Section 2: Fitting PQI Models

PQIs of Interest

For these models, we will be looking at modeling the relationship between various PQIs at the HRR (hospital-referral region) level and Medicaid expansion status. For model selection, we started with the base model and added in potential covariates one by one from our list of potential covariates that did not have significant missingness in order to improve the model fit. We using likelihood ratio tests at each step to determine if adding the covariate was an appropriate addition to the model (checking the reduced model against the full model).

Exploratory analysis on covariates

First we quantify the missingness in the outcomes:

```
tbl <- hrr %>%
    select( `pqi05_copd_or_asthma_in_older_adults_admission_rate_(age_40-64)`, `pqi05_copd_or_asthma_in_o
    summarize_all(.funs = function(x) return(paste0(round(sum(is.na(x))/length(x), 3)*100, "%"))) %>% t()
names(tbl) <- c("% of Missing values")
kableExtra::kable(tbl)</pre>
```

	% of Missing values
pqi05_copd_or_asthma_in_older_adults_admission_rate_(age_40-64)	1.3%
pqi05_copd_or_asthma_in_older_adults_admission_rate_(age_65-74)	0.6%
pqi05_copd_or_asthma_in_older_adults_admission_rate_(age_75+)	0.6%
pqi07_hypertension_admission_rate_(age_<_65)	22.1%
pqi07_hypertension_admission_rate_(age_65-74)	17.9%
pqi07_hypertension_admission_rate_(age_75+)	6.8%
pqi08_chf_admission_rate_(age_65-74)	0.6%
pqi08_chf_admission_rate_(age_75+)	0.6%
pqi08_chf_admission_rate_(age_<_65)	1%

We have a very small percentage of missing data in our target covariates and 2 of the 3 PQIs. We believe PQI05 and PQI08 will be reasonable metrics to evaluate outpatient quality and it's relation to Medicaid expansion.

Check distribution of outcomes

```
hrr %>%
  filter(!is.na(expansion_status)) %>%
  select(year, `pqi05_copd_or_asthma_in_older_adults_admission_rate_(age_40-64)`, `pqi05_copd_or_asthma
  gather(age, pqi05, -year) %>%
  mutate(
    age = str_sub(age, -10)
) %>% ggplot(aes( x = pqi05)) + geom_histogram(color = "black") +
  scale_x_continuous(labels = scales::comma) +
  scale_y_continuous(labels = scales::comma) +
  xlab("PQI 05") +
  ylab("Count") +
```

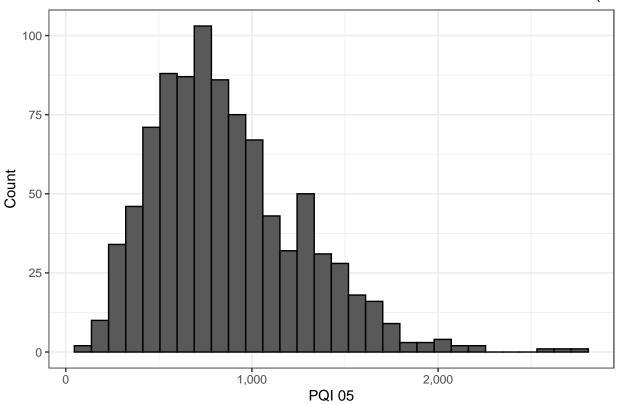
```
ggtitle("Distribution of PQI 05: COPD/Asthma in Older Adults Admissions Rate (2007-2018)") +
theme_bw()
```

PQI05

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.

Warning: Removed 2 rows containing non-finite values (stat_bin).

Distribution of PQI 05: COPD/Asthma in Older Adults Admissions Rate (20)



The distribution has a slight right skewe.

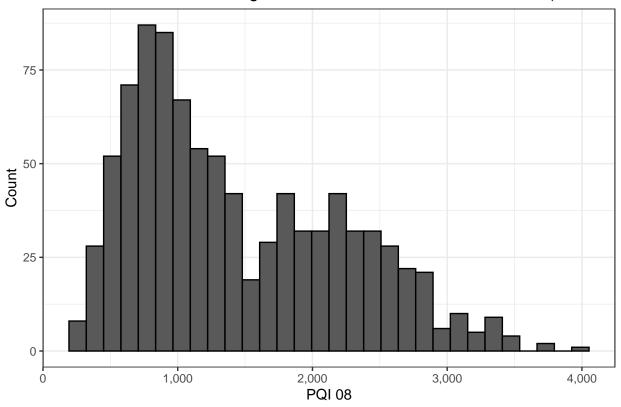
```
hrr %>%
  filter(!is.na(expansion_status)) %>%
  select(year, `pqi08_chf_admission_rate_(age_65-74)`, `pqi08_chf_admission_rate_(age_75+)`, `pqi08_chf
  gather(age, pqi08, -year) %>%
  mutate(
    age = str_sub(age, -10)
) %>% ggplot(aes( x = pqi08)) + geom_histogram(color = "black") +
    scale_x_continuous(labels = scales::comma) +
    scale_y_continuous(labels = scales::comma) +
    xlab("PQI 08") +
    ylab("Count") +
    ggtitle("Distribution of PQI 05: Congestive Heart Failure Admissions Rate (2007-2018)") +
    theme_bw()
```

PQI08

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.

Warning: Removed 1 rows containing non-finite values (stat_bin).

Distribution of PQI 05: Congestive Heart Failure Admissions Rate (2007–20



This outcome is almost bi-modally normally distributed (or just has a large right skew).

Model Fitting

PQI05 Since these variables are rates, we will want to use Poisson models. There may be overdispersion, so I'm going to start fitting a negative binomial and then check if the poisson version has overdispersion.

```
pqi05_data <- hrr %>%
  filter(!is.na(expansion_status)) %>%
  select(year, hrr, state, expansion_status, percent_male, percent_african_american, `percent_hispanic
  gather(age, pqi05, c("pqi05_copd_or_asthma_in_older_adults_admission_rate_(age_40-64)", "pqi05_copd_or_asthma_in_older_adults_admission_rate_(age_40-64)", "pqi05_copd_or_asthma_in_older_adults_admiss_
```

```
mod.nb_pqi05 <- MASS::glm.nb(pqi05 ~ `expansion_status` + offset(log(year)), data = pqi05_data)
summary(mod.nb_pqi05)</pre>
```

Start with the base model

```
##
## Coefficients:
##
                    Estimate Std. Error z value Pr(>|z|)
                                0.03805 -31.299 < 2e-16 ***
## (Intercept)
                    -1.19097
## expansion_status2  0.37661
                                0.04682
                                          8.044 8.72e-16 ***
                                          8.657 < 2e-16 ***
## expansion_status3 0.44497
                                0.05140
## expansion_status4 0.38405
                                0.04461
                                          8.609 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for Negative Binomial(5.1978) family taken to be 1)
##
##
      Null deviance: 1028.72 on 912 degrees of freedom
## Residual deviance: 942.22 on 909 degrees of freedom
     (2 observations deleted due to missingness)
## AIC: 13314
##
## Number of Fisher Scoring iterations: 1
##
##
##
                Theta: 5.198
##
            Std. Err.: 0.238
##
   2 x log-likelihood: -13304.003
```

