

Cicli:

do/while : input di variabile entro limiti  $[a, b]$

for : # iterazioni: noto

while : prime verif. cond. poi: esegue

## Trovare zeri di una funzione

$$f(x) = 0 \Rightarrow x_1, \dots, x_n : f(x_i) = 0$$

$$\underbrace{3x - 4x^2 + 7}_{f(x)} = 0$$

$$\sin(x) = 0$$

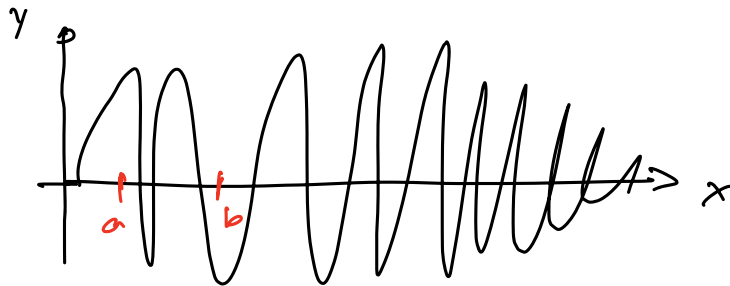
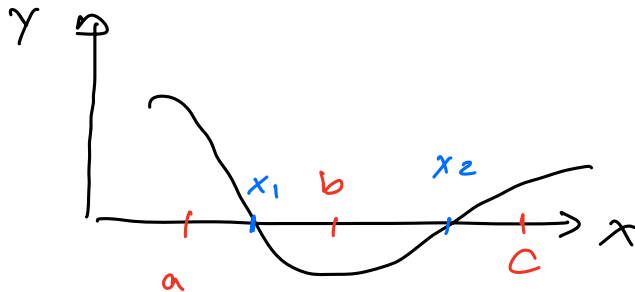
$$x^2 \sin(x) = 0$$

$$x^2 + \tanh^2 x = 0$$

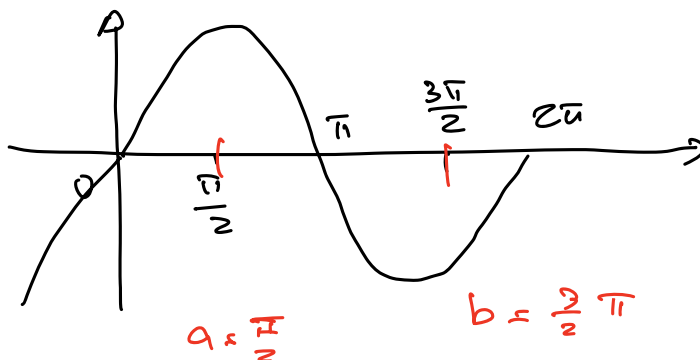
Funzioni: non troppo oscillanti  $\Rightarrow$  Metodo di bisezione

$$x_1 \in [a, b]$$

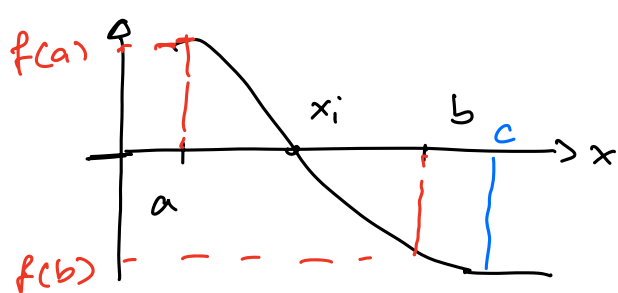
$$x_2 \in [b, c]$$



non funzione  
bene



$\sin(x)$



se  $x_i \in [a, b]$

$$f(a) > 0$$

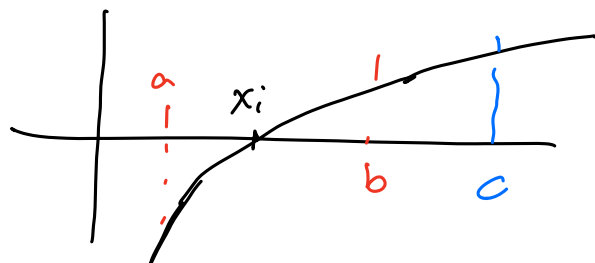
$$f(x_i) = 0 \quad \text{Zero della funz.}$$

