

# On hydrogen-induced plastic flow localization during void growth and coalescence

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## Abstract

Hydrogen-enhanced localized plasticity (HELP) is recognized as a viable mechanism of hydrogen embrittlement. A possible way by which the HELP mechanism can bring about macroscopic material failure is through hydrogen-induced accelerated void growth and coalescence. Assuming a periodic array of spherical voids loaded axisymmetrically, we investigate the hydrogen effect on the occurrence of plastic flow localization upon void growth and its dependence on macroscopic stress triaxiality. Under a macroscopic stress triaxiality equal to 1 and prior to void coalescence, the finite element calculation results obtained with material data relevant to A533B steel indicate that a hydrogen-induced localized shear band forms at an angle of about 45° from the axis of symmetry. At triaxiality equal to 3, void coalescence takes place by accelerated hydrogen-induced localization of plasticity mainly in the ligament between the voids. Lastly, we discuss the numerical results within the context of experimental observations on void growth and coalescence in the presence of hydrogen.

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**Keywords:** Hydrogen; Embrittlement; Void growth; Coalescence; Plasticity

## 1. Introduction

It is well known that hydrogen-enhanced localized plasticity (HELP) is a mechanism for hydrogen embrittlement whereby hydrogen promotes macroscopic material failure through localized deformation processes [1,2]. The objective of this work is to investigate the hydrogen effect on plastic flow localization during void growth and coalescence as a function of the hydrostatic constraint, that is, low and high stress triaxiality prevalent in cylindrical bar specimens strained uniaxially and ahead of blunting crack tips, respectively. The study is important toward understanding the conditions under which the HELP mechanism promotes ductile crack propagation at load levels that a hydrogen-free material can safely sustain.

There exists ample experimental evidence that hydrogen affects void growth and coalescence. Performing three-point bending tests on U-notched bend bars of spheroidized AISI 1095 and AISI 1090 steels, Hirth and co-workers [3,4] found

that hydrogen reduces the critical strain for void nucleation and increases the population of voids. They suggested that hydrogen by enhancing void nucleation and growth promotes plastic instability along characteristic slip traces beneath the notch. Cialone and Asaro [5] using smooth and notched tensile specimens of spheroidized plain-carbon steels found that hydrogen assists void growth and accelerates void coalescence [6]. Garber et al. [7,8] carried out tensile experiments using cylindrical specimens of 1018 and 1080 steels. While they did not observe a significant hydrogen effect on void growth at the initial stages of growth, they found a strong effect during the coalescence stage. Park and Thompson [9] also observed a similar effect in 1520 steel and Fan and Koss [10] in low carbon steels. Maier et al. [11] studied the hydrogen effect on void behavior in a spheroidized low alloy steel using smooth unnotched tensile specimens. They observed that hydrogen enhances void nucleation and promotes final brittle failure by plastic shear localization.

Liang et al. [12] simulated void growth and coalescence in the presence of hydrogen in a niobium system under the assumption that hydrogen is in equilibrium with local stress in

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the matrix around a void. Their finite element calculation results support the argument that while hydrogen has a negligible effect on void growth at the early stages of straining, it does accelerate the coalescence stage. The underlying mechanism by which hydrogen was found to promote void coalescence is localized material softening that varied point-wise in the matrix depending on the corresponding hydrogen distribution around the void. In fact, Liang et al. found out that at the final stages of growth hydrogen promotes the localization of plasticity in the ligament between voids which leads to final void coalescence. We note that Liang et al. found that such localization of plasticity during the coalescence stage is the case at all levels of triaxiality, even in the absence of hydrogen. They identified the role of hydrogen in the triggering of the localization process at lower macroscopic strains than in the absence of hydrogen.

In the present study, we analyze the hydrogen effect on void growth and coalescence using material data pertinent to the nuclear reactor steel A533B. Unlike the niobium system used in the investigation of Liang et al. [12], A533B steel is an iron system that can trap hydrogen in vast amounts as deformation proceeds [13–15]. Trapping of hydrogen can drastically affect the material constitution and this can have a significant effect on the conditions for plastic flow localization even at small triaxialities. It will be shown that at small triaxialities and before void coalescence the presence of strong hydrogen trapping leads to the formation of a localized band at an angle of about 45° from the direction defined by the intervoid-ligaments.

Following Liang et al. [12] we simulate the hydrogen effect on void growth and coalescence at a unit cell containing a spherical void and loaded remotely by principal axisymmetric stresses. Results obtained under various levels of applied stress triaxiality can be viewed as representing the behavior of a void at different locations in the neighborhood of a blunting crack tip (Fig. 1).

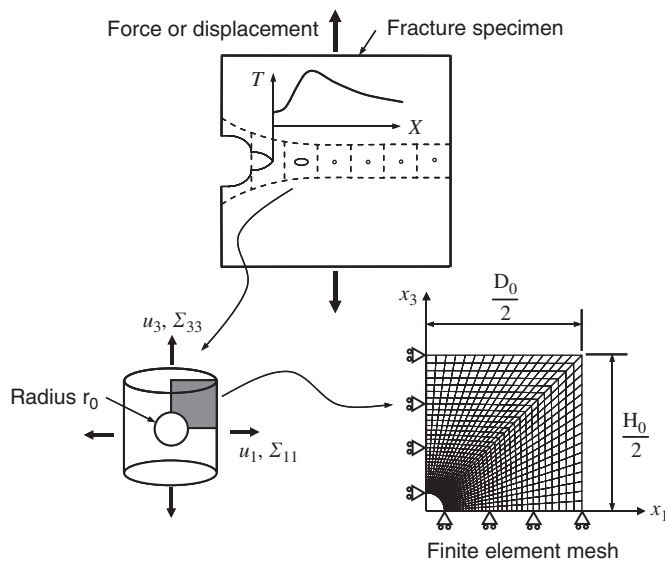


Fig. 1. The axisymmetric unit cell model and the finite element mesh for the first quadrant. The cell is strained while the triaxiality  $T = (2\Sigma_{11} + \Sigma_{33})/3|\Sigma_{33} - \Sigma_{11}|$  is maintained constant.

