

Electric field Monte Carlo simulation of coherent backscattering of polarized light by a turbid medium containing Mie scatterers

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Abstract: A method for directly simulating coherent backscattering of polarized light by a turbid medium has been developed based on the Electric field Monte Carlo (EMC) method. Electric fields of light traveling in a pair of time-reversed paths are added coherently to simulate their interference. An efficient approach for computing the electric field of light traveling along a time-reversed path is derived and implemented based on the time-reversal symmetry of electromagnetic waves. Coherent backscattering of linearly and circularly polarized light by a turbid medium containing Mie scatterers is then investigated using this method.

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References and links

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1. Introduction

The study of light propagation in turbid media is a fundamental problem in applied science that has vast applications in many different fields [1-4]. Inside turbid media, light is multiply scattered and the behavior of light propagation is usually described by radiative transfer, where the interference effects of light are ignored. The interference of light, however, does survive inside the coherent backscattering cone around the exact backscattering direction for incident coherent light [5, 6]. This is the celebrated phenomenon of coherent backscattering (CBS), also known as weak localization of light.

Formally, CBS is the consequence of constructive interference of photons which travel in a pair of time-reversed paths. The phase difference between two partial waves traveling in a pair of time-reversed paths annihilates when the backscattered light remits in the direction close to that of exact backscattering. Inside the backscattering cone, the intensity of light needs to be written as $|\mathbf{E}_{out} + \mathbf{E}_{out}^{Rev}|^2$, where $\mathbf{E}_{out}, \mathbf{E}_{out}^{Rev}$ are the electric fields of the two partial waves, roughly double the intensity $|\mathbf{E}_{out}|^2 + |\mathbf{E}_{out}^{Rev}|^2$ when backscattered light is assumed to be incoherent.

Most conventional Monte Carlo simulations trace the Stokes vector [7-11]:

$$\mathbf{I} = (I, Q, U, V)^T,$$

where

$$I = \langle |E_x|^2 + |E_y|^2 \rangle, Q = \langle |E_x|^2 - |E_y|^2 \rangle, U = \langle E_x^* E_y + E_x E_y^* \rangle, V = -i \langle E_x^* E_y - E_x E_y^* \rangle$$

and $E_{x,y}$ are the complex electric field components perpendicular to each other and the propagation direction of light. The superscript T refers to the transpose of the matrix and $\langle \rangle$ denotes ensemble average. Recently, the Electric field Monte Carlo (EMC) method was developed by us to simulate polarized light propagating through turbid media [12,13]. The electric field, rather than the Stokes vector, of light is traced in EMC. The complete phase of light is accrued from both light scattering by particles and propagation through the host medium. EMC is hence most amenable to study coherence phenomena of multiple scattering light, in particular, CBS.

In this paper, we first derive a relation between the electric fields of light traveling in a pair of time-reversed paths based on the time reversal symmetry of electromagnetic waves. This is done in section 2 and the electric field of light traveling in the time-reversed path is shown to be computed from that of light traveling in the forward path, greatly reducing the computation time. The coherent backscattering of circularly polarized light and linearly polarized light is then studied in section 3. Their differences in the dependence of the coherent backscattered light on the azimuthal angle and the dependence of the coherent enhancement on the polar angle are investigated. Concluding remarks are presented in section 4.

2. Theory

The underlying equation for the updating rule of the electric field of scattered light [14] in EMC is:

$$\mathbf{E}' = S\mathbf{R}\mathbf{E}, \quad (1)$$

where \mathbf{E} is the complex electric field with components parallel and perpendicular to the previous scattering plane, \mathbf{E}' is the complex electric field with components parallel and perpendicular to the present scattering plane, S is the amplitude scattering matrix dependent on the scattering angle θ between the incoming propagation direction and outgoing propagation direction, and R is the rotation matrix dependent on the angle ϕ between the

incoming perpendicular electric field component and the outgoing perpendicular electric field component. The rotation matrix R rotates the reference frame ϕ degrees azimuthally to align the incoming perpendicular electric field component to the normal of the present scattering plane. Equation (1) can be explicitly written as the following for Mie scatterers:

$$\begin{pmatrix} E'_1 \\ E'_2 \end{pmatrix} = \begin{bmatrix} S_2(\theta) & 0 \\ 0 & S_1(\theta) \end{bmatrix} \begin{bmatrix} \cos \phi & \sin \phi \\ -\sin \phi & \cos \phi \end{bmatrix} \begin{pmatrix} E_1 \\ E_2 \end{pmatrix}, \quad (2)$$

where E_1 and E_2 are the complex parallel and perpendicular components of the incoming electric field and E'_1 and E'_2 are the complex electric field components after the scattering event. The properties of the scattering particle are contained in the S matrix: S_1 and S_2 dependent on the refractive indices inside and outside the particle as well as the size of the particle and the wavelength of the incident light.