$$f(b) < 0$$

$$f(b) \times f(c) > 0$$

$$x_i \notin [b, c]$$

$$f(a) \times f(b) < 0$$



$$f(a) < 0$$

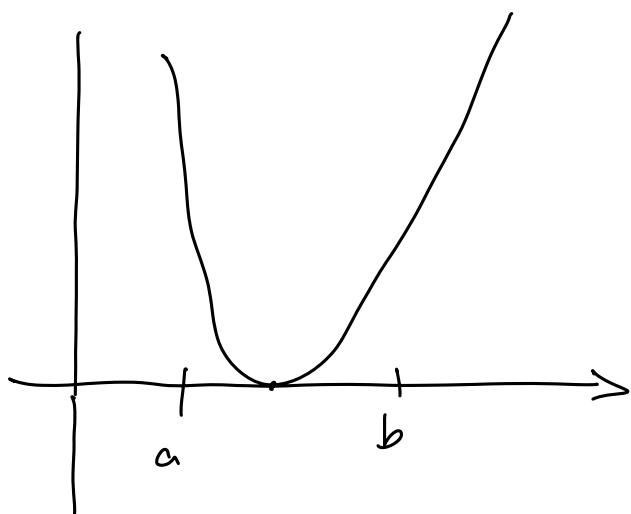
$$f(x_i) = 0$$

$$f(b) > 0$$

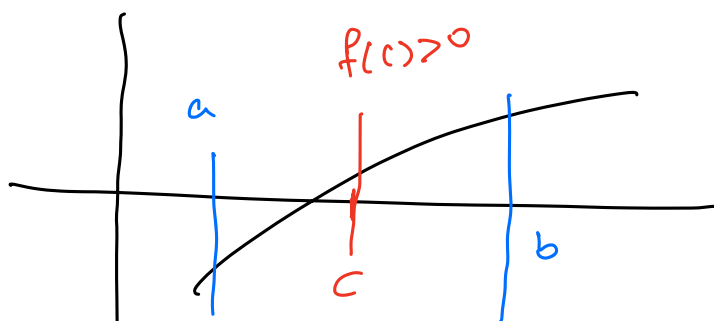
$$x_i \notin [b, c]$$

$$f(b) \times f(c) > 0$$

$$f(a) \times f(b) < 0$$



Richiede cura  
perché  $f(x)$  non  
attraversa a sé x



$$f(a) < 0$$

$$f(b) > 0$$

$$f(c) \times f(b) < 0.$$

$$\Rightarrow x_i \in [a, b]$$

$$c = \frac{a+b}{2}$$

I<sup>a</sup> iterazione.

$$f(a) \times f(c) < 0$$

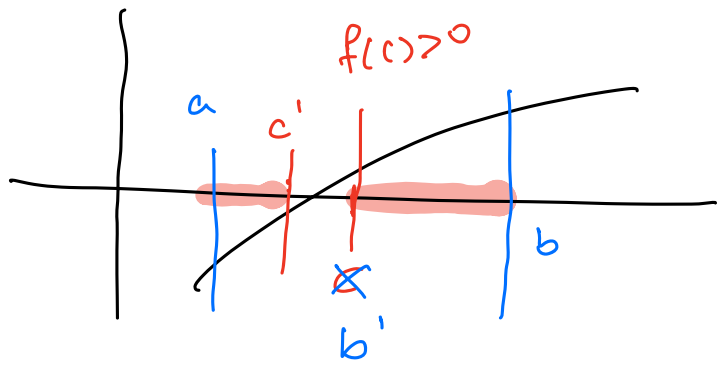
$$f(b) \times f(c) > 0 \Rightarrow \text{scarto } [b, c]$$