We'll start adding in potential covariates and use likelihood ratio tests to determine if they should be added to the model.

```
mod.nb_pqi05_c1 <- MASS::glm.nb(pqi05 ~ `expansion_status` + percent_male + offset(log(year)), data = summary(mod.nb_pqi05_c1)</pre>
```

Percent Male

```
##
## Call:
## MASS::glm.nb(formula = pqi05 ~ expansion_status + percent_male +
       offset(log(year)), data = pqi05_data, init.theta = 5.485463972,
##
##
       link = log)
##
## Deviance Residuals:
      Min
                1Q
##
                     Median
                                   3Q
                                          Max
## -3.6564 -0.7822 -0.1444
                              0.5367
                                        3.0758
##
## Coefficients:
##
                    Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                     2.28027
                                0.46638 4.889 1.01e-06 ***
## expansion_status2 0.36410
                                          7.982 1.44e-15 ***
                                0.04562
                                          7.906 2.67e-15 ***
## expansion_status3 0.39757
                                0.05029
                                          8.417 < 2e-16 ***
## expansion_status4 0.36599
                                0.04348
                                1.01389 -7.471 7.94e-14 ***
## percent_male
                    -7.57507
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for Negative Binomial(5.4855) family taken to be 1)
```

```
##
##
      Null deviance: 1085.21 on 912 degrees of freedom
## Residual deviance: 940.77 on 908 degrees of freedom
     (2 observations deleted due to missingness)
## AIC: 13264
##
## Number of Fisher Scoring iterations: 1
##
##
##
                 Theta: 5.485
##
             Std. Err.: 0.251
##
   2 x log-likelihood: -13252.224
anova(mod.nb_pqi05, mod.nb_pqi05_c1)
## Likelihood ratio tests of Negative Binomial Models
## Response: pqi05
##
                                                             theta Resid. df
                                                   Model
                    expansion_status + offset(log(year)) 5.197820
## 2 expansion_status + percent_male + offset(log(year)) 5.485464
                                                                        908
        2 x log-lik.
                       Test
                               df LR stat.
                                                Pr(Chi)
## 1
           -13304.00
           -13252.22 1 vs 2
                                1 51.77882 6.211698e-13
By the LRT, we add percent male into the model.
mod.nb_pqi05_c2 <- MASS::glm.nb(pqi05 ~ `expansion_status` + percent_male + percent_african_american +
summary(mod.nb_pqi05_c2)
Percent African American
##
## Call:
## MASS::glm.nb(formula = pqi05 ~ expansion_status + percent_male +
      percent_african_american + offset(log(year)), data = pqi05_data,
       init.theta = 5.567089558, link = log)
##
##
## Deviance Residuals:
      Min
                 10
                     Median
                                   30
                                           Max
## -3.5948 -0.8405 -0.1495
                               0.5058
                                        3.1249
## Coefficients:
                            Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                             1.44437
                                        0.51041
                                                  2.830 0.004658 **
## expansion_status2
                             0.36225
                                        0.04529
                                                  7.998 1.27e-15 ***
## expansion_status3
                             0.38344
                                        0.05019
                                                  7.641 2.16e-14 ***
                                        0.04418
                                                  7.469 8.08e-14 ***
## expansion_status4
                             0.33001
                                                 -5.290 1.22e-07 ***
## percent_male
                            -5.83219
                                        1.10243
## percent_african_american 0.71312
                                        0.18361
                                                  3.884 0.000103 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

(Dispersion parameter for Negative Binomial(5.5671) family taken to be 1)

```
##
##
      Null deviance: 1101.23 on 912 degrees of freedom
## Residual deviance: 940.37 on 907 degrees of freedom
     (2 observations deleted due to missingness)
## AIC: 13252
##
## Number of Fisher Scoring iterations: 1
##
##
##
                 Theta: 5.567
##
             Std. Err.: 0.255
##
   2 x log-likelihood: -13238.041
anova(mod.nb_pqi05_c1, mod.nb_pqi05_c2)
## Likelihood ratio tests of Negative Binomial Models
## Response: pqi05
##
                                                                               Model
## 1
                                expansion_status + percent_male + offset(log(year))
## 2 expansion_status + percent_male + percent_african_american + offset(log(year))
        theta Resid. df
                           2 x log-lik.
                                          Test
                                                  df LR stat.
                                                                  Pr(Chi)
## 1 5.485464
                    908
                              -13252.22
## 2 5.567090
                    907
                              -13238.04 1 vs 2
                                                   1 14.18301 0.000165861
By the LRT, we add in percent African American into the model.
mod.nb_pqi05_c3 <- MASS::glm.nb(pqi05 ~ `expansion_status` + percent_male + percent_african_american +
summary(mod.nb_pqi05_c3)
Percent Hispanic
##
## Call:
## MASS::glm.nb(formula = pqi05 ~ expansion_status + percent_male +
      percent_african_american + percent_hispanic + offset(log(year)),
       data = pqi05_data, init.theta = 5.591227791, link = log)
##
##
## Deviance Residuals:
      Min
                 10
                     Median
                                   30
                                           Max
## -3.6061 -0.8156 -0.1640
                               0.5104
                                        3.1390
## Coefficients:
                            Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                             1.43579
                                        0.50938
                                                  2.819 0.004822 **
## expansion_status2
                             0.33745
                                        0.04647
                                                  7.262 3.82e-13 ***
## expansion_status3
                             0.35339
                                        0.05204
                                                  6.791 1.11e-11 ***
## expansion_status4
                             0.31299
                                        0.04475
                                                  6.994 2.67e-12 ***
## percent_male
                            -5.72874
                                        1.10156
                                                -5.201 1.99e-07 ***
## percent_african_american 0.69132
                                        0.18350
                                                  3.767 0.000165 ***
## percent_hispanic
                            -0.32974
                                        0.16179 -2.038 0.041540 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

