

Name _____

Enrollment No. _____

Jaypee Institute of Information Technology, NOIDA
End Term Examination, EVEN Semester 2022
B.Tech IV Sem

Course name: Digital Systems/ Introduction to Digital Systems
Course Code: 18B11EC213/15B11EC314

Maximum Time: 2 Hr
Maximum Marks: 35

After the completion of the course, students will be able to:

- CO1: Familiarize with the fundamentals of number systems, Boolean algebra and Boolean function minimization techniques.
- CO2: Analyze and design combinational circuits using logic gates.
- CO3: Analyze state diagram and design sequential logic circuits using flip flops.
- CO4: Understand the classification of signals and systems and learn basic signal operations and Fourier analysis.
- CO5: Understand various steps involved in digitization and transmissions of a signal.

Note: Attempt All Questions

Q.1. [CO1] Find the simplest SOP expression using K-map for the following function:

$$F(w, x, y, z) = \sum m(0, 1, 4, 6, 8, 9, 10, 12) + d(5, 7, 14)$$

Also find Essential Prime Implicants (EPI) for the above given function.

[4]

Q.2. [CO2] Design a BCD to Excess-3 (XS-3) code converter.

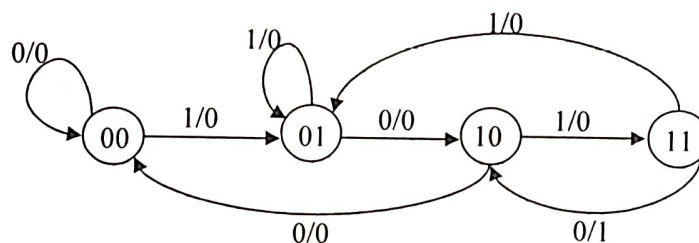
[4]

Q.3. [CO3] Explain the working of 4 bit ring counter using D flip flop and draw its timing diagram.

[3]

Q.4. [CO3] Implement the synchronous sequential circuit using D flip flop for the given state diagram.

[4]

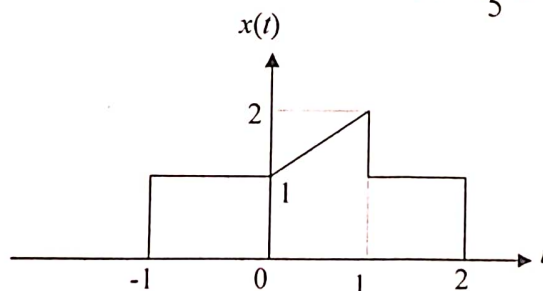


Q.5. [CO4] For the signal $x(t)$ as shown in below Figure, draw the graph of following signals:

(a) $x(-t + 2)$

(b) $x(\frac{3}{5}t)$

[3]



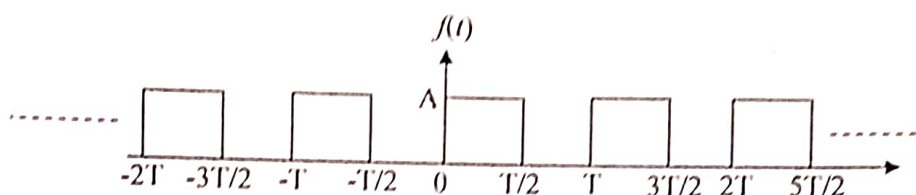
Q.6. [CO4] Determine whether the following signals are periodic or not? If periodic, determine the fundamental period.

(a) $\sin\left(\frac{2\pi}{3}n\right) + \cos\left(\frac{2\pi}{5}n\right)$ (b) $\sin(2t) + \cos(\sqrt{3}t)$ [3]

Q.7. [CO4] Check the causality and linearity properties of following system:

$$y(t) = x^2(t) + x(t-4)$$
 [2]

Q.8. [CO4] Find the complex Fourier series coefficient for $k = 0$ (DC component) for the given periodic waveform. [2]



Q.9. [CO4] Find the Fourier transform of the signal defined as:

$$x(t) = e^{-t} \sin(5t) u(t)$$
 [3]