2.1 Electric field of the partial waves in the forward and time-reversed paths

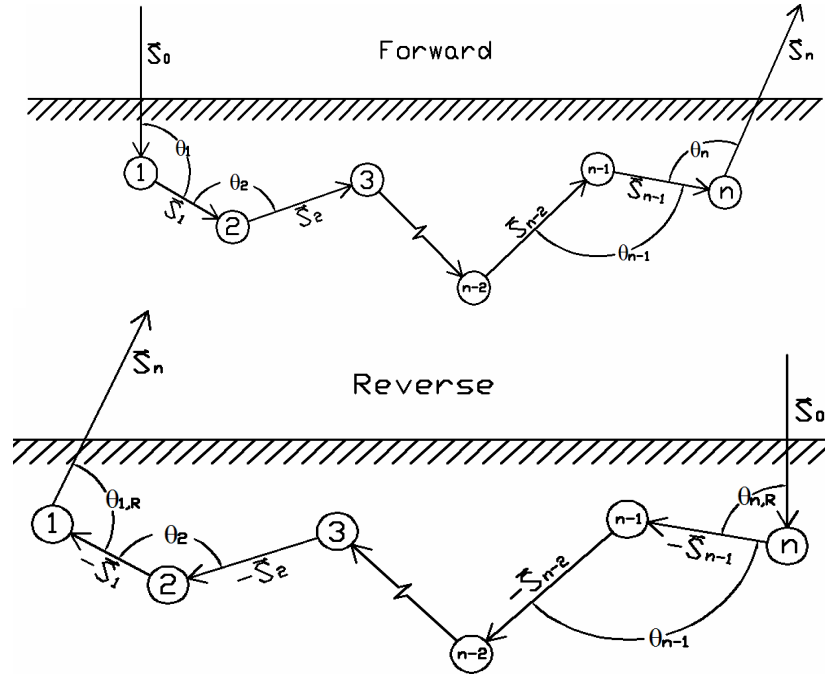


Fig. 1. A pair of partial waves propagating along the forward and reverse paths. The numbered circles are the scatterers. In the forward direction, light enters the media in the direction \mathbf{S}_0 and encounters the first scattering event at the site "1". After being scattered with an angle of θ_1 , light propagates in the \mathbf{S}_1 direction. Light leaves in the \mathbf{S}_n direction after the last scattering at the site "n". In the reverse path, light is incident in the direction \mathbf{S}_0 and is first scattered by the scatterer "n", the last scatterer in the forward path, with a scattering angle of $\theta_{n,R}$ and to the $-\mathbf{S}_{n-1}$ direction. At the last scattering event in the reverse path, light is scattered at the site "1" with a scattering angle of $\theta_{1,R}$ and escapes the medium in the same direction \mathbf{S}_n that light remits in the forward path.

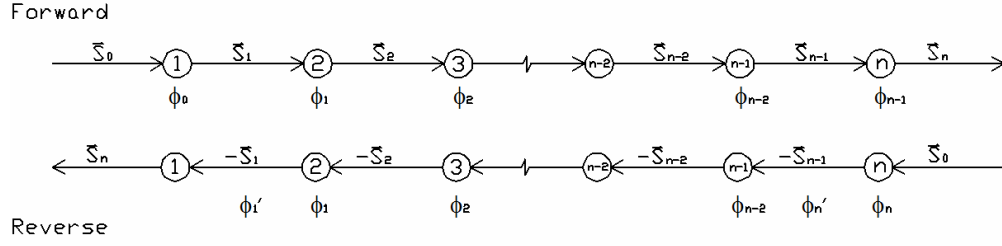


Fig. 2. The azimuthal rotations of the normal of the scattering plane along the forward and reverse paths. In the forward path, light is rotated for an azimuthal angle of ϕ_{i-1} at the i -th scattering event. In the reverse path, except for three special rotations of angles ϕ_n, ϕ'_n , and ϕ'_1 , all the other rotations in the reverse path use the same ϕ angles as those in the forward path. See the text for details.

The local coordinate system described by three vectors \mathbf{m} , \mathbf{n} , and \mathbf{s} is rotated after every scattering event. Here \mathbf{m} is the direction of the parallel electric field component and \mathbf{n} is the direction of the perpendicular electric field component. The vector \mathbf{n} is perpendicular to the scattering plane spanned by the previous propagation direction and the current propagation direction, \mathbf{s} .

