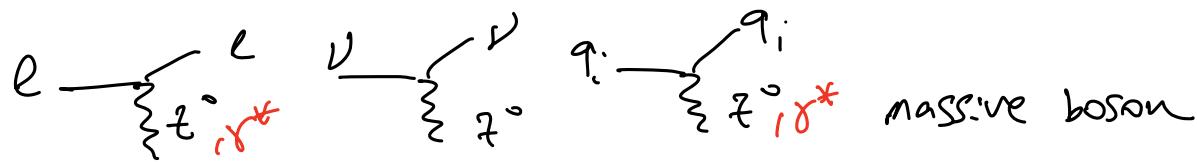


Neutral Weak Current



Indirect evidence

$$\nu \xrightarrow{g_Z} Z^0 \xrightarrow{g_Z} e^-$$

$$g_Z^2 = \frac{1}{q_e m_Z^2}$$

Direct evidence: produce Z^0 on shell.

$$q_i, \bar{q}_i \rightarrow Z^0$$

$$g_Z = m_Z$$

1961: Glashow proposed unification of weak and EM interaction.
mixtare of τ and Z^0 fields.

1967: Weinberg-Salam: unification as spontaneous symmetry
 $SU(2)_{\text{weak}} \times U(1)_{\text{EM}}$ breaking of gauge fields

1971: 't Hooft proved that gauge theory is renormalizable

If theory correct: find experimental evidence for W, Z

1979: Nobel Glashow-Weinberg-Salam (GWS)

Find direct experimental evidence

$$\nu_e \xrightarrow{Z^0*} \nu_e$$

No electric charge $q=0 \Rightarrow$ No EM
No color \Rightarrow No QCD

$$\nu_e + X \rightarrow \nu_e + X \quad X = e^-, p, n$$

Challenges

- 1) beam of neutrinos
- 2) high intensity
- 3) focused beam

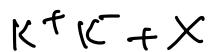
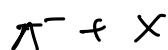
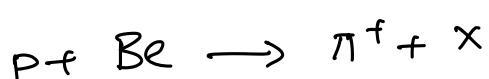
4) Cross section very small.

$$\bar{\nu} + p \rightarrow e^+ + n \quad (\text{Reines-Cowen experiment})$$

$$\sigma \approx 10^{-55} \text{ cm}^2$$

$$\frac{dN_r}{dt} = \sigma \frac{dN_p}{dt} \underbrace{n_{\text{target}}}_{\substack{\Delta X \\ \hookrightarrow \text{thickness}}} \underbrace{\Delta X}_{\text{target density}}$$

Experiment @ CERN 1973



$X: \geq 1 \text{ charged} \geq 0 \text{ neutral particles}$

$$\pi^\pm \rightarrow \mu^\pm \nu_\mu / \bar{\nu}_\mu \quad \approx 100\% \quad \left. \begin{array}{c} \text{Signal} \\ \text{ } \end{array} \right\}$$

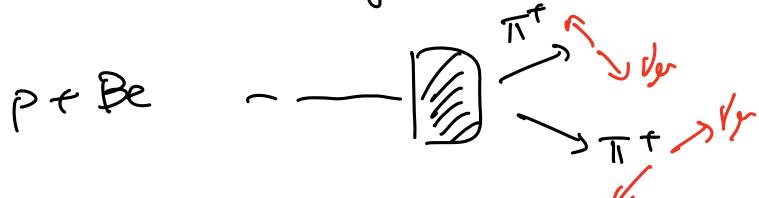
$$K^\pm \rightarrow \mu^\pm \nu_\mu / \bar{\nu}_\mu \quad \approx 60\% \quad \left. \begin{array}{c} \text{ } \\ \text{ } \end{array} \right\}$$