## 2. Hydrogen concentration and constitutive law

Hydrogen dissolved in metals and alloys resides either at normal interstitial lattice sites (NILS) or reversible trapping sites at microstructural defects generated by plastic straining such as dislocations. The two populations are assumed to be in equilibrium according to Oriani's theory [16] such that

$$\frac{\theta_T}{1 - \theta_T} = \frac{\theta_L}{1 - \theta_L} \exp\left(\frac{W_B}{R\Theta}\right), \quad (1)$$

where  $\theta_L$  denotes the occupancy of the interstitial sites,  $\theta_T$  denotes the occupancy of the trapping sites,  $W_B$  is the trap binding energy,  $R$  is the gas constant equal to  $8.31 \text{ J mol}^{-1} \text{ K}^{-1}$ , and  $\Theta$  is the absolute temperature. The hydrogen concentration at trapping sites  $C_T$ , measured in hydrogen atoms per unit volume, can be expressed as  $C_T = \theta_T \alpha N_T$ , where  $\alpha$  denotes the number of sites per trap, and  $N_T = N_T(\varepsilon^P)$  denotes the trap density in traps per unit volume as a function of the local plastic straining measured in terms of the effective plastic strain  $\varepsilon^P$ . The hydrogen concentration  $C_L$  at NILS, measured in hydrogen atoms per unit volume, can be phrased as  $C_L = \theta_L \beta N_L$ , where  $\beta$  denotes the number of NILS per solvent atom, and  $N_L$  denotes the number of solvent atoms per unit volume given by  $N_L = N_A/V_M$  in which  $N_A = 6.0232 \times 10^{23}$  atoms per mole is Avogadro's number and  $V_M$  is the molar volume of the host lattice.

Using Fermi–Dirac statistics [17], we calculate the hydrogen concentration  $C_L$  in terms of the NILS concentration  $C_L^0$  in the stress-free lattice by assuming equilibrium with local stress  $\sigma$ :

$$\frac{\theta_L}{1 - \theta_L} = \frac{\theta_L^0}{1 - \theta_L^0} \exp\left(\frac{\sigma_{kk} V_H}{3R\Theta}\right), \quad (2)$$

where  $\theta_L^0 = C_L^0/\beta N_L$  is the initial occupancy of NILS,  $\sigma_{kk}$  is the local hydrostatic stress,  $V_H$  is the partial molar volume of hydrogen in solution, and a repeated index implies standard summation convention. Occupancy  $\theta_L$  is a function of the hydrostatic stress as regions under tension attract hydrogen solutes [13,17].

Combining Eqs. (1) and (2), we find the total hydrogen concentration  $c = (C_L + C_T)/N_L$ , measured in hydrogen atoms per solvent atom, as a function of both the hydrostatic stress and the equivalent plastic strain as

$$c = c_L + c_T = \beta \left[ \theta_L(\sigma_{kk}) + \frac{\alpha N_T(\varepsilon^P)}{\beta N_L} \theta_T \right], \quad (3)$$

where  $c_L = C_L/N_L$  and  $c_T = C_T/N_L$ . Eq. (3) defines the total hydrogen concentration at a point as a function of the effective plastic strain  $\varepsilon^P$  and hydrostatic stress  $\sigma_{kk}$ .

Based on experimental observations of hydrogen-induced dislocation velocity enhancement in iron, Tabata and Birnbaum [18] suggested that the local flow stress of the material is a decreasing function of the hydrogen concentration. Sofronis et al.

[19] and Liang et al. [20] described the hydrogen effect on the local flow stress  $\sigma_Y$  through a phenomenological relation,

$$\sigma_Y(\varepsilon^p, c) = \sigma_0(c) \left( 1 + \frac{\varepsilon^p}{\varepsilon_0} \right)^N, \quad (4)$$

in which  $c$  is the total hydrogen concentration in trapping sites and NLS measured in hydrogen atoms per solvent atom,  $N$  is the hardening exponent,  $\sigma_0(c)$  is the initial yield stress in the presence of hydrogen,  $\sigma_0 = \sigma_0(0)$  is the initial yield stress in the absence of hydrogen, and  $\varepsilon_0 = \sigma_0/E$  is the corresponding yield strain with  $E$  being Young's modulus. A possible suggestion for  $\sigma_0(c)$  is

$$\sigma_0(c) = \begin{cases} \left[ (\xi - 1) \frac{c}{c_L^0} + 1 \right] \sigma_0 & \text{for } \sigma_0(c) > \eta \sigma_0, \\ \eta \sigma_0 & \text{for } \sigma_0(c) \leq \eta \sigma_0, \end{cases} \quad (5)$$

where  $\xi \leq 1$  is a softening parameter,  $\eta \sigma_0$  is the lowest value of the yield stress with  $\eta$  varying between 0 and 1, and  $c_L^0$  is the initial hydrogen concentration in the unstressed lattice measured in hydrogen atoms per solvent atom.

