an we do any random experiment then we find lot of act come. A variable which sepersent this outcome is called <u>Random Variable</u>, whereas a function or onle which assigns a time function to every outcome of a random experiment is called random process. Mean of random process [X(t)] M(x) = E {X(x)} Autocorrelation Roc (t_1,t_2) = $R(t_1)t_2$) = $E\{X(t_1)|X(t_2)\}$ Autoc ovariance Coultist2) = C(t1,t2) = $E[\{X(t_1) - M(t_1)\} \{X(t_2) - M(t_2)\}]$ = $\mathcal{R}(\pm_1,\pm_2)$ - $\mathcal{M}(\pm_1)\mathcal{M}(\pm_2)$ Correlation coefficient $e_{101}(\pm_{11}\pm_{2}) = e(\pm_{11}\pm_{2})$ $= \frac{C(t_1, t_2)}{\sqrt{C(t_1, t_1)} \times C(t_2 \times t_2)}$ Cross - correlation of 2 processes {X(t)} &{Y(t)} (jointly) Ray $(\pm_1,\pm_2) = E\left\{X(\pm_1) Y(\pm_2)\right\}$ Cross - Covariance = $C_{ny}(t_1,t_2) = R_{ny}(t_1,t_2) - A_{n}(t_1) M_y(t_2)$ Cross - correlation coefficient lny (tists) Cny (t1, t2)

(2)

(2)

(2)

(2)

(3) Strongly stationary Process: (SSS Process) (strict sense stationary process) If SSS then densities of X(1) & X(1+h) are the same i.e. f(x,t) = f(x,t+h) =) f(n,t) is independent of t. = E {X(x)} is independent of time $E\{x(t)\}$ = Constt.

```
Wide sense stationary process (WSS);-
      E[X(±)] = Constt
        R(t_1, t_2) = function of (t_1-t_2)
  (X(±)) red not be SSS.
0-21- 5= {(1,1) (1,2) (1,3) (1,4) (1,5) (1,6)
             (3,1) (2,2) (2,3) (2,4) (2,5) (2,6)
             (311) (312) (313) (314) (315) (316)
              (411) (4,2) (4,3) (4,4) (4,5) (4,6)
             (511) (512) (513) (514) (515) (5,6)
             (611) (612) (613) (614) (615) [616)}
    prime sum
                2- (1,1)
                    3 - (1,2)(2,1)
                     5 - (1,4) (2,3) (3,2) (4,1)
                     7 - (1,6) (2,5) (3,4) (4,3) (5,2) (6,1)
                     11 - (5,6) (6,5)
      f(\beta) = \frac{15}{36} = \frac{5}{12}
                                  E(XLt) = Enibi
      P(\text{ not prime sum}) = \frac{21}{3L} = \frac{7}{12}
    E\{x(t)\} = \{x(t) = x \in \mathbb{Z}, x \in \mathbb{Z} + \{x(t) = 2t+1\} = 2t+1\}
                 = 5 sinTt + 4 (2x+1)
  It depends upon + 10 it is not stationary.
0.3i \{X(t)\} = A cost + B sint
       with R.V A taking values 143 equal probability
   f R.V B taking values -1 +1 with Prob. 443
  E{X(L)) = E { A CONT+ B sint}
            = COSAt E(A) + SinAt E(B)
     E(A) = 1x\frac{1}{2} + \frac{1}{2}x3 = 2
```

$$\begin{split} & = \underbrace{E\{\lambda(k_1) | \chi(k_2)\}}_{\{L_1,L_2\}} : E\{\omega_1(\lambda L_1 + \gamma) + \cos(\lambda L_2 + \gamma)\}}_{\{L_2,L_2\}} \\ & = \underbrace{E}_{\{L_2,L_2\}}_{\{L_1,L_2\}} + \cos(\lambda L_1 + \gamma - \lambda L_2 - \gamma)\}}_{\{L_2,L_2\}} \\ & = \underbrace{E}_{\{L_2,L_2\}}_{\{L_1,L_2\}}_{\{L_2,L_2\}} + \cos(\lambda L_1 - L_2)\}}_{\{L_2,L_2\}}_{\{L_2,L_2\}} \\ & = \underbrace{E}_{\{L_2,L_2\}}_{\{L_1,L_2\}}_{\{L_2,L_2\}}_{\{L$$