$$K^+ \rightarrow \pi^0 \mu^+ \nu_\mu$$

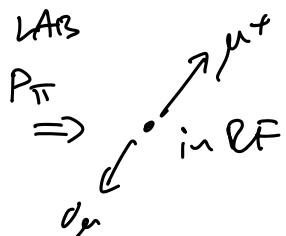
$\pi^0 e^+ \nu_e$

K^+ DECAY MODES	Fraction (Γ_i/Γ)	Scale factor/ Confidence level(MeV/c)
Leptonic and semileptonic modes		
$e^+ \nu_e$	(1.582 ± 0.007) $\times 10^{-5}$	247
$\mu^+ \nu_\mu$	(63.56 ± 0.11) %	S=1.2 236
$\pi^0 e^+ \nu_e$	(5.07 ± 0.04) %	S=2.1 228
Called K_{e3}^+ .		
$\pi^0 \mu^+ \nu_\mu$	(3.352 ± 0.033) %	S=1.9 215
Called $K_{\mu 3}^+$.		
$\pi^0 \pi^0 e^+ \nu_e$	(2.55 ± 0.04) $\times 10^{-5}$	S=1.1 206
$\pi^+ \pi^- e^+ \nu_e$	(4.247 ± 0.024) $\times 10^{-5}$	203
$\pi^+ \pi^- \mu^+ \nu_\mu$	(1.4 ± 0.9) $\times 10^{-5}$	151
$\pi^0 \pi^0 \pi^0 e^+ \nu_e$	< 3.5×10^{-6}	CL=90% 135
Hadronic modes		
$\pi^+ \pi^0$	(20.67 ± 0.08) %	S=1.2 205
$\pi^+ \pi^0 \pi^0$	(1.760 ± 0.023) %	S=1.1 133
$\pi^+ \pi^+ \pi^-$	(5.583 ± 0.024) %	125

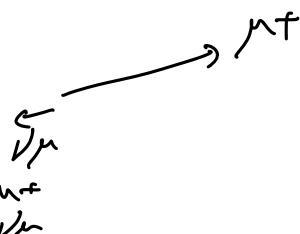
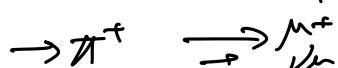
Select $\pi^\pm \rightarrow \mu^\pm \nu_\mu / \bar{\nu}_\mu$ pure at 99%

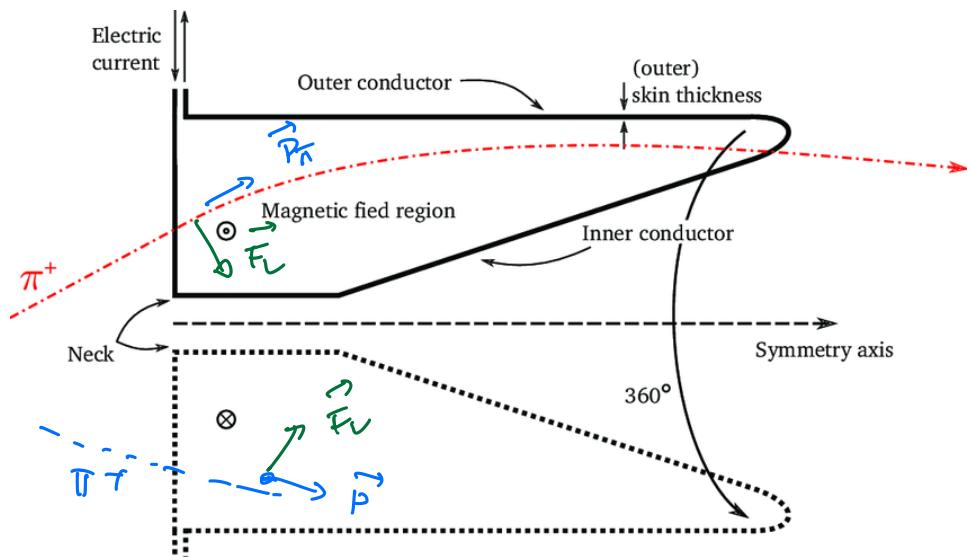


In π^+ rest frame $\mu^+ \leftarrow \bar{u}^+ \rightarrow \nu_\mu$



\Rightarrow in the LAB





Magnetic horn

Simon van der Meer

$$\vec{F}_L = q \vec{v} \times \vec{B}$$



Focus π^+ beam

\Rightarrow Focus $\nu_e/\bar{\nu}_e$

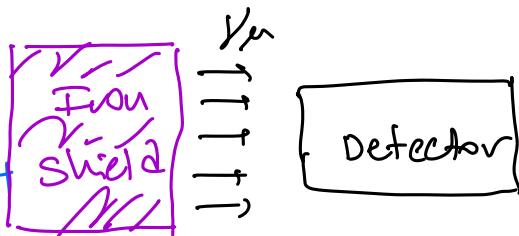
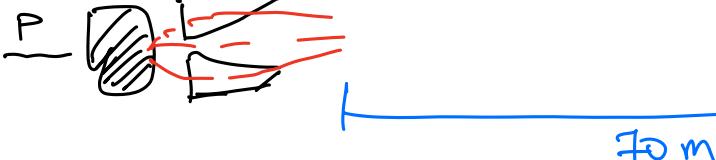
$$\mu^+ \leftarrow \bar{a}^r \rightarrow \nu_\mu$$