For the elastoplastic constitutive law of the material in the presence of hydrogen, we assume that the total deformation rate tensor  $\mathbf{D}$ —the symmetric part of the velocity gradient—is the sum of an elastic part  $\mathbf{D}^e$ , a plastic part  $\mathbf{D}^p$ , and a part due to the presence of hydrogen  $\mathbf{D}^h$ :

$$\mathbf{D} = \mathbf{D}^e + \mathbf{D}^p + \mathbf{D}^h. \quad (6)$$

We assume that the elastic behavior of the material is linear and isotropic:

$$\mathbf{D}^e = \mathbf{C}^{e-1} : \overset{\nabla}{\boldsymbol{\sigma}} = \left( \frac{1}{2\mu} \mathbf{K} + \frac{1}{3K} \mathbf{J} \right) : \overset{\nabla}{\boldsymbol{\sigma}}, \quad (7)$$

where  $\mathbf{C}^e$  is the fourth order tensor of the elastic moduli,  $\mathbf{K} = \mathbf{I} - \mathbf{J}$  is the deviatoric part of the fourth order identity tensor  $\mathbf{I}$  whose Cartesian components are  $I_{ijkl} = (\delta_{ik}\delta_{jl} + \delta_{jk}\delta_{il})/2$  with  $\delta_{ij}$  being the Kronecker delta,  $\mathbf{J} = \delta \delta / 3$  is the hydrostatic part of the identity tensor  $\mathbf{I}$ ,  $\delta$  is the second order identity tensor,  $\boldsymbol{\sigma}$  is the Cauchy stress,  $\mu$  and  $K$  are, respectively, the shear and bulk moduli, a superposed  $\nabla$  denotes the Jaumann rate, the superscript  $-1$  denotes tensor inverse, and  $\mathbf{A} : \mathbf{B} = A_{ijkl} B_{kl}$ , where  $\mathbf{A}$  and  $\mathbf{B}$  are, respectively, fourth and second order tensors.

We write the rate of dilatational [21] deformation  $\mathbf{D}^h$  due to dissolved hydrogen as

$$\mathbf{D}^h = \frac{d}{dt} \left[ \ln \left( 1 + \frac{1}{3} (c - c_0) \frac{\Delta v}{\Omega} \right) \right] \delta = \frac{1}{3} A(c) \dot{c} \delta, \quad (8)$$

where the parameter  $c_0$  is the initial hydrogen concentration in NLS and trapping sites measured in hydrogen atoms per solvent atom,  $\Delta v = V_H/N_A$  is the volume dilatation per atom of hydrogen introduced into solution,  $V_H$  the partial molar volume of hydrogen in solution,  $\Omega$  the mean atomic volume of the host atom, and a superposed dot denotes material time derivative. For the plastic behavior, we assume that the material is rate

independent, obeys von-Mises yielding, and hardens isotropically under plastic straining. The yield criterion is of the form

$$f = \sigma_e - \sigma_Y(\varepsilon^p, c), \quad (9)$$

where  $\sigma_e = \sqrt{3\boldsymbol{\sigma}' : \boldsymbol{\sigma}'}/2$  is the von-Mises equivalent stress,  $\boldsymbol{\sigma}'$  is the deviatoric part of the Cauchy stress defined through  $\boldsymbol{\sigma}' = \mathbf{K} : \boldsymbol{\sigma}$ , and  $\varepsilon^p = \int \sqrt{2\mathbf{D}^p : \mathbf{D}^p}/3 dt$  is the effective plastic strain. Assuming normality for the derivation of the flow rule for  $\mathbf{D}^p$  and using Eqs. (7)–(9), we derive the constitutive law accounting for hydrogen-induced material softening and lattice dilatation:

$$\overset{\nabla}{\boldsymbol{\sigma}} = \left( \mathbf{C}^e - \frac{9\mu^2}{h+3\mu} \frac{\boldsymbol{\sigma}'\boldsymbol{\sigma}'}{\sigma_e^2} \right) : (\mathbf{D} - \mathbf{D}^h) + \frac{3\mu}{h+3\mu} \frac{\partial \sigma_Y}{\partial c} \dot{c} \frac{\boldsymbol{\sigma}'}{\sigma_e}, \quad (10)$$

where  $h = \partial \sigma_Y / \partial \varepsilon^p$ . Eqs. (1)–(10) show that the problem of determining the hydrogen concentration, stress, and plastic strain fields is fully coupled.

### 3. Unit cell

We model the behavior of an axisymmetric unit cell containing a spherical void [12,22] as shown in Fig. 1. The cell is loaded macroscopically by principal axisymmetric stresses  $\Sigma_{11}$  and  $\Sigma_{33}$  while the stress triaxiality  $T = (2\Sigma_{11} + \Sigma_{33})/3|\Sigma_{33} - \Sigma_{11}|$  measuring the ratio of the hydrostatic stress over the deviatoric stress is forced to remain constant during deformation through a Newton iteration scheme [12]. We investigate the behavior of the cell at triaxialities varying from 1 to 3. Such levels of triaxiality are representative of the hydrostatic constraint in uniaxial tension specimens and in the neighborhood of a blunting crack tip. The diameter and height of the unit cell in the undeformed state are  $D_0$  and  $H_0$ , respectively. The outer surfaces of the cell are free of shear traction and are forced to remain straight during deformation; the cell remains always axisymmetric with a diameter  $D$  and a height  $H$ . The macroscopic strains in response to the applied stresses are  $E_{11} = \ln(D/D_0)$  and  $E_{33} = \ln(H/H_0)$ , and the macroscopic effective strain is  $E_e = |E_{33} - E_{11}|$ . We solve the boundary value problem for the calculation of the hydrogen, stress, and deformation fields in the matrix surrounding the void numerically by using the general purpose finite element program ABAQUS with a “user subroutine” (UMAT) incorporating the material model described in Section 2. Due to symmetry, we analyze only the first quadrant of the unit cell (Fig. 1).

