

Evolutionary Multi-Objective Optimization: A Parallel Computing Approach

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Outline

Background

- Multi-Objective Problem

Models

- DTLZ2
- XOMO
- POM3

Algorithms

- Evolutionary Algorithm
- Differential Evolution
- GALE: Geometric Active Learner

Parallelization Strategies

- The Island Model
- Master-Slave Model

Evaluation Metrics

- Evaluation
- Measures

Experimental Setup

Results

- Island Model
- Master-Slave Model

Future Work

- Feature Models
- Results: Feature Models
- Other Extensions:

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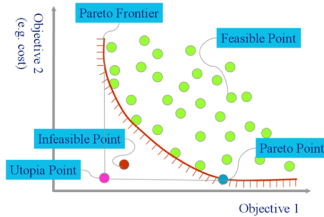


Figure: Sample Pareto Frontier

Multi-Objective Problem

- **Pareto Frontier** State of solutions which are equally good.

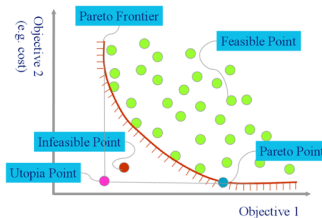


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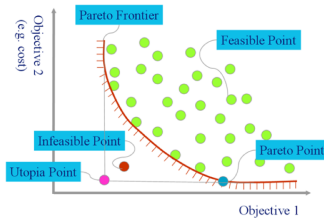


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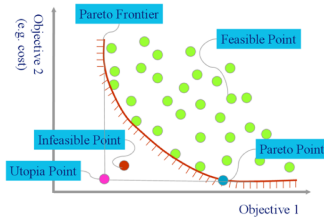


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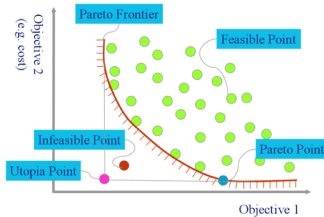


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- **Utopia Point** The ideal theoretical solution we would love to reach but practically its not possible

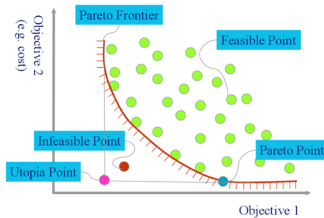


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- **Decisions** DTLZ-2 has 30 decisions where each decision ranges between 0 and 1.

$$0 \leq x_i \leq 1 \quad \text{where } i = 1, 2, 3, \dots, 30$$

- **Objectives** A point that lies on the Pareto frontier.

$$f_1(x) = (1 + g(x_M)) \cos(x_1 \pi / 2) \dots \cos(x_{M-1} \pi / 2)$$

$$f_2(x) = (1 + g(x_M)) \cos(x_1 \pi / 2) \dots \cos(x_{M-1} \pi / 2)$$

$$f_3(x) = (1 + g(x_M)) \sin(x_1 \pi / 2)$$

$$\text{where } g(x_M) = \sum_{x \in x_M} (x_i - 0.5)^2$$

- **Optimal Solution:** Ideal Decisions are $x_i = 0.5$ where $i = 1, 2, 3, \dots, 30$
Ideal objectives should satisfy the equation $\sum_{m=1}^3 f_m^2 = 1$

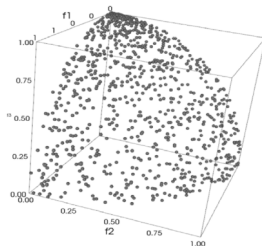


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- ▶ Monte Carlo Simulator modelling NASA's space program software.

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- ▶ 23 decisions - lines of code, storage, cyclometric complexity etc.
- ▶ 4 objectives all minimized
 - ▶ Total Developer **Effort**.
 - ▶ **Months** to complete project.
 - ▶ Total **Defects** in project.
 - ▶ **Risk** involved in project.