As is displayed in Figs. 1 and 2, in the forward path, light is scattered to the \mathbf{s}_1 direction after the first scattering event; ϕ_0 is the angle formed between the incoming perpendicular electric field component and $\mathbf{n}_1 = \mathbf{s}_0 \times \mathbf{s}_1 / |\mathbf{s}_0 \times \mathbf{s}_1|$. After a total of n scattering events, light is scattered into the direction \mathbf{s}_n and escapes the medium. ϕ_{n-1} is the angle formed between $\mathbf{n}_{n-1} = \mathbf{s}_{n-2} \times \mathbf{s}_{n-1} / |\mathbf{s}_{n-2} \times \mathbf{s}_{n-1}|$ and $\mathbf{n}_n = \mathbf{s}_{n-1} \times \mathbf{s}_n / |\mathbf{s}_{n-1} \times \mathbf{s}_n|$. When the path is reversed, the first scattering event occurs at the n^{th} scatterer, where light is scattered from \mathbf{s}_0 to $-\mathbf{s}_{n-1}$. ϕ_n is the angle formed between the incoming perpendicular electric field component and $\mathbf{n}' = \mathbf{s}_0 \times (-\mathbf{s}_{n-1}) / |\mathbf{s}_0 \times (-\mathbf{s}_{n-1})|$ and ϕ'_n is the angle formed between \mathbf{n}' and $-\mathbf{n}_{n-1} = (-\mathbf{s}_{n-1}) \times (-\mathbf{s}_{n-2}) / |(-\mathbf{s}_{n-1}) \times (-\mathbf{s}_{n-2})|$. After the ϕ'_n rotation, the second scattering event in the time-reversed path occurs at the $n-1$ scatterer, followed by a rotation of ϕ_{n-2} azimuthally along $-\mathbf{s}_{n-2}$ from $-\mathbf{n}_{n-1}$ to $-\mathbf{n}_{n-2}$. This continues until the last site that scatters light in the reverse path, which is the first site in the forward path. At this last scattering event, light is scattered into \mathbf{s}_n from $-\mathbf{s}_1$. ϕ_1 is the angle between $-\mathbf{n}_2 = (-\mathbf{s}_2) \times (-\mathbf{s}_1) / |(-\mathbf{s}_2) \times (-\mathbf{s}_1)|$ and $-\mathbf{n}_1 = (-\mathbf{s}_1) \times (-\mathbf{s}_0) / |(-\mathbf{s}_1) \times (-\mathbf{s}_0)|$ and ϕ'_1 is the angle between $-\mathbf{n}_1$ and $\mathbf{n}'' = (-\mathbf{s}_1) \times \mathbf{s}_n / |(-\mathbf{s}_1) \times \mathbf{s}_n|$. The angle $\phi'_1 = 0$ if $\mathbf{s}_n = -\mathbf{s}_0$. After a total of n scattering events the electric field in the forward path is hence given by:

$$\mathbf{E}_{\text{out}} = S^{(n)}(\mathbf{s}_n, \mathbf{s}_{n-1}) R(\phi_{n-1}) S^{(n-1)}(\mathbf{s}_{n-1}, \mathbf{s}_{n-2}) R(\phi_{n-2}) \dots R(\phi_2) S^{(2)}(\mathbf{s}_2, \mathbf{s}_1) R(\phi_1) S^{(1)}(\mathbf{s}_1, \mathbf{s}_0) R(\phi_0) \mathbf{E}_{\text{in}}, \quad (3)$$

and the electric field in the reverse path is given by:

$$\mathbf{E}_{\text{out}}^{\text{Rev}} = S^{(1)}(\mathbf{s}_n, -\mathbf{s}_1) R(\phi'_1) R(\phi_1) S^{(2)}(-\mathbf{s}_1, -\mathbf{s}_2) R(\phi_2) \dots R(\phi_{n-2}) S^{(n-1)}(-\mathbf{s}_{n-2}, -\mathbf{s}_{n-1}) R(\phi'_n) S^{(n)}(-\mathbf{s}_{n-1}, \mathbf{s}_0) R(\phi_n) \mathbf{E}_{\text{in}}. \quad (4)$$

Here the superscript of S denotes the site at which the scattering event takes place.

2.2 Special azimuthal rotations in the time-reversed path

Two special rotations are needed at the scatterer "n" (the first scatterer in the reverse path) in order to align the reference frame to the scattering plane spanned by $-\mathbf{s}_{n-1}$ and $-\mathbf{s}_{n-2}$. Let \mathbf{m}_0 and \mathbf{n}_0 be the directions of the incoming parallel electric field and the incoming perpendicular electric field, respectively. In the reverse path, the first two rotations can be described by the following expression:

$$\begin{pmatrix} \mathbf{m}_0 \\ \mathbf{n}_0 \\ \mathbf{s}_0 \end{pmatrix} \xrightarrow{R(\phi_n)S^{(n)}} \begin{pmatrix} \mathbf{m}' \\ \mathbf{n}' \\ -\mathbf{s}_{n-1} \end{pmatrix} \xrightarrow{R(\phi'_n)} \begin{pmatrix} \mathbf{m}_{n-1} \\ -\mathbf{n}_{n-1} \\ -\mathbf{s}_{n-1} \end{pmatrix}.$$

The first rotation, $R(\phi_n)$, aligns the perpendicular electric field of the incident beam to the normal of the scattering plane. The second rotation, $R(\phi'_n)$, aligns \mathbf{m}' to \mathbf{m}_{n-1} , and \mathbf{n}' to $-\mathbf{n}_{n-1}$. The direction, $-\mathbf{n}_{n-1}$, is the normal of the scattering plane for the upcoming scattering event at the second scatterer "n-1" in the reverse path.

