

Tutorial Sheet – Odd Semester 2022

15B11CI212 Theoretical Foundations of Computer Science

Tutorial 2

Introduction to Discrete Mathematics and Set Theory

Ques 1: How many numbers below 100 are divisible by 2,3, or 5?

Ques 2. Suppose, there are 1000 students who are taking admission in the university in the academic year 2022-2023. All these students are enrolled in a Math or an English course. 400 students are taking Maths and English, 600 students are taking English.

- a) How many are taking maths course?
- b) How many are taking a math course but not and an English course?

Ques 3. Out of 30 students in class,15 take an TFCS course, 8 take a AI course and 6 take DBMS course. It is known that 3 students take all the three courses. Show that 7 or more students take none of the courses.

Ques 4: Let $A = \{1, 2, 3, 4, 5\}$ and $B = \{0, 3, 6\}$. Find

- a) $A \cup B$.
- b) $A \cap B$.
- c) $A - B$.
- d) $B - A$.

Ques 5: Let $A = \{0, 2, 4, 6, 8, 10\}$, $B = \{0, 1, 2, 3, 4, 5, 6\}$, and $C = \{4, 5, 6, 7, 8, 9, 10\}$. Find

- a) $A \cap B \cap C$.
- b) $A \cup B \cup C$.
- c) $(A \cup B) \cap C$.
- d) $(A \cap B) \cup C$.

Ques 6: Prove that $A \cap (B - C) \subset A - (B \cap C)$

Ques 7: Show that if A, B, and C are sets, then

$$(A \cap B \cap C)^c = A^c \cup B^c \cup C^c$$

Ques 8: Show that if A and B are sets, then

- a) $A - B = A \cap B^c$.
- b) $(A \cap B) \cup (A \cap B^c) = A$.

Ques 9: List all partitions of the following sets:

- (a) $\{a\}$
- (b) $\{a, b\}$
- (c) $\{a, b, c\}$

Ques 10: The bit strings for the sets $\{1,2,3,4,5\}$ and $\{1,3,5,7,9\}$ are 11 1110 0000 and 10 1010 1010, respectively. Use bit strings to find the union and intersection of these sets.