

MANIPULATING POLYGONS

REBECCA HOBERG AND MARY SOLBRIG

ABSTRACT. We will implement various algorithms on polygons (not necessarily convex). The user will input an ordered list of vertices, or a list of such lists, and our program then initializes a corresponding list of polygons. If the vertices the user gives have adjacent colinear points, these will be removed, and if they have self-intersections, more than one polygon may be created. The user also has the option to specify holes inside the polygons. Functions we will create include `contains` (whether a point or polygon is contained in a polygon) `intersection` of two polygons.

CONTENTS

1. Segment Class	1
2. Polygons Class	1
3. Implementation Details	2
4. What is currently in Sage	2

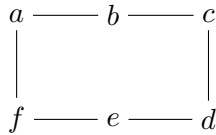
1. SEGMENT CLASS

In order to work more easily with polygons, we first created a class called `segment`. In this class is the function `intersect`. The call `intersect(segment1,segment2)` returns `(True, point)` if the two segments intersect at a point (including possibly the endpoints), and `(False, None)` if they do not intersect. If their intersection is in fact a line segment, it returns `(True, None)`. The `segment` class also has `contains`, which determines whether a point is contained in the segment, and `length`.

2. POLYGONS CLASS

The class `polygon_set` that we implemented has a list of polygons called `corners`, where each polygon in the list is a list of vertices that ends with its starting vertex.

Here is an example of how our initialization works. Suppose you input the sequence of points $[a, b, c, d, e, f]$, corresponding to the following diagram.



Our code would then set the polygons list to be $[[a, c, d, f, a]]$.

If on the same diagram we were instead given the list $[a, b, e, d, c, e, f]$, our code would set the polygons list to be $[[a, b, e, f, a], [c, e, d, c]]$.

The class `polygon_set` will also have the following functions:

- (1) Intersection
- (2) Area
- (3) Contains
- (4) Perimeter

3. IMPLEMENTATION DETAILS

The initialization of polygons calls the function `set_corners`, which does the following:

- (1) Removes any colinear points.
- (2) If any segment intersects a non-adjacent segment, it computes the point of intersection and splits the list into two separate lists of vertices.

IMPORTANT: If the list of vertices the user gives would yield interior line segments, our code will (at best) fail loudly, and (at worst) fail silently. For example, a star will fail. Hopefully will fix this by tomorrow, but may not get around to it.

4. WHAT IS CURRENTLY IN SAGE

Sage currently has some polygon capabilities, but most of it is done in much greater generality, considering polyhedra in n dimensions. While we were able to find the simple area function, we weren't able to find union and intersection and it only deals with convex polygons. Our code allows the user to compute the area of much more general 2-D polygons, and also allows the computation of intersection. Union of two polygons would also be fairly simple to create, as it would be fairly similar to intersection.

An alternative Sage object, `polygon2d`, allows for arbitrary polygons, even allowing for self-intersections, but all it does is graph. Our code uses this object to be able to graph, but it also allows for computation of intersection, union, and more.