### 4. Numerical results

We used material data relevant to the A533B nuclear reactor pressure vessel steel:  $\sigma_0 = 400$  MPa, Young's modulus  $E = 200$  GPa, Poisson's ratio  $\nu = 0.3$ , and hardening exponent  $N = 0.1$ . The molar volume of iron is  $7.116 \times 10^{-6} \text{ m}^3/\text{mol}$  and therefore  $N_L = 8.46 \times 10^{28}$  solvent lattice atoms/ $\text{m}^3$ . The hydrogen partial molar volume in solution is  $2.0 \times 10^{-6} \text{ m}^3/\text{mol}$ . The parameters  $\alpha$  and  $\beta$  used in the definitions of the trapping and NLS concentrations were both taken equal to 1. We assumed the trap density  $N_T$  to increase with plastic straining  $\varepsilon^p$  according to the experimental results of Kumnick and Johnson [23] and we obtained the function  $N_T(\varepsilon^p)$  by interpolating

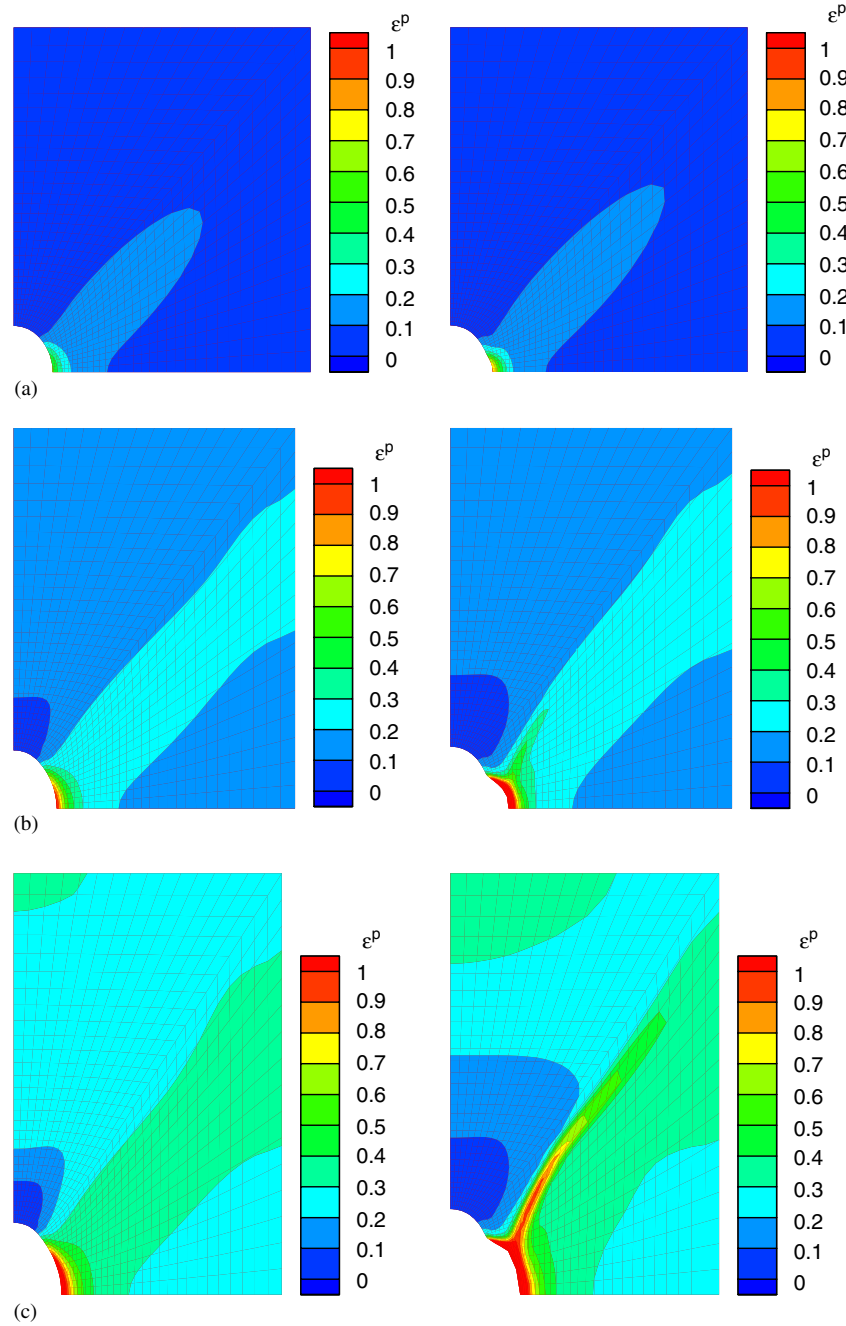


Fig. 2. Local effective plastic strain distribution at stress triaxiality  $T = 1$  and various levels of macroscopic effective strain  $E_e = |E_{33} - E_{11}|$ . The left column is for the hydrogen-free material and the right column is for the material at an initial NILS concentration of  $2.4634 \times 10^{-8}$  hydrogen atoms per solvent atom. The void volume fraction before deformation is 0.001. (a) Macroscopic effective strain  $E_e = 0.1$ ; (b) macroscopic effective strain  $E_e = 0.2$ ; (c) macroscopic effective strain  $E_e = 0.3$ .

the experimental data. We set the trap binding energy equal to 60 kJ/mol [23]. For the softening parameters  $\xi$  and  $\eta$ , we assumed to be equal to 0.99 and 0.5, respectively. A 0.99 value for  $\xi$  is associated with 1% reduction of the initial yield stress at the initial concentration of hydrogen  $c_L^0$  in NILS before the application of the load, and a 0.5 value for  $\eta$  denotes a maximum allowed reduction of 50% in the initial yield stress at all stages of straining. For the stress-free lattice, we assumed a

uniform hydrogen concentration  $C_L^0 = 2.084 \times 10^{21}$  atoms/m<sup>3</sup> ( $c_L^0 = 2.4634 \times 10^{-8}$  atoms per solvent atom) throughout in equilibrium with gas at 1 atm pressure. The unit cell dimensions  $D_0$  and  $H_0$  were both equal to 200  $\mu\text{m}$ , the initial void volume fraction was  $f_0 = 0.001$ , and the temperature of the system 300 K.