At the last scattering event in the reverse path, a special rotation is also required. That is:

$$\begin{pmatrix} \mathbf{m}_1 \\ -\mathbf{n}_1 \\ -\mathbf{s}_1 \end{pmatrix} \xrightarrow{R(\phi'_1)} \begin{pmatrix} \mathbf{n}'' \times (-\mathbf{s}_1) \\ \mathbf{n}'' \\ -\mathbf{s}_1 \end{pmatrix} \xrightarrow{S^{(1)}} \begin{pmatrix} \mathbf{m}'' \\ \mathbf{n}'' \\ \mathbf{s}_n \end{pmatrix}.$$

Prior to the last scattering event at the scatterer "1," the local coordinate system is: $(\mathbf{m}_1, -\mathbf{n}_1, -\mathbf{s}_1)^T$. The rotation $R(\phi'_1)$ aligns the perpendicular electric field component to the normal of the upcoming scattering plane spanned by $-\mathbf{s}_1$ and \mathbf{s}_n . \mathbf{m}'' and \mathbf{n}'' are the directions of the outgoing parallel and perpendicular electric field components, respectively.

2.3 Relation between electric fields in the forward and time-reversed paths

Let us take the middle portions of Eqs. (3) and (4) and call them T and T^{Rev} , respectively:

$$T = S^{(n-1)}(\mathbf{s}_{n-1}, \mathbf{s}_{n-2})R(\phi_{n-2})...R(\phi_2)S^{(2)}(\mathbf{s}_2, \mathbf{s}_1)R(\phi_1) \quad (5)$$

and

$$T^{\text{Rev}} = R(\phi_1)S^{(2)}(-\mathbf{s}_1, -\mathbf{s}_2)R(\phi_2)...R(\phi_{n-2})S^{(n-1)}(-\mathbf{s}_{n-2}, -\mathbf{s}_{n-1}). \quad (6)$$

T and T^{Rev} are related as will be shown. Indeed, the transpose of T is given by

$$T^T = R^T(\phi_1)S^{(2)T}(\mathbf{s}_2, \mathbf{s}_1)R^T(\phi_2)...R^T(\phi_{n-2})S^{(n-1)T}(\mathbf{s}_{n-1}, \mathbf{s}_{n-2}). \quad (7)$$

Noting that

$$R^T(\phi) = \begin{bmatrix} \cos \phi & -\sin \phi \\ \sin \phi & \cos \phi \end{bmatrix} = Q \begin{bmatrix} \cos \phi & \sin \phi \\ -\sin \phi & \cos \phi \end{bmatrix} Q = QR(\phi)Q, \quad (8)$$

and the scattering amplitude matrices in the forward path and its time reversal is related by [15]:

$$S^{(2)T}(\mathbf{s}_2, \mathbf{s}_1) = QS^{(2)}(-\mathbf{s}_1, -\mathbf{s}_2)Q, \quad (9)$$

where

$$Q = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix},$$

we find:

$$T^T = QR(\phi_1)QQS^{(2)}(-\mathbf{s}_1, -\mathbf{s}_2)QQR(\phi_2)Q \dots QR(\phi_{n-2})QQS^{(n-1)}(-\mathbf{s}_{n-2}, -\mathbf{s}_{n-1})Q, \quad (10)$$

$$T^T = QT^{\text{Rev}}Q, \quad (11)$$

and:

$$T^{\text{Rev}} = QT^TQ. \quad (12)$$

Finally, the electric field in the forward path is:

$$\mathbf{E}_{out} = S^{(n)}(\mathbf{s}_n, \mathbf{s}_{n-1})R(\phi_{n-1})TS^{(1)}(\mathbf{s}_1, \mathbf{s}_0)R(\phi_0)\mathbf{E}_{in}, \quad (13)$$

and in the reverse path:

$$\mathbf{E}_{out}^{\text{Rev}} = S^{(1)}(\mathbf{s}_n, -\mathbf{s}_1)R(\phi_1')QT^TQR(\phi_n')S^{(n)}(-\mathbf{s}_{n-1}, \mathbf{s}_0)R(\phi_n)\mathbf{E}_{in}. \quad (14)$$

3. Results and discussion

We performed EMC simulations of coherent backscattering of normally incident circularly polarized light and linearly polarized light by a turbid medium. Each simulation used 125,000 photon packets using the partial photon technique[12] and took less than twenty-four hours on a single 2.33 GHz Intel Xeon core to simulate the electric field in both the forward and reverse paths covering the backscattering directions at 73 azimuthal detection angles and 76 zenith detection angles. The turbid medium is composed of a water suspension of polystyrene spheres whose diameter is 0.1 micrometers and refractive index is 1.58984. The wavelength of the incident light is 0.5145 micrometers. The thickness of the turbid medium is 20 scattering mean free paths.