$$Q = m_\pi - m_\mu - m_\nu \approx 89 \text{ MeV}$$

$$\text{in rest frame } E_\pi = m_\pi = E_\mu + E_\nu = \sqrt{m_\mu c^2 + p^2} + p$$

$$\Rightarrow p = \frac{1}{2m_\pi} (m_\pi^2 - m_\mu^2) \approx 25 \text{ MeV.}$$

Be magnetic horn



Iron Shield

$\pi, K, \text{hadrons}$: nuclear interaction, ionization

e^\pm : ionization, EM shower

μ^\pm : ionization (not stopped)



Gargamelle

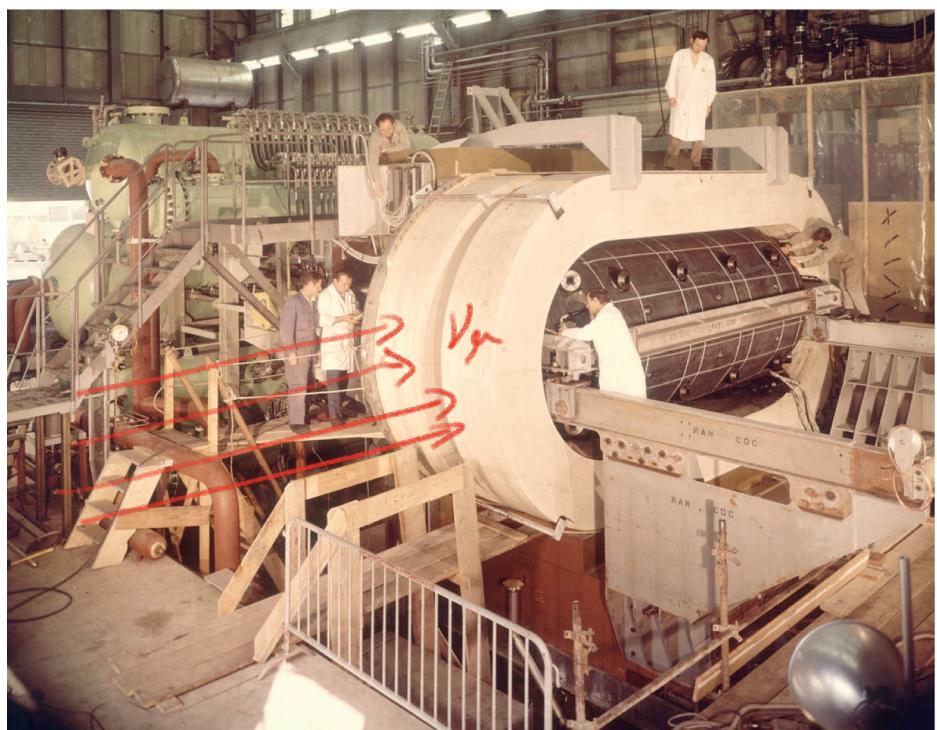
Steel cylinder

filled with Freon

CF_3Br (liquid)