Figs. 2 and 3 show the effective plastic strain distribution at the unit cell both in the absence of hydrogen (left column) and



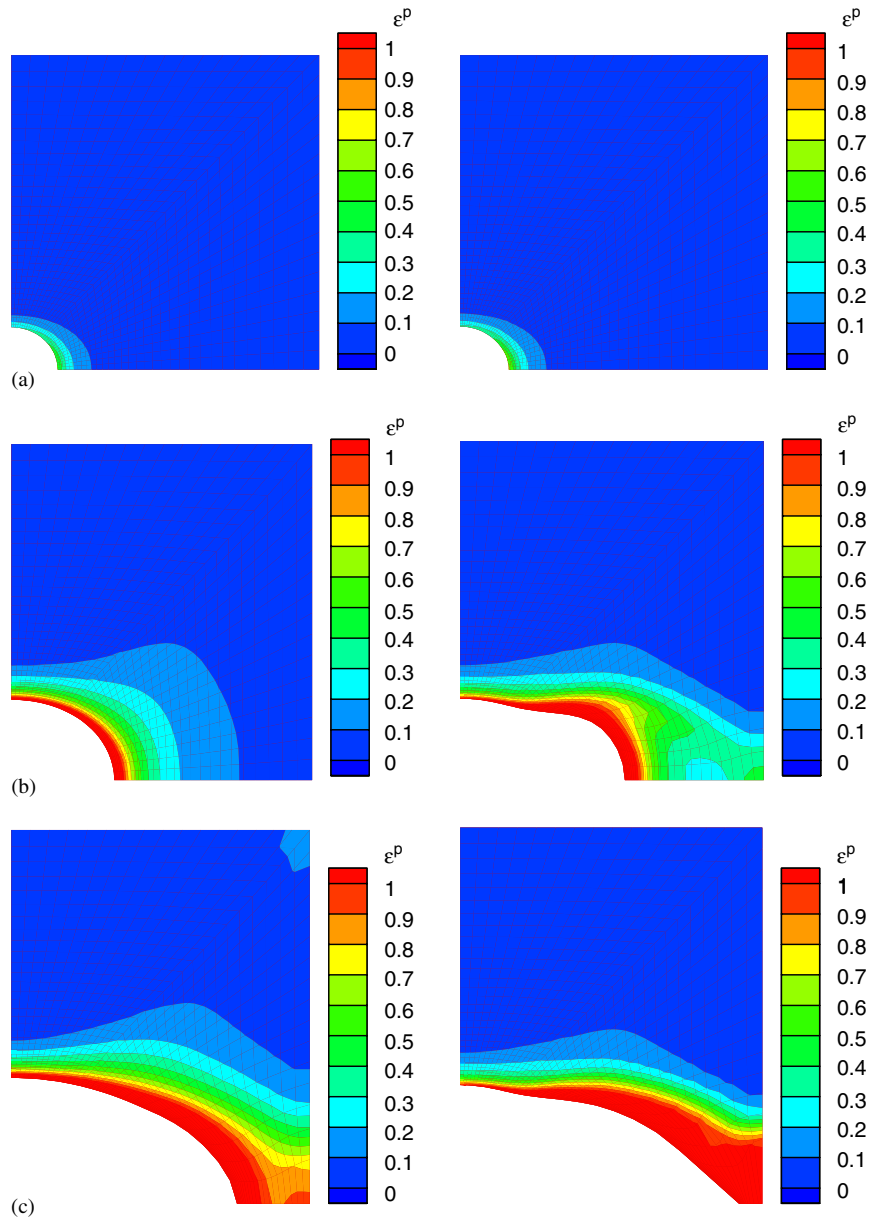


Fig. 3. Local effective plastic strain distribution at stress triaxiality  $T = 3$  and various levels of macroscopic effective strain  $E_e$ . The left column is for the hydrogen-free material and the right column is for the material at an initial NILS concentration of  $2.4634 \times 10^{-8}$  hydrogen atoms per solvent atom. The void volume fraction before deformation is 0.001. (a) Macroscopic effective strain  $E_e = 0.015$ ; (b) macroscopic effective strain  $E_e = 0.075$ ; (c) macroscopic effective strain  $E_e = 0.15$ .

in the presence of hydrogen (right column) when the applied stress triaxiality  $T$  equals 1 and 3, respectively. At triaxiality  $T = 1$ , hydrogen induces a localized shear band initiating at the void surface and propagating toward the interior bulk material. At triaxiality  $T = 3$ , hydrogen causes the void to grow into an oblate spheroid faster than in the absence of hydrogen. It is interesting that no localized shear deformation is observed at this high triaxiality of 3. Instead, the plastic deformation is confined close to the void surface and in the ligament between the voids. The normalized hydrogen concentrations  $c_L/c_L^0$  at NILS and  $c_T/c_L^0$  at trapping sites are shown in Fig. 4 at triaxiality 1 and in Fig. 5 at triaxiality 3. At  $T = 1$  and macroscopic

effective strain of 0.3, Fig. 4b shows that hydrogen accumulates preferentially in the narrow shear band in which severe plastic deformation takes place (see Fig. 2c) and close to the void surface in the ligament between the voids. On the other hand, at triaxiality  $T = 3$ , Fig. 5b shows that hydrogen accumulates in a narrow zone around the deformed void surface. It is clear from Figs. 4 and 5 that hydrogen predominantly resides at traps generated by plastic straining. Fig. 6 shows the distribution of the normalized yield stress  $\sigma_0(c)/\sigma_0$  at the unit cell. At triaxiality  $T = 1$ , localized softening is observed within the shear band location (Fig. 2c) in accordance with the localized hydrogen accumulation (Fig. 4b). In contrast, at triaxiality