3.1 Intensity and enhancement of circularly polarized light around the exact backscattering direction

Figure 3 illustrates coherent backscattering of normally incident circularly polarized light. The top row displays the backscattering intensities of incident coherent light of circular polarization (left: $I_+ + I_-$, middle: I_+ , right: I_-). I_{\pm} is the intensity of the backscattered light of the same (or opposite) helicity as that of the incident beam. The second row displays the corresponding intensities for incident incoherent light of circular polarization. As one can see from Fig. 3, concentric circles of equal intensity are visible with or without coherence. The intensity also drops off as the zenith angle θ_b of detection increases in all cases. This azimuthal angle ϕ_b independence is expected as circularly polarized light has by definition centric symmetry.

As displayed in Fig. 4, for coherent backscattered intensities, I_+ is greater than I_- close to exact backscattering direction and is smaller than I_- for all other angles; for incoherent backscattered intensities, I_+ is less than I_- for all θ_b simulated. Enhancement is higher for I_+

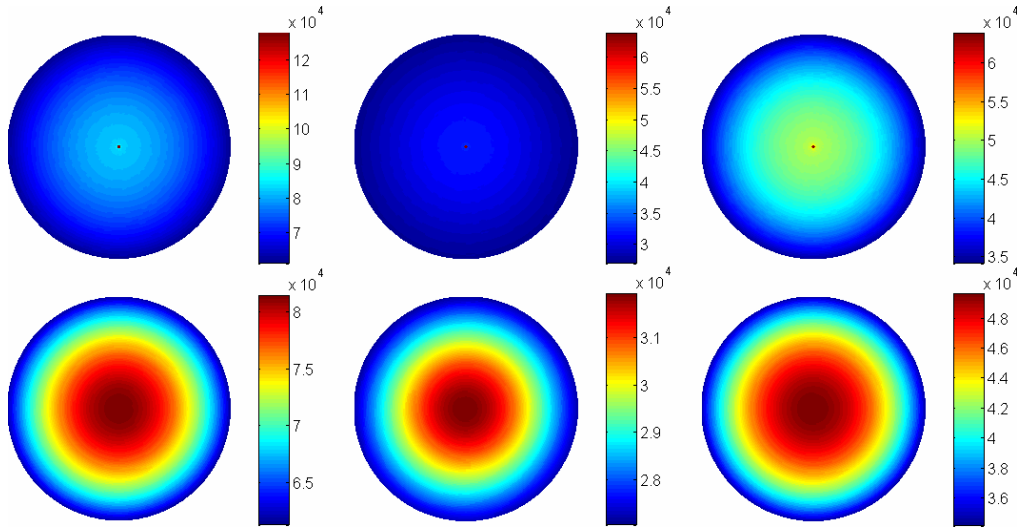


Fig. 3. (Color) Backscattering of normally incident circularly polarized light. The first row displays $I_+ + I_-$, I_+ , and I_- from left to right for incident coherent light; the bottom row displays the corresponding intensities for incident incoherent light. Each circle depicts the view around the exact backscattering direction such that the zenith angle (θ_b) is the circle's radius, in degrees, and the azimuthal angle (ϕ_b) is the polar angle, in degrees. θ_b starts at zero degrees exactly in the center, the exact backscattering direction, and ends at the edge (75 degrees). ϕ_b is zero degrees in the direction of a standard Cartesian positive x-axis and increases counterclockwise until 360 degrees. Notice all I 's are not dependent on the azimuthal angle.

near the exact escape direction but falls off more sharply than I_- as θ_b increases. Incoherent backscattered light is stronger in the negative helicity channel than in the positive helicity one ($I_+ > I_-$) because the helicity asymmetry is negative for backscattered light by small Mie scatterers in a turbid medium [16]. Multiply scattered light loses coherence and helicity simultaneously upon scattering. The enhancement factor is larger for the helicity preserved channel than the helicity flipped channel near the exact backscattering direction. This boosts the intensity of the coherent backscattered I_+ beyond I_- within a narrow angular range around the exact backscattering direction.