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- ▶ Teams select tasks as they appear in the scrum backlog.
- ▶ 9 decisions like size of project, project plan, team size etc.
- ▶ The model contains 4 objectives
 - ▶ Minimize **Cost**.
 - ▶ Maximize **Utility**.
 - ▶ Maximize **Completion Percentage**.
 - ▶ Minimize **Idle Time** for Developers.

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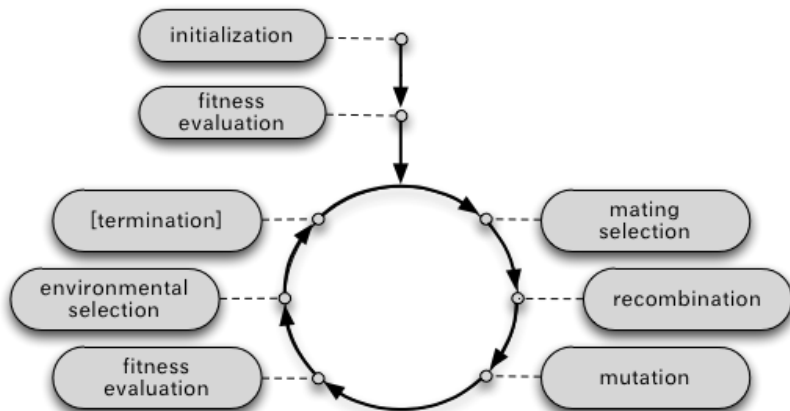
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- ▶ Iteratively approximates the shape of the Pareto Frontier
- ▶ Advantages:
 - ▶ Simple & Computationally Inexpensive.
 - ▶ High dimensional problems can be handled easily.
 - ▶ Solutions are very stable.

Pseudo-code 3.2 Differential Evolution

Begin

 Generate randomly an initial population of solutions.

 Calculate the fitness of the initial population.

 Repeat

 For each parent, select three solutions at random.

 Create one offspring using the DE operators.

 Do this a number of times equal to the population size.

 For each member of the next generation

 If offspring(x) is more fit than parent(x)

 Parent(x) is replaced.

 Until a stop condition is satisfied.

End.

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Geometric Active LEarner (GALE)

- ▶ Near linear time Multi-Objective Evolutionary Algorithm.

Geometric Active LEarner (GALE)

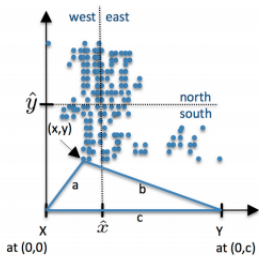
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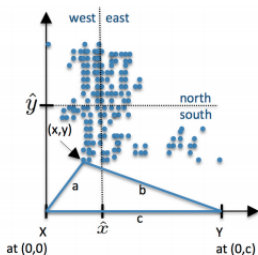
- ▶ Near linear time Multi-Objective Evolutionary Algorithm.
- ▶ Builds piecewise approximation to the best solutions of the pareto frontier.
- ▶ Based on WHERE which is a recursive clustering technique based on Dimensionality Reduction.
- ▶ Advantages:
 - ▶ Less Number of Computations.
 - ▶ Adept at handling problems that are **non-differentiable**, **non-linear**, **multi-dimensional** or **multi-constraint**.
 - ▶ Concise representation of problem space.

GALE - Algorithm

- Cluster data based on WHERE

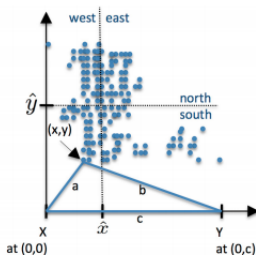


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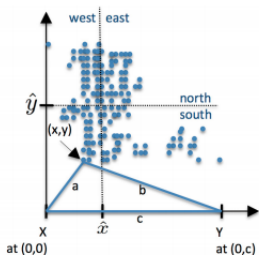
- Pick point **X** from the cluster. Then pick point **East** furthest from **X** and point **West** furthest from **East**. Let **c** be the distance between **East** and **West**.