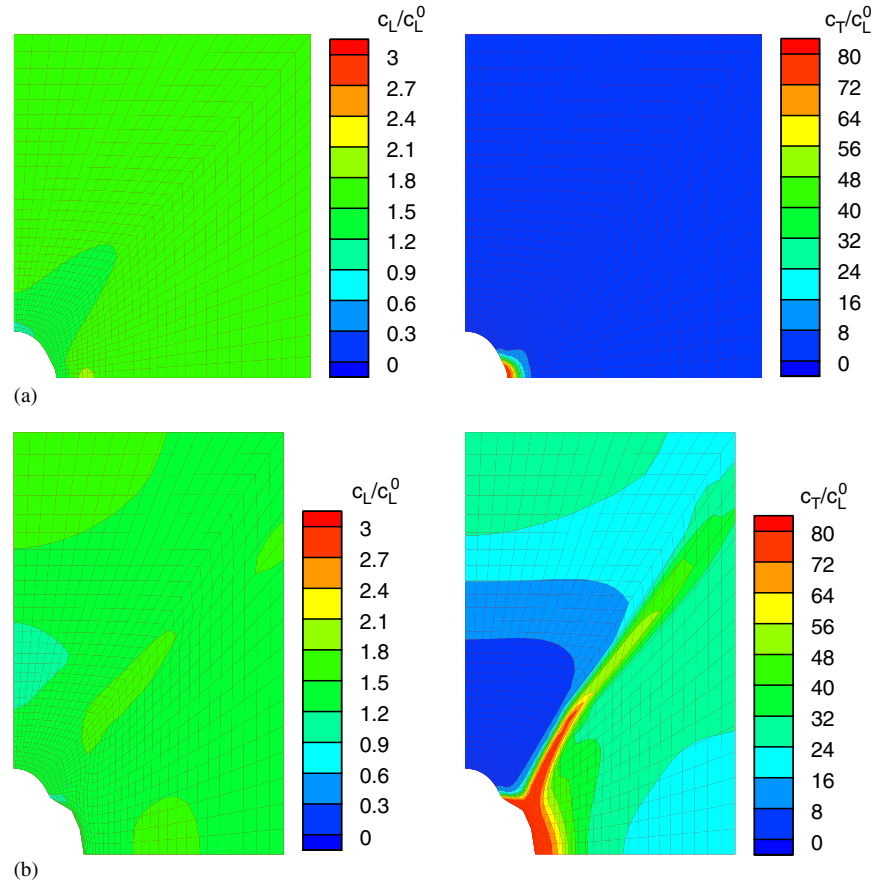


Fig. 4. Distribution of the normalized hydrogen concentration  $c_L/c_L^0$  at NILS (left column) and  $c_T/c_L^0$  at trapping sites (right column) at stress triaxiality  $T = 1$  and two levels of macroscopic effective strain  $E_e$ . (a) Macroscopic effective strain  $E_e = 0.1$ ; (b) macroscopic effective strain  $E_e = 0.3$ .

$T = 3$ , substantial softening is the case around the void and at the ligament between the voids (Figs. 3b and 5b). At both triaxialities, softening is associated with trapped hydrogen. Fig. 7 shows the normalized void volume fraction as a function of the macroscopic effective strain at various levels of triaxiality. Significantly, hydrogen increases the rate of growth as the macroscopic strain increases and reduces the macroscopic strain at which coalescence occurs.

Investigating void growth in a niobium system with a void volume fraction  $f_0 = 0.0013$ , Liang et al. [12] found almost a negligible hydrogen effect on void growth and coalescence at triaxialities  $T = 2$  and 3, but a marked effect at triaxiality  $T = 1$  (see their Fig. 3b). Thus, whereas the hydrogen effect on void growth and coalescence in the niobium system is mainly observed at small triaxialities, in iron systems it affects both growth and coalescence at all triaxialities as shown by Fig. 7.

## 5. Discussion

Figs. 2, 3, and 7 show that as straining increases hydrogen progressively accentuates void growth and accelerates the coalescence stage at all levels of stress triaxialities. In particular, the effect on void coalescence is more pronounced at small tri-

axialities, e.g.  $T = 1$ . Since hydrogen solutes in iron and steel accumulate at much larger quantities at trapping sites [14,15] than at NILS, the hydrogen softening effect on void growth and coalescence becomes stronger at larger plastic strains at which hydrogen tends to get trapped at microstructural defects. It is noted that the density of traps, e.g. dislocations, increases with plastic deformation. Indeed, at large macroscopic strains, namely  $E_e = 0.3$  under triaxiality  $T = 1$  and  $E_e = 0.075$  under triaxiality  $T = 3$ , hydrogen resides predominantly at trapping sites (see Figs. 4b and 5b) in the neighborhood of the void surface.

