## Tutorial Sheet – EVEN 2021 15B11Cl411 – Algorithms and Problem Solving

## Instructions

- 1. Tutorials in APS course would majorly be doubt removal sessions.
- 2. Students are advised to come prepared in tutorial by revising the lectures of that particular week so that doubts related to topics covered in that week are resolved.
- 3. Few practice questions will also be posted as Tutorial Sheet on your Google Classrooms. You can try solving them before the scheduled tutorial and discuss the doubts.
- 4. As tutorials will be purely problem solving based, always join the tutorial with a notebook and pen with you.
- 5. Whatever questions are discussed in tutorial, you are supposed to submit them on your respective classrooms every week.

## Week 3 (1st February to 6th February 2021) Recurrence Relations

- 1. Solve the following recurrences using Master method
  - a) T(n) = T(2n/3) + 1
  - b)  $T(n) = 3T(n/4) + n \log n$
  - c)  $T(n) = 4T(n/2) + n^2$
- 2. Solve the following recurrence Relation using Recursion tree method
  - a) T(n) = 4T(n/2) + n
  - b) T(n) = T(n/2) + T(n/4) + T(n/8) + n
- 3. Solve the following recurrences using Iterative method
  - a)  $T(n) = 8T(n/2) + n^2$ , (T(1) = 1)
  - b) T(n) = n.T(n-1) if n>1
    - =1 if  $n \le 1$
  - c) T(n) = T(n/2) + c if n > 1= 1 if n=1
- 4. Consider a situation where swap operation is very costly. Which of the following sorting algorithms should be preferred so that the number of swap operations are minimized in general?
  - a) Merge Sort b) Selection Sort c) Insertion Sort d) Heap Sort
- 5. Running merge sort on an array of size n which is already sorted is
  - a) O(n) b) O(nlogn) c) O(n<sup>2</sup>) d) None
- 6. For merging two sorted lists of size m and n into sorted list of size m+n, we require comparisons of
  - a) O(m) b) O(n) c) O(m+n) d)  $O(\log m + \log n)$