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\frac{\text{Con}\left(\lambda(\pm_1-\pm_2)\right)-\text{Con}\left(\lambda(\pm_1\pm\pm_2)\right)}{\text{Un}_3}\cdot \pi^3
        Con(A(+1-+2)) - Con (A(+1+22))
               Not a function of titz
               So not WSS Process.
 (5)
           Auto Correlation Function Kny (ti,te)
         X(x) = A contx + Brindt
          Y(1) = BOALT - A sin/t
          A & B are uncorrelated r.v
                  E(AB) = E(A) E(B)
       E(A) = -4x_{\frac{1}{2}} + 4x_{\frac{1}{2}} = 0
          E(B) = 0
     1.e. E(AB) = 0
        E (A2) = 16x1 + 16x1 = (6 Van(A).
         E 1B2) = 16 = Var(8)
 Rnn(t1, t2) = E {X(t1) X(t2)} = E {(Acon At+ B sin At1)
                                           (A Cod Atat Boin Ata)}
       = ElA2) CONAti CONAtz + ELBA) sinAti CONAtz + ElAB)
                 CONALICON Atz + ELB2) sin Ati sin Atz
         = 16 (Cos At, CosAtz + Sin At, Sin Atz)
          = 16 CON ( )(t1-t2))
             E (Y(*) Y(*))
Kyy (t1, t2) =
         = E[ (BGA) At1 - Asin At1) (BGA) At2 - A sin At2)]
        = 16[ Cod At 1 €08 At2 + Sin At1 Sin At2]
           = 16 COA [A (t1-t2)]
```

```
Rany (dish) = E{x(+1) Y(12)}
       * [ ( ( NOW AL) + B AM AL) ( B COA AL2 - A Sin AL2) ]
     " I IAB CON ALI CONALO - 12 CONALI Sin Ata + B2 sin ALICA
                      - AB sinds, sind 2 }
     " ((B)) sin ALI CON Ala - EIA) CON ALI sin Ala
       * 16 [Cos sta Sin st, - Cosst, sin sta]
          = 16 sin (x(x,-20))
          Es a function of di-12
          .. Joinaly WSS.
(7)
          (XIII) in a WSS Process in T= +1-12
         RXX ($1, 12) = 44 e - 121-121/10 ] Rx ($1, 2) = E(XXXXXX)
       E(x2(t))= Rxx(t,t) = 4+e° = 5
E(XU) XUD)
        VW Lichec = E(x2(x1)) - (E(x(4)))
                    - 5-4 - 1
                                                E(x,2(x))
 2nd order moment of X(1)+X(2)+X(3)
     ie. E { x(1) + x(2) + x(3)}2
       = E { x2(1)} + E{x2(2)} + E {x2(3)} + 2E{x(1)} x(2)}
                         +2 E(X(2) X(3))+ 2 E(X(3) X(1))
          = 5+5+5+2[4+e-110+4+e-15+4+e-110]
         = 39+4e-110+2e-115 A
    : E {x11)x(2)} = R(1,2) = 4+e-1/10
```

```
Griven X(t) = Cos (3t+24)
        (6)
                       $ (2W) = E (e iwy)
           E[X(t)] = E[cos(3t+24)]
                 = E [C013t C0124 - sin 3t sin 24]
                 = C413x E(C4124) - sin3x E(sin24)
          Now find E(Cod24) = ?
                           E (sin 24) = ?
                 Φ(2ω) = E[eiwy] = E[cawy+isinwy]
                    E(COAWY) + i E(sinwY) = \phi(2w)
                · Put W=2
                $(4) = E (col24) ti E (sin24)
                     Put 9(4) =0
                  0 = E(G/124) + i F(Sin24)
                      7 E(CO124) =0, E(sin24)=0
        E(x(t)) = 0
               = E[XU1) X(t2)]
    R(t1, t2)
               = E [ COA (3t, +24) COA (3t2 +24)]
              =\frac{E}{2}\left[\cos\left(3t_{1}+2y+3t_{2}+2y\right)+\cos\left(3t_{1}+2y-3t_{2}-2y\right)\right]
                = E [(01) (3/41+22)+44) + (01) (3/21-22))
                 = \frac{1}{2} (0) 3(\frac{1}{2} - \frac{1}{2}) + \frac{1}{2} E [(0) 3(\frac{1}{2} + \frac{1}{2}) (0) 44 - \frac{1}{2} \index (\frac{1}{2} + \frac{1}{2})
         = f 60/3(41-22) + & E(60/44) CO/3(21+22)+ & E(sin 44)
                                                           sin3(titte)
           = 1 Cod3(t1-t2)+2x0 +2x0
            = 2 CON 3 (ti-te) is WSS PRECESS.
            $(2W) = E (60/204) HE (8inwy)
             φ(8) = E (C0/44) + i E (xin 44)
fut w=4
                     E(6,144)=0 E(sin44)=0
  · (8) =0
```