At high-constraint configurations, e.g., at triaxiality  $T = 3$ , as in the neighborhood of *U*-notched bend specimens or notched tensile specimens, the present numerical simulations indicate a strong hydrogen effect on void coalescence [1,2,5]. Fig. 3 shows clearly that as straining increases, hydrogen enhances the void growth rate and accelerates the coalescence stage. It is well known that void growth is strongly dependent on stress triaxiality [22,24,25]. As shown from Figs. 2a and 3b, with both cells strained at macroscopic effective strain  $E_e \leq 0.1$ , the void grows larger at triaxiality  $T = 3$  than at  $T = 1$  in the absence of hydrogen. Such larger void growth is associated with larger plastic straining, which in the presence of hydrogen brings about larger hydrogen accumulations at trapping sites causing more extensive material softening, which in turn brings

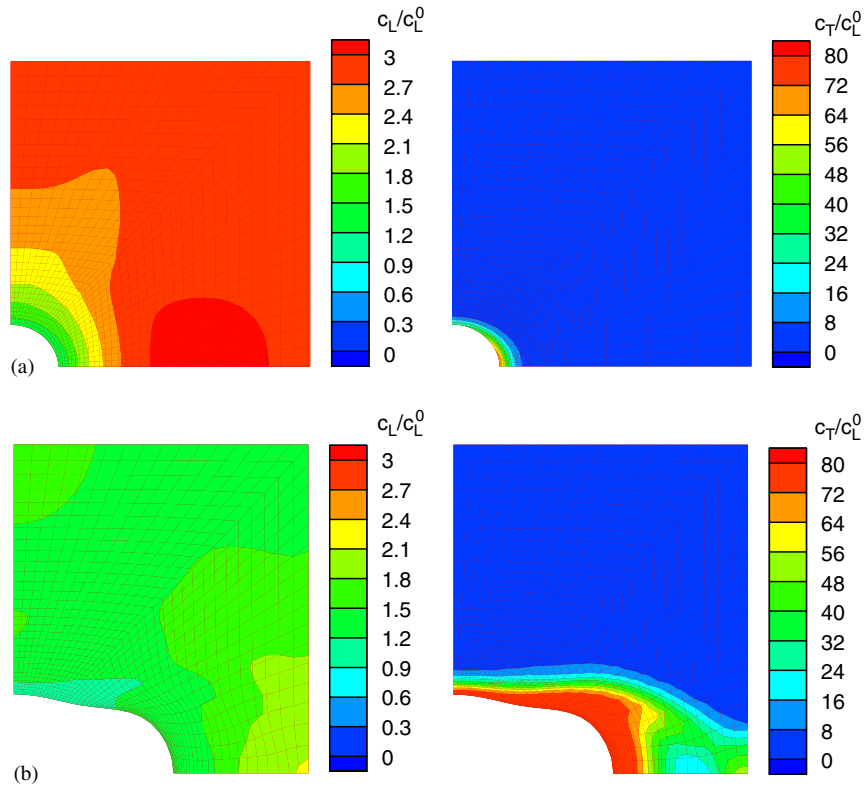


Fig. 5. Distribution of the normalized hydrogen concentration  $c_L/c_L^0$  at NILS (left column) and  $c_T/c_L^0$  at trapping sites (right column) at stress triaxiality  $T = 3$  and two levels of macroscopic effective strain  $E_e$ . (a) Macroscopic effective strain  $E_e = 0.015$ ; (b) macroscopic effective strain  $E_e = 0.075$ .

about the coalescence stage at lower macroscopic strains. Thus, at large triaxialities, e.g.  $T = 3$ , the synergistic effect of triaxiality and hydrogen-induced softening promotes substantial void growth even at low macroscopic strains ( $E_e = 0.075$ , see Figs. 3b and 7).

Acceleration of void coalescence has been observed to be the case in the failure of specimens strained in uniaxial tension [5–10]. At triaxiality  $T = 1$ , Fig. 2c shows that hydrogen-induced material softening causes the deformation around a void to concentrate in a localized shear band emanating from the void surface. No such intense shear band is observed in the absence of hydrogen (Fig. 2c). Thus, if hydrogen-induced failure occurs at low triaxialities, which in uniaxial tension may be the case in the absence of substantial specimen necking, it is facilitated by localized shear bands emanating from the void surfaces at  $45^\circ$ . Park and Thompson [9] observed that hydrogen-assisted ductile fracture in cylindrical specimens of spheroidized 1520 steel is caused by enhanced shear localization in the matrix ligaments between the voids and in the presence of some hydrogen-induced reduction-of-area loss, though not substantial.

At triaxiality  $T = 1$ , hydrogen accumulates inside the band of intense shear emanating from the void surface (Fig. 4b). Notably, the surrounding area is depleted of hydrogen. Further, no similar localized shear band was observed in the simulations of Liang et al. [12] in the niobium system under the same triaxiality of 1. The difference in the plastic response

between the two systems at  $T = 1$  can be explained by the fact that (i) softening in the work of Liang et al. was characterized by  $\eta = 0.9$  whereas  $\eta = 0.5$  in the present study. Thus, hydrogen-induced softening is modeled as more intense in the present study than in the work of Liang et al. at the same hydrogen concentration; (ii) softening in niobium is effectively a result of NILS hydrogen whereas softening in iron is a result of trapped hydrogen. In the niobium system, softening tends to be more uniform throughout the matrix as it is the NILS hydrogen that dominates the hydrogen populations. The gradients of NILS populations which follow the hydrostatic stress distribution are not as strong as those of the trapping site concentrations which follow the plastic strain distribution. Moreover, the dominant trapping site populations in the iron systems develop at the void surface—where they initiate localized shear—whereas the dominant NILS populations in the niobium system develop at the center of the inter-void ligament.