##

```
## (Dispersion parameter for Negative Binomial(5.5912) family taken to be 1)
##
       Null deviance: 1105.97 on 912 degrees of freedom
##
## Residual deviance: 940.26 on 906 degrees of freedom
##
     (2 observations deleted due to missingness)
## AIC: 13250
## Number of Fisher Scoring iterations: 1
##
##
##
                 Theta: 5.591
                        0.256
##
             Std. Err.:
##
   2 x log-likelihood: -13233.900
anova(mod.nb_pqi05_c2, mod.nb_pqi05_c3)
## Likelihood ratio tests of Negative Binomial Models
## Response: pqi05
##
                                                                                                   Model
## 1
                        expansion_status + percent_male + percent_african_american + offset(log(year))
## 2 expansion_status + percent_male + percent_african_american + percent_hispanic + offset(log(year))
        theta Resid. df
                           2 x log-lik.
                                                   df LR stat.
                                          Test
## 1 5.567090
                    907
                              -13238.04
## 2 5.591228
                    906
                              -13233.90 1 vs 2
                                                    1 4.141419 0.04184607
By the LRT, we add in percent hispanic into the model.
Age category We add in the age category by which the data was originally split up.
mod.nb_pqi05_c4 <- MASS::glm.nb(pqi05 ~ `expansion_status` + percent_male + percent_african_american +
summary(mod.nb_pqi05_c4)
##
## Call:
## MASS::glm.nb(formula = pqi05 ~ expansion_status + percent_male +
       percent_african_american + percent_hispanic + age + offset(log(year)),
##
##
       data = pqi05_data, init.theta = 9.312393762, link = log)
##
## Deviance Residuals:
##
                 1Q
                                   30
       Min
                      Median
                                           Max
## -3.8996 -0.7410 -0.0816
                               0.5543
                                         3.3060
##
## Coefficients:
##
                            Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                        0.39607
                                                   3.414 0.00064 ***
                             1.35219
                                                   9.392 < 2e-16 ***
## expansion_status2
                             0.33926
                                        0.03612
## expansion_status3
                             0.35952
                                        0.04044
                                                   8.889 < 2e-16 ***
                                        0.03479
                                                   8.981 < 2e-16 ***
## expansion_status4
                             0.31244
## percent_male
                            -4.95142
                                        0.85590
                                                 -5.785 7.25e-09 ***
## percent_african_american 0.79997
                                        0.14250
                                                   5.614 1.98e-08 ***
## percent_hispanic
                            -0.30207
                                        0.12575 -2.402 0.01630 *
## age65-74
                            -0.67622
                                        0.02674 -25.284 < 2e-16 ***
                            -0.28164
                                        0.02671 -10.545 < 2e-16 ***
## age75+
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
  (Dispersion parameter for Negative Binomial(9.3124) family taken to be 1)
##
      Null deviance: 1832.48 on 912 degrees of freedom
## Residual deviance: 930.39 on 904 degrees of freedom
     (2 observations deleted due to missingness)
## AIC: 12772
##
## Number of Fisher Scoring iterations: 1
##
##
                 Theta: 9.312
##
             Std. Err.: 0.434
##
   2 x log-likelihood: -12752.317
anova(mod.nb_pqi05_c3, mod.nb_pqi05_c4)
## Likelihood ratio tests of Negative Binomial Models
## Response: pqi05
##
## 1
           expansion_status + percent_male + percent_african_american + percent_hispanic + offset(log(y
## 2 expansion_status + percent_male + percent_african_american + percent_hispanic + age + offset(log(y
                                                  df LR stat. Pr(Chi)
       theta Resid. df
                           2 x log-lik.
                                          Test
## 1 5.591228
                    906
                              -13233.90
## 2 9.312394
                    904
                              -12752.32 1 vs 2
                                                   2 481.583
By the LRT, we add age category into the model.
mod.nb_pqi05_c5 <- MASS::glm.nb(pqi05 ~ `expansion_status` + percent_male + percent_african_american +
summary(mod.nb_pqi05_c5)
Percent Eligible for Medicaid
##
## Call:
## MASS::glm.nb(formula = pqi05 ~ expansion_status + percent_male +
       percent_african_american + percent_hispanic + age + percent_eligible_for_medicaid +
##
       offset(log(year)), data = pqi05_data, init.theta = 10.56586819,
##
       link = log)
## Deviance Residuals:
      Min
                 1Q
                     Median
                                   3Q
                                           Max
## -3.8638 -0.7618 -0.0617
                               0.5606
                                        3.7466
##
## Coefficients:
##
                                 Estimate Std. Error z value Pr(>|z|)
                                                      5.651 1.60e-08 ***
## (Intercept)
                                  2.12508
                                             0.37606
## expansion_status2
                                  0.38198
                                             0.03429 11.141 < 2e-16 ***
## expansion status3
                                 0.35968
                                             0.03801
                                                       9.463 < 2e-16 ***
                                             0.03390 12.223 < 2e-16 ***
## expansion_status4
                                 0.41442
## percent_male
                                 -7.48105
                                             0.82676 -9.049 < 2e-16 ***
## percent_african_american
                                 0.13527
                                             0.14682
                                                      0.921
                                                                0.357
```

```
## percent_hispanic
                                                                     -0.92578
                                                                                             0.13065 -7.086 1.38e-12 ***
                                                                                              0.02513 -27.327 < 2e-16 ***
## age65-74
                                                                     -0.68677
                                                                     -0.28341
                                                                                              0.02509 -11.294 < 2e-16 ***
## age75+
                                                                                              0.18317 11.299 < 2e-16 ***
## percent_eligible_for_medicaid 2.06973
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for Negative Binomial(10.5659) family taken to be 1)
##
##
              Null deviance: 2075.52 on 912 degrees of freedom
## Residual deviance: 928.39 on 903 degrees of freedom
          (2 observations deleted due to missingness)
## AIC: 12657
##
## Number of Fisher Scoring iterations: 1
##
##
##
                                   Theta: 10.566
##
                           Std. Err.: 0.495
##
     2 x log-likelihood: -12634.718
anova(mod.nb_pqi05_c4, mod.nb_pqi05_c5)
## Likelihood ratio tests of Negative Binomial Models
## Response: pqi05
##
## 1
                                                                             expansion_status + percent_male + percent_african_american + percent_african_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_america
## 2 expansion_status + percent_male + percent_african_american + percent_hispanic + age + percent_elig
                                                          2 x log-lik.
                                                                                                          df LR stat. Pr(Chi)
                  theta Resid. df
                                                                                          Test
## 1 9.312394
                                            904
                                                                -12752.32
## 2 10.565868
                                            903
                                                                -12634.72 1 vs 2
                                                                                                             1 117.5989
                                                                                                                                                 0
By the LRT, we add in the percent eligible for Medicaid.
mod.nb_pqi05_1 <- MASS::glm.nb(pqi05 ~ `expansion_status` + percent_male + percent_african_american + ;
summary(mod.nb_pqi05_1)
Check for quadratic effects of percent_eligible_for_medicaid
##
## Call:
## MASS::glm.nb(formula = pqi05 ~ expansion_status + percent_male +
##
              percent_african_american + percent_hispanic + age + percent_eligible_for_medicaid +
##
              percent_eligible_for_medicaid_2 + offset(log(year)), data = pqi05_data %>%
##
              mutate(percent_eligible_for_medicaid_2 = percent_eligible_for_medicaid^2),
##
              init.theta = 10.73197305, link = log)
##
## Deviance Residuals:
                                           Median
                                                                         3Q
##
              Min
                                   1Q
                                                                                          Max
## -3.7449 -0.7610 -0.0724 0.5409
                                                                                   3.9483
##
## Coefficients:
##
                                                                         Estimate Std. Error z value Pr(>|z|)
```

```
## expansion_status2
                                    0.39179
                                               0.03413 11.479 < 2e-16 ***
## expansion_status3
                                    0.35426
                                               0.03773
                                                        9.390 < 2e-16 ***
## expansion_status4
                                                                < 2e-16 ***
                                    0.41901
                                               0.03368 12.439
## percent_male
                                   -7.79114
                                               0.82379 -9.458
                                                                < 2e-16 ***
## percent_african_american
                                   0.13263
                                               0.14571
                                                         0.910
                                                                  0.363
## percent_hispanic
                                   -0.68909
                                               0.14343 -4.804 1.55e-06 ***
## age65-74
                                   -0.68874
                                               0.02494 -27.617 < 2e-16 ***
## age75+
                                   -0.28437
                                               0.02490 -11.421
                                                               < 2e-16 ***
## percent_eligible_for_medicaid
                                    4.79309
                                               0.71814
                                                         6.674 2.48e-11 ***
## percent_eligible_for_medicaid_2 -6.01438
                                               1.53259 -3.924 8.70e-05 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for Negative Binomial(10.732) family taken to be 1)
##
##
       Null deviance: 2107.66 on 912 degrees of freedom
## Residual deviance: 928.16 on 902 degrees of freedom
     (2 observations deleted due to missingness)
##
## AIC: 12644
##
## Number of Fisher Scoring iterations: 1
##
##
##
                 Theta: 10.732
##
             Std. Err.: 0.503
##
   2 x log-likelihood: -12620.248
anova(mod.nb_pqi05_c4, mod.nb_pqi05_1)
## Likelihood ratio tests of Negative Binomial Models
##
## Response: pqi05
##
## 1
                                                                       expansion_status + percent_male
## 2 expansion_status + percent_male + percent_african_american + percent_hispanic + age + percent_elig
         theta Resid. df
                            2 x log-lik.
                                           Test
                                                   df LR stat. Pr(Chi)
                               -12752.32
## 1 9.312394
                     904
## 2 10.731973
                     902
                               -12620.25 1 vs 2
                                                    2 132.0694
                                                                     0
By the LRT, we add the quadratic effects of the percent eligible for medicaid.
```

