

Greedy graph colouring

→ Ensure usage of not more than $d+1$ colours where $d \Rightarrow$ max degree of any vertex in graph

Time Complexity : $O(V^2 + E)$
↓

As we have to check adjacency by list of the vertex v for v vertex to check availability of colour

Best Algorithm

Dsatur
↓

$O(V^2)$

Welsh-Powell
 $O(V^2)$

These are best algorithms in terms of no of ~~colours~~ colours used for the given graph

Shannon's theorem

↳

$$T(n) = T(k) + T(n-k) + O(n)$$

↓

Worst case

$$\text{if } k = n-1$$

$$\hookrightarrow O(n^2)$$

Best case

$$\text{if } k = \frac{n}{2}$$

$$\hookrightarrow O(n \log n)$$

Min Heap Concept is used

Huffman Encoding

- ↳ ~~Heap~~ Heapifying of n nodes $\Rightarrow O(n)$
- ↳ Extract Min Heap $\Rightarrow O(\log n) \times 2$
- ↳ Insert in heap $\Rightarrow O(\log n)$
- ↳ Traverse the Tree $\Rightarrow O(n)$

So, Time Complexity $\Rightarrow O(n \log n)$
↳ worst

Best $\rightarrow O(n) \rightarrow$ (if frequencies are already sorted)

N Queen problem

$$T(n) = n \times T(n-1) + O(n^2)$$

$$T(n) = n!$$

Rat in a Maze problem

$$\hookrightarrow O(2^{n^2})$$

↳ Using upper bound method.

M - Coloring Backtrack
 $\hookrightarrow O(m^v)$

\hookrightarrow If BFS method used instead of backtracking $O(V+E)$

Hamiltonian Path

$$T(N) = N \times T(N-1) + O(1)$$

$$\hookrightarrow T(N) = N!$$

Ford Fulkerson / Edmond Karp

$$\hookrightarrow O(\max flow \times E)$$

$$\hookrightarrow O(VE^2)$$

Kruskal

$$\hookrightarrow O(n^2)$$

Bridge problem $\Rightarrow O(n^2)$

Longest common subsequence $\Rightarrow O(n^2)$

Matrix Chain Multiplication $\Rightarrow O(n^3)$

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All pair shortest path

~~(~~Brute force~~)~~

(Floyd Warshall)

$\Rightarrow O(V^3)$

Longest Increasing
Subsequence

$\Rightarrow O(n^2)$

(\hookrightarrow)

But a better approach
is $O(n \log n)$