

$$\textcircled{1} I_L = I_0 e^{g L} \Rightarrow 1.1 = 1 e^{g(0.1)} \Rightarrow \underline{g = 0.95 \text{ m}^{-1}}$$

$$\textcircled{2} g_{th} \geq \alpha_{eff} + \frac{1}{2L} \ln\left(\frac{1}{R_1 R_2}\right)$$

$$\Rightarrow g_{th} = 0 + \frac{1}{2 \times 0.5} \ln\left(\frac{1}{0.9 \times 0.9}\right) = \underline{0.210 \text{ m}^{-1}}$$

$$\textcircled{3} \Delta \nu = 10^8 \text{ Hz} \Rightarrow g(\omega) = \frac{1}{\Delta \omega} = \frac{1}{2\pi \Delta \nu} = 1.59 \times 10^{-9} \text{ s}$$

$$\approx \underline{1.6 \text{ ns}}$$

$$\textcircled{4} g_{th} = \alpha_{eff} + \frac{1}{2L} \ln\left(\frac{1}{R_1 R_2}\right)$$

$$\Rightarrow g_{th} = \left[ 0.1 + \frac{1}{2 \times 0.1} \ln\left(\frac{1}{0.96 \times 0.96}\right) \right] = \underline{0.508 \text{ m}^{-1}}$$

$$\therefore \text{cavity lifetime } t_c = \frac{n_0}{c g_{th}} = \frac{1.78}{3 \times 10^8 \times 0.508}$$

$$\Rightarrow t_c = 1.168 \times 10^{-8} \text{ s} \approx \underline{11.7 \text{ ns}}$$

$$\textcircled{5} g_{th} = \alpha_{eff} + \frac{1}{2L} \ln\left(\frac{1}{R_1 R_2}\right)$$

$$\Rightarrow 0.02 = 0 + \frac{1}{2 \times 1} \ln\left(\frac{1}{1 \times R_2}\right) \Rightarrow 0.04 = \ln\left(\frac{1}{R_2}\right)$$

$$\Rightarrow R_2 = 0.961 \approx \underline{96\%}$$

$$\textcircled{6} g_{th} = \alpha_{eff} + \frac{1}{2L} \ln\left(\frac{1}{R_1 R_2}\right) = 0 + \frac{1}{2 \times 0.2} \ln\left(\frac{1}{0.98 \times 0.98}\right)$$

$$= \underline{0.101 \text{ m}^{-1}}$$

$$\therefore t_c = \frac{n_0}{c g_{th}} = \frac{1}{3 \times 10^8 \times 0.101} = 3.3 \times 10^{-8} \text{ s} \approx \underline{33 \text{ ns}}$$

$$\textcircled{7} g_{th} = \alpha_{eff} + \frac{1}{2L} \ln\left(\frac{1}{R_1 R_2}\right) = 30 + \frac{1}{(2 \times 600 \times 10^{-4})} \ln\left(\frac{1}{0.3 \times 0.3}\right)$$

$$\Rightarrow g_{th} = 30 + \frac{1}{0.12} \ln\left(\frac{1}{0.09}\right) = \underline{50 \text{ cm}^{-1}}$$

$\textcircled{8}$  To be theoretically discussed.