0.37547 5.259 1.45e-07 ***

1.97470

(Intercept)

##

Effect Modification We think there may be effect modification between % eligible for medicaid and expansion status, since in general Medicaid expansion means a higher percentage of the population qualifies for Medicaid.

```
mod.nb_pqi05_2 <-MASS::glm.nb(pqi05 ~ `expansion_status` + percent_male + percent_african_american + p
summary(mod.nb_pqi05_2 )

##
## Call:
## MASS::glm.nb(formula = pqi05 ~ expansion_status + percent_male +
## percent_african_american + percent_hispanic + age + percent_eligible_for_medicaid +
## percent_eligible_for_medicaid_2 + expansion_status * percent_eligible_for_medicaid +</pre>
```

offset(log(year)), data = pqi05_data %>% mutate(percent_eligible_for_medicaid_2 = percent_eligib

```
##
       init.theta = 10.81176474, link = log)
##
## Deviance Residuals:
##
      Min
                10
                    Median
                                   30
                                           Max
## -3.8050 -0.7623 -0.0844
                               0.5308
                                        4.1183
##
## Coefficients:
                                                   Estimate Std. Error z value
##
## (Intercept)
                                                    1.97190
                                                               0.37866
                                                                         5.208
                                                    0.32494
## expansion_status2
                                                               0.10302
                                                                          3.154
## expansion_status3
                                                    0.56754
                                                               0.13497
                                                                         4.205
## expansion_status4
                                                    0.48624
                                                               0.09793
                                                                         4.965
## percent_male
                                                   -7.80840
                                                               0.83033 -9.404
## percent_african_american
                                                    0.20430
                                                               0.15024
                                                                         1.360
## percent_hispanic
                                                   -0.65931
                                                               0.14620 -4.510
## age65-74
                                                   -0.68823
                                                               0.02485 -27.697
## age75+
                                                               0.02481 -11.418
                                                   -0.28327
## percent_eligible_for_medicaid
                                                    4.72213
                                                                0.85160
                                                                         5.545
## percent_eligible_for_medicaid_2
                                                                1.57719 -3.611
                                                   -5.69466
## expansion_status2:percent_eligible_for_medicaid 0.37762
                                                                0.44829
                                                                         0.842
## expansion_status3:percent_eligible_for_medicaid -0.98168
                                                               0.59522 -1.649
## expansion_status4:percent_eligible_for_medicaid -0.35142
                                                                0.41896 -0.839
##
                                                   Pr(>|z|)
## (Intercept)
                                                   1.91e-07 ***
## expansion_status2
                                                   0.001610 **
## expansion_status3
                                                   2.61e-05 ***
## expansion_status4
                                                   6.85e-07 ***
                                                    < 2e-16 ***
## percent_male
## percent_african_american
                                                   0.173880
## percent_hispanic
                                                   6.50e-06 ***
## age65-74
                                                    < 2e-16 ***
## age75+
                                                    < 2e-16 ***
## percent_eligible_for_medicaid
                                                   2.94e-08 ***
## percent_eligible_for_medicaid_2
                                                   0.000305 ***
## expansion_status2:percent_eligible_for_medicaid 0.399586
## expansion_status3:percent_eligible_for_medicaid 0.099092 .
## expansion_status4:percent_eligible_for_medicaid 0.401593
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for Negative Binomial(10.8118) family taken to be 1)
##
       Null deviance: 2123.10 on 912 degrees of freedom
##
## Residual deviance: 928.07 on 899
                                       degrees of freedom
     (2 observations deleted due to missingness)
## AIC: 12643
## Number of Fisher Scoring iterations: 1
##
##
##
                 Theta: 10.812
             Std. Err.: 0.507
##
##
## 2 x log-likelihood: -12613.388
```

```
anova(mod.nb_pqi05_1, mod.nb_pqi05_2)
## Likelihood ratio tests of Negative Binomial Models
##
## Response: pqi05
##
## 1
                                                         expansion_status + percent_male + percent_afric
## 2 expansion_status + percent_male + percent_african_american + percent_hispanic + age + percent_elig
       theta Resid. df
                           2 x log-lik.
                                          Test
                                                  df LR stat.
                                                                 Pr(Chi)
## 1 10.73197
                    902
                              -12620.25
                              -12613.39 1 vs 2
                                                    3 6.859423 0.07651599
## 2 10.81176
                    899
By the LRT, we do not add the interaction term to the model.
AIC(mod.nb_pqi05)
Model Diagnostics
## [1] 13314
AIC(mod.nb_pqi05_c1)
## [1] 13264.22
AIC(mod.nb_pqi05_c2)
## [1] 13252.04
AIC(mod.nb_pqi05_c3)
## [1] 13249.9
AIC(mod.nb_pqi05_c4)
## [1] 12772.32
AIC(mod.nb_pqi05_c5)
## [1] 12656.72
AIC(mod.nb_pqi05_1)
## [1] 12644.25
The full model has the lowest AIC.
BIC(mod.nb_pqi05)
## [1] 13338.09
BIC(mod.nb_pqi05_c1)
## [1] 13293.12
BIC(mod.nb_pqi05_c2)
## [1] 13285.76
BIC(mod.nb_pqi05_c3)
## [1] 13288.43
```

```
## [1] 12820.48

BIC(mod.nb_pqi05_c5)

## [1] 12709.7

BIC(mod.nb_pqi05_1)

## [1] 12702.05
```

The full model has the lowest AIC and BIC of all the models.

