




1. (a) Can a charge free region be associated with the electric potential $V = x^2 + y^2 + z^2$ (volts)?
 (b) Using uncertainty principle, establish that absolute zero temperature is not reachable.
 (c) Write the normalized wave function of a particle confined in a box of dimension L_x , L_y and L_z .
 (d) Which of the radiation X-rays or visible light is used to determine the crystal structure of crystalline solid. Why?
 (e) Calculate $\langle x \rangle$ for the following wave function $\psi_1 = \sqrt{\frac{2}{L}} \sin \frac{\pi x}{L}$ for $-\frac{L}{2} \leq x \leq \frac{L}{2}$ (5×1)
2. (a) A long cylinder carries a uniform charge density ρ_0 . Calculate the electric field everywhere.
 (b) The pressure exerted by EM radiation on a perfect absorber is 35.4 N/m^2 . Calculate the amplitude of electric and magnetic field. (3+2)
3. (a) Two Carnot engines A and B are operated in series. The first one A, receives heat at 800K and rejects heat to reservoir at temperature T . The second engine B receives the heat rejected by the first engine and in turn rejects heat to a reservoir at 200K . Calculate the temperature T when (i) the work outputs of the two engines are equal and (ii) the efficiencies of the two engines are equal.
 (b) A step index fiber has a core refractive index 1.466 , cladding refractive index 1.46 . If the operating wavelength of the rays is $0.85 \mu\text{m}$, calculate the cut-off parameter and the number of modes which the fiber will support. The diameter of the core is $50 \mu\text{m}$. (3+2)
4. (a) Sketch the wave function and probability density of linear harmonic oscillator as a function of x for $n=0$ and $n=1$. Also show graphically that the quantum probability density approaches the classical probability density for $n=10$.
 (b) Calculate the probability of finding the particle between $0.45L$ and $0.55L$ trapped in one dimensional box of width L . (3+2)
5. (a) Find the tunnelling probability (T) in fusing two protons at 10^7 K (Nuclear fusion), assuming Coulombic repulsion between two protons forms a square barrier of width $10 \times 10^{-15} \text{ m}$.
 (b) Calculate the $\langle K.E. \rangle$ in ground state of a particle confined in 1D box of width L . (3+2)
6. Calculate the c/a ratio and the volume of hcp unit cell. Magnesium has hcp structure. Radius of the atom is 0.1605 nm . Calculate the density. Given atomic mass of $\text{Mg} = 24.3 \text{ gm/mol}$. (5)
7. (a) Derive the expression for the inter-planer spacing between two parallel planes with Miller indices $(h \ k \ l)$ and show that for the cubical lattice it is given by $\frac{a}{\sqrt{h^2 + k^2 + l^2}}$.  JIT SIMPLIFIED
 In a crystal, a lattice plane cuts intercepts of a , $b/2$ and $3c$ along crystallographic axes. Calculate miller indices of the plane and draw a neat diagram showing the plane.
 (b) Atoms A and B are 0.5nm apart, atom A has ionization energy 5eV , and an atom B has an electron affinity of 4 eV . What is the energy required to transfer an electron from A to B? (3+2)

Constants: mass of electron = $9.1 \times 10^{-31} \text{ kg}$, mass of proton = $1.67 \times 10^{-27} \text{ kg}$, $h = 6.63 \times 10^{-34} \text{ Js}$, $K_B = 1.38 \times 10^{-23} \text{ J/K}$, $N_A = 6.023 \times 10^{23} \text{ atoms/mol}$