II<sup>a</sup> iterazione

$$a = a$$

$$b' = c$$

$$c' = \frac{a+b'}{2}$$



$$f(a) \times f(c') > 0$$

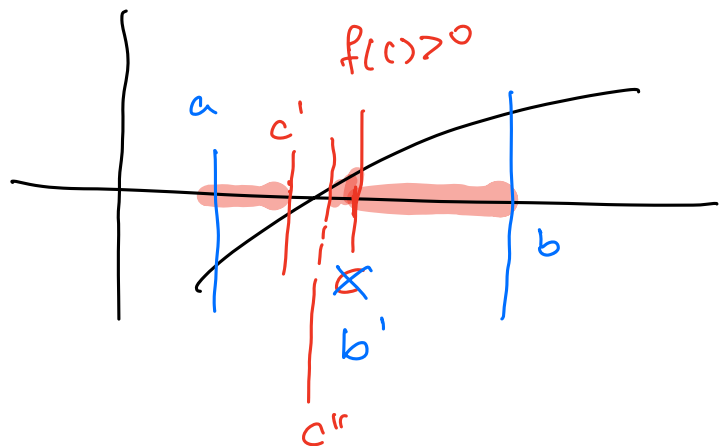
$$f(c') \times f(b) < 0 \Rightarrow x_i \in [c', b']$$

III<sup>a</sup> iterazione

$$a'' = c'$$

$$b'' = b'$$

$$c'' = \frac{a''+b''}{2}$$



$$f(a'') \times f(c'') < 0$$

$$f(c'') \times f(b'') > 0$$

Ciclo si ferma quando raggiungo precisione prestabilita

si ferma if ( fabs(a-b) ) < precisione

$$\text{fabs}(x-y) \equiv |x-y|$$

$$|a-b| < \varepsilon$$

```

bisezione.c
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#include <math.h>
#include <stdlib.h>
#include <stdio.h>

#define EPS 1.e-5 → 10-5

int main() {
    double a = 0., b = 0.7*M_PI, c;
    double delta = fabs(a-b);

    double p;
    int iter = 0;
    double eps = EPS;

    printf("inserisci la precisione:");
    scanf("%lf", &eps);

    printf("calcolo zeri di cos(x)\n");

    while(delta > eps) {
        iter++;

        c = 0.5*(a+b);
        p = cos(a)*cos(c);

        if( p > 0.) {
            a = c;
        } else if ( p < 0. ) {
            b = c;
        } else {
            a = b = c;
        }

        printf("iter: %3d x = %.15f gradi\n", iter, c*180./M_PI);
        delta = fabs(a-b);
    }
}

```

$$f(x) = \cos(x)$$

$$a = 0 \quad b = 0.7 \times \pi$$

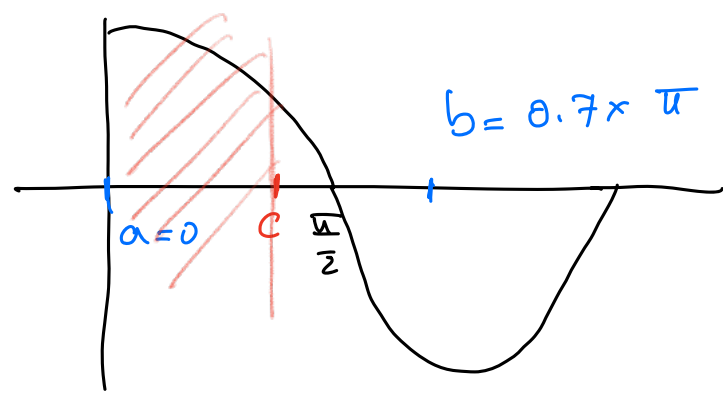
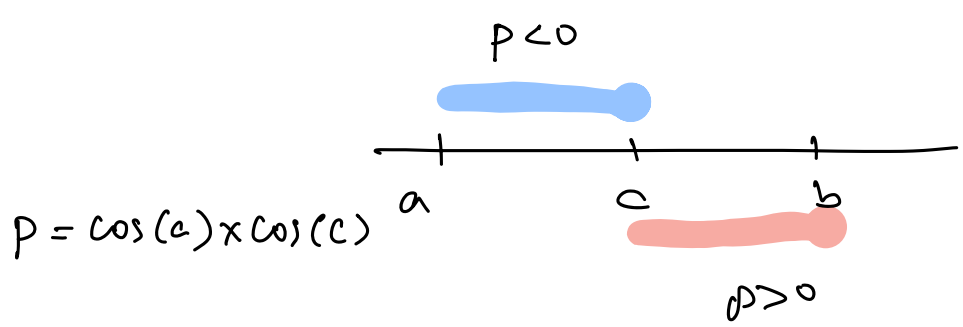
$$\delta = |a - b|$$