Q.10. [CO5] State Sampling theorem and hence determine the Nyquist rate and Nyquist interval corresponding to each of the following signals:

(a) $m(t) = 1 + \cos(200\pi t) + \sin(400\pi t)$

(b) $m(t) = 10 \cos(40\pi t) \cos(300\pi t)$ [3]

Q.11. [CO5] For the binary sequence given as 10110, draw the output waveforms for the following modulation schemes and signalling formats:

(a) BASK

(b) BPSK

(c) Bipolar NRZ (AMI NRZ)

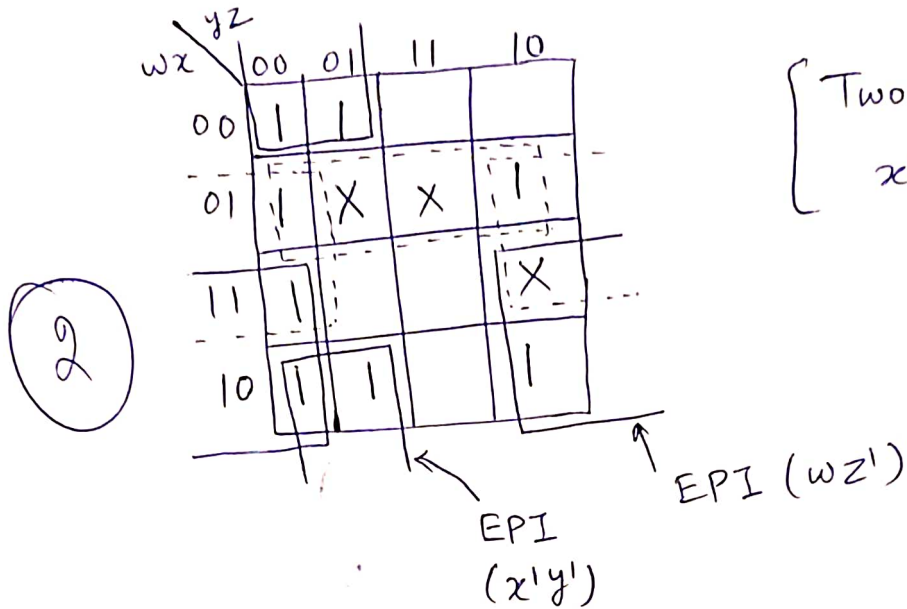
(d) Manchester (Split phase)

[4]

T3 Solution.

Sol. & $F(w, x, y, z) = \sum m(0, 1, 4, 6, 8, 9, 10, 12) + d(5, 7, 14)$

Q1



Two EPIs
x'y', wz'

(1)

Simplest form

$$F(w, x, y, z) = x'y' + wz' + xz'$$

or

$$F(w, x, y, z) = x'y' + wz' + w'x$$

(1)

BCD to XS-3 Code Converter

BCD Code				XS-3 Code			
A	B	C	D	W	X	Y	Z
0	0	0	0	0	0	1	1
0	0	0	1	0	1	0	0
0	0	1	0	0	1	0	1
0	0	1	1	0	1	1	0
0	1	0	0	0	1	1	1
0	1	0	1	1	0	0	0
0	1	1	0	1	0	0	1
0	1	1	1	1	0	1	0
1	0	0	0	1	0	1	1
1	0	0	1	1	1	0	0