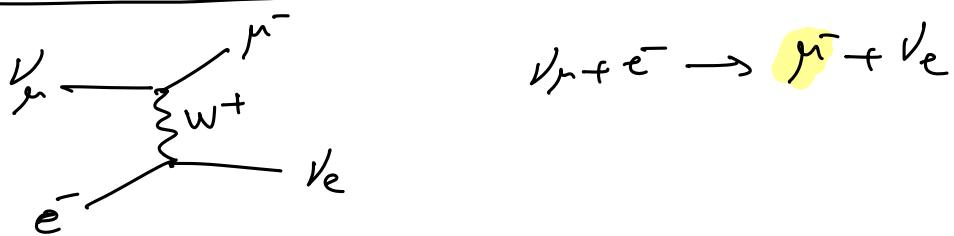
$\mathcal{E}\mathcal{T}$ magnetic field

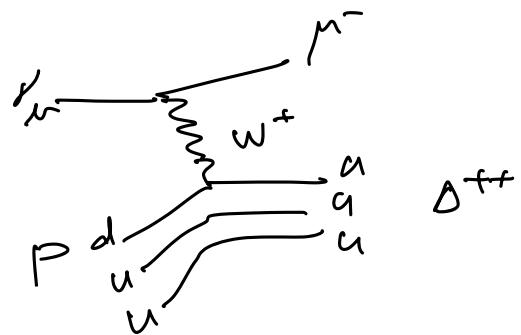
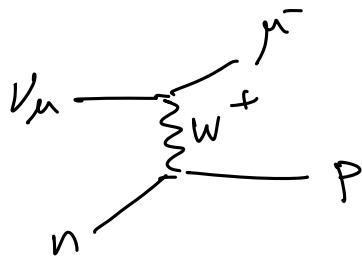
Bubble Chamber



$$\nu + \left\{ \begin{matrix} e^- \\ p \\ n \end{matrix} \right\} \rightarrow \nu + X$$

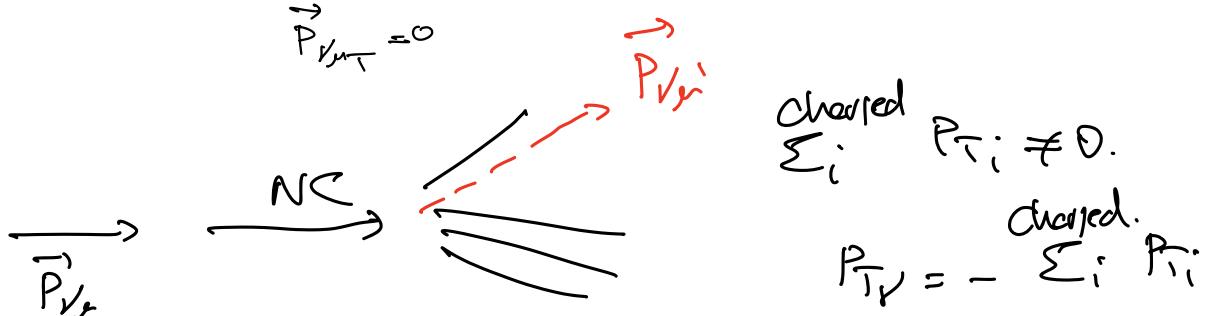
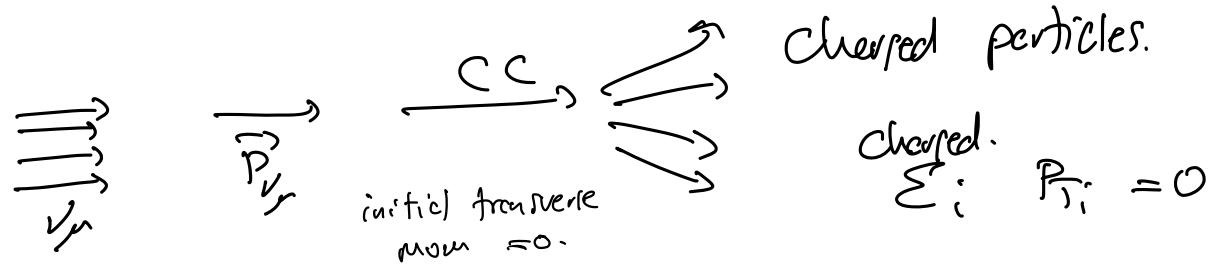
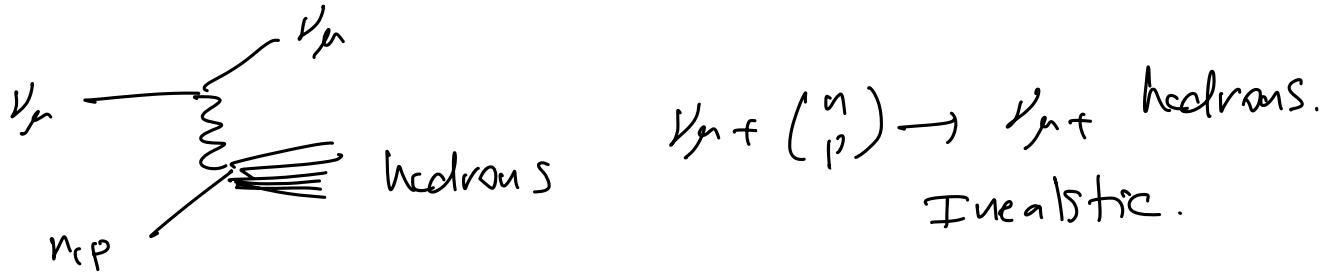
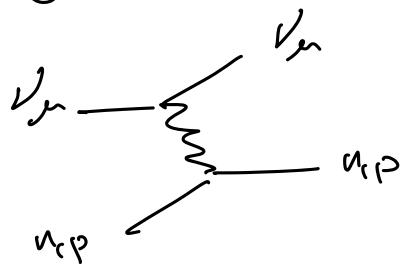
Charged current process (CC)