~~scanf("%lf", &EPS) ?~~  
~~scanf("%lf", &1.e-5);~~

p: variabile di approssimazione  
 ausiliaria

EPS: costante pre-compilata

eps: variabile double



```

shamacmini:material rahatlou$ gcc -o /tmp/app bisezione.c
shamacmini:material rahatlou$ /tmp/app
inserisci la precisione:0.1
calcolo zeri di cos(x)
iter: 1 x = 63.000000000000000 gradi
iter: 2 x = 94.500000000000000 gradi
iter: 3 x = 78.750000000000000 gradi
iter: 4 x = 86.625000000000014 gradi
iter: 5 x = 90.562500000000014 gradi
shamacmini:material rahatlou$ /tmp/app
inserisci la precisione:0.001
calcolo zeri di cos(x)
iter: 1 x = 63.000000000000000 gradi
iter: 2 x = 94.500000000000000 gradi
iter: 3 x = 78.750000000000000 gradi
iter: 4 x = 86.625000000000014 gradi
iter: 5 x = 90.562500000000014 gradi
iter: 6 x = 88.593750000000000 gradi
iter: 7 x = 89.578125000000000 gradi
iter: 8 x = 90.070312500000000 gradi
iter: 9 x = 89.824218750000000 gradi
iter: 10 x = 89.947265625000000 gradi
iter: 11 x = 90.008789062500000 gradi
iter: 12 x = 89.978027343750000 gradi
shamacmini:material rahatlou$ █

```

90.000

89.978

$\epsilon = 0.001$

90.0

90.6

$\epsilon = 0.1$

## Numeri Primi

N primo ?

int n, m

$n = 3$

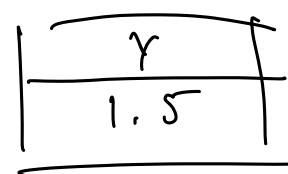
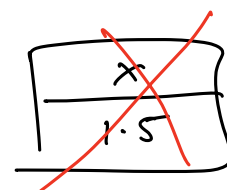
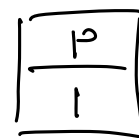
$m = 2$

int p = n/m ;

float x = n/m ;

$x = 1.0000$

float y = (float) n / m  
= 1. \* n / m



$$\text{int } \text{resto} = n \% m;$$

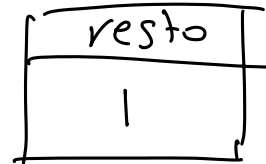
resto di  $n/m$  (int)

$$n = 123$$

$$m = 295$$

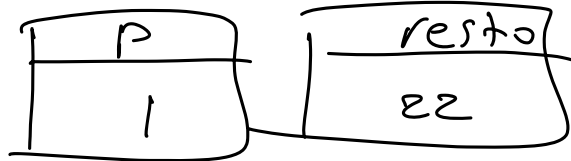
$$p = n/m$$

$$\text{resto} = n \% m$$



$$n = 317$$

$$m = 295$$



$$1 \frac{22}{295}$$

$$n = 17$$

primi ?