Such continued accumulation of hydrogen inside shear bands is a key issue in the HELP mechanism for hydrogen embrittlement. Hydrogen by triggering a localized shear band continues to promote the localization of deformation by continuing to accumulate preferentially in the band. Thus, macroscopic failure can take place easily through localized shear sustained by hydrogen. In agreement with this discussion, Fig. 6 shows that hydrogen-induced material softening when expressed in terms of the reduction in the yield stress follows the corresponding

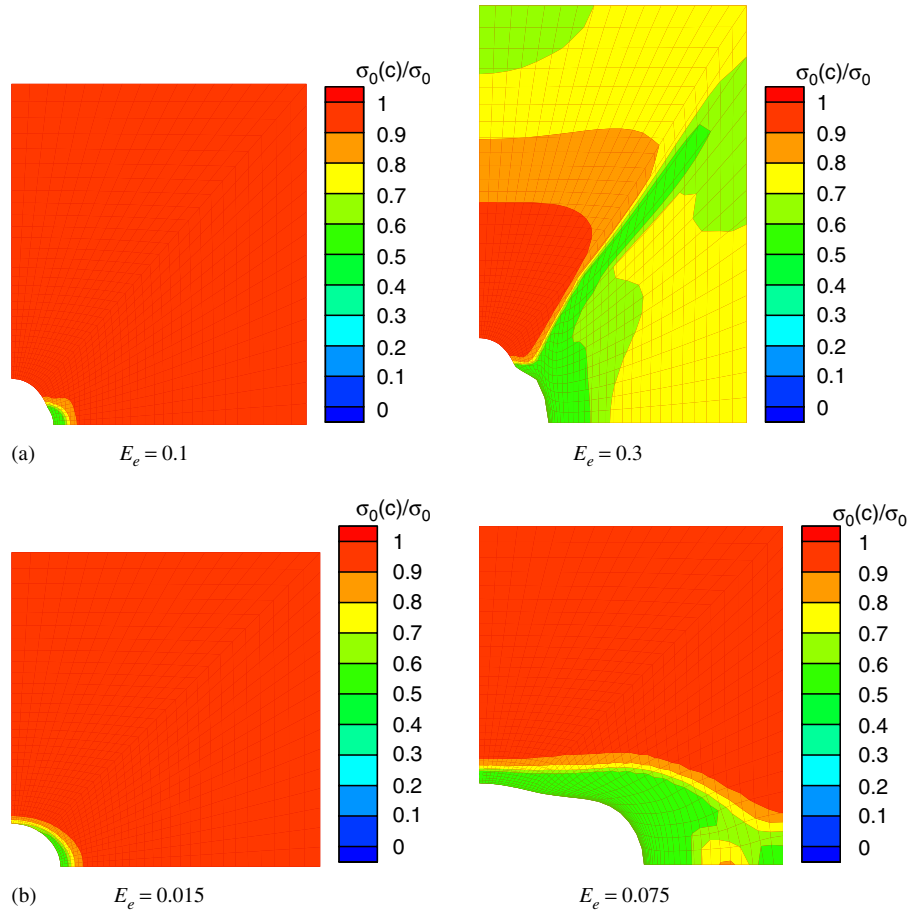


Fig. 6. Distribution of the normalized yield stress  $\sigma_0(c)/\sigma_0$  in the presence of hydrogen. The parameter  $\sigma_0$  denotes the yield stress in the absence of hydrogen. (a) Stress triaxiality  $T = 1$ ; (b) stress triaxiality  $T = 3$ .

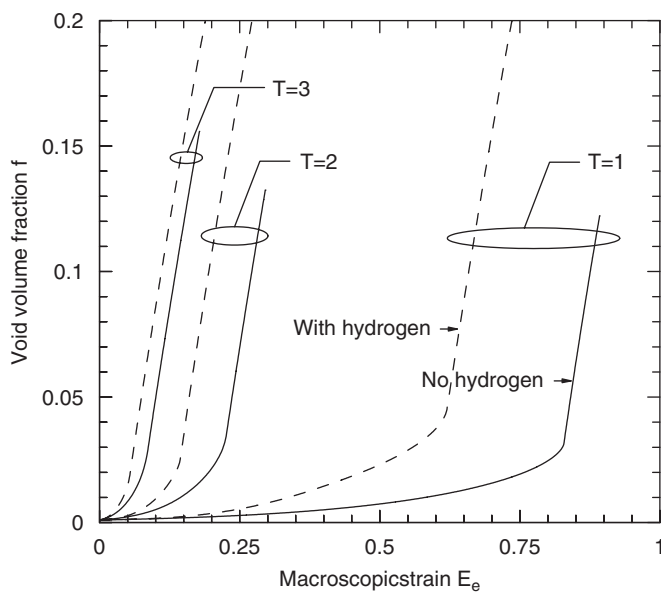


Fig. 7. Plot of the void volume fraction  $f$  versus the macroscopic effective strain  $E_e$  at various levels of stress triaxiality  $T$ . The initial void volume fraction is  $f_0 = 0.001$ .

hydrogen accumulation at all magnitudes of macroscopic strain and applied stress triaxiality.

## 6. Conclusion

The effect of hydrogen on void growth and coalescence in A533B nuclear reactor pressure vessel steel has been studied at a unit cell containing a spherical void under axisymmetric stress conditions and while hydrogen is in equilibrium with local hydrostatic stress and plastic strain. Hydrogen was found to promote void growth and coalescence at all levels of triaxiality and applied macroscopic strain. At triaxiality equal to 3, the synergistic effect of high stress triaxiality and hydrogen-induced softening enhances void growth. The effect of hydrogen on void coalescence increases as the triaxiality decreases. Remarkably, at triaxiality equal to 1, the calculations reveal that hydrogen assists in the formation of a localized shear band emanating from the void surface. The present results can be used to investigate the conditions for the onset and propagation of a crack by void growth and coalescence in the presence of hydrogen as shown in Fig. 1. Such a study is the subject of a subsequent investigation.



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