Sol 2

Q2

1

AB \ CD	00	01	11	10
00				
01		1	1	1
11	X	X	X	X
10	1	1	X	X

1

$$W = A + BC + BD$$

AB \ CD	00	01	11	10
00		1	1	1
01	1			
11	X	X	X	X
10		1	X	X

1

$$X = B'C + B'D + BC'D'$$

AB \ CD	00	01	11	10
00	1		1	
01	1		1	
11	X	X	X	X
10	1		X	X

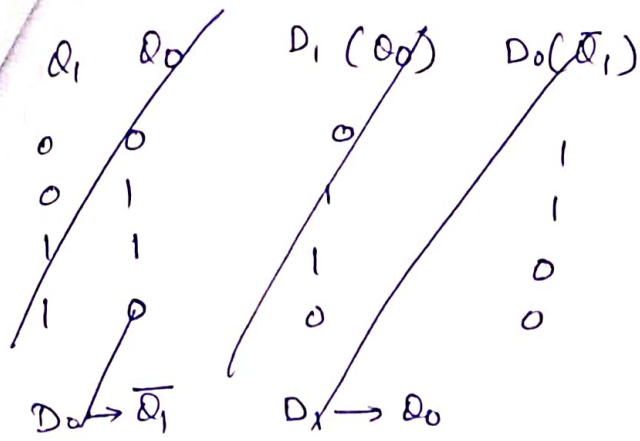
1

$$Y = CD + C'D'$$

AB \ CD	00	01	11	10
00	1			1
01	1			1
11	X	X	X	X
10	1		X	X

1

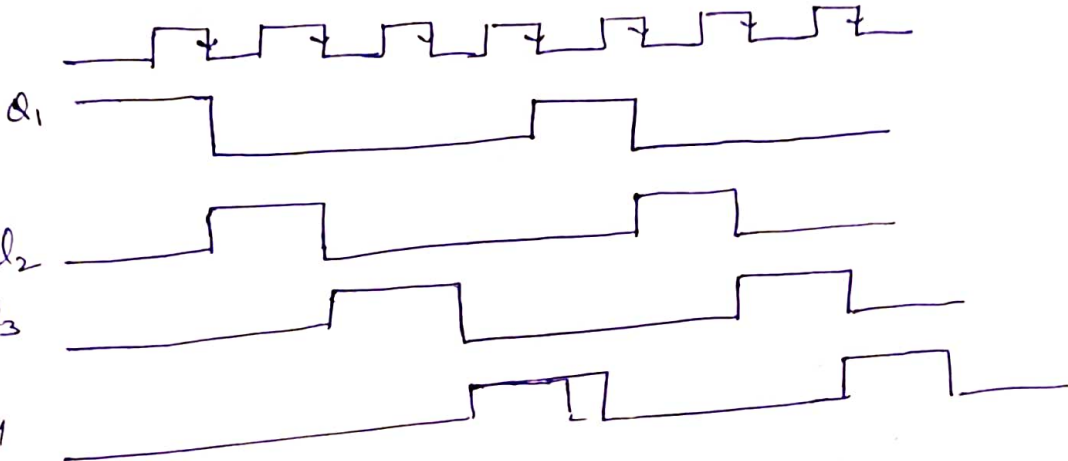
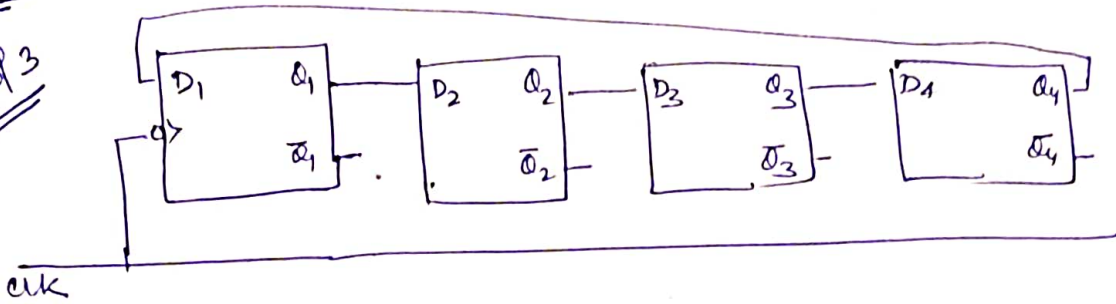
$$Z = D'$$