$$n/2$$

$$n \% 2 \neq 0$$

$$n \% 3 \neq 0$$

$$n \% 4 \neq 0$$

$$n \% 5 \neq 0$$

$$n/.$$

$$\text{div-min} = 2$$

$$\text{div-max} = \sqrt{n} + 1$$

$$n = 15$$

$$n \% 2 \neq 0$$

$$n \% 3 = 0$$

```

#include <math.h>
#include <stdio.h>
#include <stdlib.h>

#define N 100

int main() {
    int n, j, jMax;
    printf("inserisci un numero intero: ");
    scanf("%d", &n);

    // valori tra cui cercare divisori
    j = 2;
    jMax = (int)sqrt(n)+1;

    printf("verifica fino jMax: %d\n", jMax);

    // aumenta j solo se i non divisibile per j
    for(j = 2; j < jMax; j++) {
        printf("provo con %d\n", j);
        if( n%j == 0) {
            printf("%d multiplo di %d ... non primo :(\n", n, j);
            break; // interrompe il ciclo. non molto elegante
        }
    }
    printf("j dopo ciclo: %d\n", j);
    if(j == jMax) printf("Numero primo %d\n", n);
}

```

$n : j : \text{resto di } \frac{n}{j}$

$\neq 0$

↳

non divisibile per j

$\Rightarrow$  continua  
con  $j++$

```

[shamacmini:material rahatlou$ gcc -o /tmp/app primi1.c
[shamacmini:material rahatlou$ /tmp/app
inserisci un numero intero: 16
verifica fino jMax: 5
provo con 2
16 multiplo di 2 ... non primo :(
j dopo ciclo: 2

```

```

[shamacmini:material rahatlou$ /tmp/app
inserisci un numero intero: 127
verifica fino jMax: 12
provo con 2
provo con 3
provo con 4
provo con 5
provo con 6
provo con 7
provo con 8
provo con 9
provo con 10
provo con 11
j dopo ciclo: 12
Numero primo 127

```

for  $j < jMax = 12$

```
#include <math.h>
#include <stdio.h>
#include <stdlib.h>
```

```
#define N 100
```

```
int main() {
```

```
    int i, j, jMax;
```

```
    printf("Numeri primi tra 1 e %d:\n", N);
```

```
    // ciclo sui numeri da 1 a N
```

```
    for(i=1; i<=N; i++) {
```

```
        // valori tra cui cercare divisori
```

```
        j = 2;
```

```
        jMax = (int)sqrt(i)+1;
```

```
        // aumenta j fino jMax solo se i non divisibile per j
```

```
        while( (j<jMax) && (i%j) ) {
```

```
            j++;
```

```
        }
```

```
        if(j == jMax) printf("%d\n", i);
```

```
    } // ciclo for
```

```
} // main
```

$j < j_{Max}$ .

$resto \frac{i}{j} \neq 0$

$resto(i/j) \neq 0 \Rightarrow TRUE$

```
shamacmini:material rahatlou$ gcc -o /tmp/app primi.c
shamacmini:material rahatlou$ /tmp/app
Numeri primi tra 1 e 100:
```

```
1
2
3
5
7
11
13
17
19
23
29
31
37
41
43
47
53
59
61
67
71
73
79
83
89
97
```

$if ( i/j \neq 0 )$

$if ( i \% j )$

$\neq 0 \equiv TRUE$

$if ( i \% 100 == 0 ) \{$

    printf(" iterazione i.d n ", i);

$\}$



```

if ( ! ( i > 100 ) ) {
    printf ( "iterazione %d\n", i );
}

```

Conversione base

n = 5	div	resto
5 / 2	2	1
2 / 2	1	0
1 / 2	0	1

```

Ciclo {
    - divisione
    - resto
    - stampa resto
}

```

	n / 2	resto
n = 8	4	0
4	2	0
2	1	0
1	0	1

```

Ciclo {
    - divisione
    - resto
    - stampa resto
}

```

printf ( "%d", resto )

0001

Sbagliato.