3.2 Intensity and enhancement of linearly polarized light around the exact backscattering direction

Figure 5 illustrates the intensity of backscattered light for normally incident linearly polarized light around the exact backscattered direction. The first row in Fig. 5 is, from left to right, backscattered $I_x + I_y$, I_x , and I_y for incident coherent light polarized along the x direction. The second row is the same except the incident light is incoherent. The third row is the same as the first row but the zenith detection angle goes from 0 degrees to 2.25 degrees instead. Figure 6 displays the angular profiles for coherent backscattering light, incoherent backscattering light, and the enhancement factor along three directions corresponding to the azimuthal angle of 0, 45, and 90 degrees, respectively.

Like the case of circularly polarized light with and without coherence, the linearly polarized light shows symmetry about the x,y axes, but it no longer has circular symmetry. The intensity of the backscattered light of x polarization from the incident coherent or

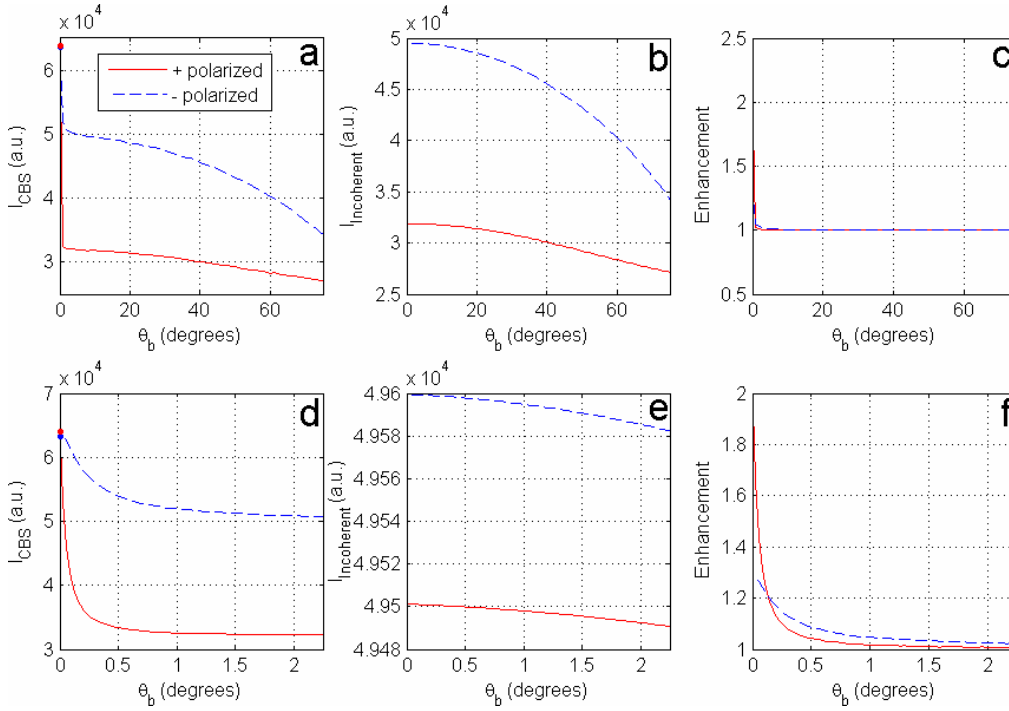


Fig. 4. (Color) Angular profiles of backscattering of circularly polarized light versus the zenith detection angle. Coherent backscattered intensities, incoherent backscattered intensities, and the enhancement factor are displayed in (a,d), (b,e), and (c,f), respectively. Near exact backscattering direction $\theta_b \sim 0$, coherent backscattered I_+ is greater than coherent backscattered I_- and the enhancement factor for I_+ is larger than I_- . Incoherent backscattered I_+ is less than incoherent backscattered I_- for all θ_b . (Note that I_- in (f) is raised for 1.75×10^4 to show how it compares with I_+ within the angular range).

incoherent x -polarized light is, in general, greater than that of y polarization because the preference in linear polarization only gets lost after multiple scattering. As with circularly polarized coherent light, backscattering of linearly polarized coherent light is enhanced relative to that of incoherent light within the backscattering cone. I_x is enhanced greater than I_y because photons contributing to I_x preserve the original linear polarization and suffer less scattering events than photons contributing to I_y and hence maintain coherence better. Unlike the case involving circularly polarized light, the magnitude of the intensity of linearly polarized light, $I_x + I_y$, is no longer circular symmetric. This shows that there is a dependence on the azimuthal angle ϕ_b for backscattering of linearly polarized light. As to understand why the patterns for I_x 's and $I_x + I_y$'s are elongated along the y -axis and the pattern for I_y 's is elongated along the x -axis, we point out that light tends to be scattered preferably into directions out of the plane of its polarization when scattered by a Mie scatterer. Thus the x -component is elongated along the y -axis and squeezed in along the x -axis and the

y-component is elongated along the x -axis and squeezed in along the y -axis. Both coherent and incoherent I_x 's increase slightly with the zenith angle, mostly owing to the influence of single scattered light.

