

## Answer Key of Tutorial 8

1. (i)

$$\text{Eigenvectors for } \lambda = -2: \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}$$

$$\text{Eigenvectors for } \lambda = 4: \begin{pmatrix} -1 \\ 0 \\ 1 \end{pmatrix}$$

$$\text{Eigenvectors for } \lambda = 6: \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$$

(ii)

$$\text{Eigenvectors for } \lambda = 0.38563\dots: \begin{pmatrix} -0.68591\dots \\ 0.03577\dots \\ 1 \end{pmatrix}$$

$$\text{Eigenvectors for } \lambda = -1.31255\dots: \begin{pmatrix} 1.36207\dots \\ -1.83731\dots \\ 1 \end{pmatrix}$$

$$\text{Eigenvectors for } \lambda = 5.92692\dots: \begin{pmatrix} 1.54606\dots \\ 1.69043\dots \\ 1 \end{pmatrix}$$

(iii)

$$\text{Eigenvectors for } \lambda = -0.88202\dots: \begin{pmatrix} -0.44101\dots \\ 0.15302\dots \\ 1 \end{pmatrix}$$

$$\text{Eigenvectors for } \lambda = 1.77653\dots: \begin{pmatrix} 0.88826\dots \\ -3.97503\dots \\ 1 \end{pmatrix}$$

$$\text{Eigenvectors for } \lambda = 5.10548\dots: \begin{pmatrix} 2.55274\dots \\ 0.82201\dots \\ 1 \end{pmatrix}$$

2. Not in T2 exam

3. Not in T2 exam

5. (i)  $\lambda \in D_1 \cup D_2 \cup D_3$  where  $D_1 = \{z \in \mathbb{C} : |z - 1| \leq 5.88\}$ ,  $D_2 = \{z \in \mathbb{C} : |z + 5| \leq 10.388\}$ ,  $D_3 = \{z \in \mathbb{C} : |z - 6| \leq 7.245\}$  and  $\mathbb{C}$  is complex plane.

(ii)  $\lambda \in D_1 \cup D_2 \cup D_3$  where  $D_1 = \{z \in \mathbb{C} : |z - 1| \leq 3\}$ ,  $D_2 = \{z \in \mathbb{C} : |z + 5| \leq 4\}$ ,  $D_3 = \{z \in \mathbb{C} : |z - 4| \leq 5\}$  and  $\mathbb{C}$  is complex plane.