Check Poisson model As a last step, we'll check the model as a Poisson model, and check if there is truly overdispersion.

```
# Evidence of overdispersion
mean(pqi05_data$pqi05, na.rm = T) # 866.4775
```

```
## [1] 866.4775
var(pqi05_data$pqi05, na.rm = T) # 157324.5
```

[1] 157324.5

By these, we can say the negative binomial is the right choice.

```
exp(coef(mod.nb_pqi05_1))
```

Interpretation

```
##
                        (Intercept)
                                                   expansion_status2
##
                       7.204430e+00
                                                        1.479632e+00
##
                 expansion_status3
                                                   expansion_status4
##
                      1.425125e+00
                                                        1.520460e+00
##
                                           percent_african_american
                       percent_male
##
                       4.133815e-04
                                                        1.141825e+00
                                                            age65-74
##
                  percent_hispanic
##
                       5.020330e-01
                                                        5.022104e-01
##
                             age75+
                                      percent_eligible_for_medicaid
##
                       7.524900e-01
                                                        1.206742e+02
##
  percent_eligible_for_medicaid_2
##
                       2.443356e-03
```

```
exp(confint(mod.nb_pqi05_1))
## Waiting for profiling to be done...
                                           2.5 %
                                    3.396255e+00 1.527924e+01
## (Intercept)
## expansion_status2
                                    1.383489e+00 1.581847e+00
                                   1.323337e+00 1.534566e+00
## expansion_status3
## expansion status4
                                   1.422925e+00 1.623995e+00
                                    7.882399e-05 2.173371e-03
## percent male
## percent_african_american
                                   8.501881e-01 1.536220e+00
## percent_hispanic
                                    3.782871e-01 6.684109e-01
## age65-74
                                    4.782099e-01 5.274140e-01
## age75+
                                    7.165962e-01 7.901798e-01
## percent_eligible_for_medicaid 2.862236e+01 5.036960e+02
## percent_eligible_for_medicaid_2 1.155054e-04 5.291054e-02
PQI08 Since these variables are rates, we will want to use Poisson models. There may be overdispersion,
so I'm going to start fitting a negative binomial and then check if the poisson version has overdispersion.
pqi08_data <- hrr %>%
  filter(!is.na(expansion_status)) %>%
  select(year, hrr, state, expansion_status, percent_male, percent_african_american, `percent_hispanic
  gather(age, pqi08, c("pqi08_chf_admission_rate_(age_<_65)", "pqi08_chf_admission_rate_(age_65-74)", "</pre>
  mutate(age = str_extract(age, "(?<=age_).+(?=\\))"))</pre>
mod.nb_pqi08 <- MASS::glm.nb(pqi08 ~ `expansion_status` + offset(log(year)), data = pqi08_data)</pre>
summary(mod.nb_pqi08)
Start with the base model
##
## MASS::glm.nb(formula = pqi08 ~ expansion_status + offset(log(year)),
       data = pqi08_data, init.theta = 3.471413904, link = log)
##
##
## Deviance Residuals:
##
                                    3Q
       Min
                 1Q
                      Median
                                            Max
## -2.6165
           -0.9591 -0.3042
                               0.7107
                                         2.0079
##
## Coefficients:
##
                     Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                     -0.46835
                                 0.04626 -10.125 < 2e-16 ***
## expansion_status2 0.10140
                                  0.05701
                                            1.779 0.075314 .
## expansion_status3 0.23732
                                 0.06262
                                            3.790 0.000151 ***
                                            2.965 0.003026 **
## expansion status4 0.16100
                                 0.05430
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for Negative Binomial(3.4714) family taken to be 1)
##
       Null deviance: 973.41 on 913 degrees of freedom
## Residual deviance: 957.34 on 910 degrees of freedom
     (1 observation deleted due to missingness)
```

```
## AIC: 14579
##
## Number of Fisher Scoring iterations: 1
##
##
## Theta: 3.471
##
## Std. Err.: 0.156
##
## 2 x log-likelihood: -14569.068
```

We'll start adding in potential covariates and use likelihood ratio tests to determine if they should be added to the model.

```
mod.nb_pqi08_c1 <- MASS::glm.nb(pqi08 ~ `expansion_status` + percent_male + offset(log(year)), data = ;
summary(mod.nb_pqi08_c1)</pre>
```