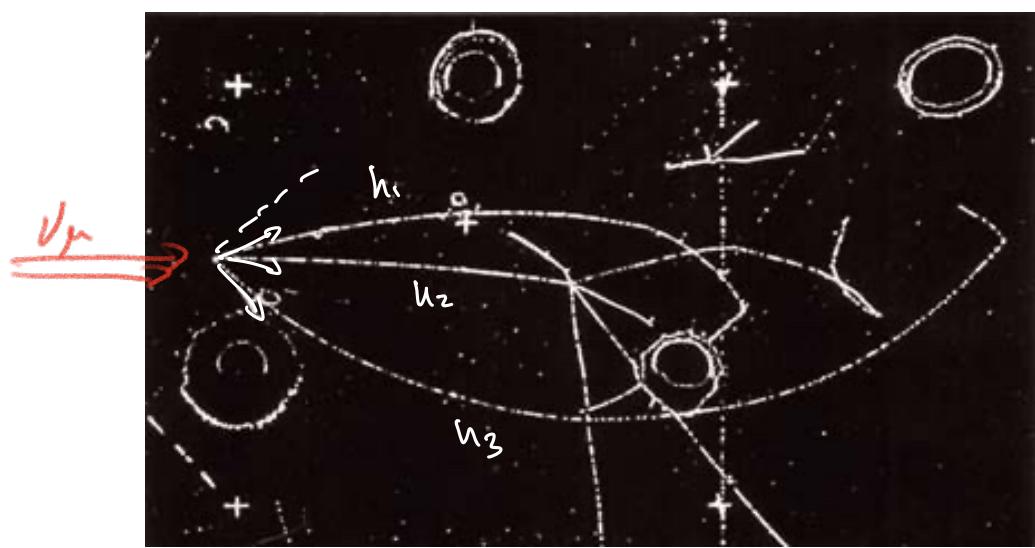
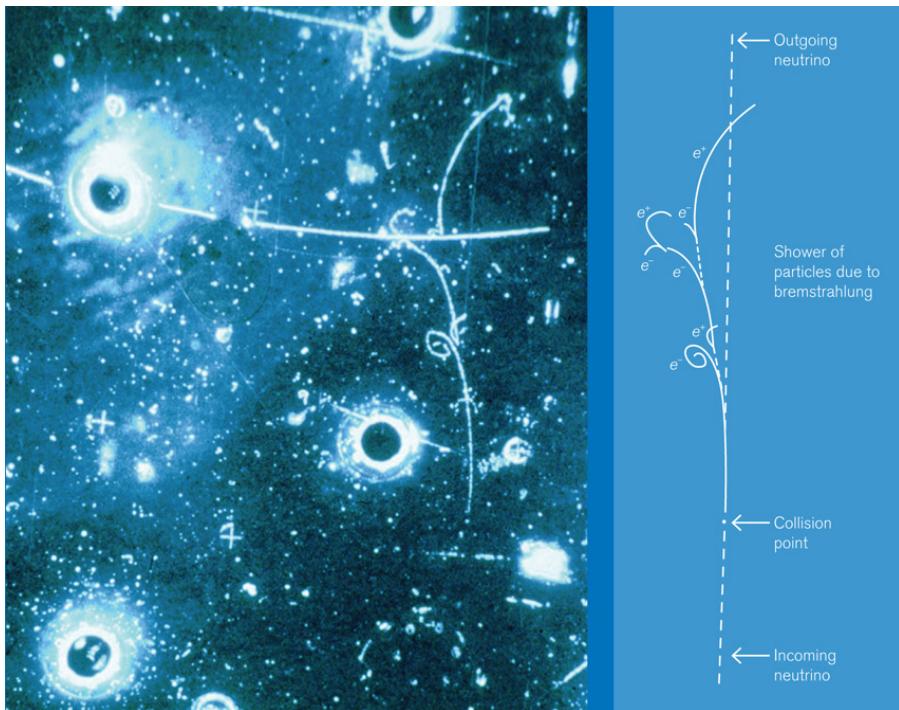