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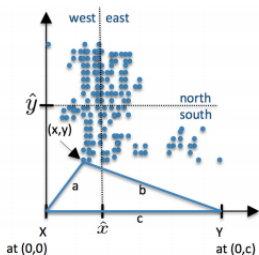
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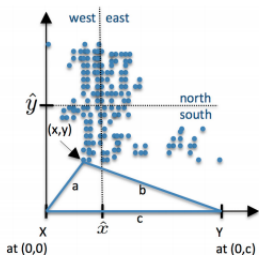
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$$x = (a^2 + c^2 - b^2)/2c$$

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- ▶ Cluster data based on WHERE



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- ▶ Repeat for **n** generations.

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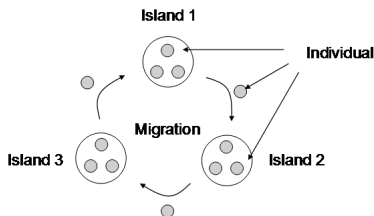
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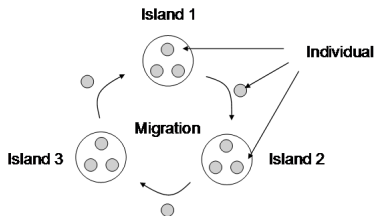
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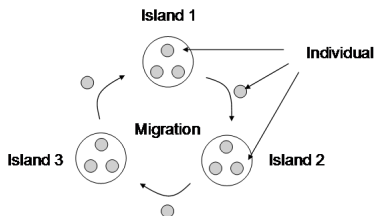
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- ▶ Evolve each sub-population independently.
- ▶ Aggregate the final population of each processor after the total number of generations.



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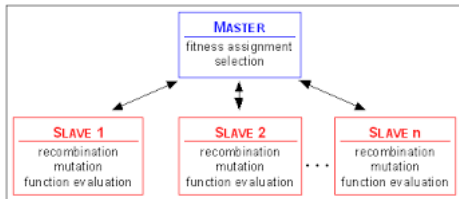
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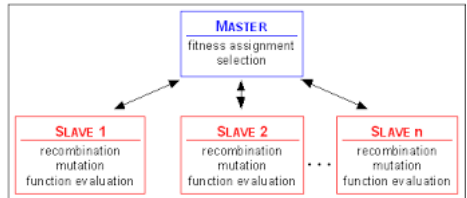
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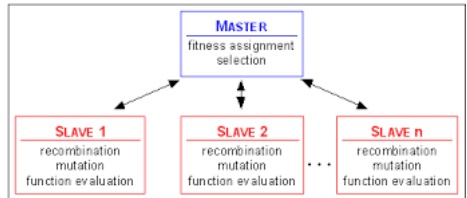
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- ▶ Slave performs mutation on each population subset and sends it to master for next generation.



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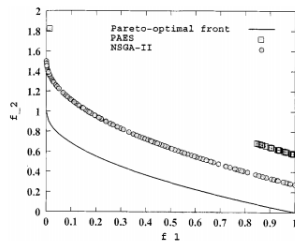
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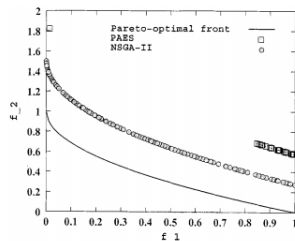
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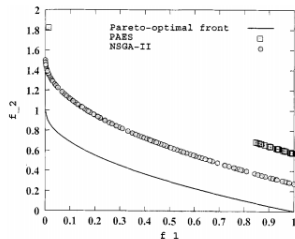
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 - ▶ Represents the HyperVolume between the obtained solutions and Pareto Frontier
- ▶ **Diversity:**
 - ▶ Spread of the proposed solutions.
 - ▶ Ideally the solutions should be well distributed across the Pareto Frontier