Percent Male

```
##
## Call:
## MASS::glm.nb(formula = pqi08 ~ expansion_status + percent_male +
      offset(log(year)), data = pqi08_data, init.theta = 3.600767565,
##
      link = log)
##
## Deviance Residuals:
      Min
##
                                 3Q
                1Q
                   Median
                                        Max
## -2.4705 -0.9875 -0.3146 0.7153
                                     2.0902
##
## Coefficients:
##
                   Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                    ## expansion_status2 0.08506
                              0.05602 1.518 0.12889
## expansion_status3 0.18719
                              0.06179
                                        3.029 0.00245 **
## expansion_status4 0.14328
                              0.05338 2.684 0.00727 **
## percent_male
                   -7.75935
                              1.24876 -6.214 5.18e-10 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for Negative Binomial(3.6008) family taken to be 1)
##
##
      Null deviance: 1009.57 on 913 degrees of freedom
## Residual deviance: 955.81 on 909 degrees of freedom
    (1 observation deleted due to missingness)
## AIC: 14545
##
## Number of Fisher Scoring iterations: 1
##
##
                Theta: 3.601
##
##
            Std. Err.: 0.162
##
  2 x log-likelihood: -14532.644
```

```
anova(mod.nb_pqi08, mod.nb_pqi08_c1)
## Likelihood ratio tests of Negative Binomial Models
## Response: pqi08
##
                                                   Model
                                                            theta Resid. df
## 1
                    expansion_status + offset(log(year)) 3.471414
                                                                        910
## 2 expansion_status + percent_male + offset(log(year)) 3.600768
                                                                        909
       2 x log-lik.
                      Test
                               df LR stat.
                                                Pr(Chi)
## 1
           -14569.07
## 2
           -14532.64 1 vs 2
                                1 36.42389 1.587457e-09
By the LRT, we add percent_male into the model.
mod.nb_pqi08_c2 <- MASS::glm.nb(pqi08 ~ `expansion_status` + percent_male + percent_african_american +</pre>
summary(mod.nb_pqi08_c2)
Percent African American
##
## Call:
## MASS::glm.nb(formula = pqi08 ~ expansion_status + percent_male +
       percent_african_american + offset(log(year)), data = pqi08_data,
##
       init.theta = 3.769564704, link = log)
##
## Deviance Residuals:
                     Median
      Min
                10
                                   3Q
                                           Max
## -2.4891 -0.9775 -0.3492 0.6786
                                        2.2747
##
## Coefficients:
##
                            Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                       0.61895 2.062
                            1.27611
                                                          0.0392 *
## expansion_status2
                             0.07935
                                        0.05477
                                                  1.449
                                                          0.1474
## expansion status3
                             0.14624
                                        0.06073
                                                  2.408
                                                          0.0160 *
## expansion_status4
                             0.06457
                                       0.05343
                                                  1.209
                                                          0.2268
                            -3.98088
## percent male
                                        1.33688 -2.978
                                                          0.0029 **
## percent_african_american 1.53074
                                                  6.873 6.28e-12 ***
                                        0.22272
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for Negative Binomial(3.7696) family taken to be 1)
##
##
       Null deviance: 1056.75 on 913 degrees of freedom
## Residual deviance: 953.96 on 908 degrees of freedom
##
     (1 observation deleted due to missingness)
## AIC: 14501
## Number of Fisher Scoring iterations: 1
##
##
##
                 Theta: 3.770
##
             Std. Err.: 0.170
##
## 2 x log-likelihood: -14487.193
```

```
anova(mod.nb_pqi08_c1, mod.nb_pqi08_c2)
## Likelihood ratio tests of Negative Binomial Models
## Response: pqi08
##
                                                                              Model
## 1
                                expansion_status + percent_male + offset(log(year))
## 2 expansion_status + percent_male + percent_african_american + offset(log(year))
       theta Resid. df
                           2 x log-lik.
                                         Test
                                                  df LR stat.
                                                                   Pr(Chi)
                    909
                              -14532.64
## 1 3.600768
## 2 3.769565
                    908
                              -14487.19 1 vs 2
                                                  1 45.45124 1.564859e-11
By the LRT, we add in percent African American into the model.
mod.nb_pqi08_c3 <- MASS::glm.nb(pqi08 ~ `expansion_status` + percent_male + percent_african_american +</pre>
summary(mod.nb pgi08 c3)
Percent Hispanic
##
## Call:
## MASS::glm.nb(formula = pqi08 ~ expansion_status + percent_male +
       percent_african_american + percent_hispanic + offset(log(year)),
       data = pqi08_data, init.theta = 3.787438553, link = log)
##
##
## Deviance Residuals:
                     Median
      Min
                10
                                   3Q
                                           Max
## -2.4963 -0.9818 -0.3646 0.6812
                                        2.3433
##
## Coefficients:
##
                            Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                       0.61756 2.107 0.03515 *
                            1.30097
## expansion_status2
                            0.10917
                                       0.05621
                                                 1.942 0.05210 .
                                                  2.889 0.00387 **
## expansion status3
                            0.18193
                                       0.06298
## expansion_status4
                            0.08155
                                       0.05412
                                                 1.507 0.13185
## percent male
                            -4.13968
                                       1.33555 -3.100 0.00194 **
## percent_african_american 1.56848
                                                 7.048 1.81e-12 ***
                                       0.22254
## percent_hispanic
                            0.40554
                                       0.19598
                                                 2.069 0.03852 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for Negative Binomial(3.7874) family taken to be 1)
##
       Null deviance: 1061.74 on 913 degrees of freedom
##
## Residual deviance: 953.77 on 907 degrees of freedom
     (1 observation deleted due to missingness)
## AIC: 14499
##
## Number of Fisher Scoring iterations: 1
##
##
##
                 Theta: 3.787
            Std. Err.: 0.170
##
##
```

```
## 2 x log-likelihood: -14482.508
anova(mod.nb_pqi08_c2, mod.nb_pqi08_c3)
## Likelihood ratio tests of Negative Binomial Models
##
## Response: pqi08
##
                                                                                                  Model
                        expansion_status + percent_male + percent_african_american + offset(log(year))
## 1
## 2 expansion_status + percent_male + percent_african_american + percent_hispanic + offset(log(year))
       theta Resid. df
                           2 x log-lik.
                                          Test
                                                  df LR stat.
                                                                 Pr(Chi)
## 1 3.769565
                    908
                              -14487.19
## 2 3.787439
                    907
                              -14482.51 1 vs 2
                                                   1 4.684588 0.03043436
By the LRT, we add percent hispanic to the model.
mod.nb_pqi08_c4 <- MASS::glm.nb(pqi08 ~ `expansion_status` + percent_male + percent_african_american +
summary(mod.nb_pqi08_c4)
Age category
##
## Call:
## MASS::glm.nb(formula = pqi08 ~ expansion_status + percent_male +
##
       percent_african_american + percent_hispanic + age + offset(log(year)),
##
       data = pqi08_data, init.theta = 13.74646014, link = log)
##
## Deviance Residuals:
                      Median
      Min
                 1Q
                                   3Q
                                           Max
## -3.8050 -0.6991 -0.0622
                               0.5877
                                        3.4104
##
## Coefficients:
##
                            Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                             0.99357
                                        0.32590
                                                 3.049 0.002298 **
                                        0.02965
                                                  3.898 9.70e-05 ***
## expansion status2
                             0.11559
## expansion_status3
                             0.19052
                                        0.03322
                                                 5.735 9.73e-09 ***
## expansion status4
                             0.10545
                                        0.02855
                                                 3.694 0.000221 ***
## percent_male
                            -3.92248
                                        0.70431 -5.569 2.56e-08 ***
## percent_african_american 1.87339
                                        0.11722
                                                 15.981 < 2e-16 ***
## percent hispanic
                                        0.10330
                                                  4.753 2.00e-06 ***
                             0.49103
## age65-74
                            -0.44704
                                        0.02202 -20.301 < 2e-16 ***
## age75+
                             0.64509
                                        0.02196 29.382 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for Negative Binomial(13.7465) family taken to be 1)
##
##
       Null deviance: 3821.51 on 913 degrees of freedom
## Residual deviance: 926.26 on 905 degrees of freedom
     (1 observation deleted due to missingness)
## AIC: 13276
##
## Number of Fisher Scoring iterations: 1
##
```

```
##
                 Theta: 13.746
##
            Std. Err.: 0.644
##
  2 x log-likelihood: -13256.279
##
anova(mod.nb_pqi08_c3, mod.nb_pqi08_c4)
## Likelihood ratio tests of Negative Binomial Models
##
## Response: pqi08
##
## 1
          expansion_status + percent_male + percent_african_american + percent_hispanic + offset(log(y
## 2 expansion_status + percent_male + percent_african_american + percent_hispanic + age + offset(log(y
         theta Resid. df