CC events have μ^- in final state.

if τ^0 exists (NC) \Rightarrow additional processes





$\pi^+ \rightarrow \nu_\mu$ beam : 102 NC, 428 CC, 15n

$\pi^- \rightarrow \bar{\nu}_\mu$ beam : 64 NC, 148 CC, 12n

Expected
Background
from neutrons

Conclusions

1) $\frac{NC}{CC} \neq 0 \Rightarrow NC \text{ exists}$

2) $\frac{NC}{CC} \approx \frac{1}{3}$ $\xrightarrow{g_Z \neq g_W}$

$g_Z \neq g_W$



3) $1/3 \gg$ 2nd order effects with no Z^0



$$\mu \frac{g_W^2}{m_W^2} \frac{g_W^2}{m_W^2} \sim G_F^2$$

$$\rightarrow |\mu|^2 \sim G_F^4 \text{ much suppressed}$$

$$\frac{N_C}{CC} \approx 1/3 \gg \text{2nd order } W\text{-only diagram } (G_F^4)$$

Glashow - Weinberg - Salam Theory of Electroweak int.

f_i 	f 	$f_i = \ell^\pm, \nu_e, \bar{\nu}_e, q_i$ <i>i</i> : flavors of quarks. $\frac{i}{2\sqrt{2}} g_W \gamma^\mu (1-\gamma^5)$ V-A theory.
		$\frac{i}{2\sqrt{2}} g_Z \gamma^\mu (c_V - c_A \gamma^5)$ vector coupling axial coupling.

Theory predicts c_V, c_A for all fermions.

$SU(2)_{\text{weak}} \times U(1)_{\text{EM}}$.

$$w^1, w^2, w^3 \quad \downarrow \quad B \quad \text{Scal. bosons.}$$

$$w^1, w^2 \rightarrow (w_1 \pm i w_2) = w^\pm \text{ physical bosons.}$$

$$\begin{pmatrix} Z^0 \\ A \end{pmatrix} = \begin{pmatrix} \cos \theta_W & -\sin \theta_W \\ \sin \theta_W & \cos \theta_W \end{pmatrix} \begin{pmatrix} w_3 \\ B \end{pmatrix} \quad \theta_W: \text{weak mixing angle}$$

\hookrightarrow physical neutral vector bosons.

\Rightarrow experimentally measure θ_W

f	c_V	c_A
ν_e, ν_μ, ν_τ	$\frac{1}{2}$	$\frac{1}{2}$
e^-, μ^-, τ^-	$-\frac{1}{2} + 2 \sin^2 \theta_W$	$-\frac{1}{2}$
u, c, t	$\frac{1}{2} - \frac{4}{3} \sin^2 \theta_W$	$\frac{1}{2}$
d, s, b	$-\frac{1}{2} + \frac{2}{3} \sin^2 \theta_W$	$-\frac{1}{2}$

$$\alpha_{EM} = \frac{e^2}{4\pi\epsilon_0} \Rightarrow g_e = \frac{e}{\sqrt{4\pi\epsilon_0}}$$

$$g_W = \frac{g_e}{\sin \theta_W}$$

$$g_T = \frac{g_e}{\sin \theta_W \cos \theta_W}$$

$$M_W = M_Z \times \cos \theta_W$$

$$\Rightarrow \theta_W \approx 29^\circ \quad \sin^2 \theta_W \approx 0.23 \quad \sin \theta_W \approx 0.48$$