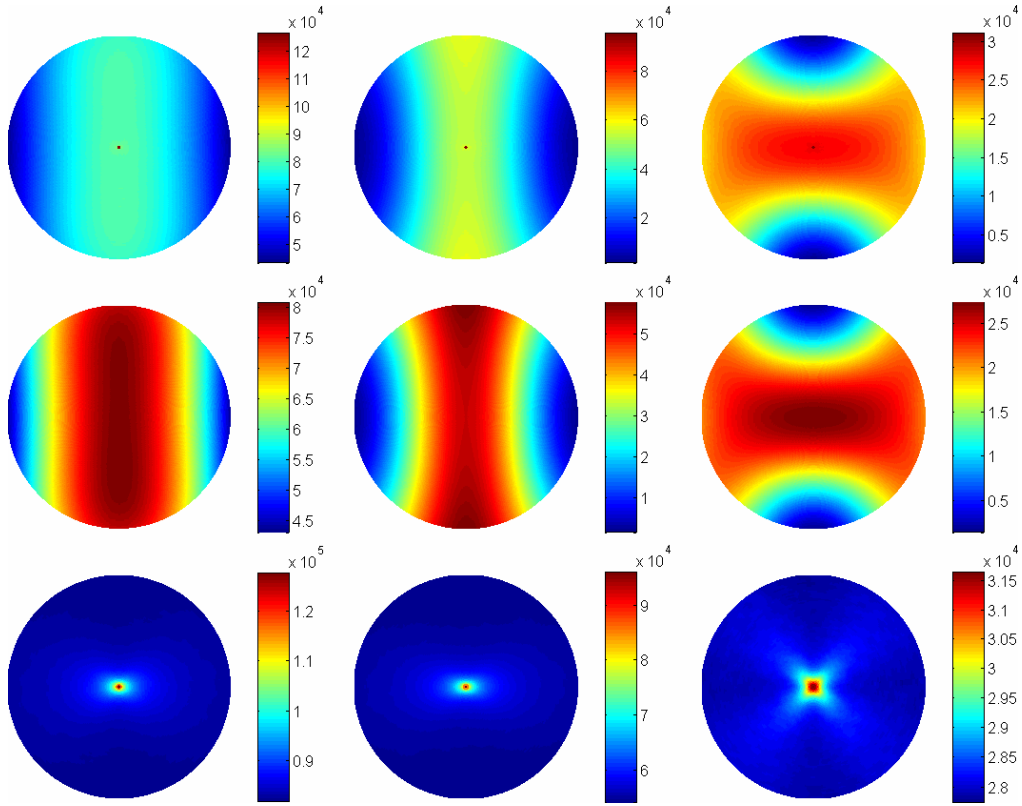


Fig. 5. (Color) Backscattering of normally incident linearly polarized light. The incident beam is polarized linearly in the x -direction. Each circle depicts the view around the exact backscattering direction such that the zenith angle (θ_b) is the circle's radius, in degrees, and the azimuthal angle (ϕ_b) is the polar angle, in degrees. θ_b starts at zero degrees exactly in the center, the exact backscattering direction, and ends at the edge at 75 degrees for the top and middle rows and ends at 2.25 degrees for the bottom row. ϕ_b is zero degrees in the direction of a standard Cartesian positive x -axis and increases counterclockwise until 360 degrees.

The first row is, from left to right, backscattered $I_x + I_y$, I_x , and I_y for incident coherent light. The second row is the same except the incident light is incoherent. The third row is the same as the first row but the zenith detection angle goes from 0 degrees to 2.25 degrees instead. In the first two rows, $I_x + I_y$ is no longer symmetric all around but is elongated along the y -axis; similarly, the x -component, I_x , is elongated along the y -axis, while the y -component, I_y , is elongated along the x -axis. The coherent backscattered light close to the exact backscattering direction in the bottom row reveals more clearly the dependence on the azimuthal angle ϕ_b .

Closer to the exact backscattering direction (bottom row of Fig. 5), backscattering of coherent linearly polarized light appears to display different symmetries. $I_x + I_y$ and I_x appear to now be elongated along the x -axis and squeezed slightly at the y -axis due to the much stronger enhancement factor for backscattered light remitting from along the x -axis [see Fig. 6(f)]. Also, I_y displays interesting 4-fold “X” symmetry closer to the exact escape direction, which is characteristic of light being multiply scattered by Rayleigh-like particles.