                            2 x log-lik.
                                                   df LR stat. Pr(Chi)
                                           Test
## 1 3.787439
                     907
                               -14482.51
                     905
                               -13256.28 1 vs 2
                                                    2 1226.229
## 2 13.746460
By the LRT, we add in age category to the model.
mod.nb_pqi08_c5 <- MASS::glm.nb(pqi08 ~ `expansion_status` + percent_male + percent_african_american +
summary(mod.nb_pqi08_c5)
Percent Eligible for Medicaid
##
## Call:
## MASS::glm.nb(formula = pqi08 ~ expansion_status + percent_male +
       percent_african_american + percent_hispanic + age + percent_eligible_for_medicaid +
##
       offset(log(year)), data = pqi08_data, init.theta = 14.35255937,
##
       link = log)
##
## Deviance Residuals:
      Min
                     Median
                                   30
                                           Max
                1Q
## -3.9043 -0.7056 -0.0705
                              0.5978
                                        3.5575
##
## Coefficients:
##
                                 Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                            0.32235
                                                     4.107 4.01e-05 ***
                                  1.32394
## expansion_status2
                                  0.14053
                                            0.02931
                                                       4.794 1.63e-06 ***
## expansion status3
                                 0.19079
                                            0.03252
                                                     5.867 4.44e-09 ***
## expansion_status4
                                 0.15683
                                            0.02897
                                                       5.413 6.20e-08 ***
                                            0.70870 -7.135 9.69e-13 ***
## percent_male
                                 -5.05646
                                 1.55864
## percent_african_american
                                            0.12588 12.382 < 2e-16 ***
## percent_hispanic
                                  0.18220
                                            0.11186
                                                      1.629
                                                                0.103
## age65-74
                                 -0.45301
                                            0.02156 -21.013 < 2e-16 ***
## age75+
                                  0.64174
                                            0.02149
                                                      29.860 < 2e-16 ***
## percent_eligible_for_medicaid 1.01699
                                            0.15702
                                                      6.477 9.36e-11 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for Negative Binomial(14.3526) family taken to be 1)
##
##
      Null deviance: 3987.99 on 913 degrees of freedom
## Residual deviance: 925.61 on 904 degrees of freedom
     (1 observation deleted due to missingness)
```

```
## AIC: 13238
##
## Number of Fisher Scoring iterations: 1
##
##
##
                                  Theta: 14.353
                          Std. Err.: 0.673
##
##
## 2 x log-likelihood: -13216.242
anova(mod.nb_pqi08_c4, mod.nb_pqi08_c5)
## Likelihood ratio tests of Negative Binomial Models
##
## Response: pqi08
##
## 1
                                                                           expansion_status + percent_male + percent_african_american + percent_african_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_american_america
## 2 expansion_status + percent_male + percent_african_american + percent_hispanic + age + percent_elig
                theta Resid. df
                                                      2 x log-lik.
                                                                                    Test
                                                                                                     df LR stat.
                                                                                                                                        Pr(Chi)
                                        905
                                                            -13256.28
## 1 13.74646
                                        904
                                                            -13216.24 1 vs 2
                                                                                                       1 40.03666 2.492413e-10
## 2 14.35256
By the LRT we add in percent eligible for medicaid into the model.
mod.nb_pqi08_1 <- MASS::glm.nb(pqi08 ~ `expansion_status` + percent_male + percent_african_american +
summary(mod.nb_pqi08_1)
Check for quadratic effects of percent_eligible_for_medicaid
##
## Call:
## MASS::glm.nb(formula = pqi08 ~ expansion_status + percent_male +
              percent_african_american + percent_hispanic + age + percent_eligible_for_medicaid +
              percent_eligible_for_medicaid_2 + offset(log(year)), data = pqi08_data %>%
##
              mutate(percent_eligible_for_medicaid_2 = percent_eligible_for_medicaid^2),
##
##
              init.theta = 14.56522529, link = log)
##
## Deviance Residuals:
                                            Median
##
              Min
                                  10
                                                                       3Q
## -3.9464 -0.7028 -0.0576
                                                                                 3.5345
                                                              0.6006
## Coefficients:
                                                                      Estimate Std. Error z value Pr(>|z|)
                                                                                               0.32198 3.744 0.000181 ***
## (Intercept)
                                                                        1.20537
## expansion_status2
                                                                        0.14902
                                                                                               0.02920 5.104 3.33e-07 ***
                                                                                               0.03229 5.791 7.00e-09 ***
## expansion_status3
                                                                        0.18700
## expansion_status4
                                                                        0.16041
                                                                                               0.02880 5.569 2.56e-08 ***
## percent_male
                                                                       -5.32774
                                                                                               0.70645 -7.542 4.64e-14 ***
## percent_african_american
                                                                        1.55893
                                                                                               0.12497 12.474 < 2e-16 ***
## percent_hispanic
                                                                                                                 3.152 0.001623 **
                                                                        0.38696
                                                                                               0.12278
## age65-74
                                                                       -0.45338
                                                                                               0.02140 -21.183 < 2e-16 ***
## age75+
                                                                        0.64182
                                                                                               0.02134 30.082 < 2e-16 ***
                                                                                               0.61531 5.299 1.17e-07 ***
## percent_eligible_for_medicaid
                                                                        3.26043
## percent_eligible_for_medicaid_2 -4.94633
                                                                                               1.31252 -3.769 0.000164 ***
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
  (Dispersion parameter for Negative Binomial(14.5652) family taken to be 1)
##
##
##
       Null deviance: 4046.37 on 913 degrees of freedom
## Residual deviance: 925.46 on 903 degrees of freedom
     (1 observation deleted due to missingness)
## AIC: 13227
##
## Number of Fisher Scoring iterations: 1
##
##
##
                 Theta: 14.565
##
             Std. Err.: 0.683
##
    2 x log-likelihood: -13202.676
anova(mod.nb_pqi08_c5, mod.nb_pqi08_1)
## Likelihood ratio tests of Negative Binomial Models
##
## Response: pqi08
##
## 1
                                        expansion_status + percent_male + percent_african_american + per
## 2 expansion_status + percent_male + percent_african_american + percent_hispanic + age + percent_elig
                                           Test
                                                   df LR stat.
                                                                    Pr(Chi)
        theta Resid. df
                           2 x log-lik.
## 1 14.35256
                    904
                               -13216.24
## 2 14.56523
                    903
                               -13202.68 1 vs 2
                                                    1 13.5666 0.000230246
By the LRT we add the quadratic effects of percent eligible for medicaid to the model.
Effect Modification We think there may be effect modification between % eligible for medicaid and
expansion status, since in general Medicaid expansion means a higher percentage of the population qualifies
for Medicaid.
mod.nb_pqi08_2 <- MASS::glm.nb(pqi08 ~ `expansion_status` + percent_male + percent_african_american + ;
summary(mod.nb_pqi08_2)
##
## Call:
## MASS::glm.nb(formula = pqi08 ~ expansion_status + percent_male +
       percent_african_american + percent_hispanic + age + percent_eligible_for_medicaid +
##
       percent_eligible_for_medicaid_2 + expansion_status * percent_eligible_for_medicaid +
##
       offset(log(year)), data = pqi08_data %>% mutate(percent_eligible_for_medicaid_2 = percent_eligib
##
       init.theta = 14.62256022, link = log)
##
##
## Deviance Residuals:
       Min
##
                 1Q
                      Median
                                    3Q
                                            Max
## -3.9506 -0.7084 -0.0503
                              0.6013
                                         3.5055
##
## Coefficients:
##
                                                    Estimate Std. Error z value
## (Intercept)
                                                     1.15321
                                                                0.32526
                                                                           3.546
## expansion_status2
                                                     0.25612
                                                                 0.08836
                                                                           2.899
```