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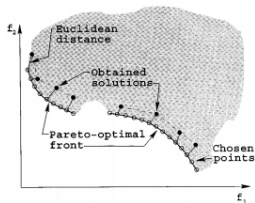
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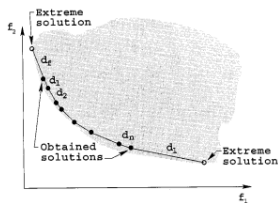
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Convergence:



- Find a set of H optimal solutions.
- For each solution, compute the minimum euclidian distance from each of the solutions to a point on the Pareto Frontier.
- The average of these distances represent convergence.

Diversity:



- d_i is the distance between consecutive solutions.
- \bar{d} is the mean of d_i
- d_f & d_l are distance between extreme and boundary solutions.

$$\Delta = \frac{d_f + d_l + \sum_{i=1}^{N-1} |d_i - \bar{d}|}{d_f + d_l + (N-1)\bar{d}}$$

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► HPC

- The henry2 shared memory linux cluster at NCSU.
- Up to 16 shared memory processor cores and up to 128GB of memory accessible through a dedicated queue.

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DTLZ-2(Island Model)

Rank	Optimizer	Median	IQR	Quartile Chart
1	DE(Parallel)	2.30×10^{-5}	2.74×10^{-6}	— —
1	DE(Serial)	2.36×10^{-5}	3.04×10^{-6}	— —
2	GALE(Serial)	5.49×10^{-4}	8.32×10^{-6}	— —
2	GALE(Parallel)	5.54×10^{-4}	2.21×10^{-5}	— —

Figure: Convergence of serial & parallel DE & GALE

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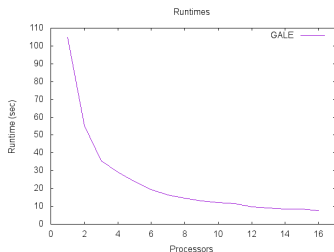
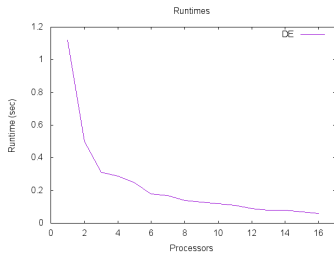
Figure: Convergence of serial & parallel DE & GALE

Rank	Optimizer	Median	IQR	Quartile Chart
1	GALE(Parallel)	0.416	0.070	— —
1	DE(Parallel)	0.417	0.049	— —
1	DE(Serial)	0.431	0.056	— —
1	GALE(Serial)	0.432	0.047	— —

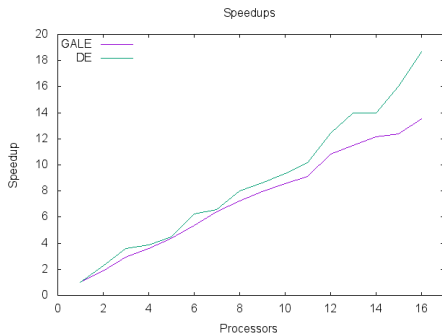
Figure: Diversity of serial & parallel DE & GALE

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Runtimes:

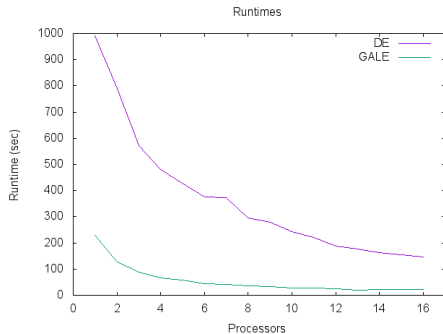


Speed Ups:

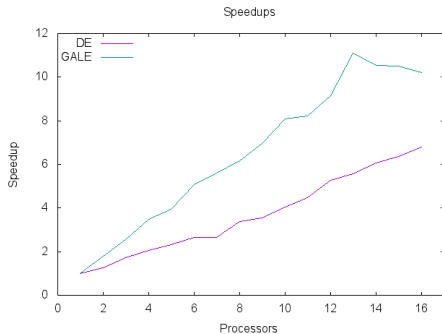


POM3(Island Model)

Runtimes:

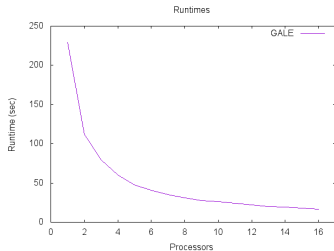
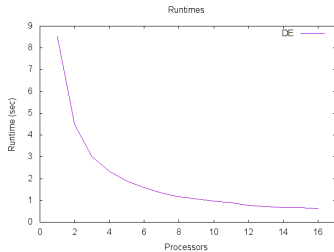


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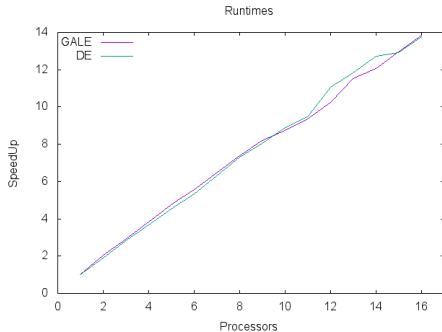


XOMO(Island Model)

Runtimes:



Speed Ups:



Outline

Background

- Multi-Objective Problem

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- DTLZ2
- XOMO
- POM3

Algorithms

- Evolutionary Algorithm
- Differential Evolution
- GALE: Geometric Active Learner

Parallelization Strategies

- The Island Model
- Master-Slave Model

Evaluation Metrics

- Evaluation
- Measures

Experimental Setup

Results

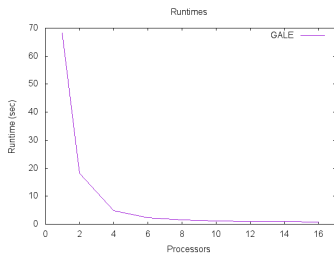
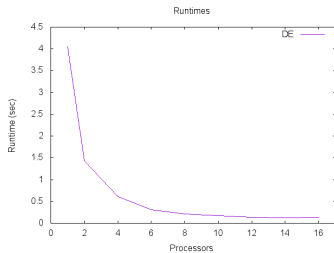
- Island Model
- **Master-Slave Model**

Future Work

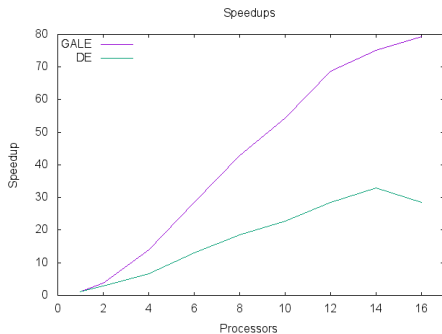
- Feature Models
- Results: Feature Models
- Other Extensions:

DTLZ-2(Master-Slave Model)

Runtimes:

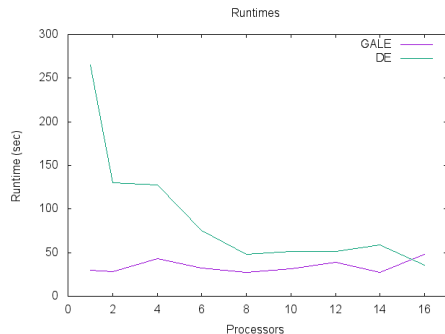


Speed Ups:

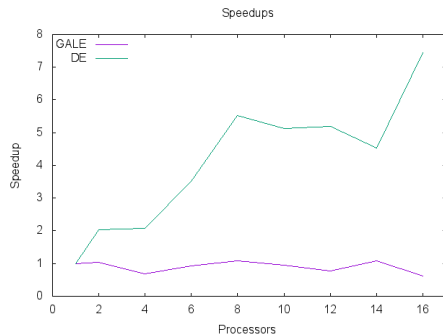


POM3(Master-Slave Model)

Runtimes:

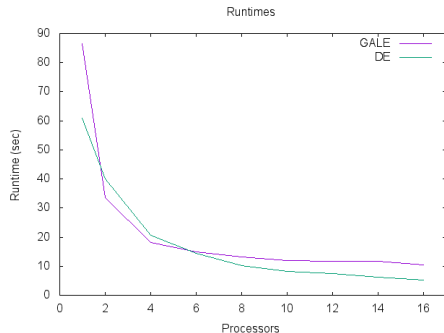


Speed Ups:

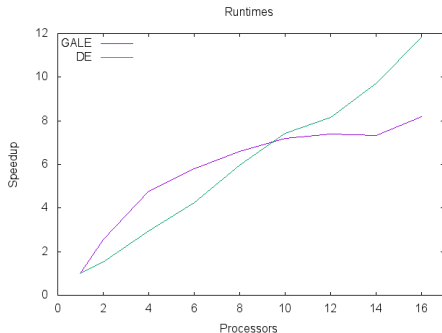


XOMO(Master-Slave Model)

Runtimes:



Speed Ups:



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- **Feature Models**
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- ▶ A **feature model** is a compact representation of all the products of the Software Product Line in terms of "features". Feature models are visually represented by means of feature diagrams.

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- ▶ Parent and Child features are categorized as
 - ▶ **Mandatory** child feature is required.
 - ▶ **Optional** child feature is optional.
 - ▶ **Or** at least one of the sub-features must be selected.
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- ▶ For our experiment we use the Emergency Response(ERS) feature model, which has **35 decisions** and **3 objectives**.

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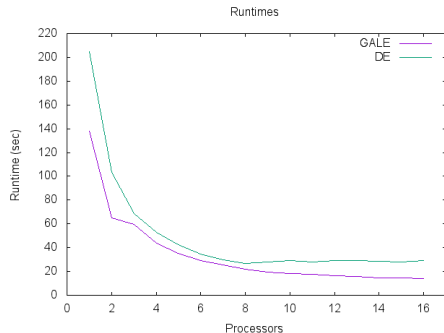
- Island Model
- Master-Slave Model

Future Work

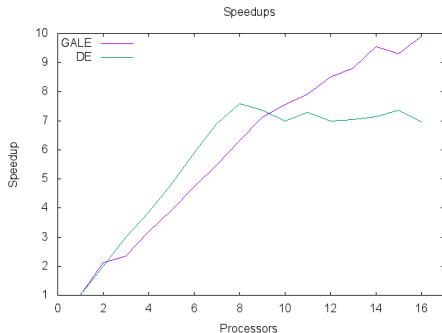
- Feature Models
- **Results: Feature Models**
- Other Extensions:

Emergency Response(Island Model)

Runtimes:



Speed Ups:



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- Other Extensions:

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- ▶ Mutation strategies for real world problems which are heavily constrained.

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- ▶ Extending these parallelization strategies for other Evolutionary algorithms like NSGA2, SPEA, IBEA etc
- ▶ Strategies for efficiently dividing the feature space for more efficient parallelization.

In Conclusion..

- ▶ Parallelization is effective for Multi Objective Evolutionary Algorithms.

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- ▶ Differential Evolution is preferred for Mathematical Problems.

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- ▶ Parallelization is effective for Multi Objective Evolutionary Algorithms.
- ▶ Differential Evolution is preferred for Mathematical Problems.
- ▶ GALE is preferred for Real-World Problems where model evaluation is expensive.