Q ~~3~~

Sol 3

1 Marks for working



1

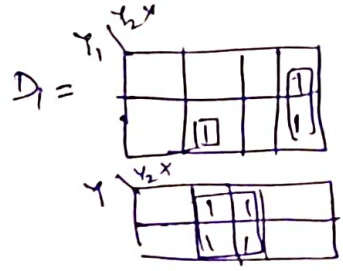
Sol 4 Transition and output table

Q4

PS (Y1, Y2)	NS (Y1, Y2)		O/P (Z)	
	X=0	X=1	X=0	X=1
A → 00	00	01	0	0
B → 01	10	01	0	0
C → 10	00	11	0	0
D → 11	10	01	1	0

1

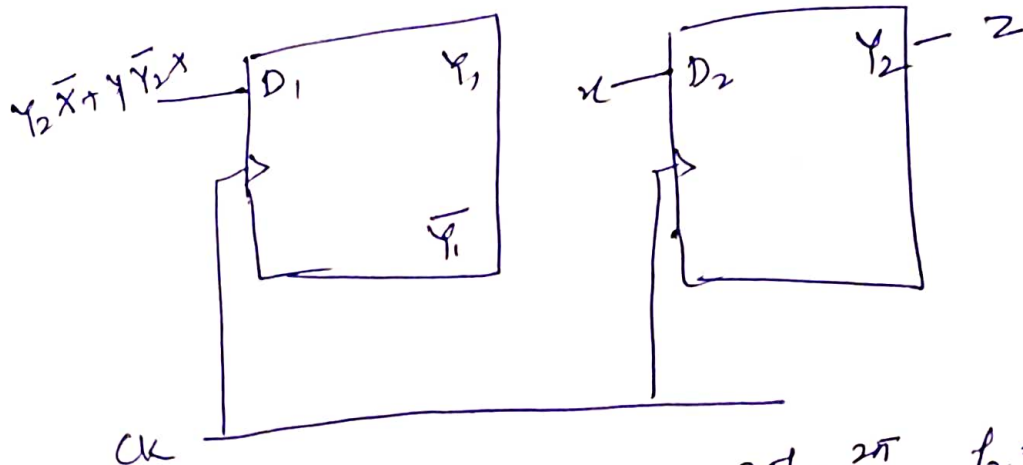
PS	I/P	NS	I/P of FF	O/P
Y1, Y2	X	Y1, Y2	D1, D2	Z
0 0	0	0 0	0 0	0
0 0	1	0 1	0 1	0
0 1	0	1 0	1 0	0
0 1	1	0 1	0 1	0
1 0	0	0 0	0 0	0
1 0	1	1 1	1 1	0
1 1	0	1 0	1 0	0
1 1	1	0 1	0 1	1



$$D_1 = Y_2 \bar{X} + Y_1 \bar{Y}_2 X$$

$$D_2 = X$$

1



1

Sol 6

(a) $2\pi f_1 = \frac{2\pi}{3}$ $f_1 = \frac{1}{3} = \frac{k_1}{N_1}$ $N_1 = 3$ $N_2 = 5$ $2\pi f_2 = \frac{2\pi}{5}$ $f_2 = \frac{1}{5} = \frac{k_2}{N_2}$ $\frac{N_1}{N_2} = \frac{3}{5}$

Periodic

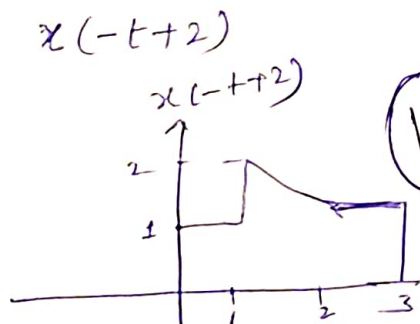
$LCM(3, 5) = 15$

1.5

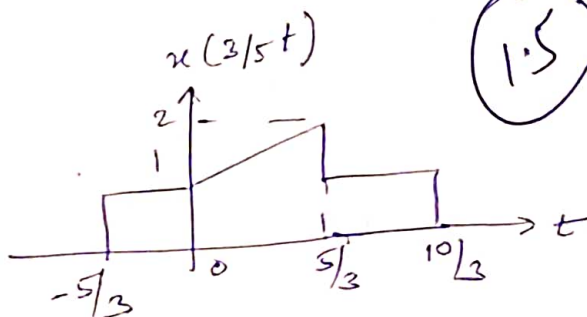
(b) Aperiodic $\omega_1 = 2$ $f_1 = \frac{1}{\pi}$ $T_1 = \pi$ $\omega_2 = \sqrt{3}$ $f_2 = \frac{\sqrt{3}}{2\pi}$ $T_2 = \frac{2\pi}{\sqrt{3}}$