0.11582

0.08396

0.31206 0.30691 2.694

3.655

expansion_status3

expansion_status4

```
0.12908 12.139
## percent_african_american
                                                    1.56698
## percent_hispanic
                                                    0.42635
                                                               0.12539
                                                                         3.400
## age65-74
                                                               0.02136 -21.181
                                                   -0.45247
## age75+
                                                    0.64285
                                                               0.02129 30.189
                                                               0.73098
## percent_eligible_for_medicaid
                                                    3.85819
                                                                        5.278
## percent_eligible_for_medicaid_2
                                                               1.35333 -3.936
                                                   -5.32649
## expansion_status2:percent_eligible_for_medicaid -0.44823
                                                               0.38483 -1.165
## expansion_status3:percent_eligible_for_medicaid -0.53568
                                                               0.51099 -1.048
## expansion_status4:percent_eligible_for_medicaid -0.66679
                                                               0.35949 -1.855
                                                   Pr(>|z|)
## (Intercept)
                                                   0.000392 ***
## expansion_status2
                                                   0.003748 **
## expansion_status3
                                                   0.007052 **
## expansion_status4
                                                   0.000257 ***
## percent_male
                                                   1.53e-14 ***
## percent_african_american
                                                    < 2e-16 ***
## percent_hispanic
                                                   0.000673 ***
## age65-74
                                                    < 2e-16 ***
## age75+
                                                    < 2e-16 ***
## percent_eligible_for_medicaid
                                                   1.31e-07 ***
## percent_eligible_for_medicaid_2
                                                   8.29e-05 ***
## expansion_status2:percent_eligible_for_medicaid 0.244125
## expansion_status3:percent_eligible_for_medicaid 0.294489
## expansion_status4:percent_eligible_for_medicaid 0.063620 .
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for Negative Binomial(14.6226) family taken to be 1)
##
##
       Null deviance: 4062.10 on 913 degrees of freedom
## Residual deviance: 925.44 on 900 degrees of freedom
     (1 observation deleted due to missingness)
## AIC: 13229
## Number of Fisher Scoring iterations: 1
##
##
##
                 Theta: 14.623
##
             Std. Err.: 0.686
##
   2 x log-likelihood: -13199.070
anova(mod.nb_pqi08_1, mod.nb_pqi08_2)
## Likelihood ratio tests of Negative Binomial Models
##
## Response: pqi08
##
## 1
                                                        expansion_status + percent_male + percent_afric
## 2 expansion_status + percent_male + percent_african_american + percent_hispanic + age + percent_elig
        theta Resid. df
                           2 x log-lik.
                                          Test
                                                  df LR stat. Pr(Chi)
                    903
## 1 14.56523
                              -13202.68
## 2 14.62256
                    900
                              -13199.07 1 vs 2
                                                   3 3.605778 0.3073
```

-5.48210

0.71333 -7.685

percent_male

By the LRT, we don't add the interaction term to the model.

```
AIC(mod.nb_pqi08)
Model Diagnostics
## [1] 14579.07
AIC(mod.nb_pqi08_c1)
## [1] 14544.64
AIC(mod.nb_pqi08_c2)
## [1] 14501.19
AIC(mod.nb_pqi08_c3)
## [1] 14498.51
AIC(mod.nb_pqi08_c4)
## [1] 13276.28
AIC(mod.nb_pqi08_c5)
## [1] 13238.24
AIC(mod.nb_pqi08_1)
## [1] 13226.68
BIC(mod.nb_pqi08)
## [1] 14603.16
BIC(mod.nb_pqi08_c1)
## [1] 14573.55
BIC(mod.nb_pqi08_c2)
## [1] 14534.92
BIC(mod.nb_pqi08_c3)
## [1] 14537.05
BIC(mod.nb_pqi08_c4)
## [1] 13324.46
BIC(mod.nb_pqi08_c5)
## [1] 13291.24
BIC(mod.nb_pqi08_1)
## [1] 13284.49
```

The full model has the lowest AIC and BIC of all the models.

```
mod.pois_pqi08 <- glm(pqi08 ~ `expansion_status` + `percent_male` + `percent_african_american` + percen
# Evaluate overdispersion
deviance(mod.pois_pqi08)/mod.pois_pqi08$df.residual # 90.85094
Check Poisson model
## [1] 90.85094
pearson.stat_pqi08 <- sum((na.omit(pqi08_data) pqi08 - fitted(mod.pois_pqi08))^2/fitted(mod.pois_pqi08)
pearson.stat_pqi08/mod.pois_pqi08$df.residual # 90.84562
## [1] 90.84562
# Evidence of overdispersion
mean(pqi08_data$pqi08, na.rm = T) # 1447.86
## [1] 1447.86
var(pqi08_data$pqi08, na.rm = T) # 606848.1
## [1] 606848.1
Due to the evidence of overdispersion, we can say the negative binomial is the right choice.
exp(coef(mod.nb_pqi08_1))
Interpretation
##
                       (Intercept)
                                                  expansion_status2
##
                       3.337991638
                                                        1.160691240
##
                 expansion_status3
                                                  expansion_status4
##
                       1.205621783
                                                        1.173990405
##
                      percent_male
                                           percent_african_american
##
                       0.004855028
                                                        4.753737917
##
                  percent_hispanic
                                                           age65-74
##
                       1.472500611
                                                        0.635477634
##
                                      percent_eligible_for_medicaid
                            age75+
                       1.899931358
                                                       26.060654335
##
##
  percent_eligible_for_medicaid_2
                       0.007109440
exp(confint(mod.nb_pqi08_1))
## Waiting for profiling to be done...
                                           2.5 %
                                                      97.5 %
##
## (Intercept)
                                   1.7487279408 6.37112217
                                   1.0958158961 1.22906501
## expansion status2
## expansion_status3
                                   1.1316335553 1.28434480
## expansion_status4
                                   1.1093966675 1.24195864
## percent_male
                                   0.0011715313 0.02015097
## percent_african_american
                                   3.6965575647 6.12163898
## percent_hispanic
                                   1.1550949235 1.88157192
## age65-74
                                   0.6093185786 0.66275913
## age75+
                                   1.8218071945 1.98140390
```

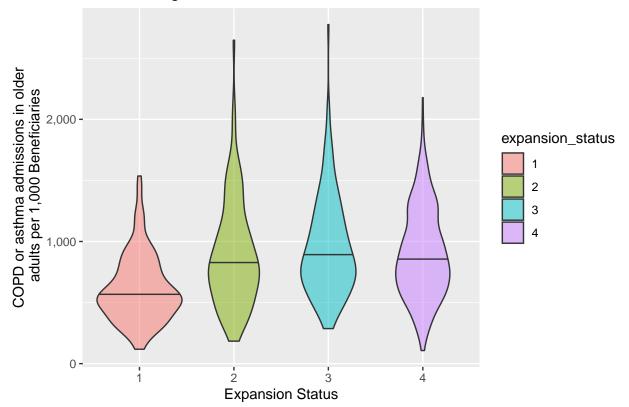
percent_eligible_for_medicaid 7.6493089640 88.13627171

```
## percent_eligible_for_medicaid_2 0.0005292642 0.09713554
```

Create plots for report

```
pqi05_data %>%
   na.omit() %>%
   ggplot(aes(x = expansion_status, y = pqi05, fill = expansion_status)) +
   geom_violin(alpha = 0.5, draw_quantiles = c(0.5)) +
   xlab("Expansion Status") +
   ylab("COPD or asthma admissions in older\n adults per 1,000 Beneficiaries") +
   scale_y_continuous(labels = scales::comma) +
   ggtitle("2018 Average PQI 05")
```

2018 Average PQI 05



```
pqi08_data %>%
  na.omit() %>%
  ggplot(aes(x = expansion_status, y = pqi08, fill = expansion_status)) +
  geom_violin(alpha = 0.5, draw_quantiles = c(0.5)) +
  xlab("Expansion Status") +
  ylab("Congestive heart failure admissions per 1,000 beneficiaries") +
  scale_y_continuous(labels = scales::comma) +
  ggtitle("2018 Average PQI 08")
```