1000

int a1, a2, a3, a4, a5, a6, a7;

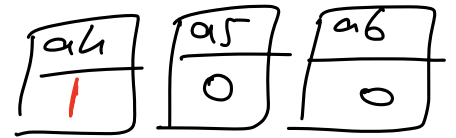
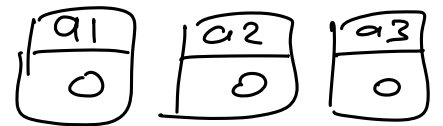
printf("%d", a7);

printf("%d", a6);

⋮

printf("%d", a1);

0001000



n = 8



⇒ array in C

int a[7];

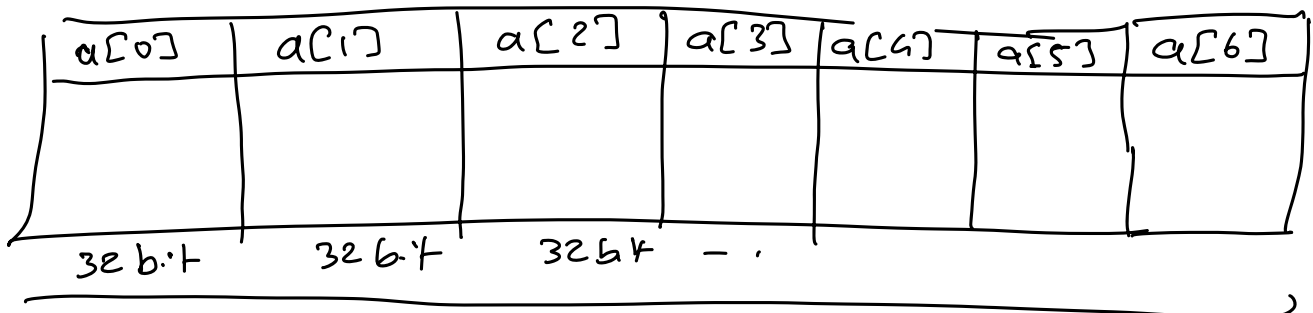
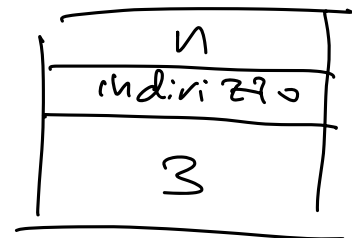
double x[100];

int n

a array di 7 elementi:  
di tipo intero;

x array di 100 elementi:  
di tipo double.

int a[7]



size int: 32 bit

structure dati a[7]  
grande 7 x 32 bit  
= 7 x 4 byte  
= 28 byte

int a[7] : a! nome di array. di tipo intero  
7: lunghezza di array.  
# celle.

a[0], ..., a[6] : 7 celle di array.

a[1] = 3;

a[6] = -2;

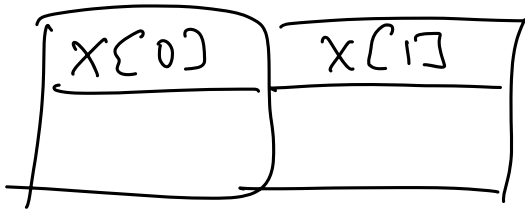
double x[100];

x[98] = 0.23;

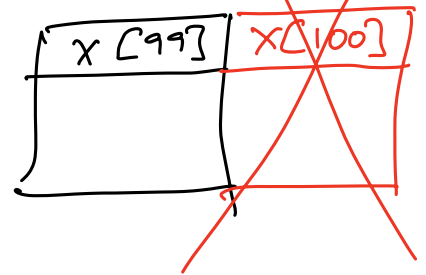
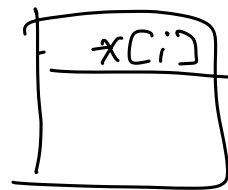
~~x[100] = 2.2;~~

indice è intero.

indice  $\in [0, \text{lunghezza} - 1]$



-

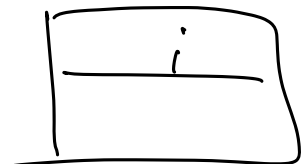


int i = 0;

for (i = 0; i < 100; i++) {

x[i] =

}



x