$\frac{T_1}{T_2} = \frac{\sqrt{3}}{2}$ irrational - Aperiodic

1.5



1.5



1.5

$$y(t) = x^2(t) + x(t-4)$$

$$t = -2 \quad y(-2) = x^2(-2) + x(-6)$$

$$t = 0 \quad y(0) = x^2(0) + x(-4)$$

$$t = 2 \quad y(2) = x^2(2) + x(-2)$$

Causal system (1)
Presents Past

Non linear system (1)

$$C_0 = \frac{1}{T} \int_0^T x(t) dt = \frac{1}{T} \int_0^{T/2} A dt = \frac{A}{T} T \int_0^{T/2} = \frac{A}{T} \times \frac{T}{2} = \frac{A}{2}$$

$$C_n = \frac{1}{T} \int_0^T x(t) e^{-jn\omega_0 t} dt = \frac{1}{T} \int_0^{T/2} A e^{-jn(2\pi/T)t} dt$$

$$= \frac{A}{T} \left[\frac{e^{-jn(2\pi/T)t}}{-jn(2\pi/T)} \right]_0^{T/2} = -\frac{A}{jn2\pi} [e^{-jn\pi} - 1]$$

$$= \frac{A}{jn2\pi} [1 - e^{-jn\pi}] = \frac{A}{jn2\pi} [1 - (-1)^n]$$

$$C_n = \begin{cases} 0 & \text{for even } n \\ A/jn\pi & \text{for odd } n \end{cases}$$

$$x(t) = e^{-t} \sin 5t u(t)$$

$$e^{-t} \left(\frac{e^{j5t} - e^{-j5t}}{2j} \right) u(t)$$

$$= \frac{1}{2j} \int_{-\infty}^{\infty} [(e^{-t} (e^{j5t} - e^{-j5t}) u(t))] e^{-j\omega t} dt$$

$$= \frac{1}{2j} \left[\frac{1}{1+j(\omega-5)} - \frac{1}{1+j(\omega+5)} \right]$$

$$= \frac{5}{(1+j\omega)^2 + 5^2}$$

Q10: - (a) $f_1 = 100 \text{ Hz}$ $f_2 = 200 \text{ Hz}$

$$f_n = 2 \times 200 \text{ Hz} = 400 \text{ Hz}$$

$$\text{Interval} = \frac{1}{400 \text{ Hz}} = 2.5 \text{ ms}$$

1.5

(b) $\omega_{m_1} = 40\pi$ $\omega_{m_2} = 300\pi$

$$f_{m_0} = \frac{340}{2} = 170 \text{ Hz}$$

$$2f_m = 340 \text{ Hz}$$

$$f_n = \frac{1}{340} \text{ sec} =$$

1.5

12
t.

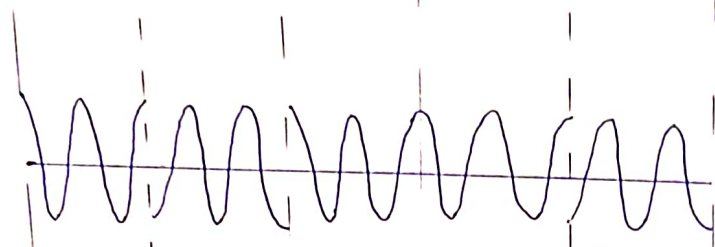
1 0 1 1 0

BASK



①

BPSK



①

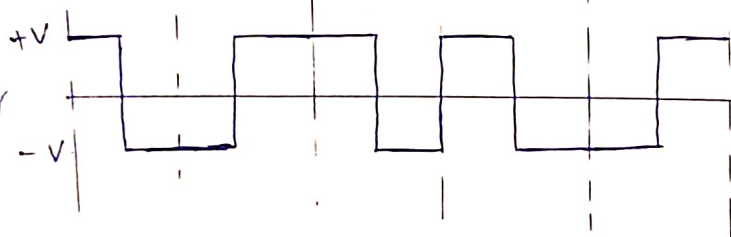
+V

AMI
NRZ



①

Manchester



①