with the ATLAS detector at the LHC
 - <http://arxiv.org/abs/1003.3124>
- Measurement of the Underlying Event Activity at the LHC with $\text{sqrt}(s)$
 - <http://cdsweb.cern.ch/record/1279345>
- Review of event generators for LHC
 - <http://arxiv.org/abs/1101.2599>
- Hard Interactions of Quarks and Gluons:A Primer for LHC Physics, J.M. Campbell, J.W. Huston, W.J. Stirling
 - Rept.Prog.Phys.70:89,2007; e-Print: [hep-ph/0611148](http://arxiv.org/abs/hep-ph/0611148)
- LHC Physics Potential vs. Energy, Chris Quigg
 - e-Print: [arXiv:0908.3660 \[hep-ph\]](http://arXiv:0908.3660)