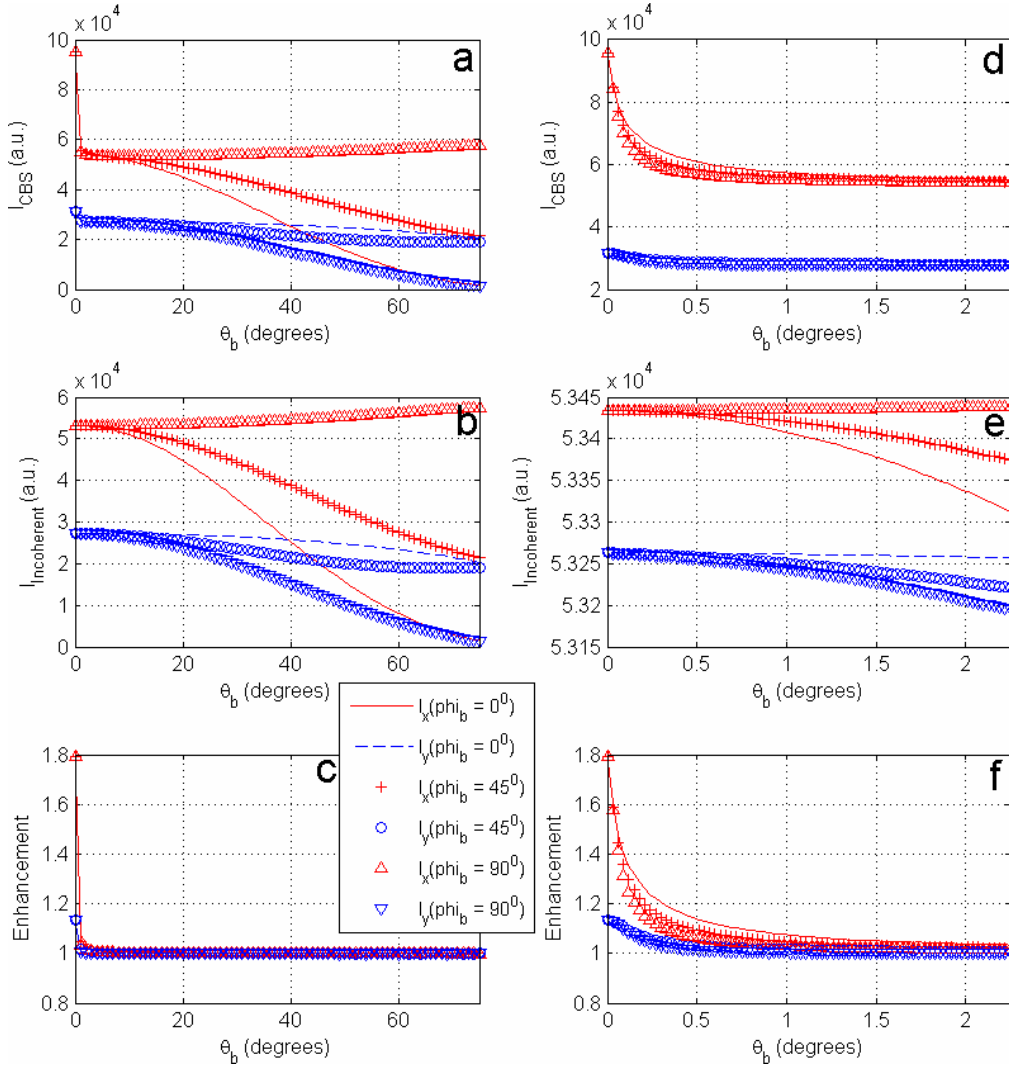


Fig. 6. (Color) Angular profiles of backscattering of linearly polarized light along three directions corresponding to the azimuthal angle of 0, 45, and 90 degrees, respectively. Coherent backscattered intensities, incoherent backscattered intensities, and the enhancement factor are displayed in (a,d), (b,e), and (c,f), respectively. (Note that I_y in (e) is raised for 2.54×10^4 to show how it compares with I_x within the angular range).

4. Conclusion

In conclusion, the Electric field Monte Carlo method for coherent backscattering of light has been developed. This approach simulates coherent backscattering of light directly by adding coherently the electric fields of backscattered light propagating in a pair of time-reversed paths. The conventional simulation of coherent backscattering of light based on the Fourier transform of the spatial distribution of incoherent backscattering light is valid for scalar waves but introduces appreciable errors for polarized light as additional amplitude and phase differences between the two partial waves propagating in a pair of time-reversed paths appear. These errors originate from the depolarization of light. The EMC approach properly takes into full account of these additional complexities and a detailed study of this issue will be published elsewhere.

The computation of the electric field of light traveling the reverse path was simplified by using the time-reversal symmetry of electromagnetic waves that allow for the reuse of the majority of the information obtained in the forward path and as a result save a great amount of computational time. The EMC method was then used to investigate coherent backscattering of linearly or circularly polarized light from a turbid medium containing Mie scatterers. The coherent backscattering patterns were shown to depend strongly on the polarization of the incident light and detection conditions.

Acknowledgments

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